

# A review of the evolution of setting observation errors in satellite DA

Niels Bormann

with material from many people

# Errors in observations

- Every observation has an error vs the truth:

- Systematic error

- Needs to be removed through bias correction (see Dick Dee's talk)

- Random error

- Mostly assumed Gaussian in DA.
    - Denoted by the observation error covariance matrix “**R**” in the observation cost function:

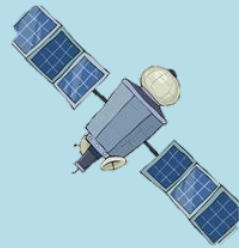
$$J(\mathbf{x}) = \frac{1}{2} (\mathbf{x} - \mathbf{x}_b)^T \mathbf{B}^{-1} (\mathbf{x} - \mathbf{x}_b) + \frac{1}{2} (\mathbf{y} - \mathbf{H}[\mathbf{x}])^T \mathbf{R}^{-1} (\mathbf{y} - \mathbf{H}[\mathbf{x}])$$

- Often specified through the square root of the diagonals (“ $\sigma_o$ ”) and a correlation matrix (which can be the identity matrix).

# Contributions to observation error

## Measurement error

E.g., instrument noise for satellite radiances

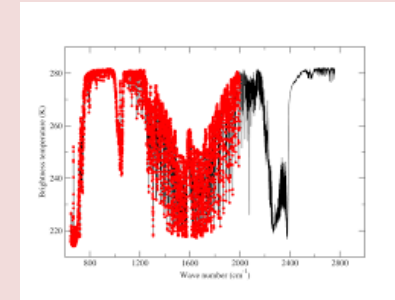


## Representation error

(e.g., Janjić et al 2017)

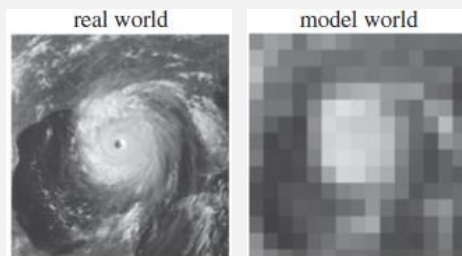
## Forward model (observation operator) error

E.g., radiative transfer error



## Representativeness error

E.g., point measurement vs model representation



## Quality control/pre-processing error

E.g., error due to the cloud detection scheme missing some clouds in clear-sky radiance assimilation



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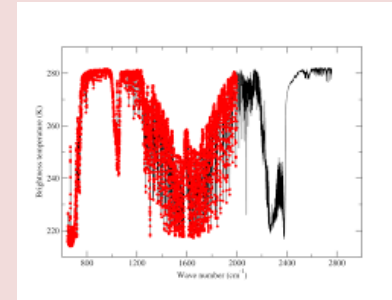


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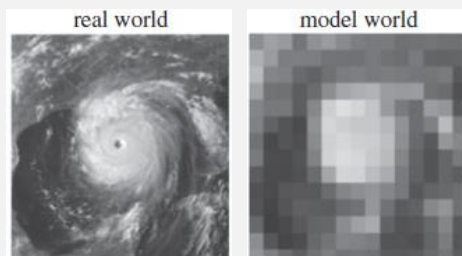


Observation errors can be:

- situation-dependent
- correlated between observations (spatially, temporally, between channels)

## Representativeness error

E.g., point measurement vs model representation



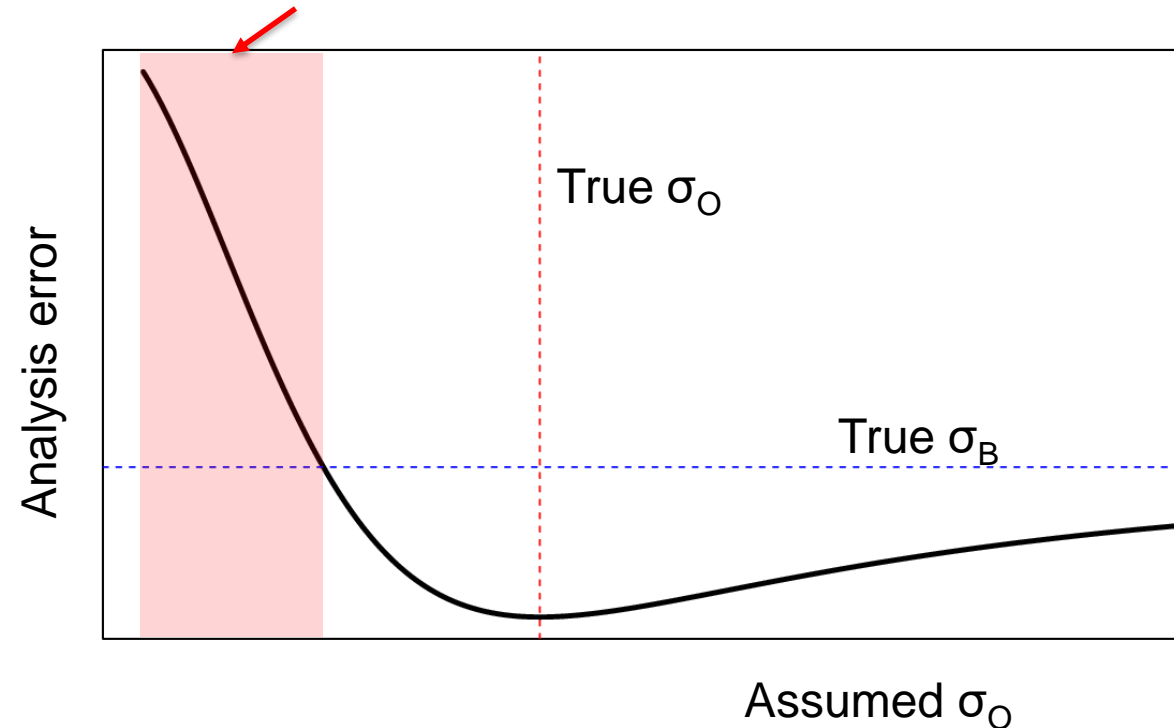
## Quality control/pre-processing error

E.g., error due to the cloud detection scheme missing some clouds in clear-sky radiance assimilation



# Observation error specification 20 years ago

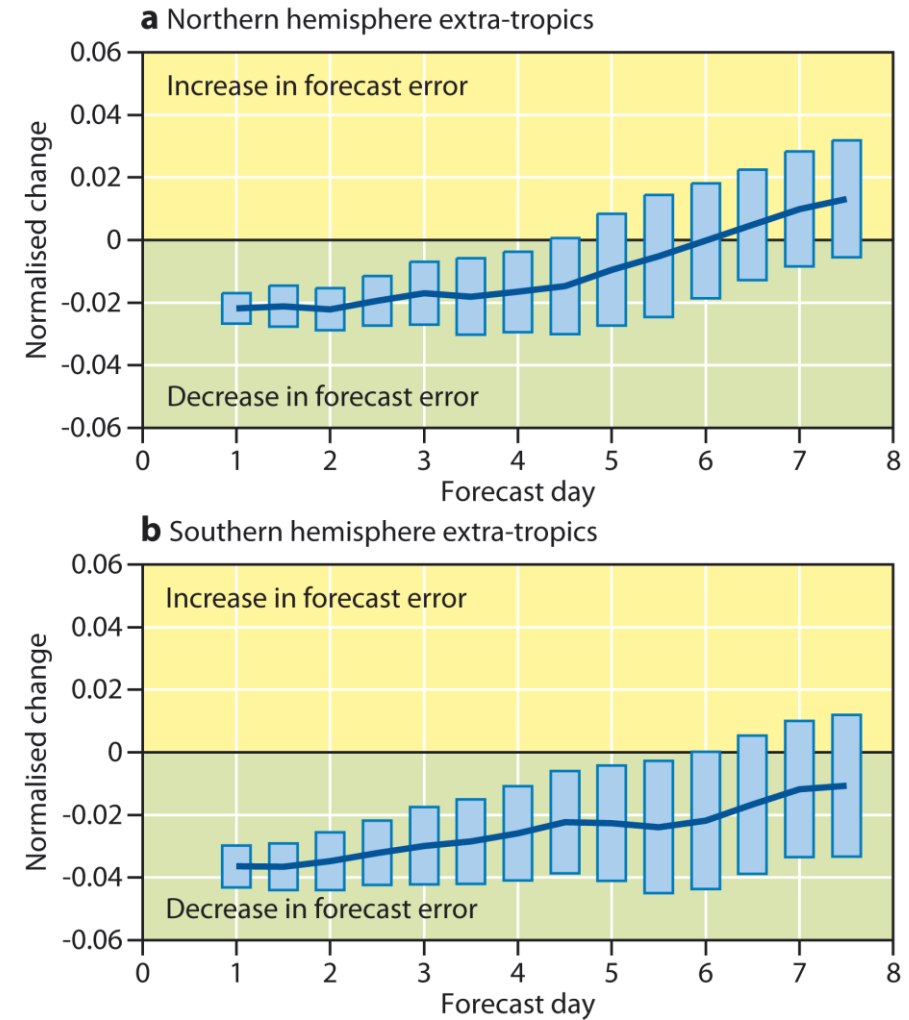
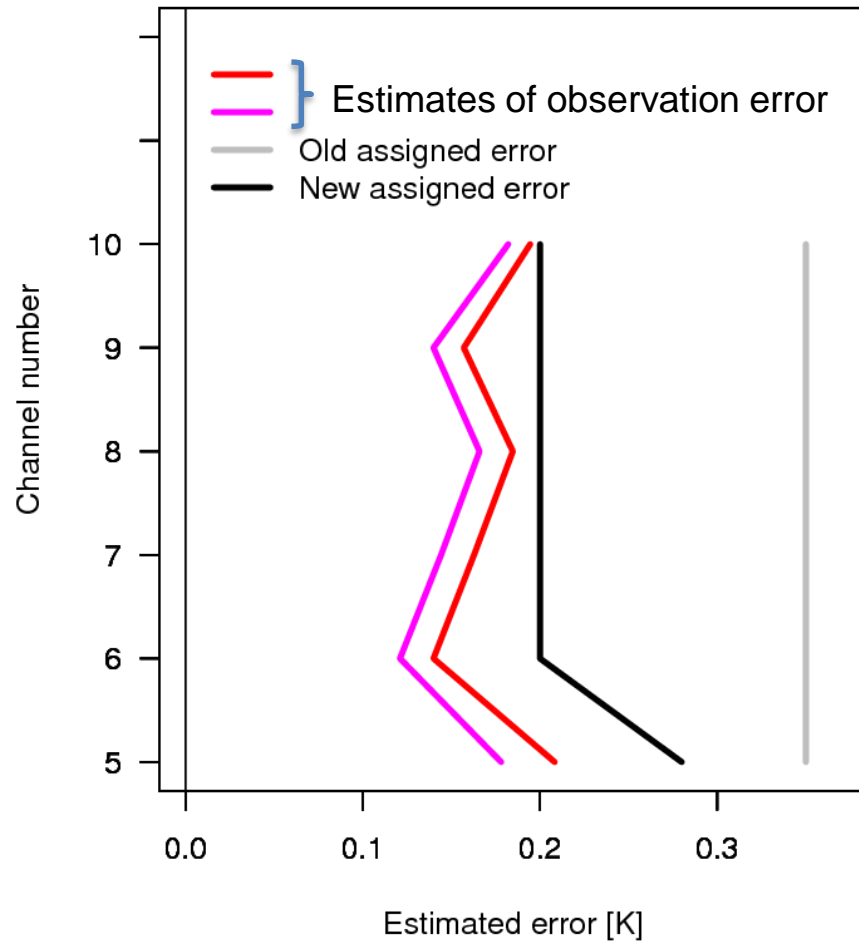
- **R diagonal**, one constant number per channel/level
- **Thin data**, to avoid spatial error correlations
- **Prevailing wisdom: Make  $\sigma_o$  large**
  - To counter-act remaining error correlations
  - To stay away from the **danger zone**



# Assigning observation errors matters

AMSU-A observation error revision at ECMWF, 37r2, 2011

Impact on Z500 RMSE



# Increased sophistication of observation error assignment

- **Current observation error setting** at ECMWF reflect **two main strands** of recent development in observation error modelling:

## Situation-dependent observation errors:

- **AMSU-A**: dependent on satellite, channel, cloudiness, surface emissivity error
- **All-sky error model for MW imagers, MW humidity sounders**: dependent on channel and cloud amount
- **AMVs**: dependent on level and wind shear (and satellite, channel, height assignment method)
- **Aeolus**: based on physically estimated error for each derived wind

## Observation errors with inter-channel error correlations taken into account (globally constant):

- **IASI, CrIS**
- **ATMS**
- WV channels from **geostationary imagers**

# Outline

1. Introduction
2. Situation-dependent observation errors
3. Correlated observation errors
4. Error inventories and closure studies
5. Summary



# Outline

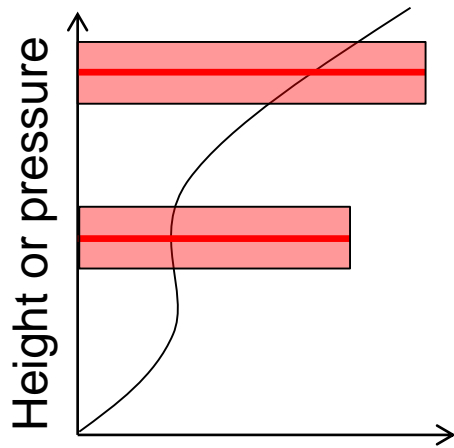
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## Situation-dependence of observation errors

- Observation errors can be situation-dependent, particularly the contributions from representation error.
- To account for this, observation errors are modelled as a function of situation-dependent parameters.

