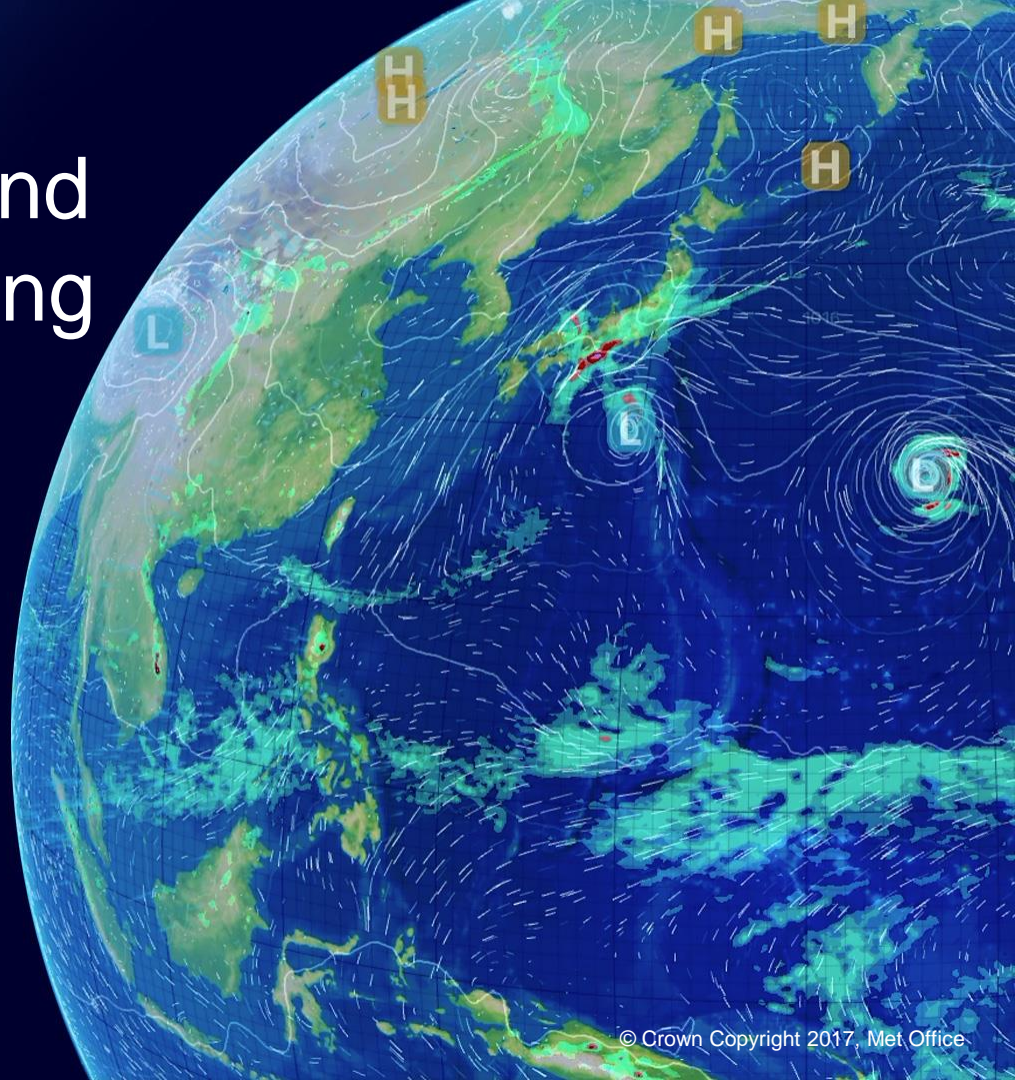


# Predictability barriers and diabatic processes during NAWDEX campaign

*Claudio Sanchez, John Methven,  
Sue Gray and Mike Cullen*

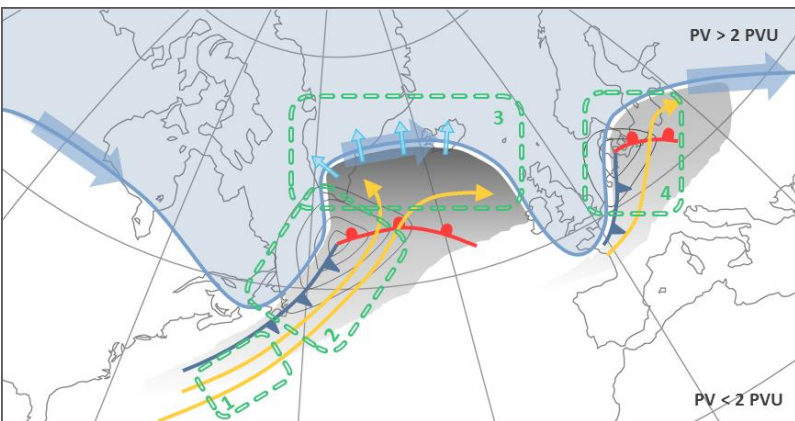
*WCB Workshop.*

*11/3/2020, ECMWF, Reading, UK*



# Introduction

- Uncertain representation of convective processes at forecast T+0 could **become large errors** at medium-range (e.g ‘forecast bust’ of Rodwell et al 2013)
- The dynamical mechanisms of error amplification are still debated



**NAWDEX Hypothesis:** Diabatic processes (1,2) have a major influence on the jet stream structure near North Atlantic, affecting the downstream development of Rossby waves (3) and eventually high impact weather (4) over Europe

**NAWDEX campaign:** Four aircraft observing diabatic processes and ridge development from 15/9 to 22/10 2016

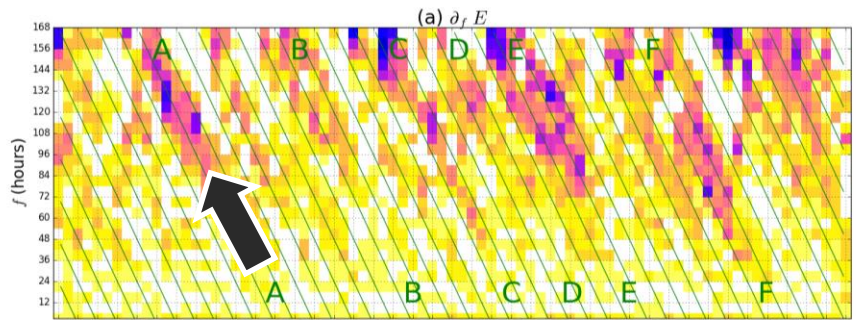
[Top]: Sketch of NAWDEX main goals: Observation of diabatic process in WCB (1,2), ridge formation (3) and downstream effects (4). From Schäfler et al. (2018, BAMS)

# Introduction (2): Goals

Test the NAWDEX hypothesis in three steps

1. Seek evidence for **flow-dependent predictability** using MetOffice and ECMWF operational forecasts during the **NAWDEX period** (Sept-Oct 2016).
2. Quantify the **diabatic influence** on the **balanced flow** through the **advection of potential vorticity mechanism**, based on a Semi-Geostrophic (SGT) inversion model that provides the **ageostrophic flow response** to diabatic heating or dynamical sources
3. Test whether or not the **situations with lowest predictability** are **associated** with **strong diabatic influence**.

