

The importance of warm conveyor belts for (upscale) error growth

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Upscale error growth



Rapid growth of unavoidable small-scale errors → Ultimate limit of predictability on larger scales



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"Butterfly effect"

Conceptual model for upscale error growth



Traditional approach/ large body of literature:

- Error energy spectra + physical interpretation based on turbulent cascade
- Error growth on different scales qualitatively related to individual processes



3-stage model (Zhang et al., 2007)

Process-based, quantitative understanding



Here:

- Focus on process-based, quantitative understanding (e.g., Snyder et al. 2003)
- Potential-vorticity framework of "error" dynamics (Davies and Didone, 2013)

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Numerical experiments using a stochastic convection scheme



Ensembles with only initial difference in stochastic Plant-Craig convective scheme



Initial error on grid scale



Ensembles with only initial difference in stochastic Plant-Craig convective scheme



Ensembles with only initial difference in stochastic Plant-Craig convective scheme

- 5 ensemble members
- 12 different cases of real weather situations (first of each month)
- lead time of 31 days

Robust results about error growth up to regime scale





- Errors of the midlatitude tropopause
- "Errors" := differences between two error-growth experiments





















PV errors grow in amplitude and scale





PV errors grow in amplitude and scale

 \rightarrow What are the processes that govern the error evolution?



Quantitative potential-vorticity diagnostic for error growth



Error growth: Why a PV perspective?



- Potential vorticity (PV) key variable for dynamical meteorology
- PV-error tendency equation (Davies and Didone, 2013)
- Well established partition-and-attribution concept



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- Potential vorticity (PV) key variable for dynamical meteorology
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- Well established partition-and-attribution concept
- Errors maximize near the tropopause in a PV framework



Partitioning into four processes (Teubler and Riemer, 2016)



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Dynamics of PV errors

PV error: $PV^* = PV_{\text{forecast}} - PV_{\text{analysis}}$

Tendency for PV error (following Davies and Didone, 2013):

$$\frac{\partial}{\partial t}PV^{*} = \frac{\partial}{\partial t}PV_{\text{forecast}} - \frac{\partial}{\partial t}PV_{\text{analysis}}$$
$$= -\overrightarrow{v^{*}} \cdot \overrightarrow{\nabla}PV - \overrightarrow{v^{*}} \cdot \overrightarrow{\nabla}PV^{*} - \overrightarrow{v} \cdot \overrightarrow{\nabla}PV^{*} + NonCons^{*}$$
with *: error fields

without *: analysis field

Tendency for "error enstrophy" amplification (Baumgart et al. 2018):

$$\frac{\partial}{\partial t} \frac{PV^{*2}}{2} = -PV^* \overrightarrow{v^*} \cdot \overrightarrow{\nabla} PV + \frac{PV^{*2}}{2} \overrightarrow{\nabla} \cdot (\overrightarrow{v} + \overrightarrow{v^*}) + NonCons^*$$

decompose (as shown above)

Results: Processes governing error growth

Growth rates associated with processes

Growth rates associated with processes

Distinct stages of upscale error growth

Error growth dominated by latent heating

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Distinct stages of upscale error growth

Distinct stages of upscale error growth

Error growth experiments vs. operational EC

Initial condition uncertainty directly projects onto amplification by nonlinear tropopause dynamics.

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Initial condition uncertainty directly projects onto amplification by nonlinear tropopause dynamics.

Locally, however, dominant processes differ.

Individual PV-variance tendencies on 325K (day 4.5)

Summary: New insight into error growth

• Confirmation of multi-stage behavior of upscale error growth

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- Novel interpretation of processes: divergent PV-advection
- Initial-condition uncertainty dominates in operational model

Interested in medium-range predictability?

Give special attention to how data (assimilation), model errors and stochastic schemes project onto <u>upper-tropospheric</u> <u>outflow</u> = <u>most effective trigger of medium-range</u> error and uncertainty amplification (by nonlinear tropopause dynamics).

Processes governing the amplification of ensemble spread in a medium-range forecast with large forecast uncertainty