# Situation-dependence of observation errors: Example: height-assignment error in AMVs

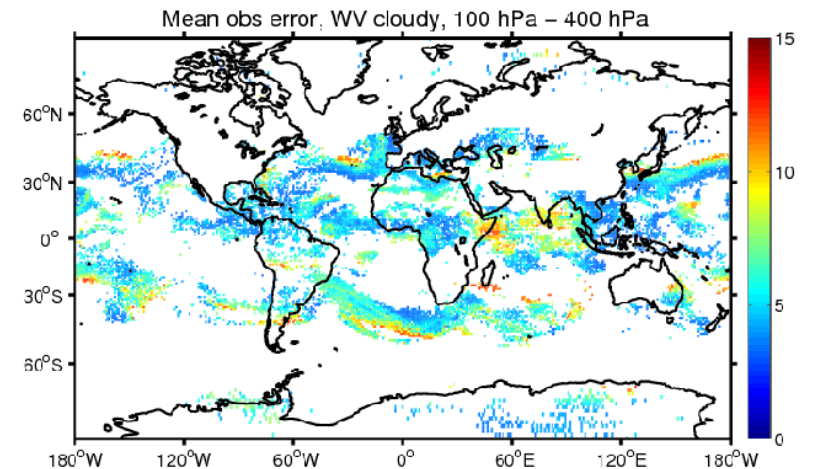
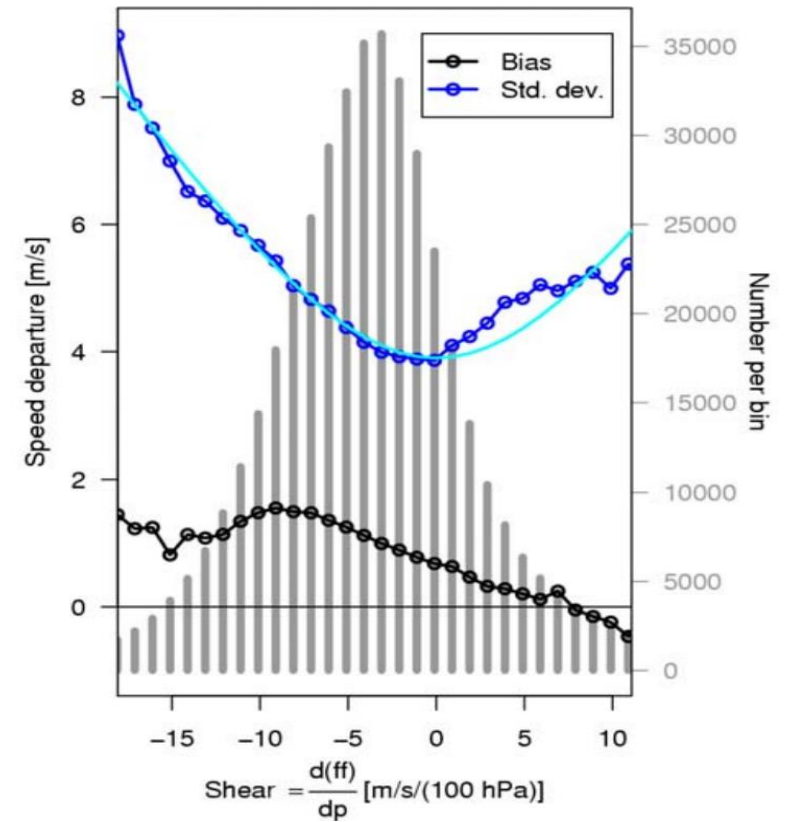
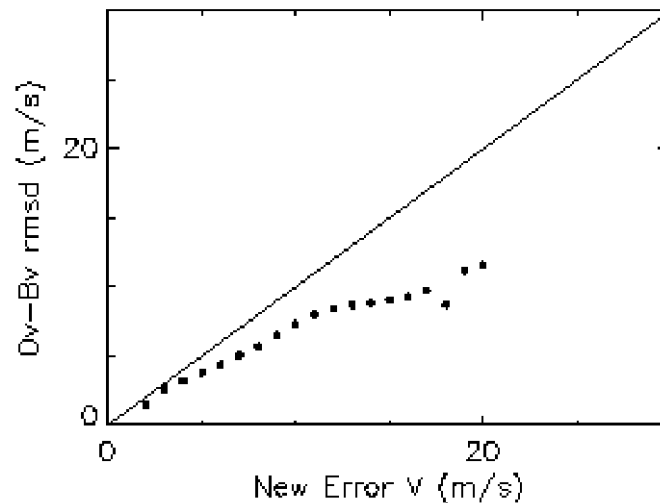
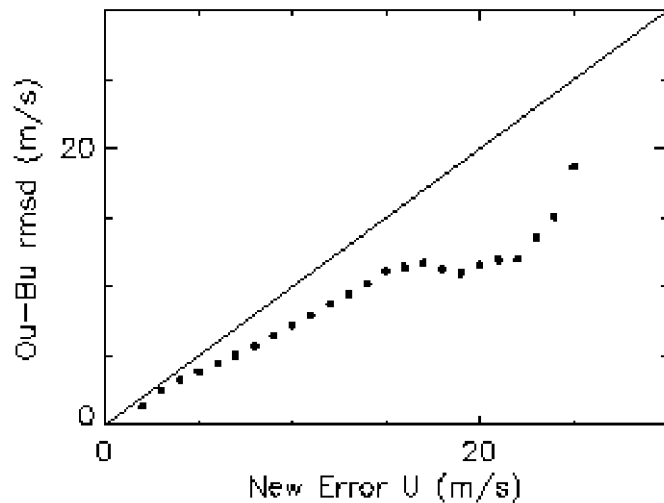
(e.g., Forsythe and Saunders 2008; Bormann et al 2008; Salonen and Bormann 2012)



Large **shear** – larger error due to **height assignment error**

Low **shear** – smaller error due to **height assignment error**

$$(\sigma_O)^2 \approx (\sigma_{O, \text{Tracking}})^2 + \left( \sigma_p \frac{dv}{dp} \right)^2$$



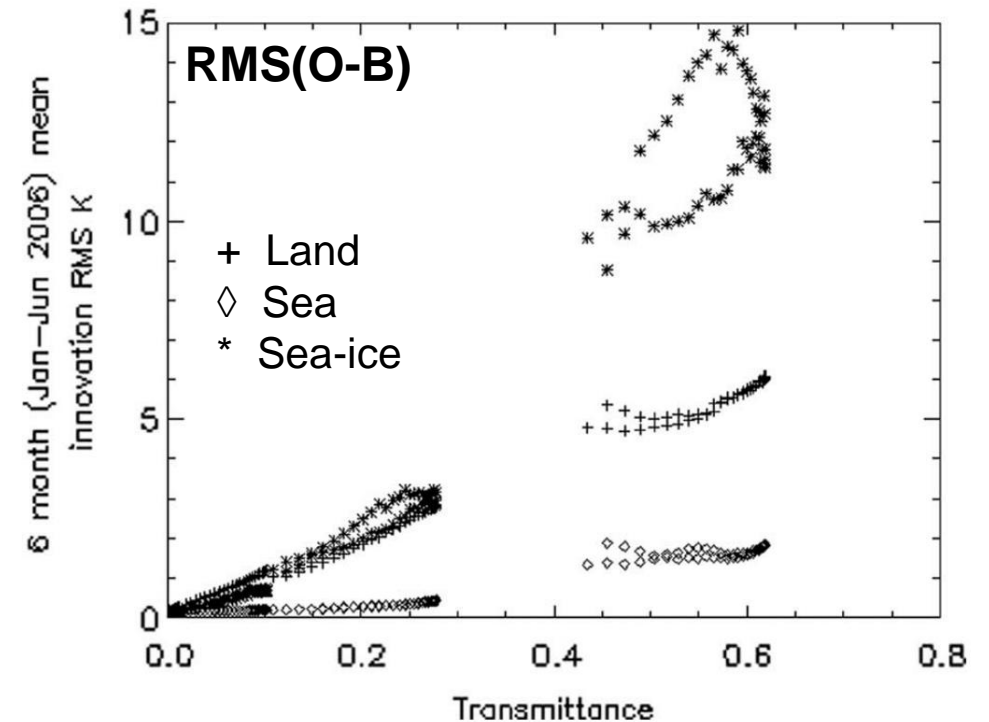
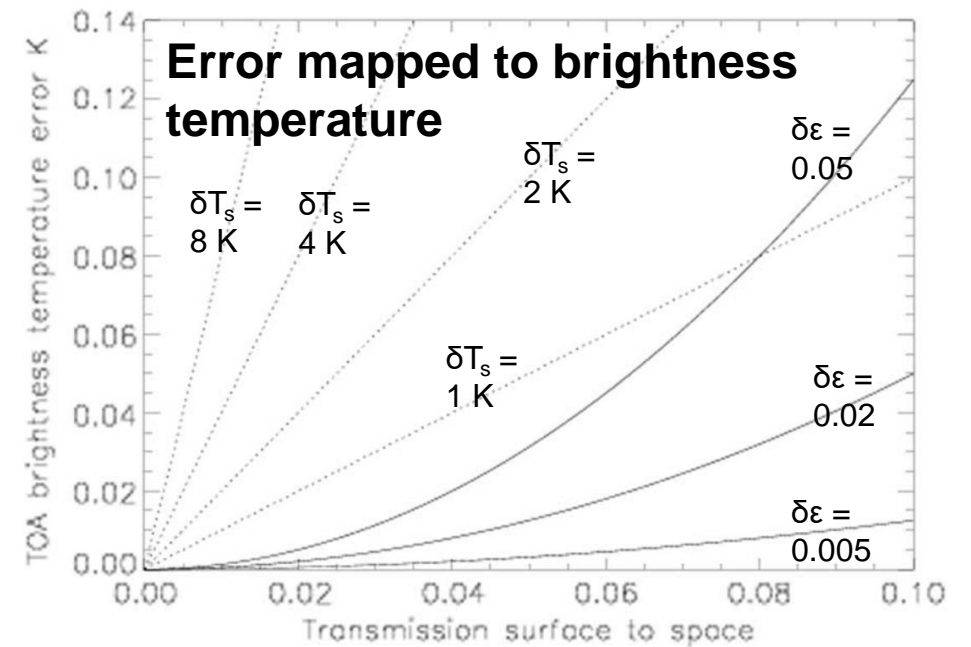
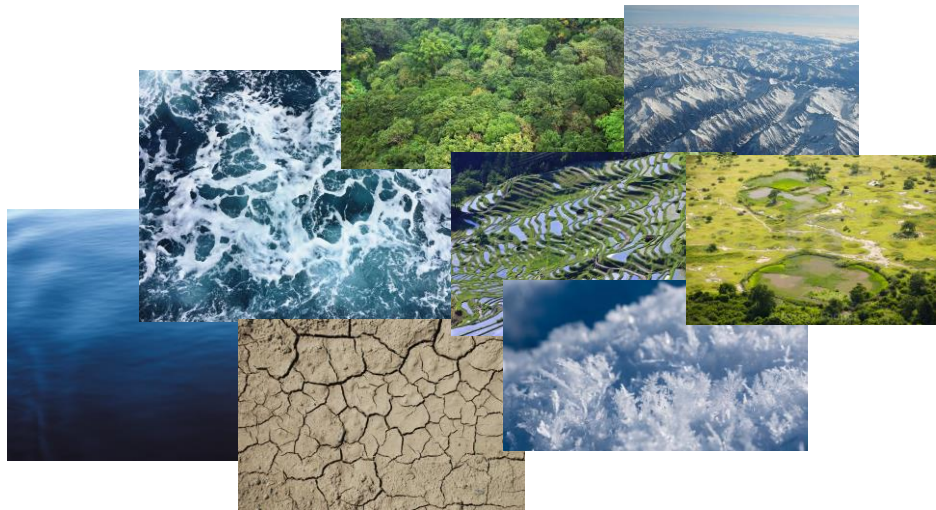
# Situation-dependence of observation errors: Example: surface-related errors

(e.g., English et al 2008;  
Lawrence et al 2015; etc)

Contributions from emissivity and skin-temperature errors to forward-modelling for surface-sensitive radiances:

$$dI = \epsilon \tau \delta T_s + ((T_s - T)\tau + (T - T_c)\tau^2) \delta \epsilon$$