# Predictability barriers (1)

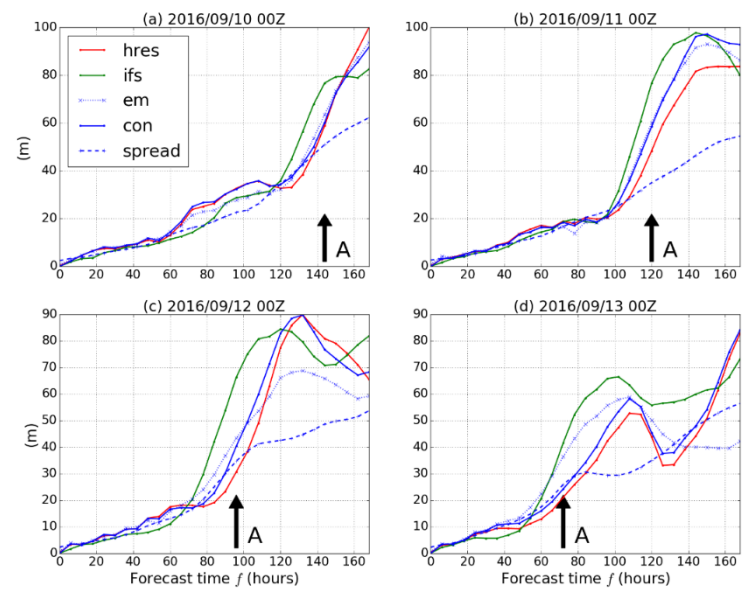
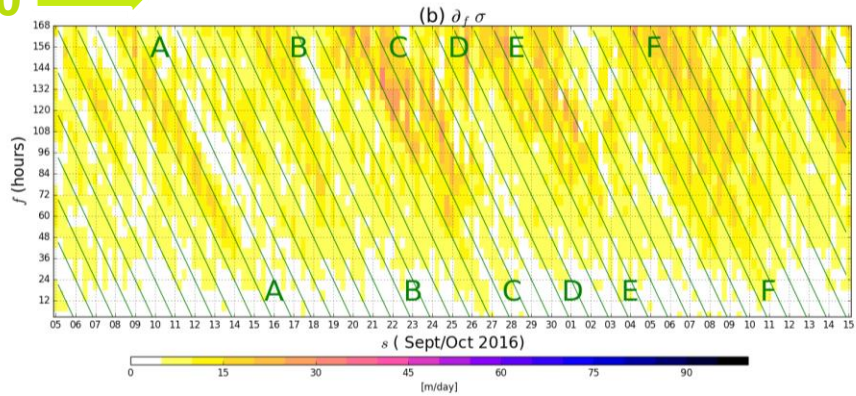


$T_+$

- $f$  Forecast lead time (hours since the start of the forecast)
- $s$  Forecast initialization time
- $t$  Validation time ( $s + f$  in forecasts)

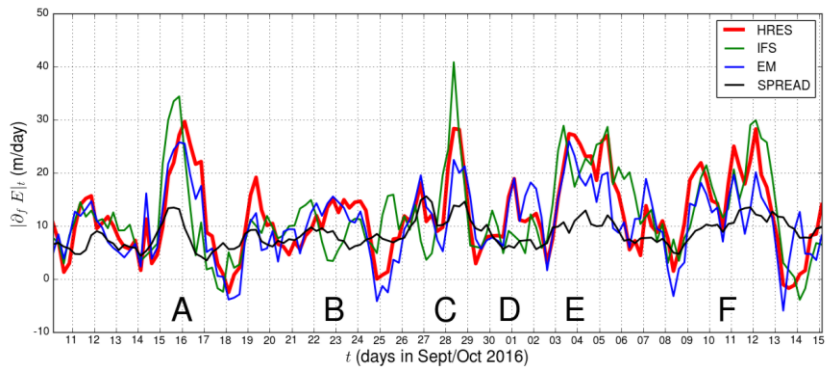
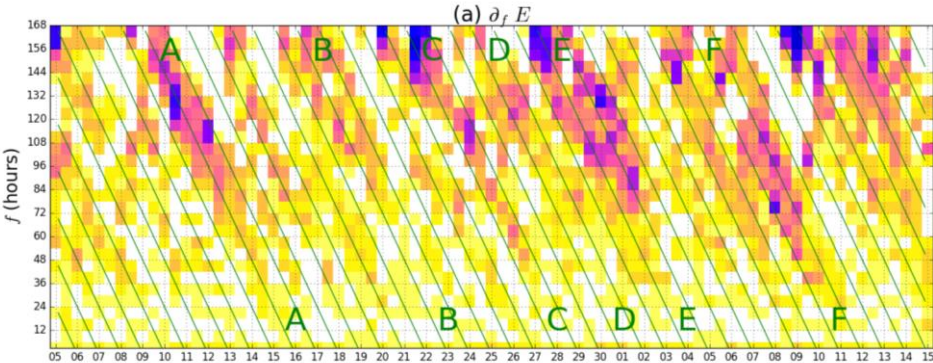
There are **times  $t$**  where error and spread grows rapidly (**UM, IFS**), **error grows faster than spread** (--); E.g. **A** (00Z 16<sup>th</sup>)

$T_0$



Z500 RMSE rate of change ( $\partial E / \partial f$ ): For all forecast start dates  $s$  and forecast lead times  $f$  over NAWDEX Period (15/9 to 15/10). **validation time  $t$**  on diagonal lines.

# Predictability barriers (2)



[Top]:  $\partial E / \partial f$  integrated across lead time for same validation time (diagonal lines)

Events with large increase of error growth at a similar validation time are defined as **predictability barriers (PB)**

- Similar for IFS and UM (HRES)
- Spread growth much smaller than EM error growth during PBs

	HRES	IFS	EM	SPREAD
HRES	.	0.725	0.849	0.488
IFS	.	.	0.608	0.567
EM	.	.	.	0.467

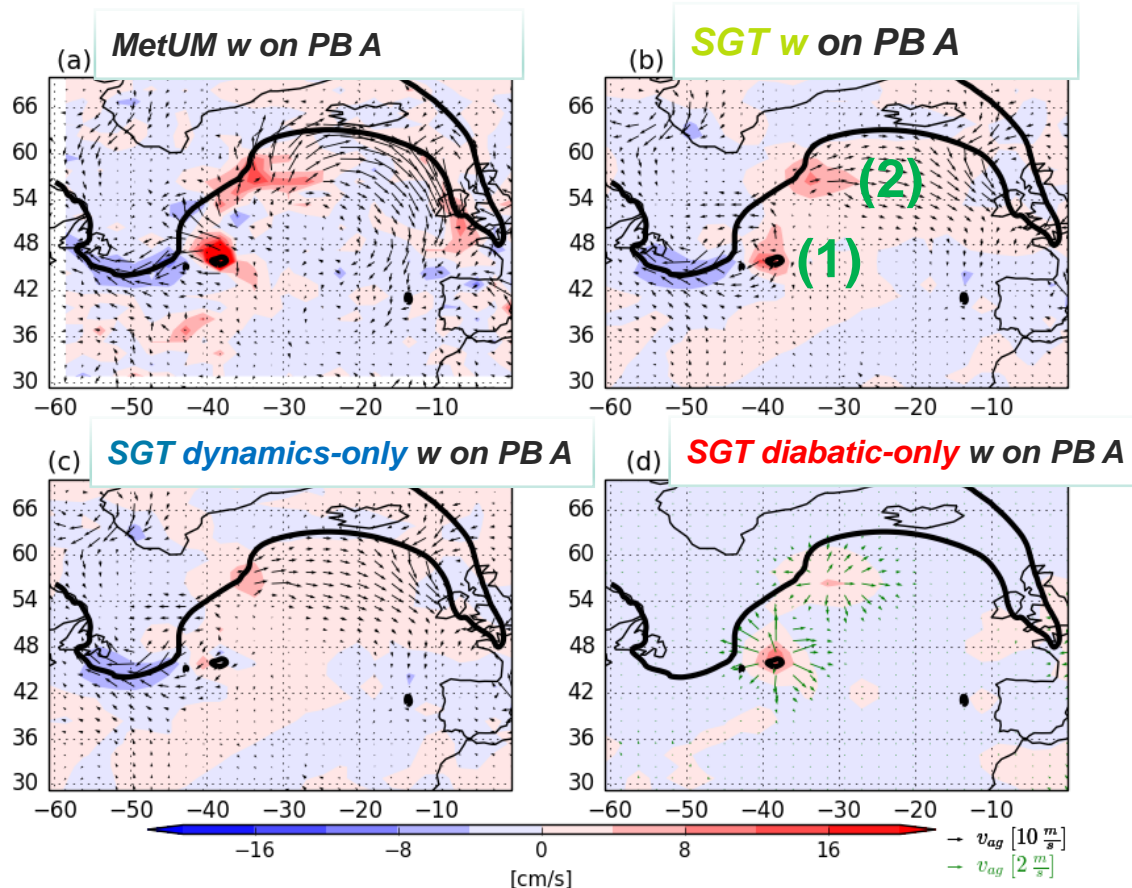
[Top]: Table with Pearson correlation coefficients from left side Figure, all significant at 99% level

PBs coincides with NAWDEX IOPs!

# Met Office Semi-Geostrophic inversion tool (SGT)

SGT model able to solve **pressure tendency, ageostrophic wind and balanced vertical wind ( $w$ )**. Source term is a linear combination of a **dynamics only** term and **diabatic sources**

- SGT  $w$  shows induced ascent on the upstream flank of a ridge for TC Ian (1) and downstream cyclone (2)
- Clear signal of diabatic process inducing vertical ascent and divergence over outflow region (d)



[Top]: SGT  $w$  (coloured),  $v_{ag}$  (vectors) and  $PV=2$  PVU (think black line)

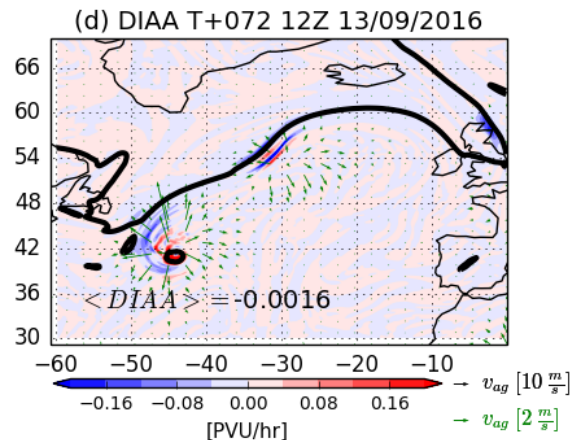
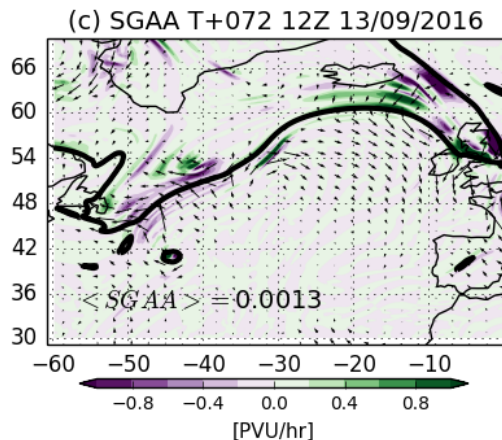
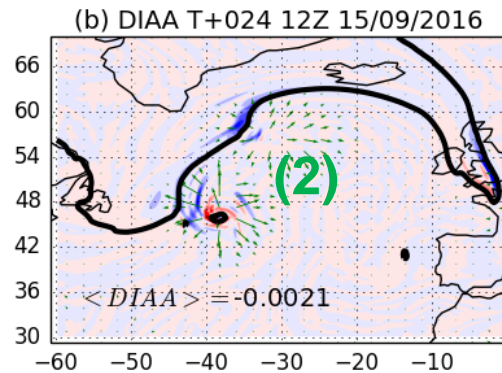
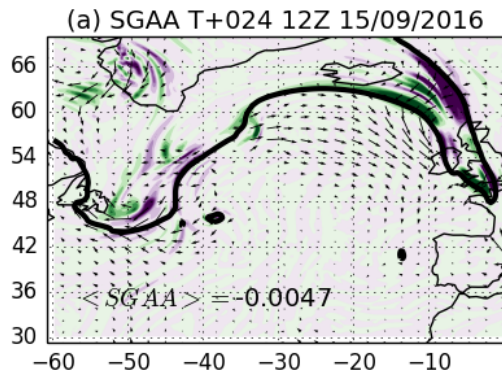
# Met Office Ageostrophic Advection of PV

**Diabatically influenced Ageostrophic Advection of PV (DIAA):** PV advected as a result of diabatically induced SG ageostrophic winds.

**Dynamic only (or geostrophic) induced ageostrophic advection of PV (SGAA)**

- Diabatically influenced (DIAA) shows clearer ridge building action for upstream cyclone (2) (b,d) than SGAA (a,c)
- Degradation of ridge building with forecast lead time (a,b to c,d), domain average value ↓

$$AAPV = -v_{ag} \cdot \nabla q$$

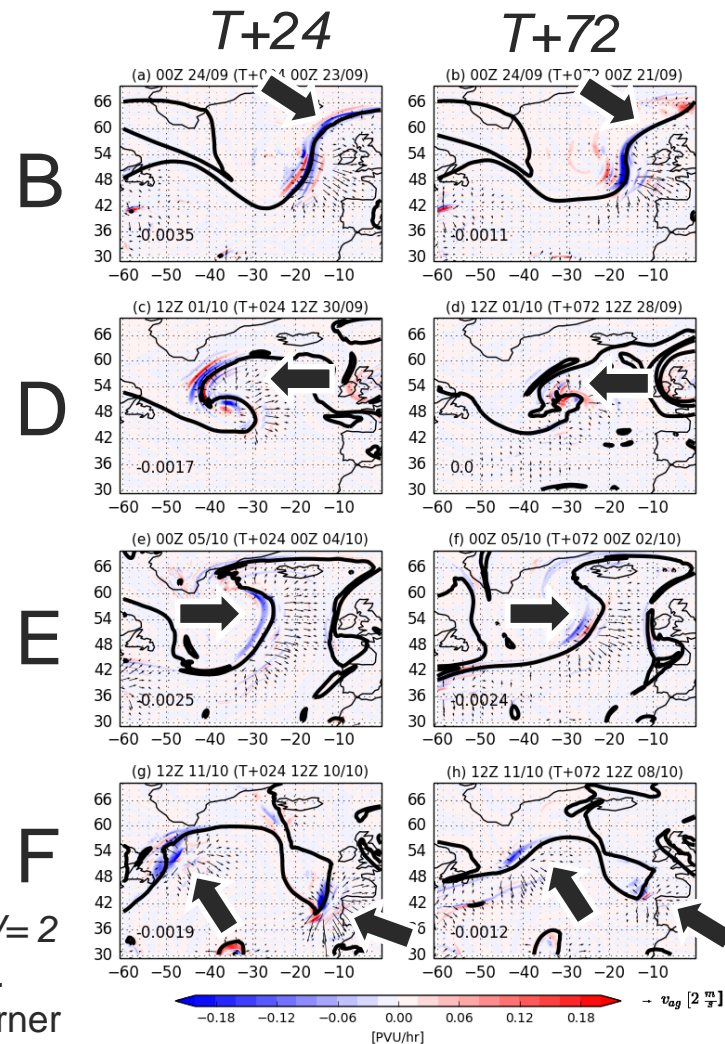


[Right]: AAPV (coloured)  $v_{ag}$  (vectors) and  $PV = 2 PVU$  (thick black line).