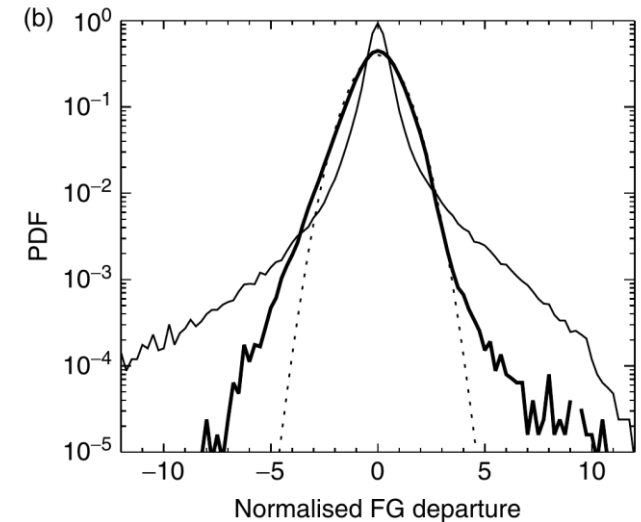
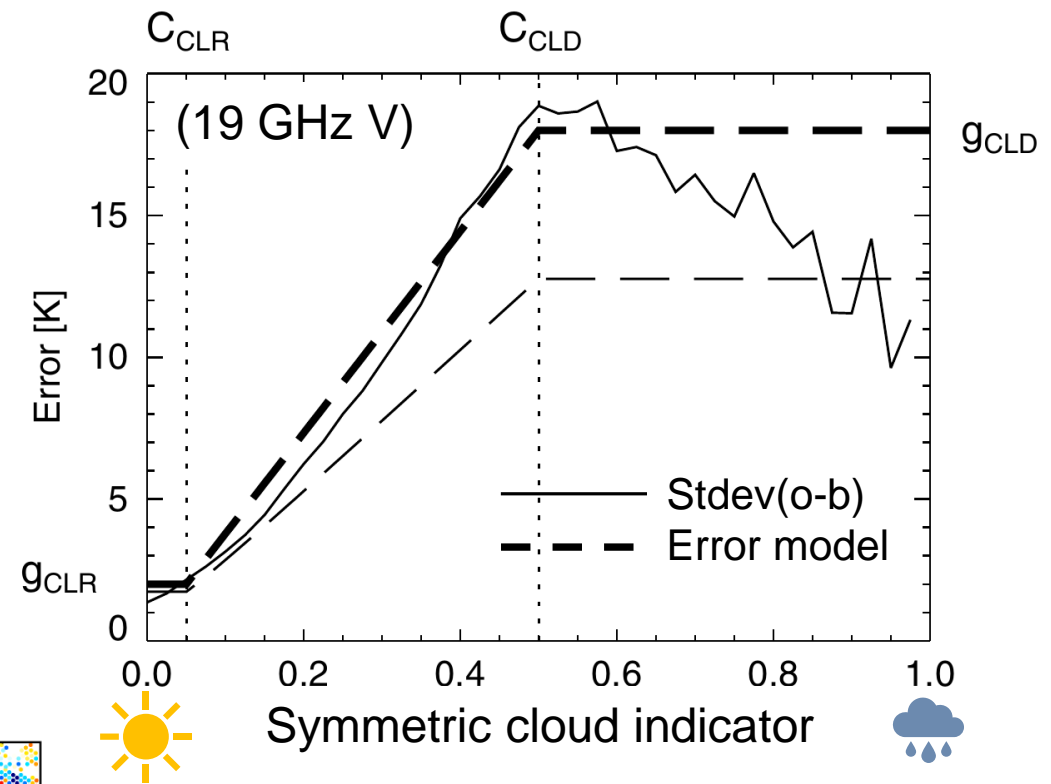
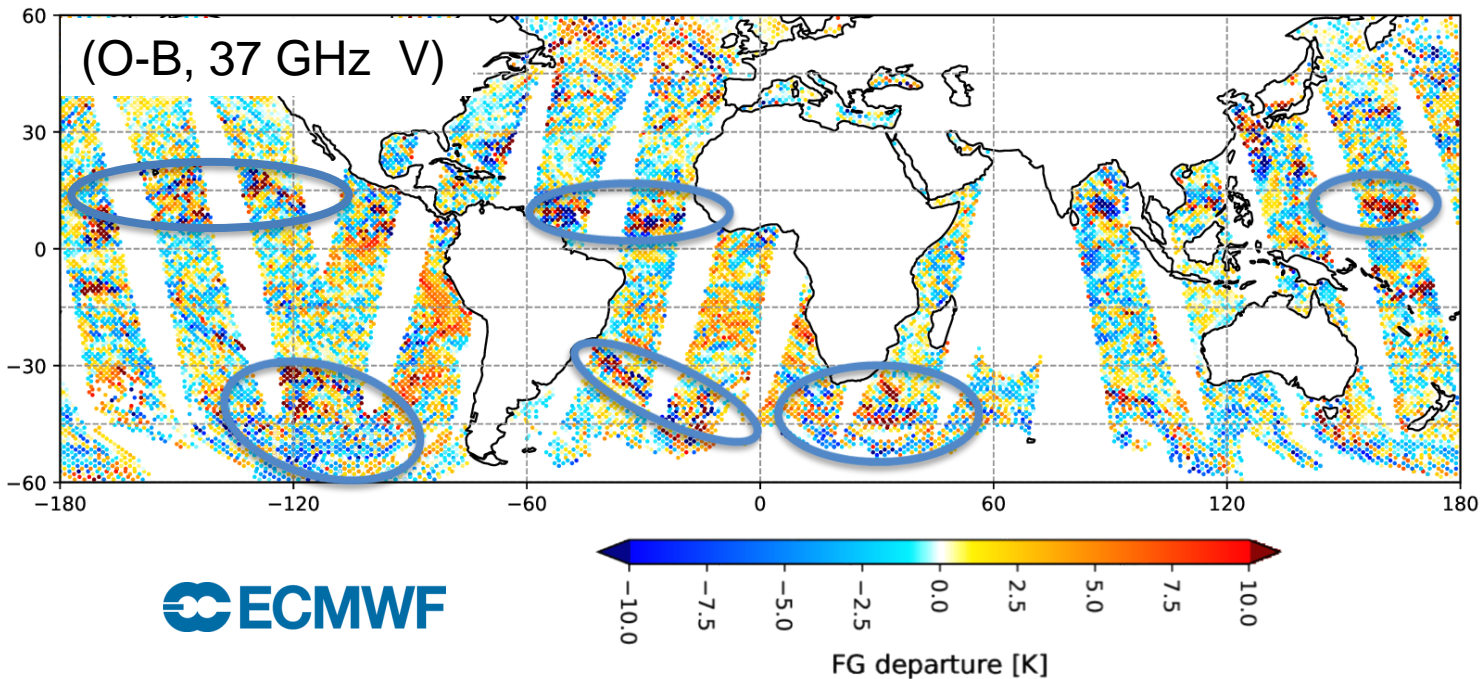
$$\sigma_o^2 = (\sigma_{O_{NeDT}})^2 + (dI)^2$$



# Situation-dependence of observation errors: Example: All-sky assimilation

(e.g., Geer and Bauer 2011;  
Okamoto et al 2014; Harnisch et al 2016)

Representation error **larger in cloudy regions**: observation error modelled as function of cloud indicator; observation error model derived from stdev(o-b)



→ Alan Geer's talk on  $R$  for all-sky IR

# Some remarks on modelling situation-dependent observation errors

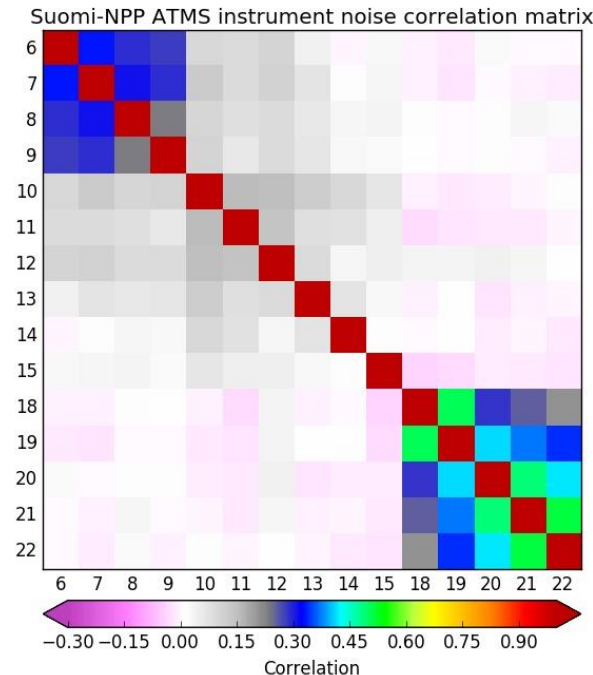
- Current approaches aim to identify and model the main situation-dependent contributions, based on physical considerations
  - Models are mostly specified based on observation departure statistics ( $\text{stdev}(o-b)$ ), with ad-hoc assumptions on the behaviour of background errors.
    - How valid are the underlying assumptions on background errors?
    - Scope for more independent specification of error sources?
- What situation-dependent variations are we currently missing?
  - E.g., convective vs stratiform clouds in all-sky; larger errors in H for obs at the end of 4D-Var window?
  - What level of sophistication is useful and desirable for situation-dependent observation errors? What can we model reliably?

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# Observation error correlations

- **Representation error** is likely to be **correlated** between different observations, e.g.:
  - An error in cloud detection is likely to be similar for other channels with similar cloud-sensitivity in clear-sky assimilation.
  - A radiative transfer error is likely to be similar for spectrally-similar channels.
  - A height-assignment error for AMVs is likely to be similar for neighbouring AMVs derived from a similar cloud.
- And even instrument noise can be correlated between channels:



ATMS instrument noise correlation, from independent instrument characterisation.

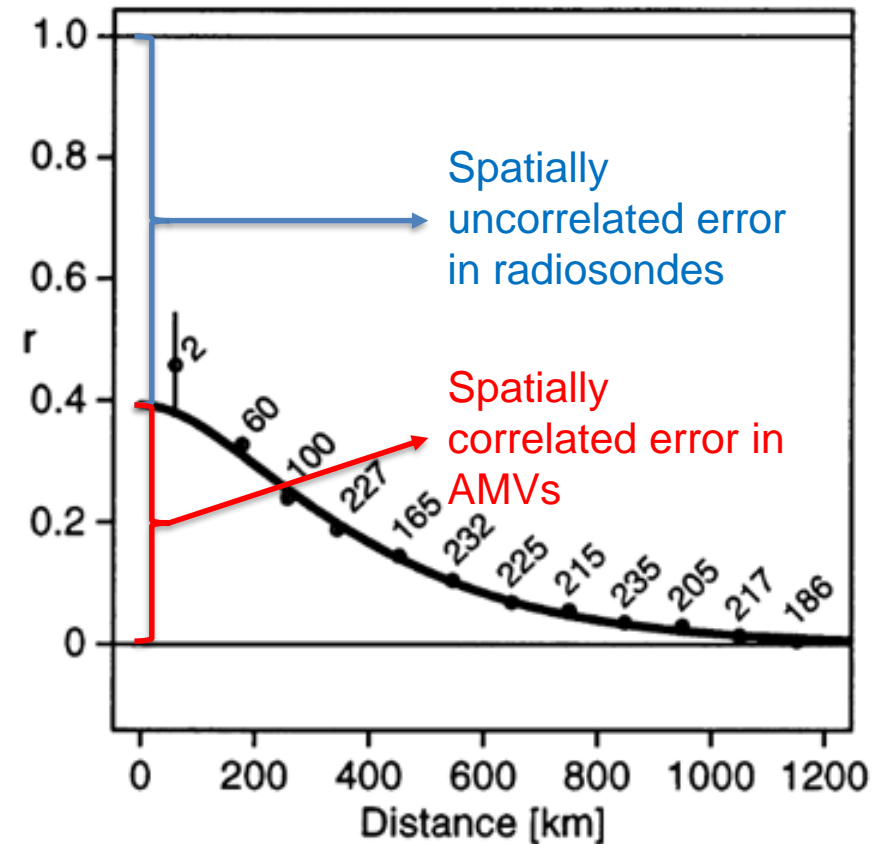


# Estimating spatial error correlations for AMVs

(e.g., Bormann et al 2003)

- Estimated using a Hollingsworth/Lönnberg approach:
  - Use pairs of collocated AMVs & radiosondes.
  - Assume errors in radiosondes uncorrelated.

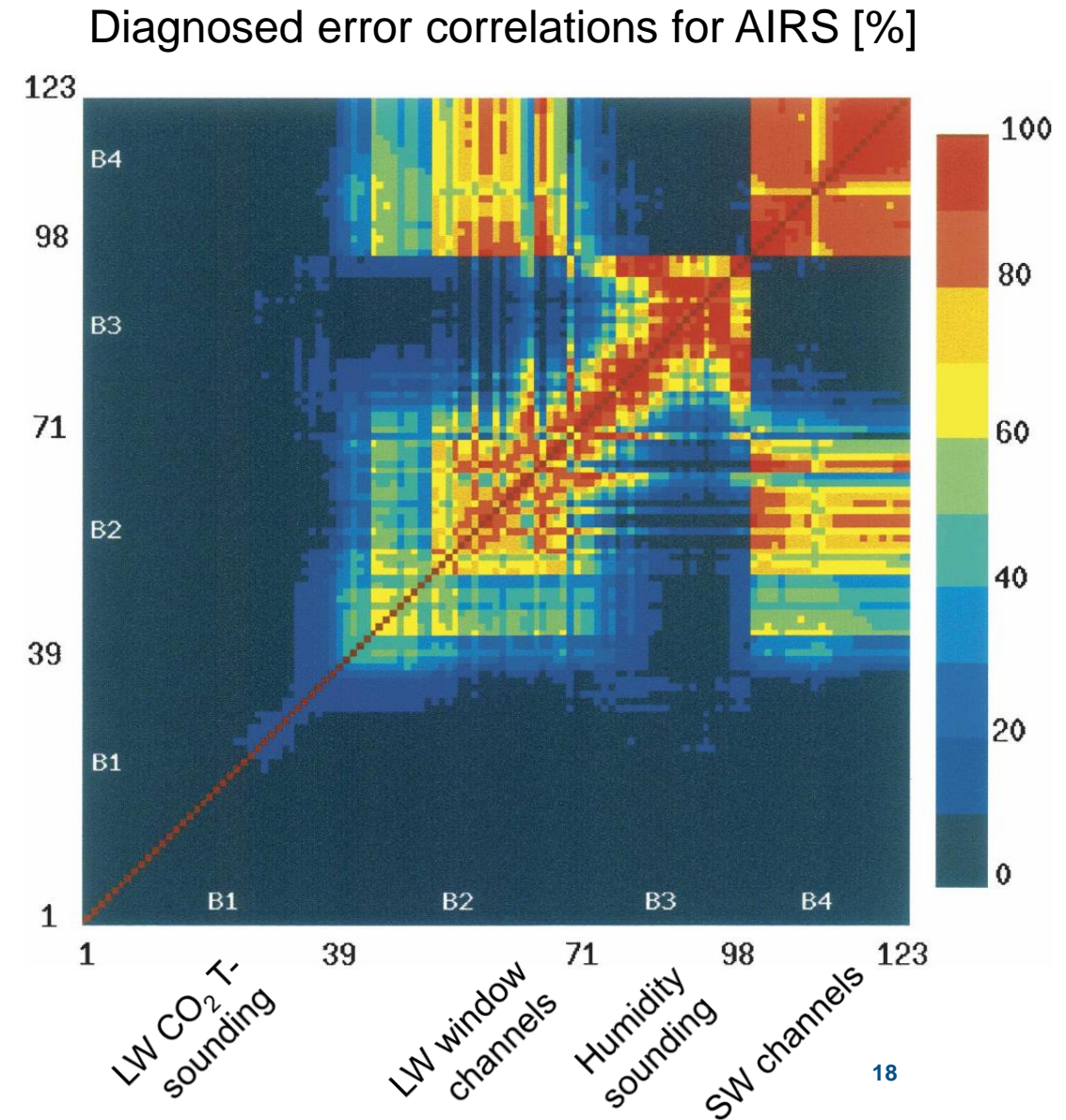
Correlations between AMV/radiosonde differences



# Estimating inter-channel error correlations for hyper-spectral IR observations

(e.g., Garand et al 2007)

- Estimated using a Hollingsworth/Lönnberg approach:
  - Use pairs of o-b for AIRS.
  - Assume AIRS observation errors are spatially uncorrelated.
- Possible source of error correlation:
  - Cloud detection
  - Spatial representativeness
  - Radiative transfer



# Estimating inter-channel error correlations for hyper-spectral IR observations and the Desroziers diagnostic

(e.g., Desroziers et al 2005)

- **Basic assumptions:**

- Linear estimation theory; errors in observation and background uncorrelated.
- Weights used in the assimilation system are consistent with true observation and background errors.

- Then the following relationship can be derived:

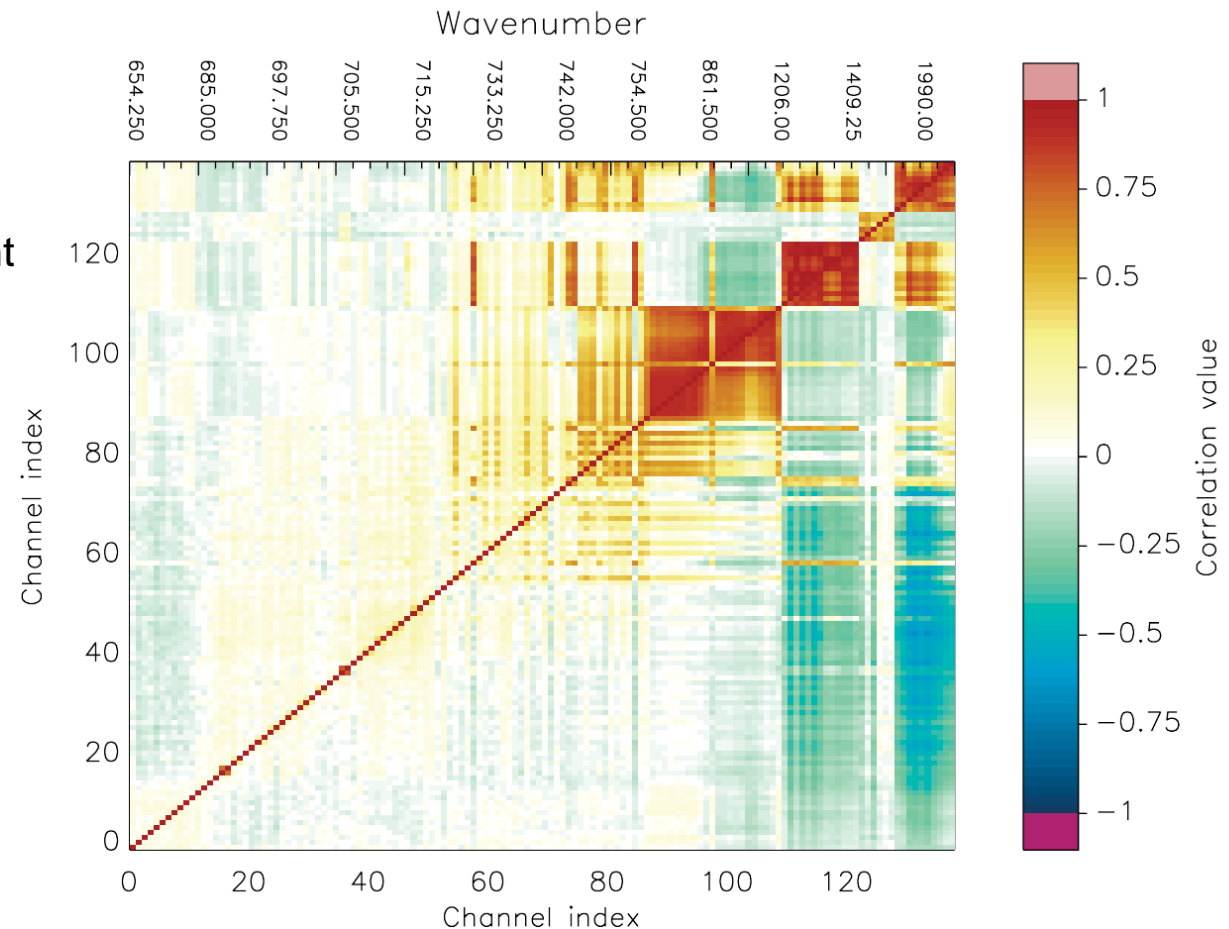
$$\mathbf{R} = \text{Cov}[\mathbf{d}_a, \mathbf{d}_b]$$

with  $\mathbf{d}_a = (\mathbf{y} - \mathbf{H}[\mathbf{x}_a])$  (analysis departure)

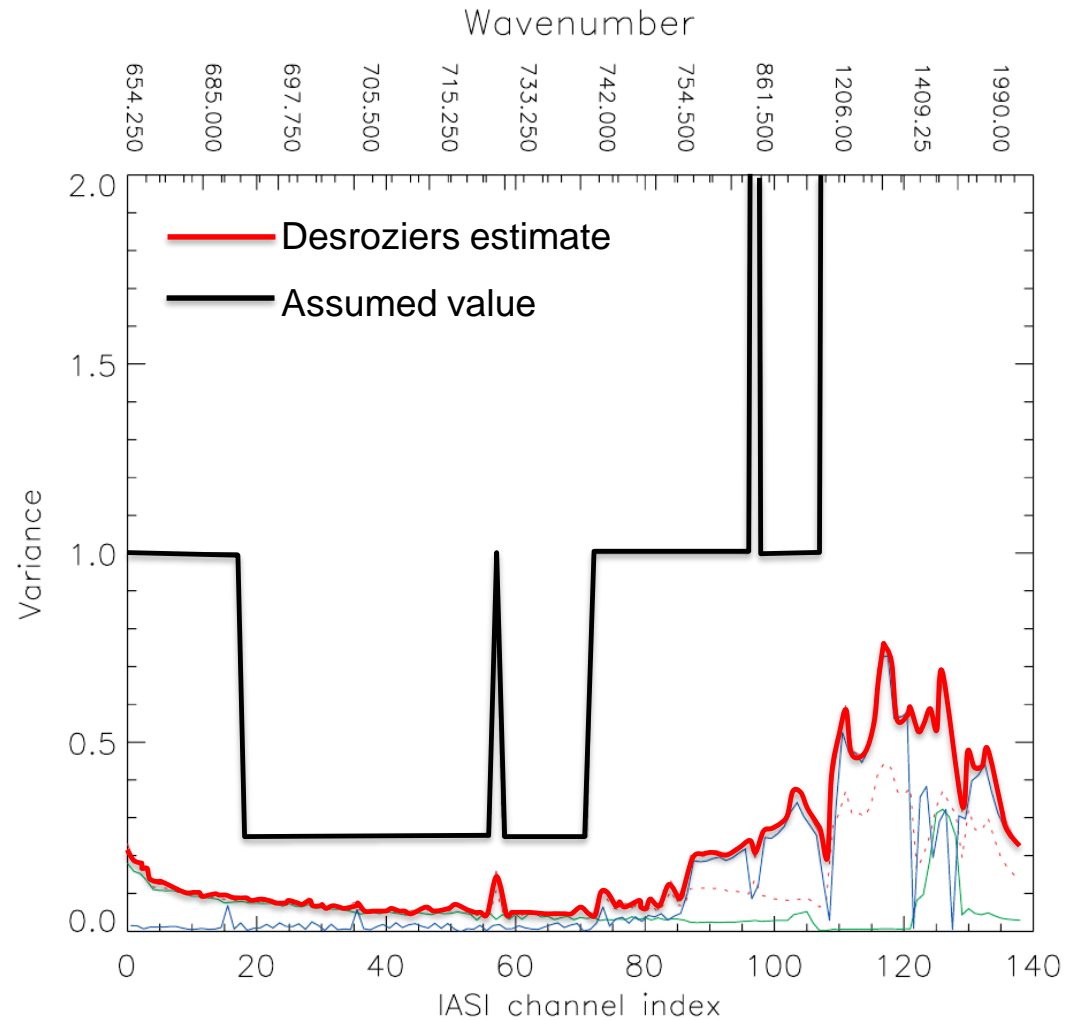
$\mathbf{d}_b = (\mathbf{y} - \mathbf{H}[\mathbf{x}_b])$  (background departure)

- **Consistency diagnostic** for the specification of  $\mathbf{R}$ . Increasingly used to estimate  $\mathbf{R}$ .

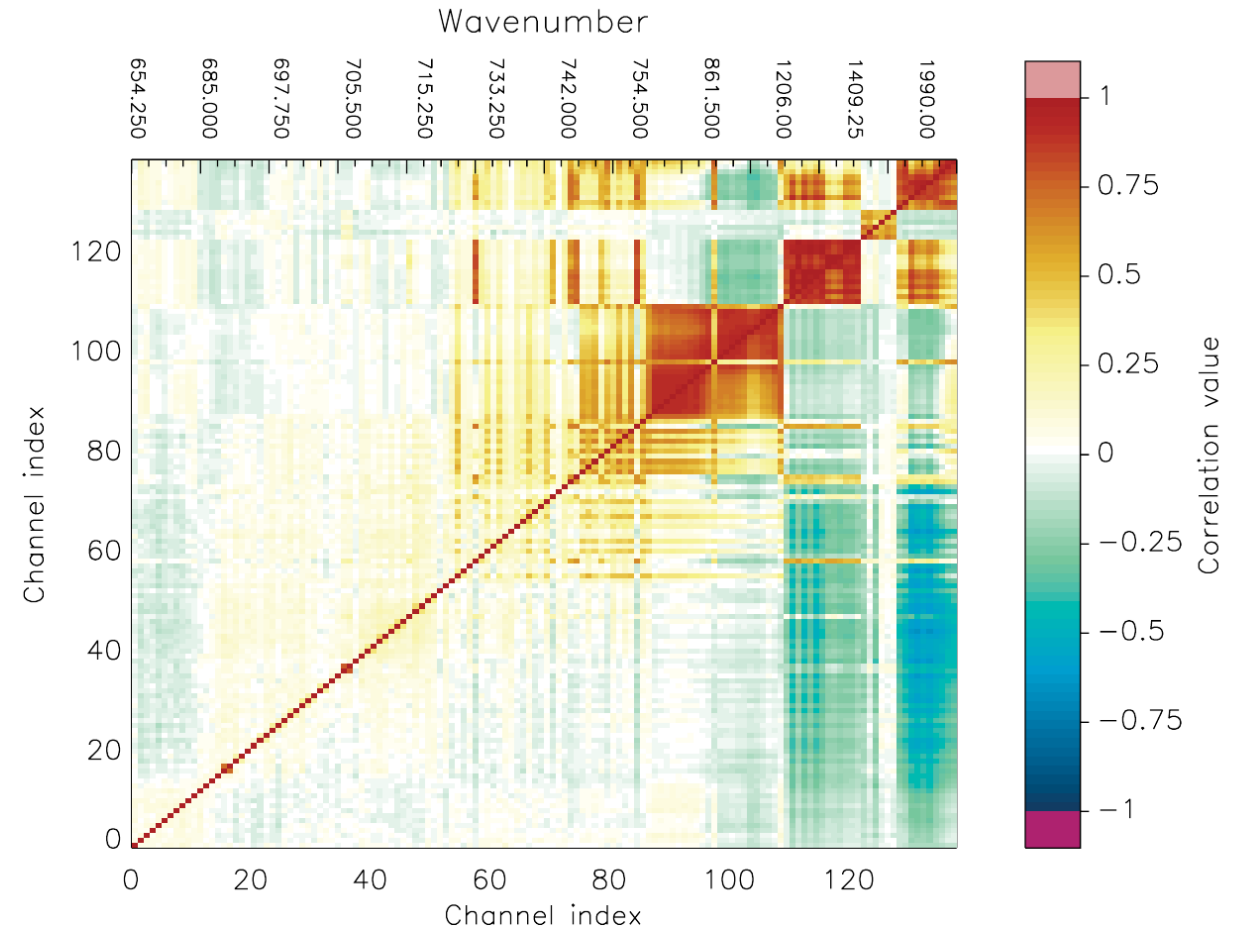
Diagnosed error correlations for IASI  
(Stewart et al 2009, 2014)