# Met Office DIAA in NAWDEX

Diabatic influence DIAA across different PB shows clear ridge building differences between  $T+24$  and  $T+72$

- **B**, Cyclone Vladiana
- **D**, Stalactite Cyclone
- **E**, Frontal cyclone
- **F**, Thor ridge and cut-off Sanchez

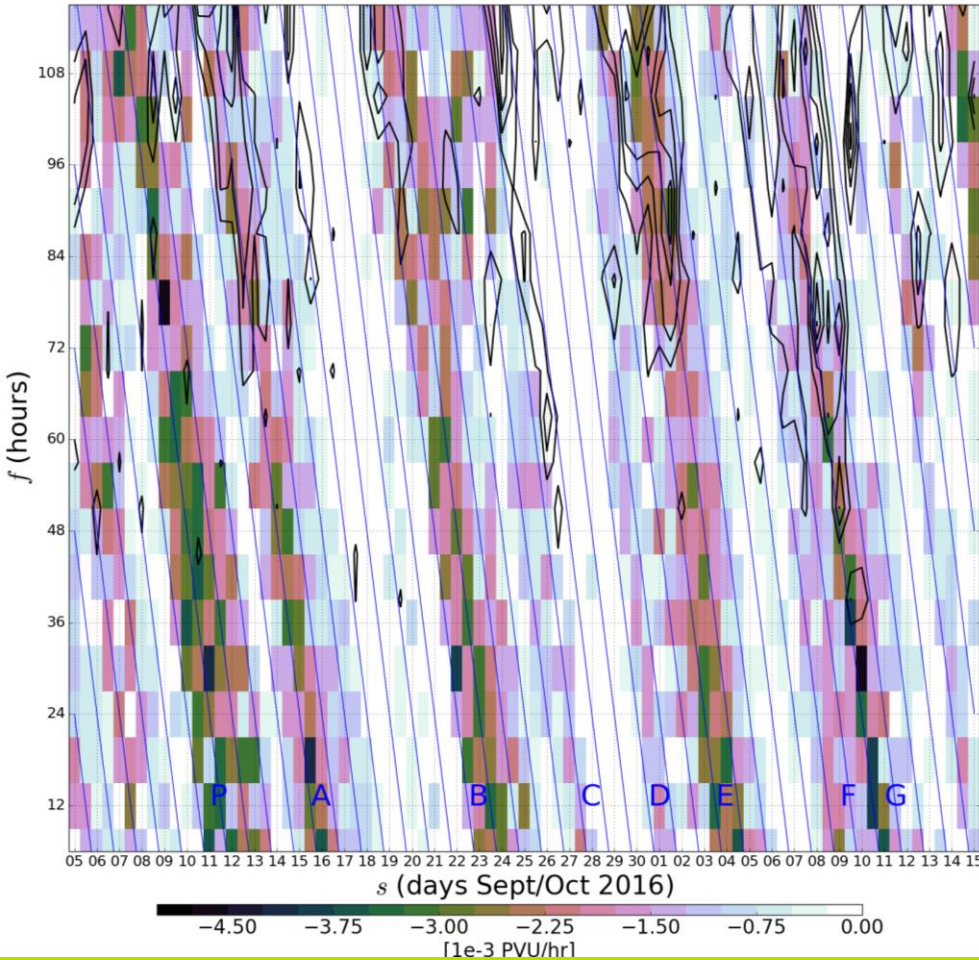


[Right]: DIAA (coloured),  $v_{ag}$  (vectors) and  $PV=2$  PVU (thick black line). T+24 (left) T+72 (right).

Mean value over box shown in bottom-left corner



# Diabatic influence and predictability barriers

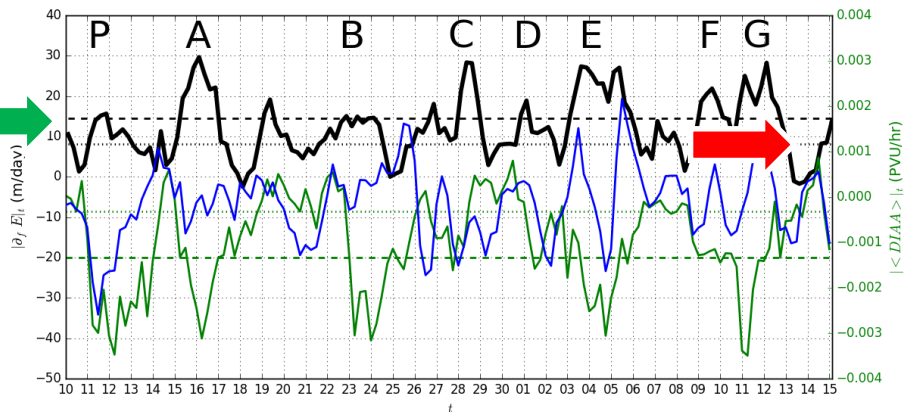


Most of PB cases coincide with high domain averaged Diabatic influence (DIAA); e.g. **A, C, E, G**

Some PB cases occur 2 days after high diabatic influence; e.g. **P-A, B-C, D-E, F-G** (“preconditioning environment”?)

[Left] Domain averaged *Diabatic influence (DIAA)* (coloured) and *error growth rate* (contoured)

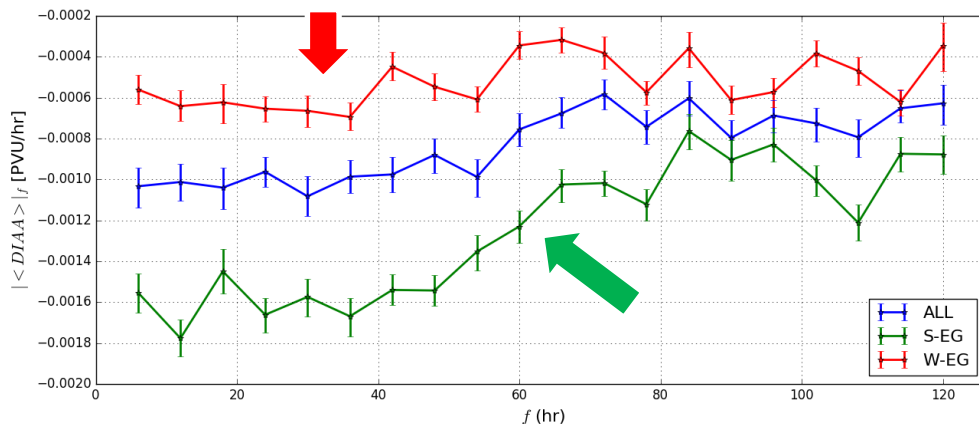
# Diabatic influence and predictability barriers (2)



[Left]: Time series of **PB**, **DIAA**, and **SGAA** integrated across  $t$

Time series A	series B	correlation	P-coefficient
$ \partial_f E _t$	$ \langle \text{DIAA} \rangle _t$	-0.395	< 0.01
$ \partial_f E _t$	$ \langle \text{SGAA} \rangle _t$	0.028	0.74
$ \langle \text{DIAA} \rangle _t$	$ \langle \text{SGAA} \rangle _t$	0.121	0.15

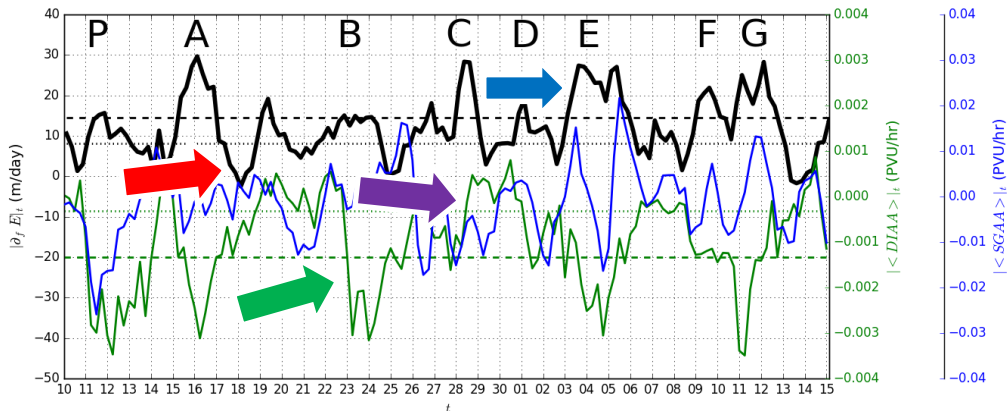
[Down]: DIAA vs  $f$  for upper (lower) and all PB events (Defined as upper lower tercile of *error growth*)