# Estimating inter-channel error correlations for hyper-spectral IR observations and the Desroziers diagnostic

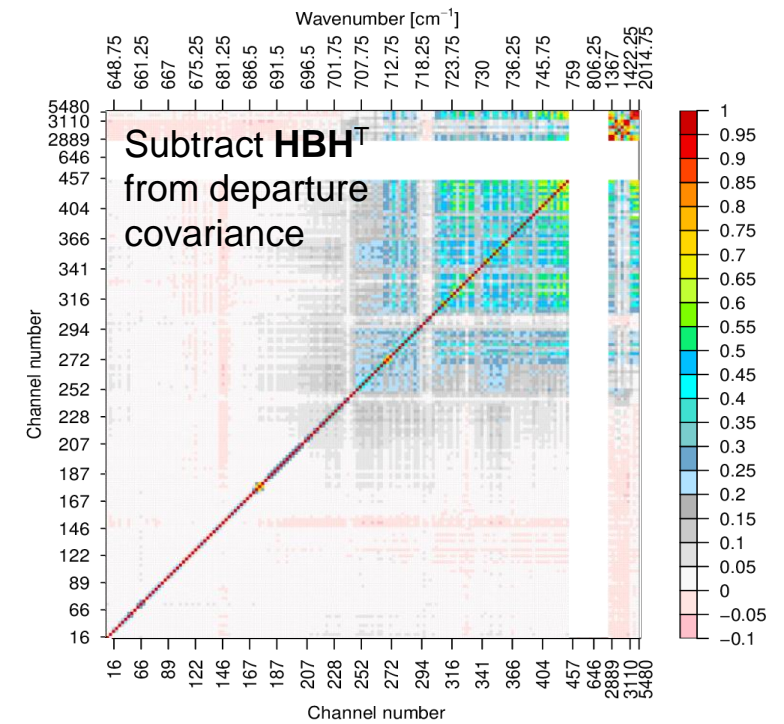
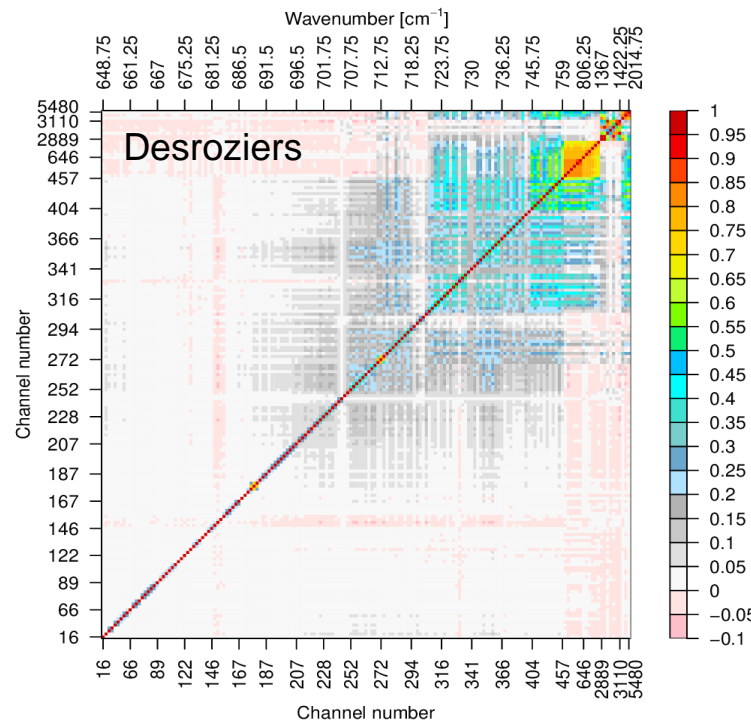
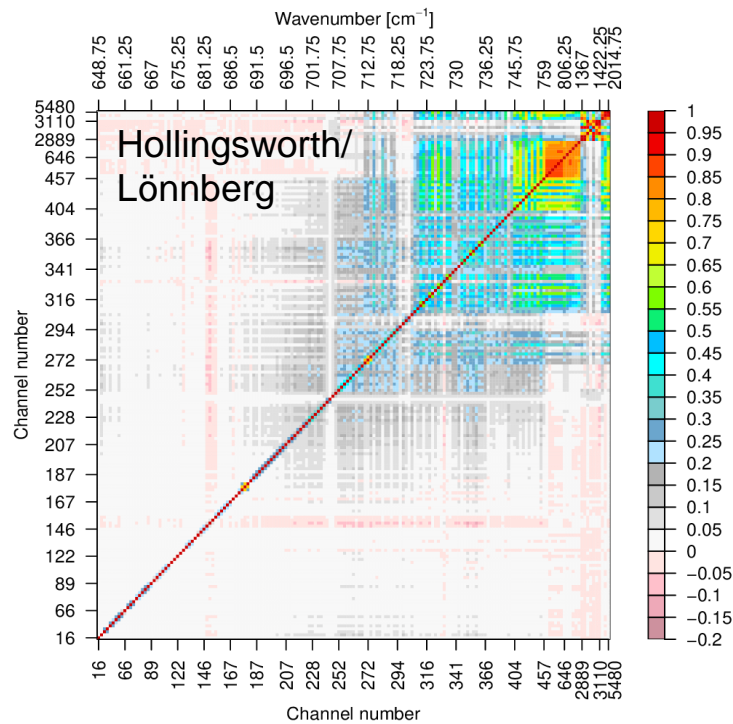
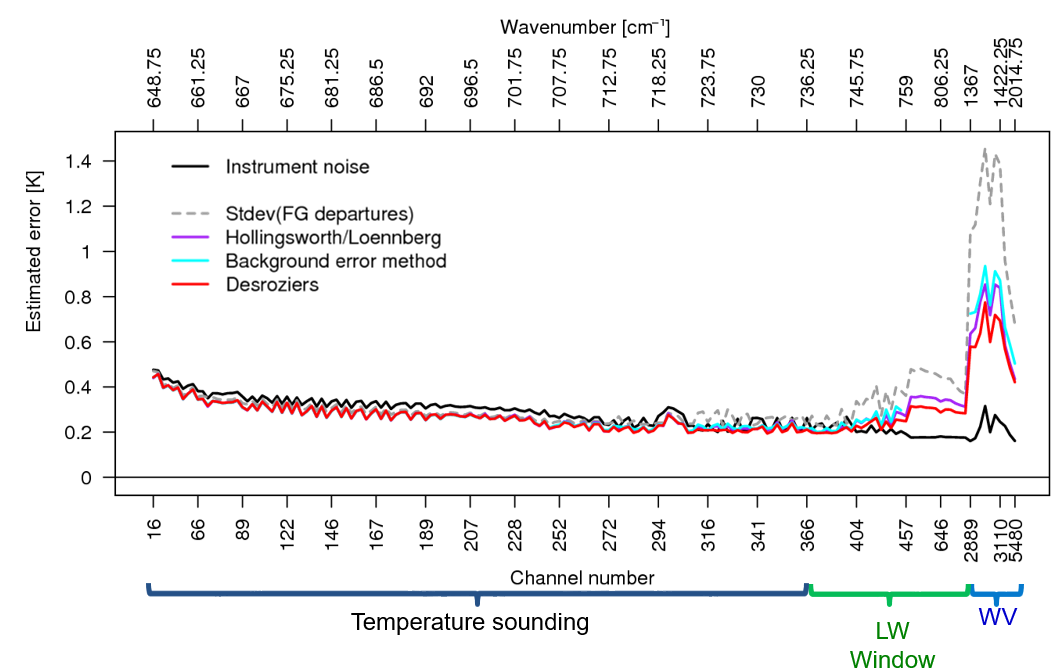


Diagnosed error correlations for IASI  
(Stewart et al 2009, 2014)



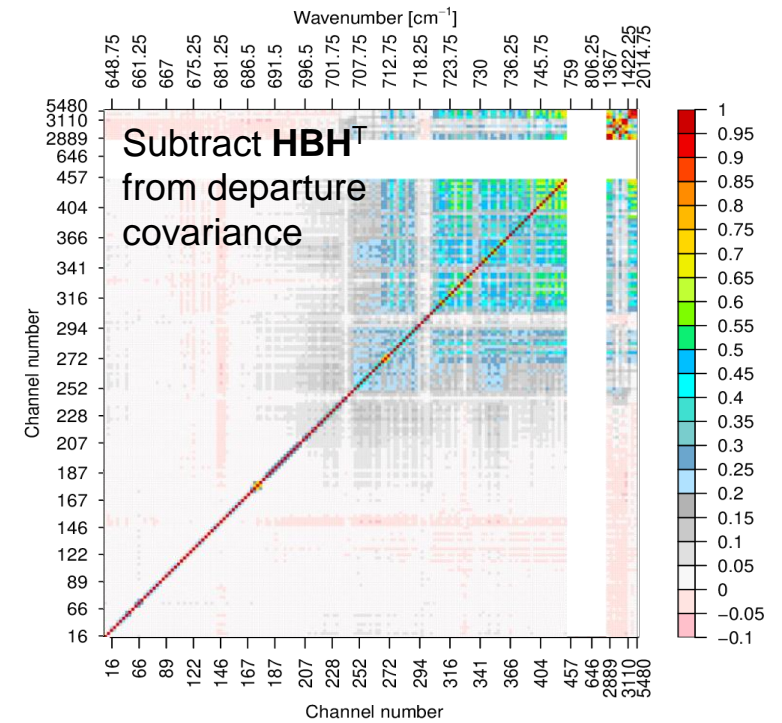
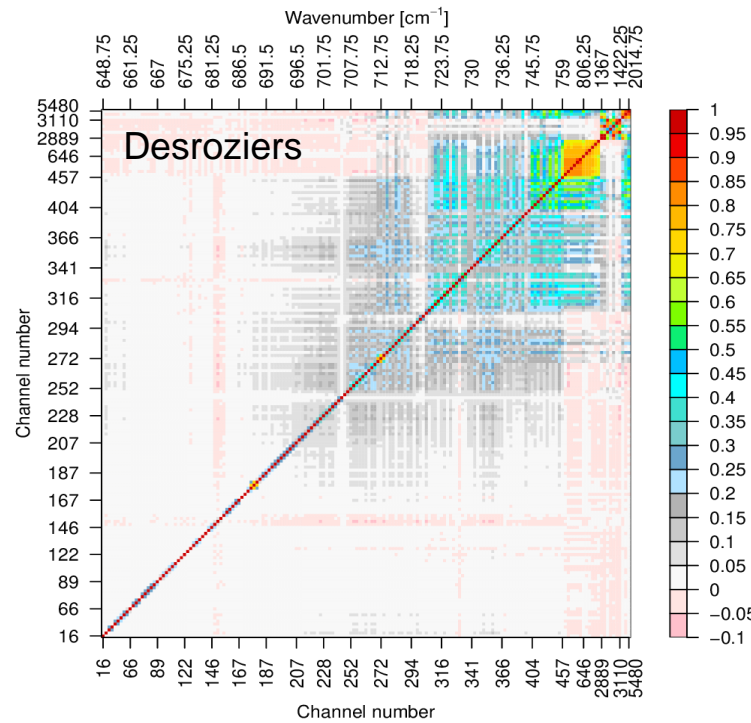
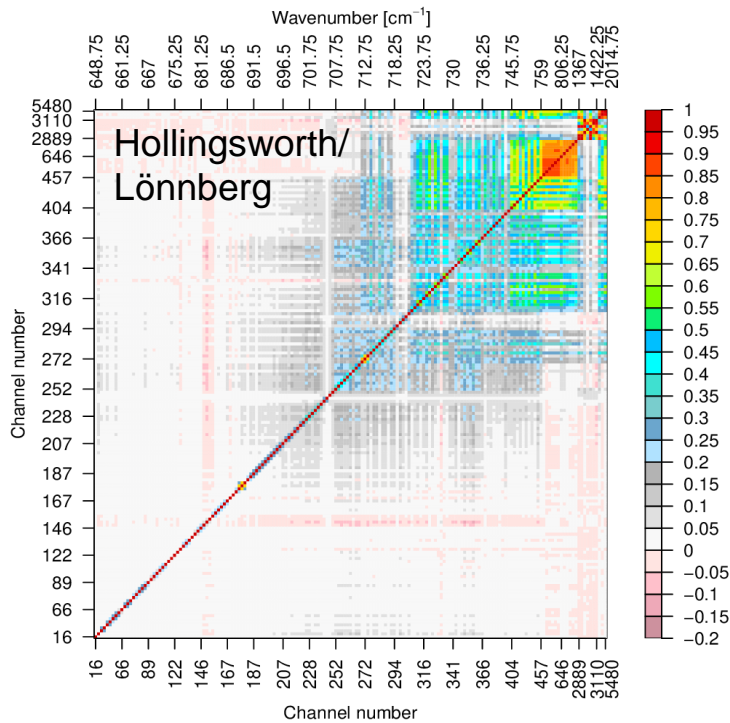
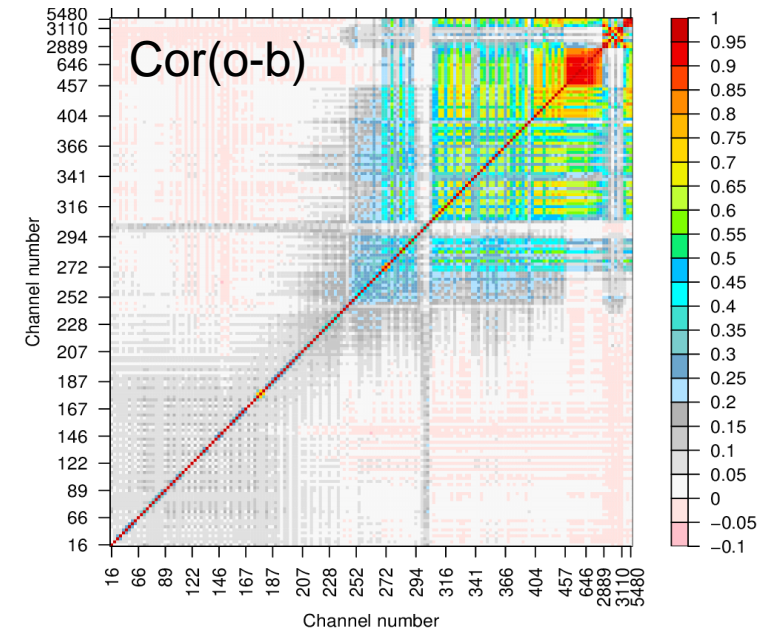
# Estimating inter-channel error correlations for hyperspectral IR: Different diagnostics, similar results

(Bormann et al 2010)



# Estimating inter-channel error correlations for hyperspectral IR: Different diagnostics, similar results

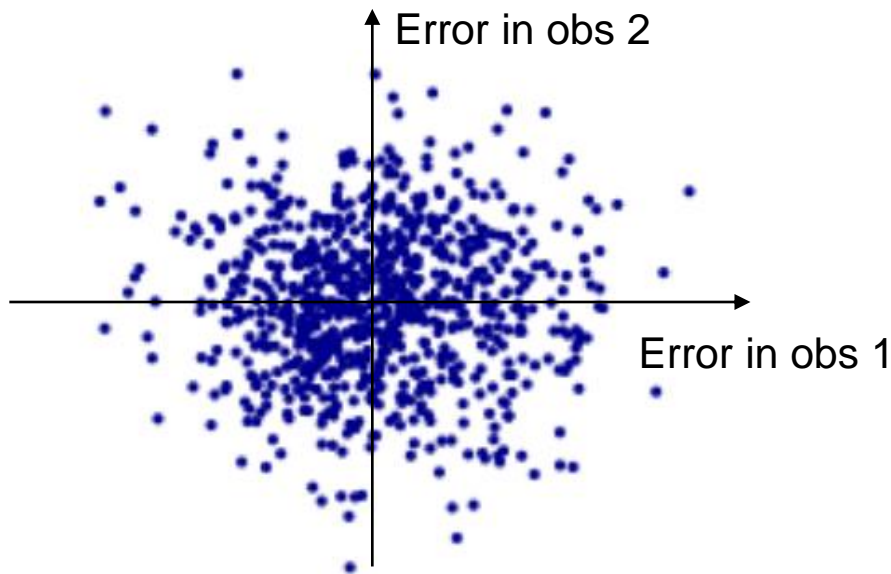
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# What is the effect of error correlations?