Error growth rate (*PB*) and diabatic influence (*DIAA*) correlation significant, unlike SG influenced (*SGAA*)

*DIAA* stronger for high strong *error growth* (upper tercile of error growth timeserie), substantial drop when  $f > 60$  hours

# SG and predictability barriers (3)

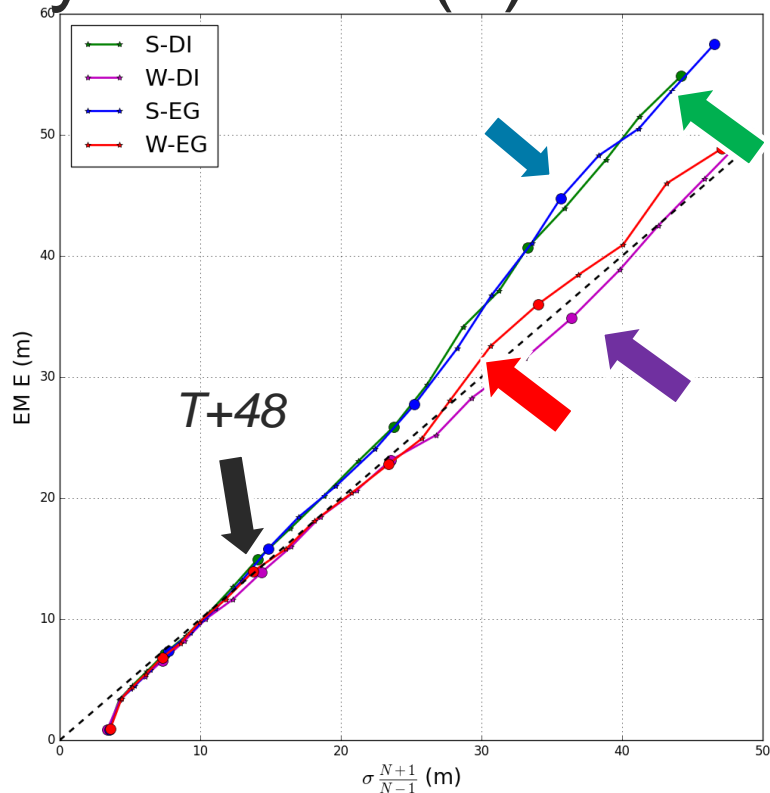


[Top]: Time series of PB, DIAA, and SGAA

Comparing EM error and spread for strong/weak (upper/lower terciles of timeseries) error growth (EG) and diabatic influence (DI):

Spread matches error when diabatic influence is weak.

Error grows 4/3 faster than spread after day 2 when DIAA is strong.



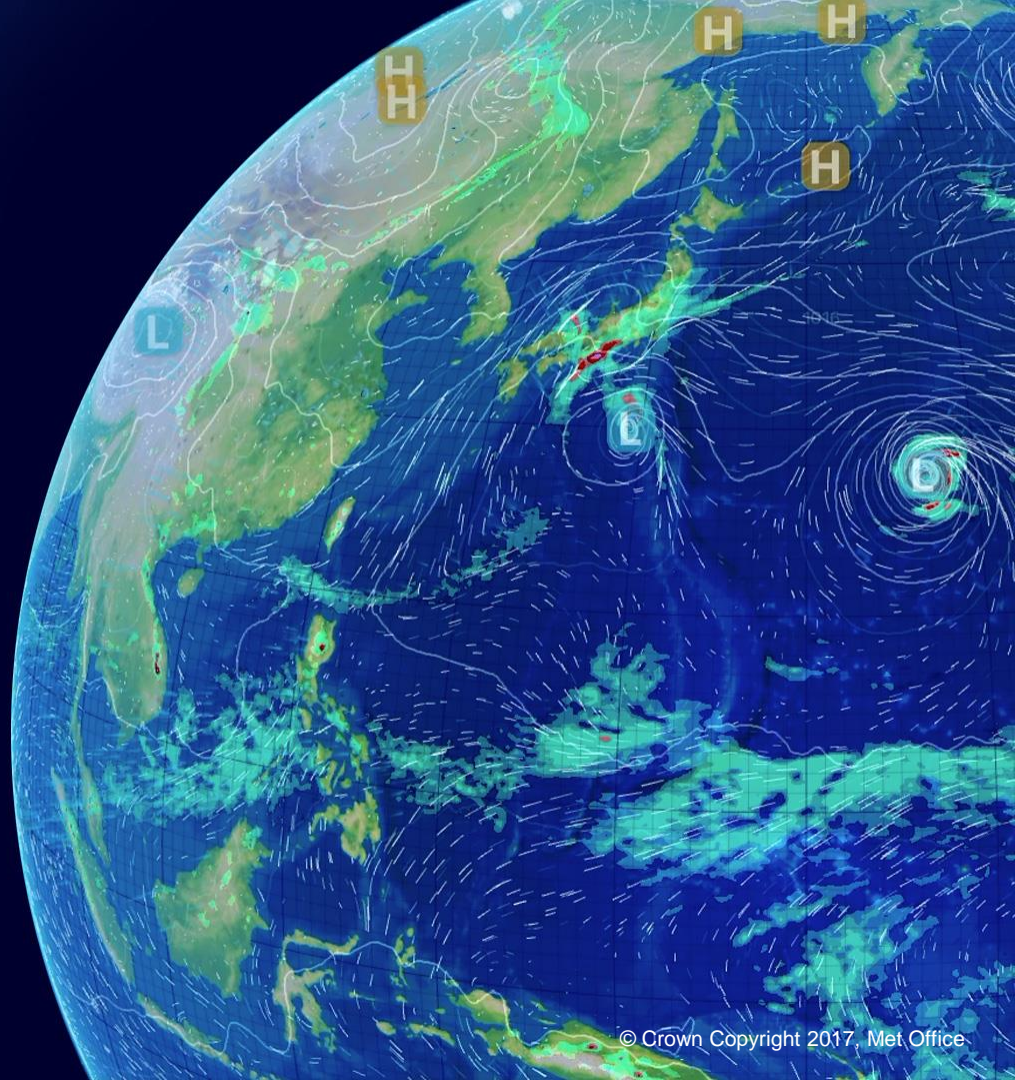
[Top]: MetUM EM RMSE ( $E$ ) vs spread ( $\sigma$ ), for Strong (Weak) Diabatic influence of error growth.

- **Rapid error** and **ensemble spread growth** was identified on particular dates, irrespective of lead times. Defined as **Predictability Barriers (PB)**
- The **Diabatically Induced Ageostrophic Advection of PV (DIAA)** from SGT model is **strong and negative** in the **western flank of developing ridges** -> **ridge expansion**
- Only **DIAA** is **correlated with error growth rate**, dynamics-only SGAA is not
- **During strong error growth events (PB)** :
  - DIAA is **~1.5x larger than average**
  - DIAA **halves beyond T+60**
  - **Error growth rate exceeds spread rate beyond T+48**

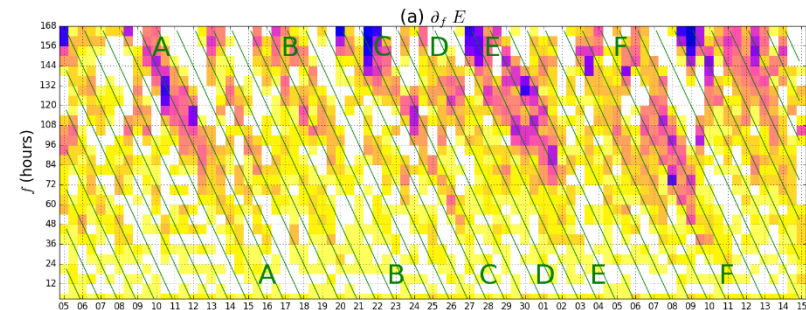
## *Unresolved questions:*

- What are the diabatic processes behind DIAA decrease on PB events?
- Are those processes misrepresented in the model? Are uncertainties in these processes not captured by the ensemble system?

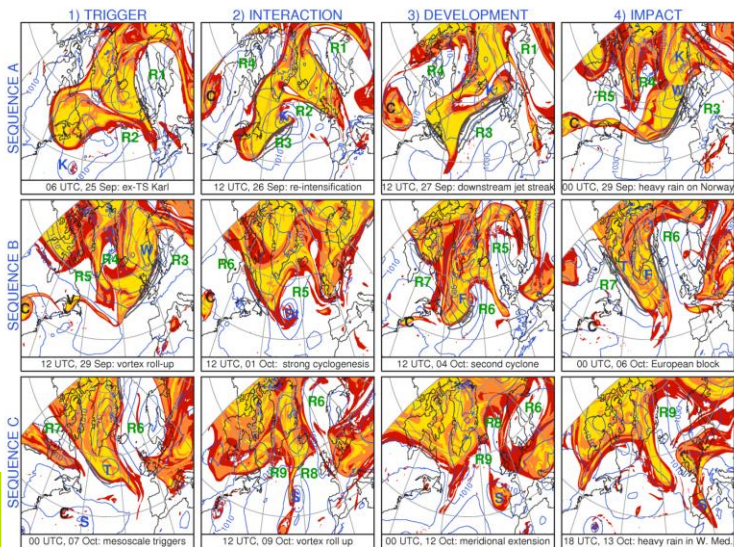
*Thanks for your  
attention!*



# Predictability barriers & NAWDEX



- (A): 16<sup>th</sup>-18<sup>th</sup> Sept. *Ex-TC Ian*. IOP 1
- (B): 22<sup>nd</sup>-23<sup>th</sup> Sept. *Vladiana* IOP 4
- (C): 28-29<sup>th</sup> Sept. *Walpurga + Ex-TC Karl*. IOP 5  
**SEQUENCE A**
- (D): 1<sup>st</sup>-2<sup>nd</sup> Oct. *Stalactite cyclone*. IOP 6
- (E): 4<sup>th</sup>-6<sup>th</sup> Oct. Downstream effects of *Stalactite cyclone* + blocking development. IOP 7  
**SEQUENCE B**
- (F): 11-13<sup>th</sup> Oct. PV cut off *Sanchez* + tropopause ridge *Thor*. IOP 9-10  
**SEQUENCE C**



[Left] NAWDEX golden cases (*aka Sequences*)  
*Fig 6. Schaffler et al. 2018*

# Final conclusions and Future work

As hypothesized in NAWDEX campaign: **Diabatic processes** induce **divergent outflow in ridges** (2<sup>nd</sup> stage of error growth of Baumgart et al. 2019), affecting the **downstream development of Rossby waves**, and thus leading to **large forecast error growth** (Predictability barriers)

*To do ...*

- What processes are responsible for high values of DIAA over western flank of ridges (e.g. *Joos and Wernli 2012*)?
- Why DIAA declines after day 2?
- Are similar conclusions found in other areas or seasons (e.g. US west-coast)

# Met Office SGT Inversion Model

$$\mathbf{BQ}' \begin{pmatrix} u - u_e \\ v - v_e \\ w \end{pmatrix} + c_{pd}\theta_v \frac{\partial}{\partial t} \begin{pmatrix} \frac{1}{r \cos \phi} \left( \frac{\partial \pi}{\partial \lambda} - \frac{\partial \pi}{\partial r} \frac{\partial r}{\partial \lambda} \right) \\ \frac{1}{r} \left( \frac{\partial \pi}{\partial \phi} - \frac{\partial \pi}{\partial r} \frac{\partial r}{\partial \phi} \right) \\ \frac{\partial \pi}{\partial r} \end{pmatrix} = \mathbf{BH}'$$

$$\mathbf{H}' = \begin{pmatrix} -(\mathbf{u}_e \theta_v) \cdot \nabla \left( \frac{v_e}{\theta_v} \right) + S_v - \frac{v_e S_{\theta_v}}{\theta_v} \\ (\mathbf{u}_e \theta_v) \cdot \nabla \left( \frac{u_e}{\theta_v} \right) - S_u + \frac{u_e S_{\theta_v}}{\theta_v} \\ -\mathbf{u}_e \cdot \nabla \theta_v + S_{\theta_v} \end{pmatrix}$$

**SGT model able to solve pressure tendency ( $d\pi/dt$ ), ageostrophic wind ( $v - v_e$ ) and balanced vertical wind ( $w$ ).**

**Source Matrix  $H'$ : linear comb. of geostrophic term plus friction and diabatic sources**

**SGT improves** the Quasi-Geostrophic (QG) model:

- SGT model includes advection by the ageostrophic velocity
- The Ertel PV is conserved by SGT to the order of accuracy of the SGT model in adiabatic and frictionless conditions

**SGT ~ SG** at the tropopause level, as we do not include source friction in the SGT model and we are above BL



# Met Office Semi-Geostrophic (SGT) Inversion Model

**UM eqs:**

$$\frac{D\mathbf{u}}{Dt} + c_{pd}\theta_v \nabla \pi + 2\Omega \times \mathbf{u} = \mathbf{g} + \frac{\partial}{\partial r} \left( K_m \frac{\partial \mathbf{u}_h}{\partial r} \right) + S_{\mathbf{u}},$$

$$\frac{D\theta_{vd}}{Dt} = S_{\theta_{vd}},$$

**+  
Balance  
eq:**

$$c_{pd}\theta_v \nabla_h \pi - (fv_e, -fu_e) = \frac{\partial}{\partial r} \left( K_m \frac{\partial \mathbf{u}_e}{\partial r} \right) \longrightarrow$$

$$c_{pd}\theta_v \frac{\partial \pi}{\partial r} = -g.$$

**BQ'**

$$\begin{pmatrix} u - u_e \\ v - v_e \\ w \end{pmatrix} + c_{pd}\theta_v \frac{\partial}{\partial t} \begin{pmatrix} \frac{1}{r \cos \phi} \left( \frac{\partial \pi}{\partial \lambda} - \frac{\partial \pi}{\partial r} \frac{\partial r}{\partial \lambda} \right) \\ \frac{1}{r} \left( \frac{\partial \pi}{\partial \phi} - \frac{\partial \pi}{\partial r} \frac{\partial r}{\partial \phi} \right) \\ \frac{\partial \pi}{\partial r} \end{pmatrix} = \mathbf{B}\mathbf{H}'$$

**SGT model able to solve pressure tendency ( $d\pi/dt$ ), ageostrophic wind ( $v - v_e$ ) and balanced vertical wind ( $w$ ).**

**$\Pi$ : Exner pressure**

**$K_m$ : BL diffusion coef.**

**$S$ : Source terms**

**$v_e$ : Geostrophic wind**

$$\mathbf{H}' = \begin{pmatrix} -(\mathbf{u}_e \theta_v) \cdot \nabla \left( \frac{v_e}{\theta_v} \right) + S_v - \frac{v_e S_{\theta_v}}{\theta_v} \\ (\mathbf{u}_e \theta_v) \cdot \nabla \left( \frac{u_e}{\theta_v} \right) - S_u + \frac{u_e S_{\theta_v}}{\theta_v} \\ -\mathbf{u}_e \cdot \nabla \theta_v + S_{\theta_v} \end{pmatrix}$$