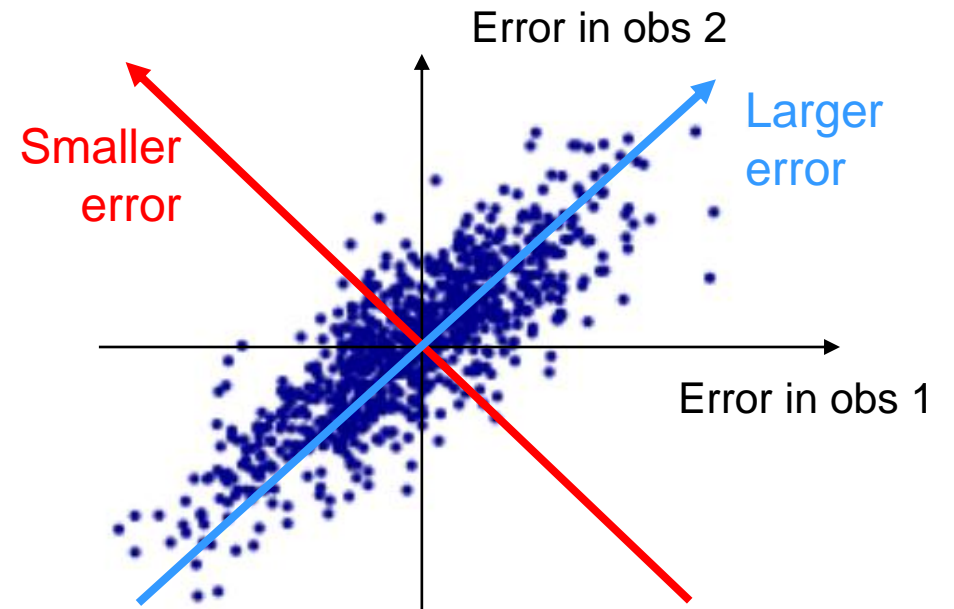
Uncorrelated error

$$\mathbf{R} = \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$$



Correlated error

$$\mathbf{R} = \begin{pmatrix} 1 & 0.8 \\ 0.8 & 1 \end{pmatrix}$$

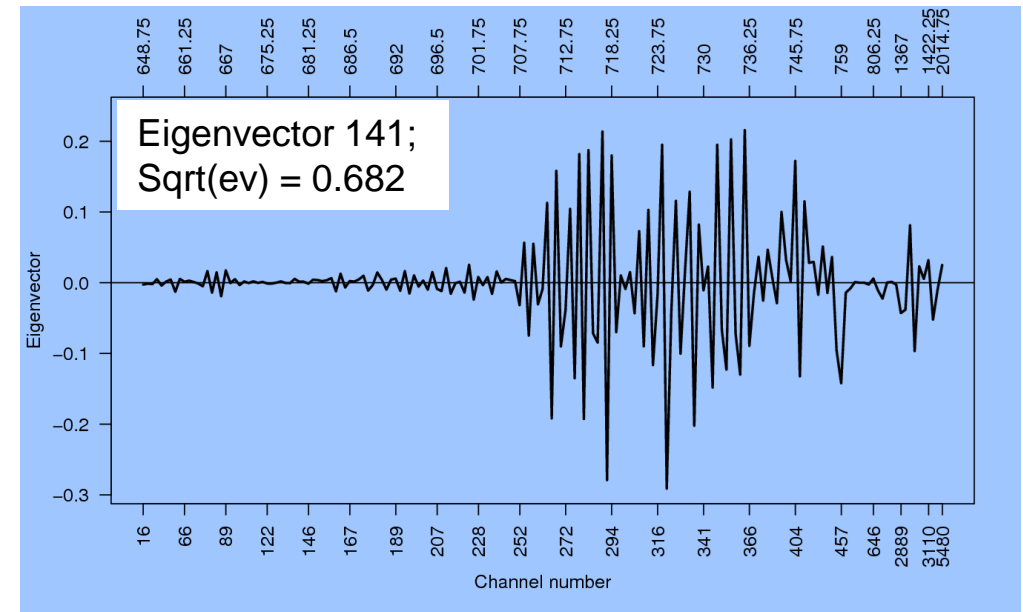
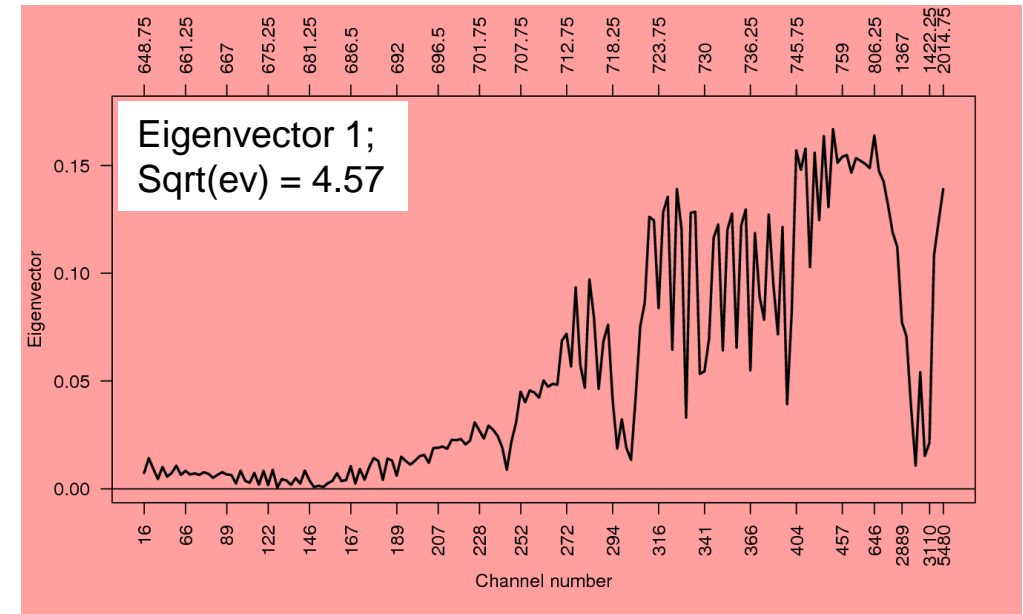
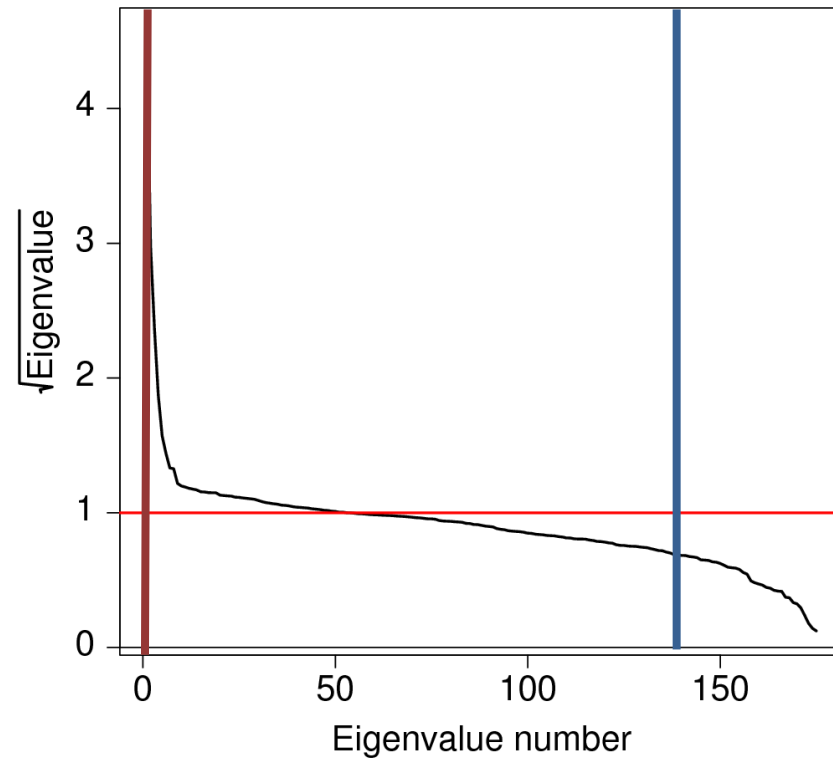


Compared to diagonal errors, **positive error correlations imply...**

- ... **larger errors** for features along the blue direction (mean-like features).
- ... **smaller errors** for features along the red direction (differencee-type features).

# Example: error correlations for IASI

Eigenvalues of the error correlation matrix:

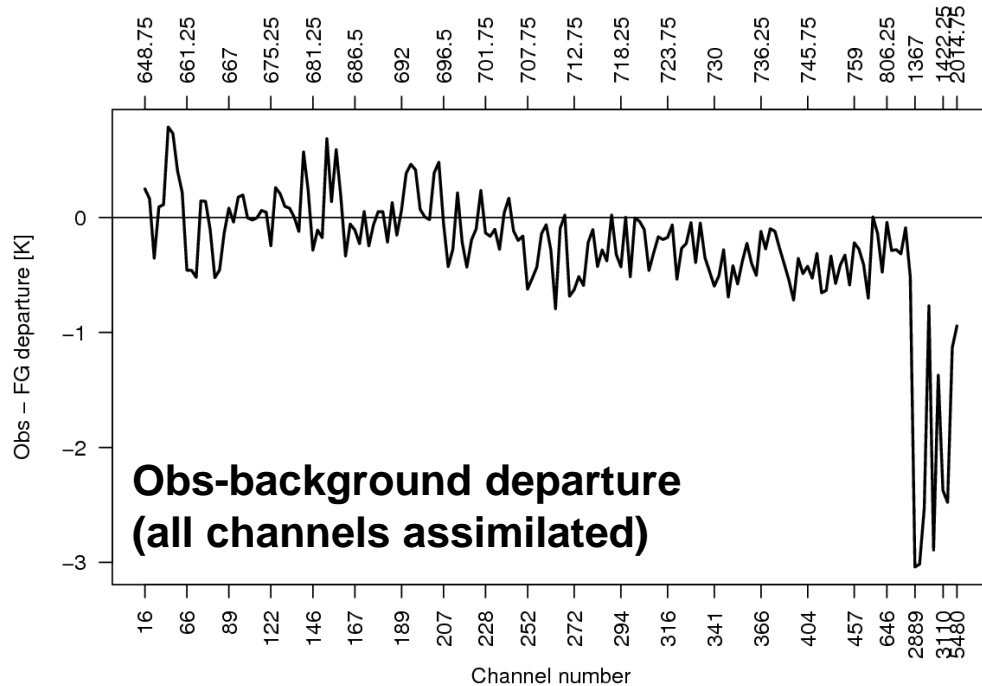




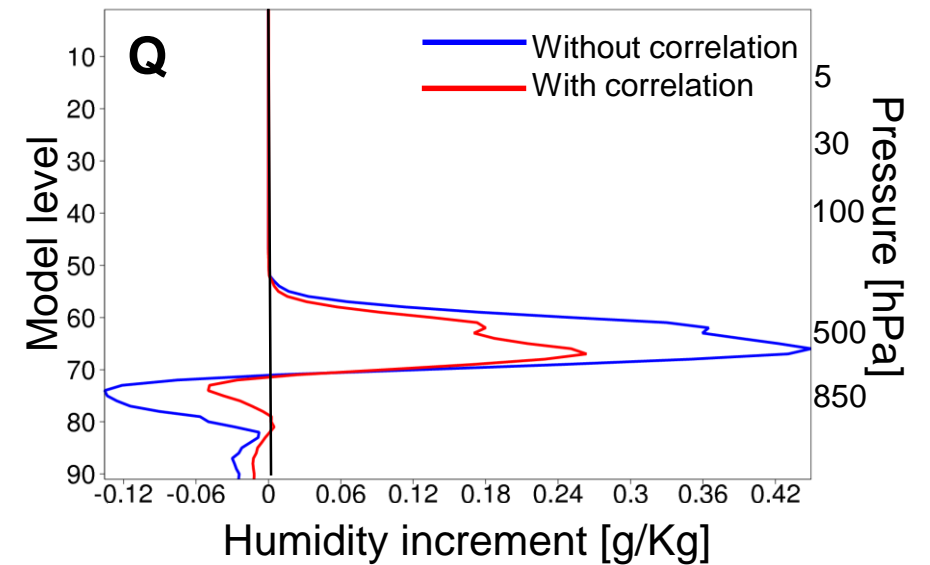
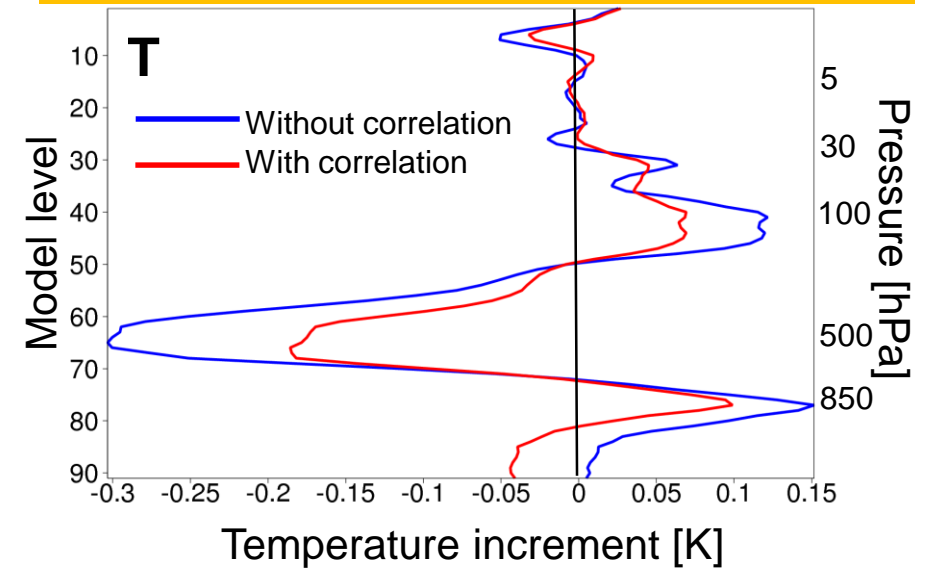
# Example: Assimilation of a single IASI spectrum (I)

Assimilate a single IASI spectrum,

- assuming **no error correlations**,
- assuming **diagnosed error correlations** ( $\sigma_o$  unchanged in both cases).



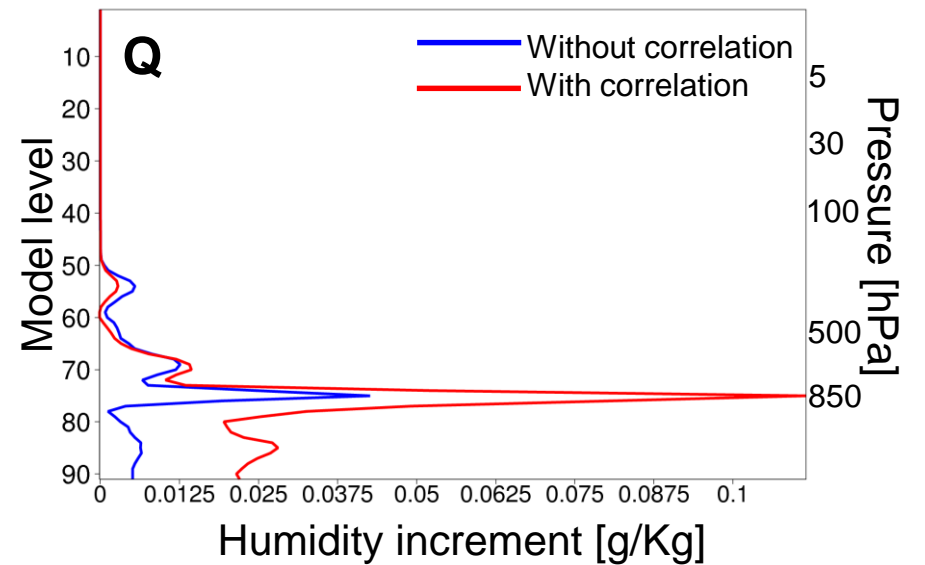
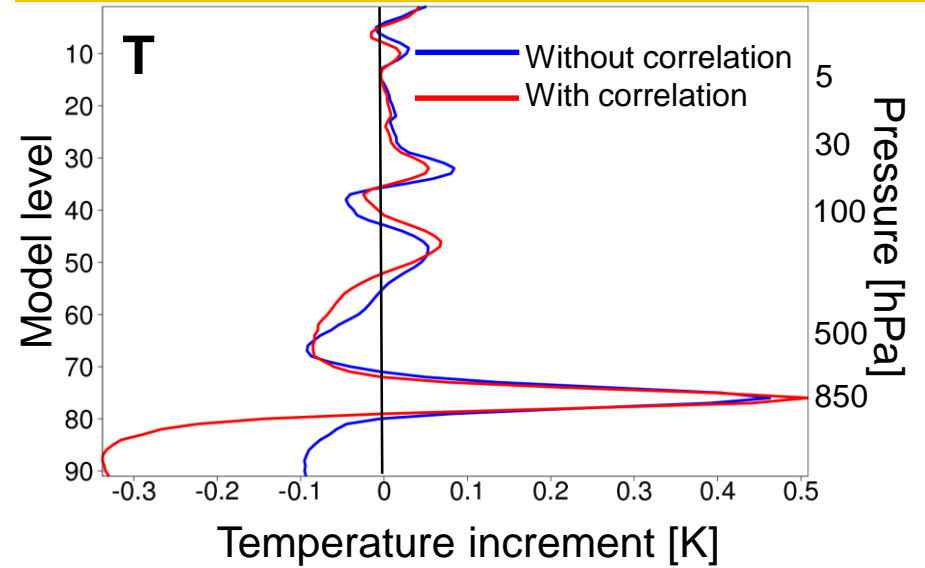
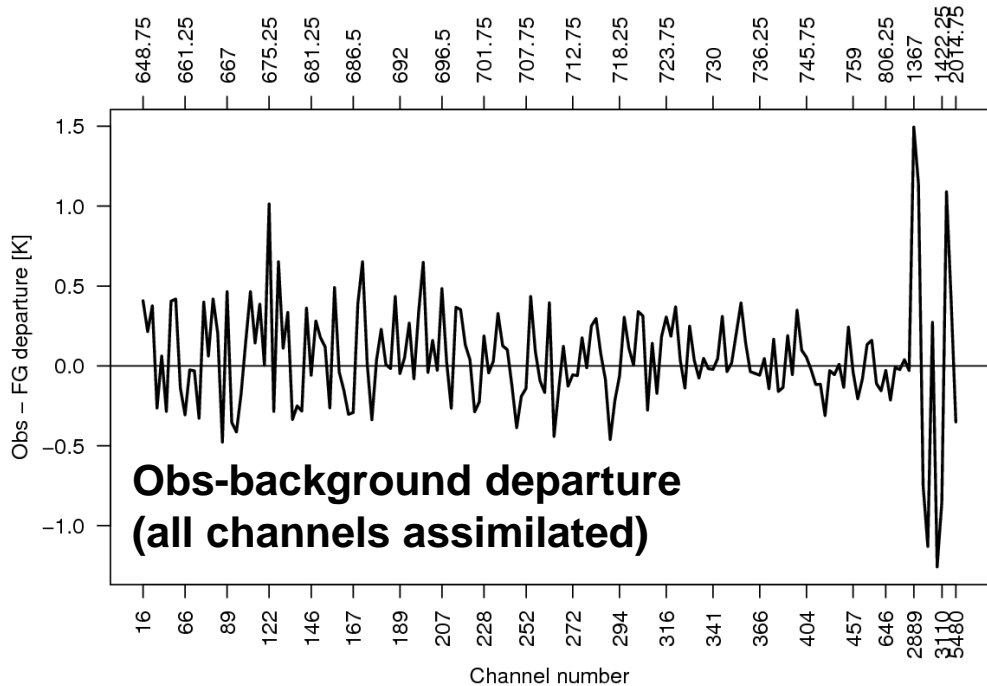
“Similar” departures → increments reduced with error correlations taken into account



# Example: Assimilation of a single IASI spectrum (II)

- Assimilate a single IASI spectrum,
  - assuming **no error correlations**,
  - assuming **diagnosed error correlations** ( $\sigma_o$  unchanged in both cases).

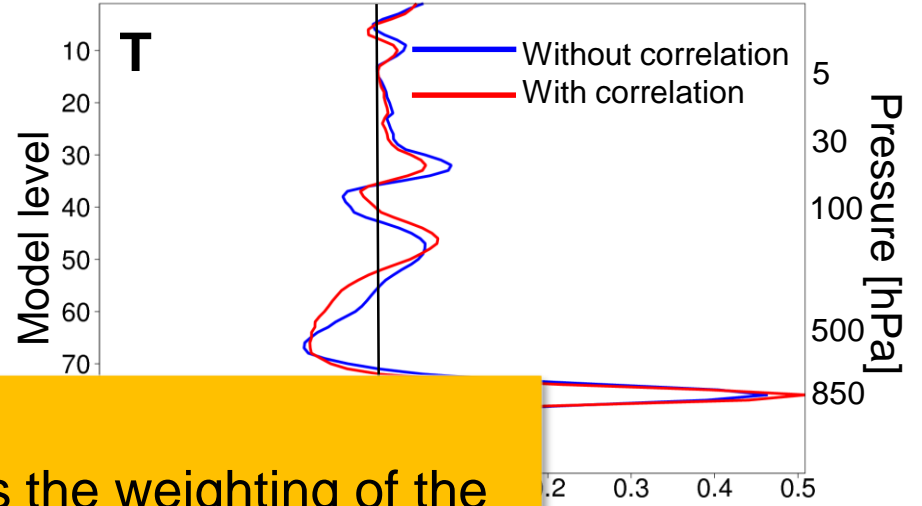
“Different” departures → increments **increased** with error correlations taken into account



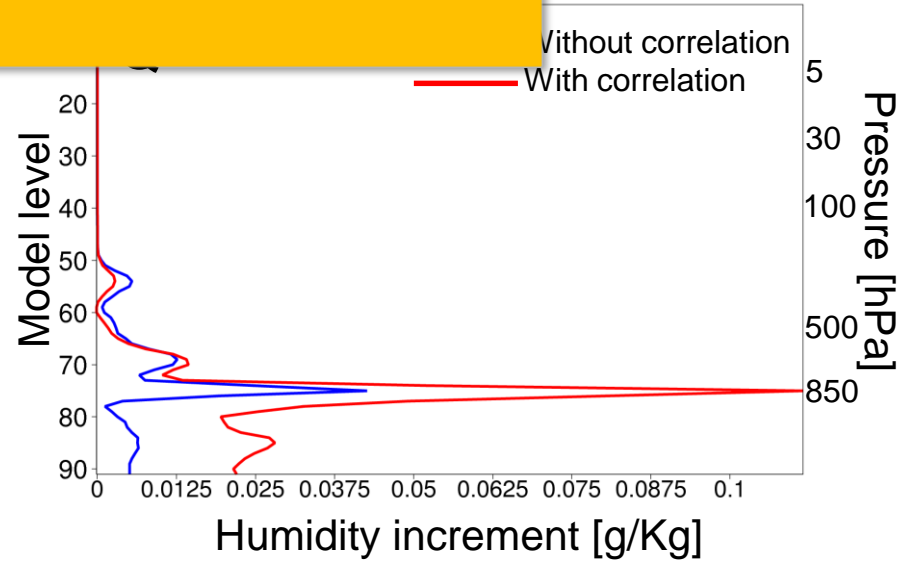
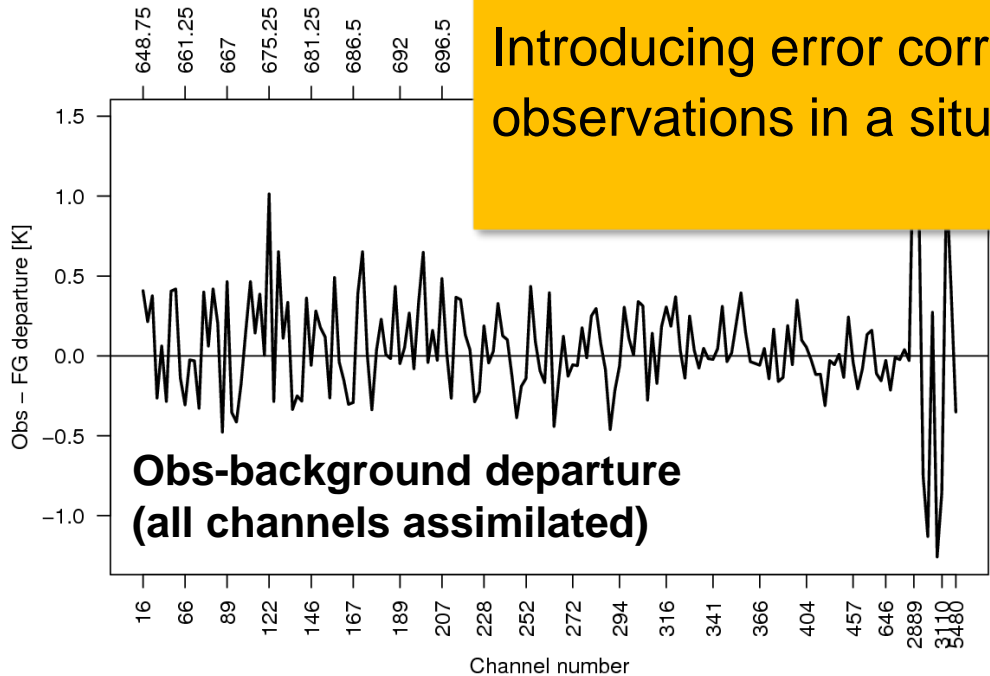
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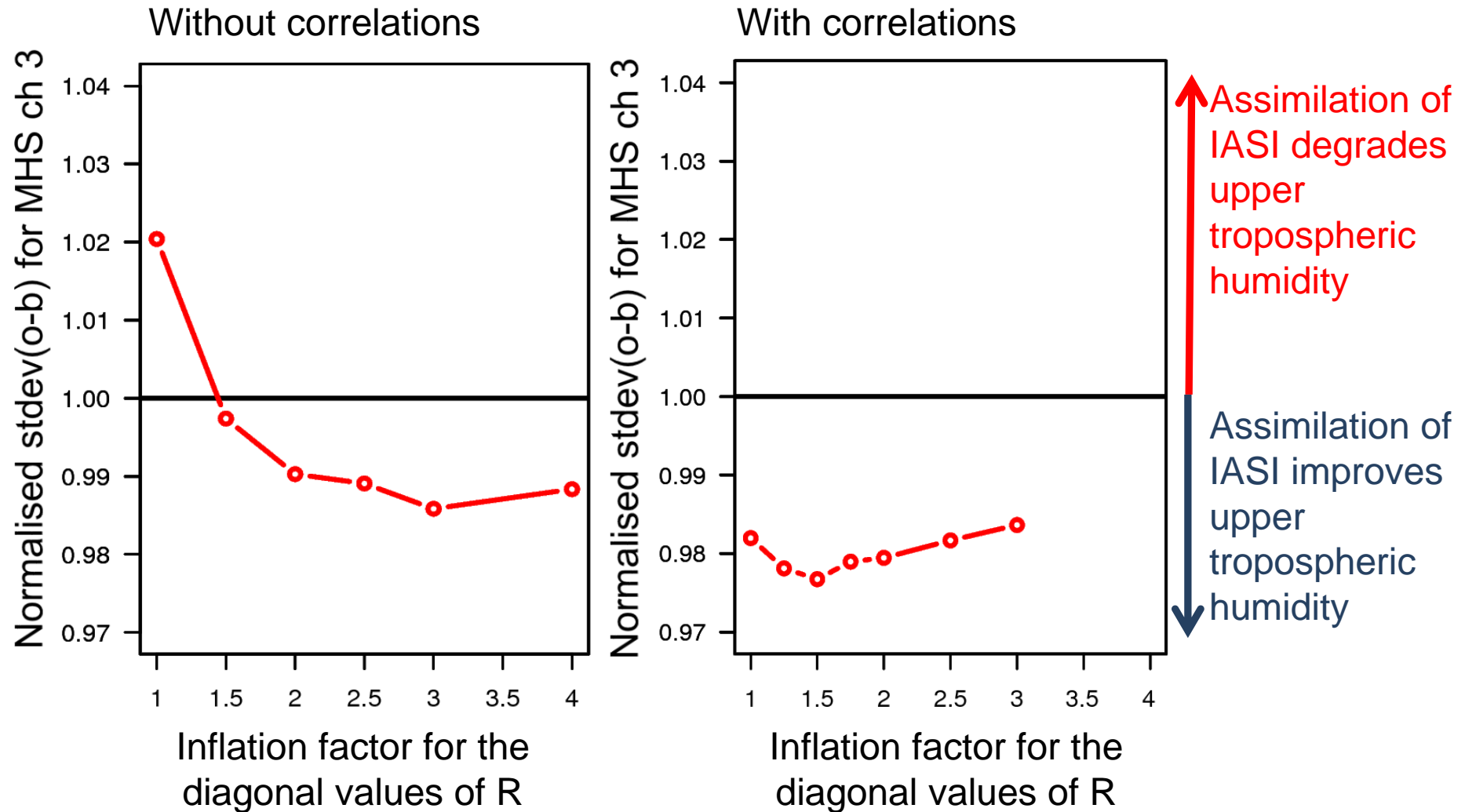
- Assimilate a single IASI spectrum,
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Introducing error correlations changes the weighting of the observations in a situation(/departure)-dependent way.