**Source Matrix  $H'$ : linear comb. of geostrophic term plus friction and diabatic sources**

# Semi-Geostrophic Inversion Model

$$\mathbf{BQ}' \begin{pmatrix} u - u_e \\ v - v_e \\ w \end{pmatrix} + c_{pd}\theta_v \frac{\partial}{\partial t} \begin{pmatrix} \frac{1}{r \cos \phi} \left( \frac{\partial \pi}{\partial \lambda} - \frac{\partial \pi}{\partial r} \frac{\partial r}{\partial \lambda} \right) \\ \frac{1}{r} \left( \frac{\partial \pi}{\partial \phi} - \frac{\partial \pi}{\partial r} \frac{\partial r}{\partial \phi} \right) \\ \frac{\partial \pi}{\partial r} \end{pmatrix} = \mathbf{BH}' \quad \text{Where}$$

$$\mathbf{B} = \begin{pmatrix} f & -\frac{\partial}{\partial r} \left( K_m \frac{\partial}{\partial r} \right) & 0 \\ \frac{\partial}{\partial r} \left( K_m \frac{\partial}{\partial r} \right) & f & 0 \\ 0 & 0 & g/\theta_v \end{pmatrix}$$

$$\mathbf{Q}' = \begin{pmatrix} f + \frac{\theta_v}{r \cos \phi} \frac{\partial}{\partial \lambda} \left( \frac{v_e}{\theta_v} \right) + \frac{u_e \tan \phi}{r} & \frac{\theta_v}{r} \frac{\partial}{\partial \phi} \left( \frac{v_e}{\theta_v} \right) + \frac{\partial}{\partial r} \left( K_m \frac{\partial}{\partial r} \right) & \theta_v \frac{\partial}{\partial r} \left( \frac{v_e}{\theta_v} \right) \\ -\frac{\theta_v}{r \cos \phi} \frac{\partial}{\partial \lambda} \left( \frac{u_e}{\theta_v} \right) + \frac{v_e \tan \phi}{r} - \frac{\partial}{\partial r} \left( K_m \frac{\partial}{\partial r} \right) & f - \frac{\theta_v}{r} \frac{\partial}{\partial \phi} \left( \frac{u_e}{\theta_v} \right) & -\theta_v \frac{\partial}{\partial r} \left( \frac{u_e}{\theta_v} \right) \\ \frac{1}{r \cos \phi} \frac{\partial \theta_v}{\partial \lambda} & \frac{1}{r} \frac{\partial \theta_v}{\partial \phi} & \frac{\partial \theta_v}{\partial r} \end{pmatrix}$$

Elliptic equation for  $\frac{\partial \pi}{\partial t}$  

$$\frac{\kappa_d - 1}{\kappa_d} \frac{\rho_d}{\pi} r^2 \frac{\partial r}{\partial \eta} \frac{\partial \pi}{\partial t} + r^2 \frac{\partial r}{\partial \eta} \frac{\rho_d c_{pd} \theta_v^2}{g \theta_{vd}} \frac{\partial}{\partial t} \left( \frac{1}{(1+\mu)} \frac{\partial \pi}{\partial r} \right) + \nabla \cdot \left( r^2 \rho_d c_{pd} \theta_v \frac{\partial r}{\partial \eta} \mathbf{R} \mathbf{P}^{-1} \frac{\partial}{\partial t} (\nabla_r \pi) \right) = \nabla \cdot \left( r^2 \rho_d \frac{\partial r}{\partial \eta} \mathbf{R} \mathbf{P}^{-1} \mathbf{G} \right) + \frac{1}{\cos \phi} \left( \frac{\partial}{\partial \lambda} \left( r \rho_d u_e \frac{\partial r}{\partial \eta} \right) + \frac{\partial}{\partial \phi} \left( r \rho_d v_e \cos \phi \frac{\partial r}{\partial \eta} \right) \right).$$

## [Improvements to S-G omega equation ...]

Its form in momentum coordinates (Hoskins & Draghici, 1977) is:

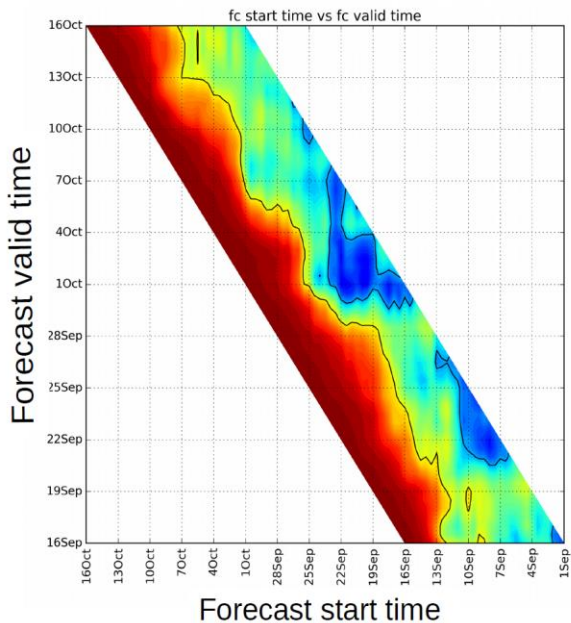
$$\nabla_X^2 \left( \frac{g \rho_r}{\theta_0 f_0} q_g w^* \right) + f_0^2 \frac{\partial^2 w^*}{\partial Z^2} = \boxed{2 \nabla_X \cdot \mathbf{Q}} + \boxed{\nabla_X^2 H} \quad H = \alpha w^* , \quad \hat{Z} = \frac{N_0}{f_0} Z$$

Geostrophic forcing

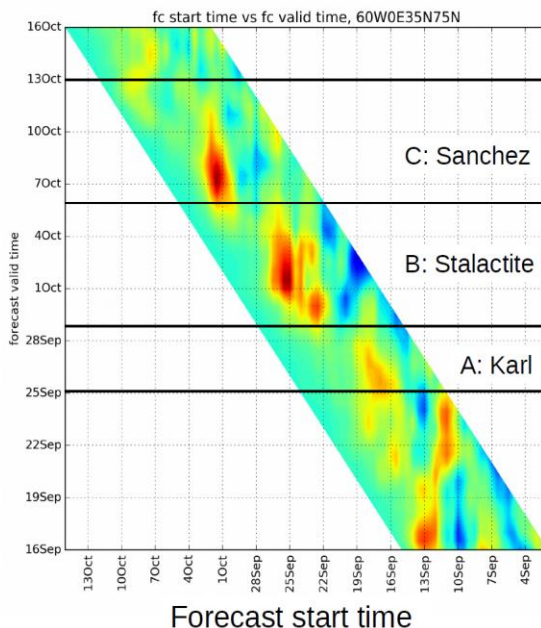
Diabatic forcing (H=heating)

# Predictability barriers

ACC as function of start and valid time



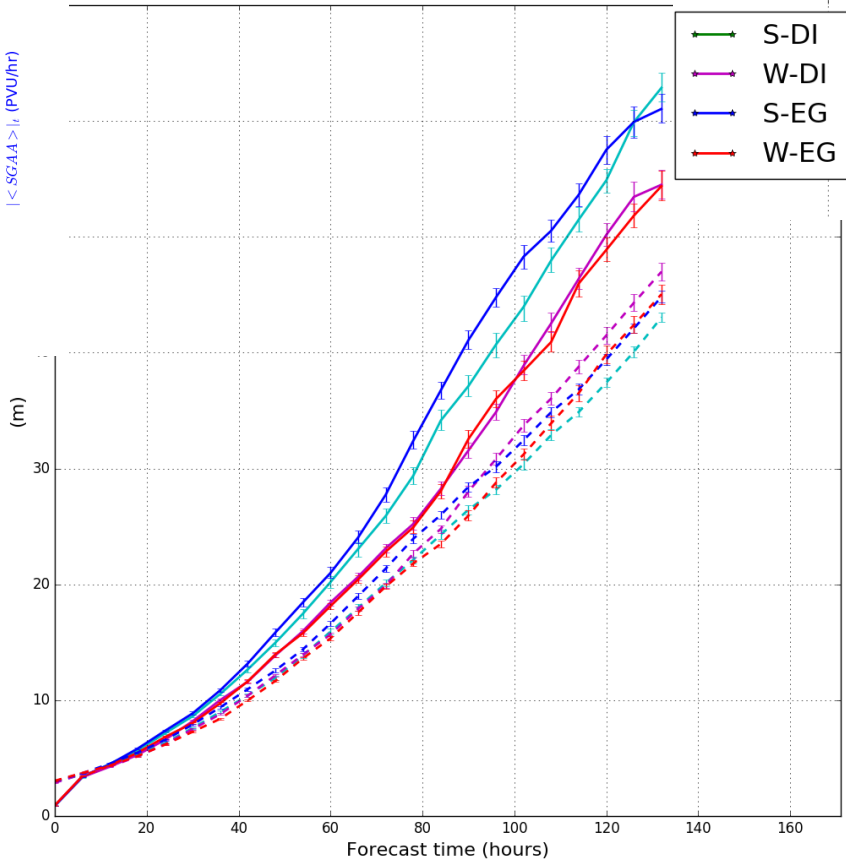
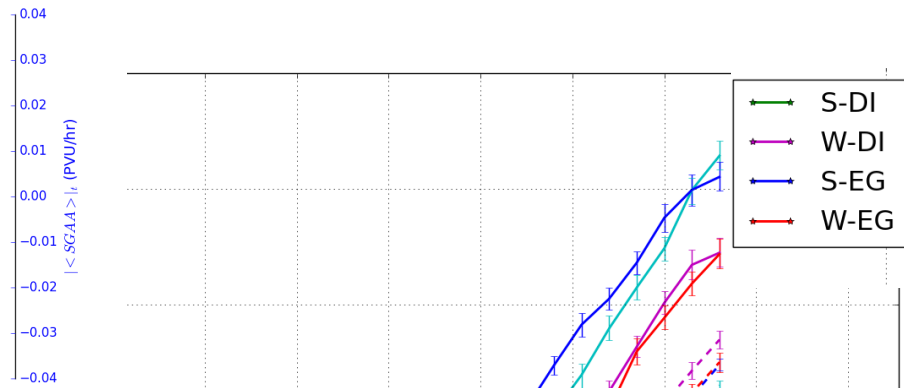
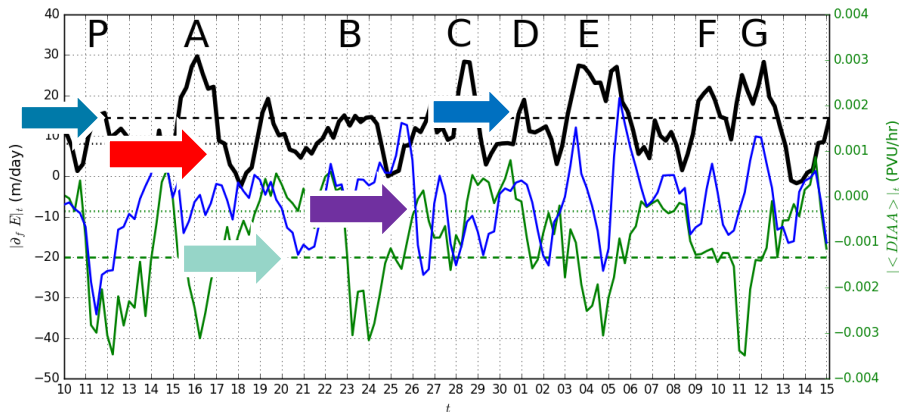
Rate of change of ACC



Rate of change of *ACC* for *IFS Z500* increases at particular validation times, defined as “predictability barriers”

Craig et al. (2018): Predictability barriers, NAWDEX 2018 workshop, Munich

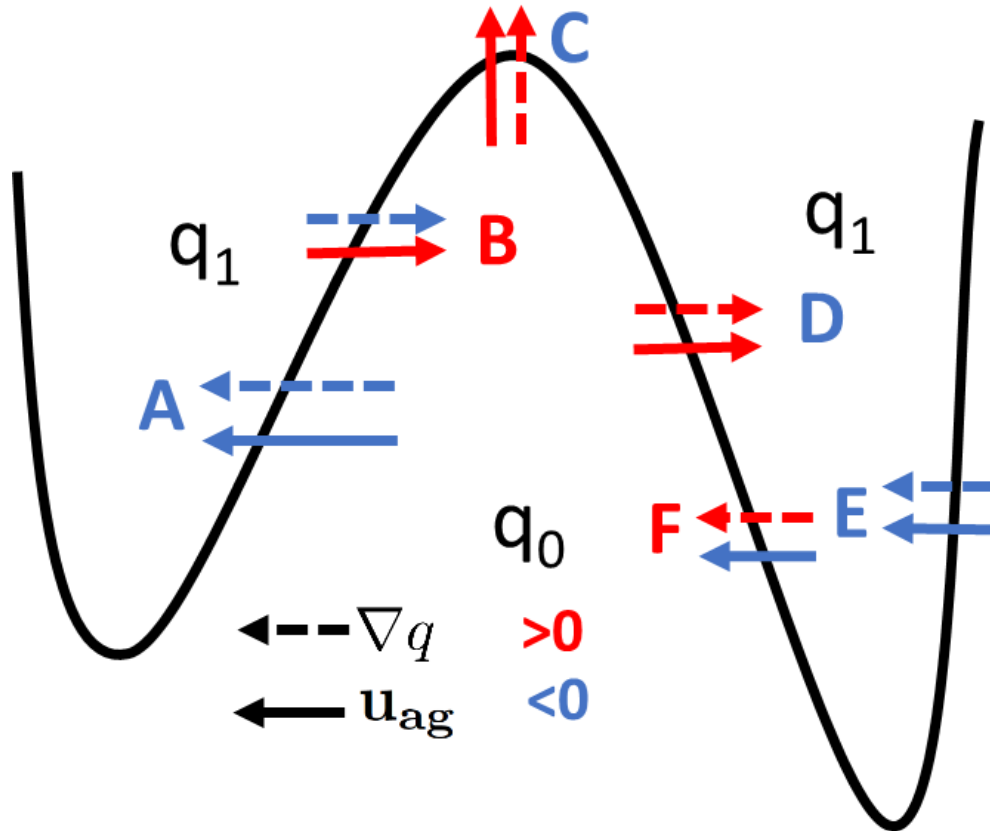
# SG and predictability barriers (+)



[Left]: Time series of PB, DIAA, and SGAA

[Left]: N768 EM RMSE ( $E,-$ ) and spread ( $\sigma,-$ ), for High (Non) Non-Diabatic Influence or PB. Def as upper (lower) threshold in PB and DI-AAPV timeseries

# DIAA sketch



$$AAPV = -v_{ag} \cdot \nabla q$$

A,C,D,E: SG wind parallel to PV gradient (troposphere advecting towards stratosphere): **DIAA negative**

B,F: SG wind antiparallel to PV gradient, **DIAA positive**

# Thoughts on Predictability Barriers

For a reliable forecast **spread should match EM error** for all lead times averaged over many forecast dates. Reasons why **forecast error growth** may be **larger than ensemble spread during PB events**:

1. **Stochastic physics** and ensemble design of **initial condition uncertainty** do **not capture well** major **sources of model error** that makes the rapid error growth during PB events
2. Very **low predictability** of PB events, flow may follow a very unlikely path

# Methodology

Operational Models employed to spot Error growth:

- Met Office Unified Model ([MetUM, H-Res](#)) operational deterministic model ([N768 ~18km, L70, GA6.1](#))
- Integrated Forecast System ([IFS](#)) operational deterministic model ([O1280 ~9 km, L137, Cy41r2](#))
- Global MetUM operational Ensemble Prediction System ([MOGREPS-G, N400, ~35km, L70, GA6.1, 24 members](#))

[H-Res](#) re-run with the [necessary diagnostics](#) to run the [Semi-Geotriptic](#) inversion model [6 hourly](#) up to T+120