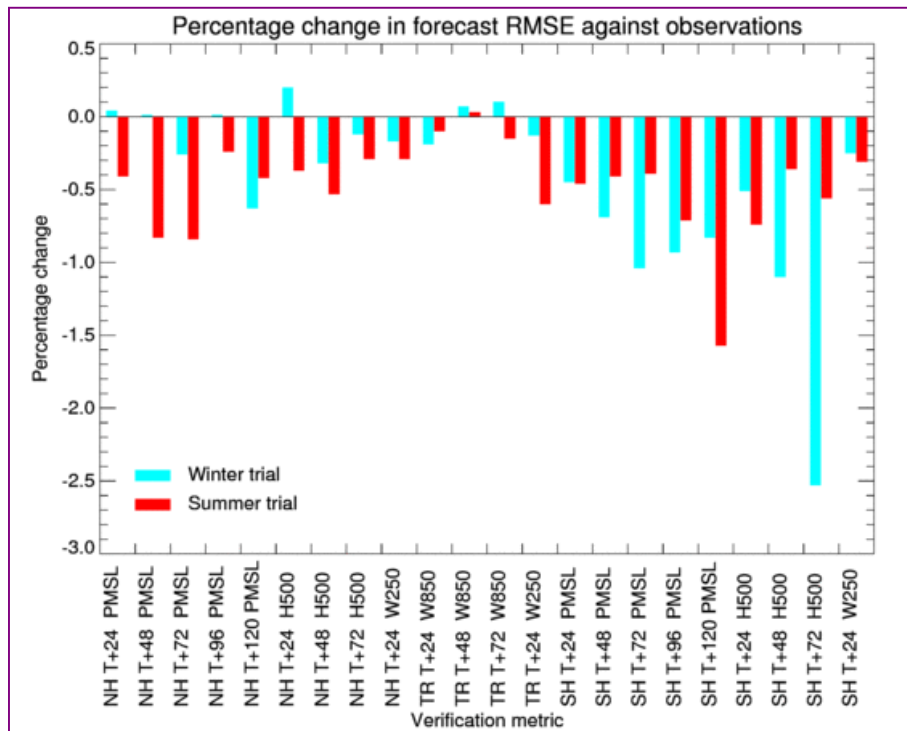
# Effect of accounting for inter-channel error correlations in the assimilation of IASI



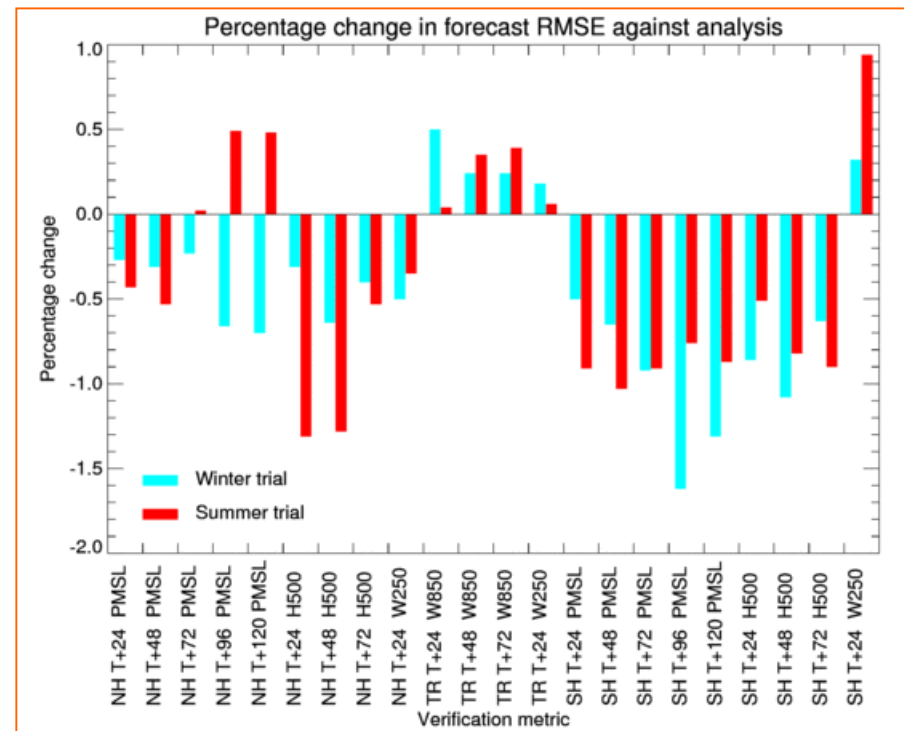
# Accounting for inter-channel error correlations in the assimilation

- Now widely used at operational centres, for hyperspectral IR, geostationary imager radiances, ATMS, etc.
- E.g., Weston et al (2014), Bormann et al (2016), Campbell et al (2017), Weston and Bormann (2018), Burrows (2018), Bathmann and Collard (2020), ...
- → *Fiona Smith's talk on the status of R for hyperspectral IR*

## Verification v Observations



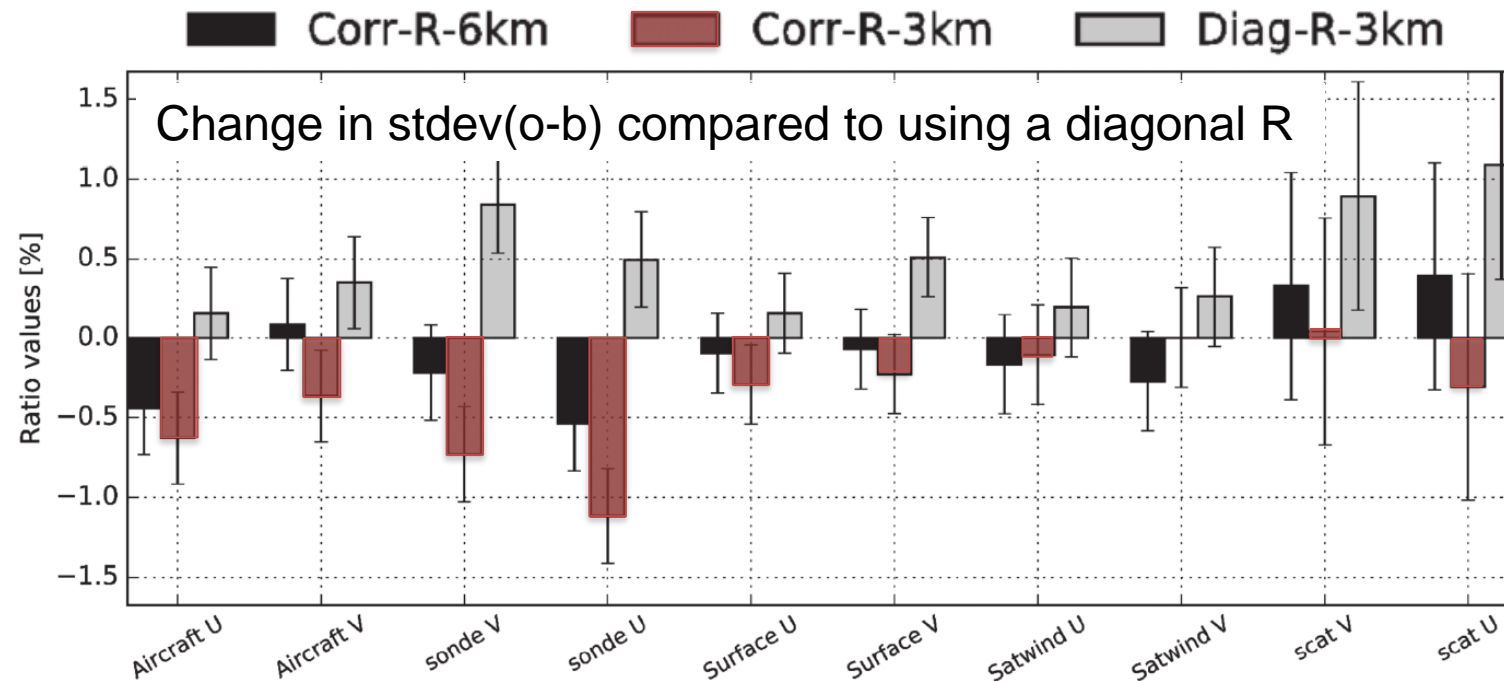
## Verification v Analyses



Weston et al (2014)

# Accounting for spatial error correlations

- Less work has been done on accounting for spatial error correlations in NWP, partly as it is **technically more difficult in variational frameworks**.
- But recent activity in several areas (→ *talks by Koji Terasaki, Oliver Guillet, Joël Bédard*)
  - First **operational application** in Met Office UKV system for radial winds from Doppler radar (Simonin et al 2019):



Accounting for spatial error correlations allows beneficial assimilation of radar winds with less thinning.

- Particular interest for regional models, to **improve small-scale representation**.

## Some further points on accounting for observation error correlations

- Accounting for error correlations puts **more weight on differences between observations.**
  - Are these differences reliable? How reliable are **inter-channel calibration/bias correction**?
  - Are the **estimates of error correlations reliable**?
- Accounting for observation error correlations can affect the **conditioning** of the assimilation and lead to slower convergence.
- The importance of accounting for error correlations may additionally depend on the structure of the **background error.**

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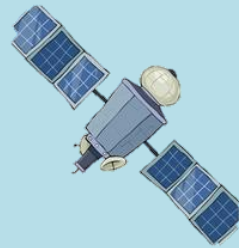
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# Contributions to observation error

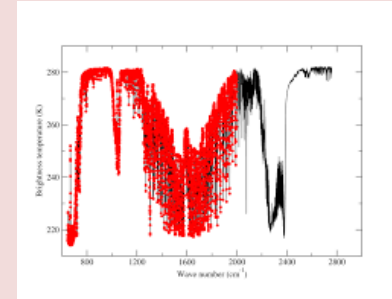
## Measurement error

E.g., instrument noise for satellite radiances



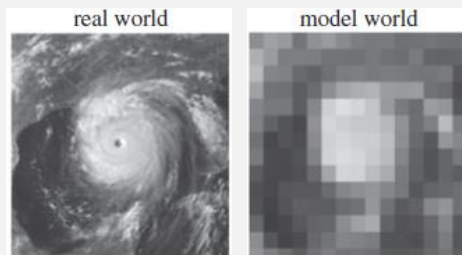
## Forward model (observation operator) error

E.g., radiative transfer error



## Representativeness error

E.g., point measurement vs model representation



## Quality control/pre-processing error

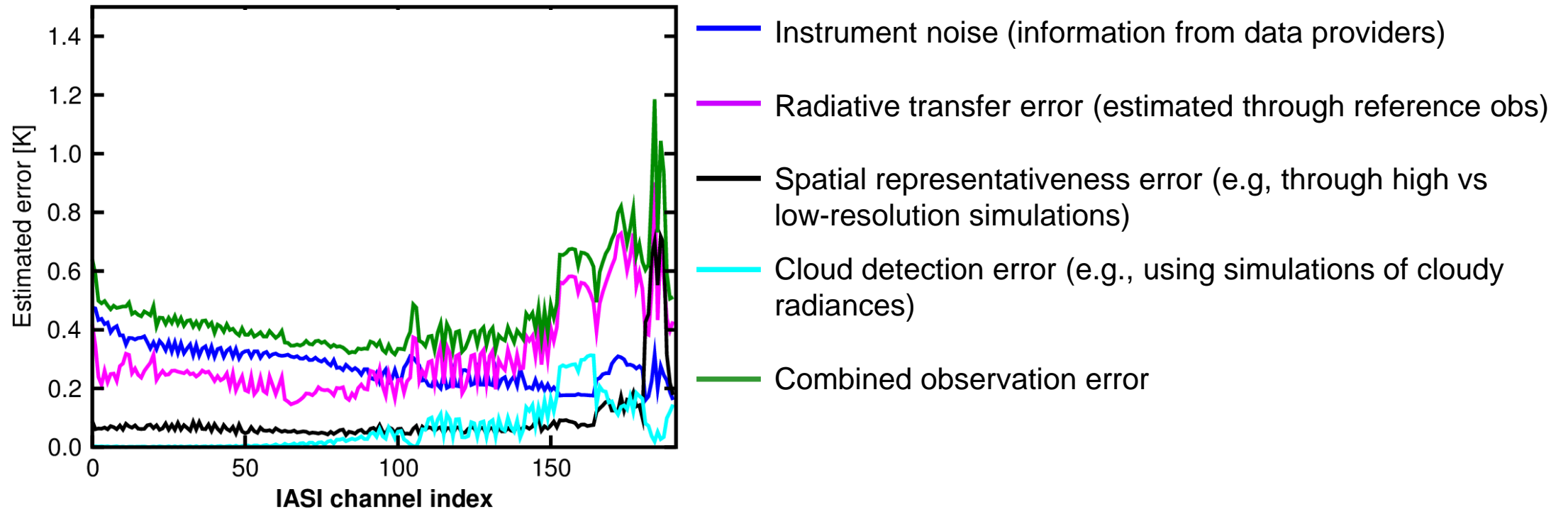
E.g., error due to the cloud detection scheme missing some clouds in clear-sky radiance assimilation



# Error inventory

(e.g., Chun et al 2015)

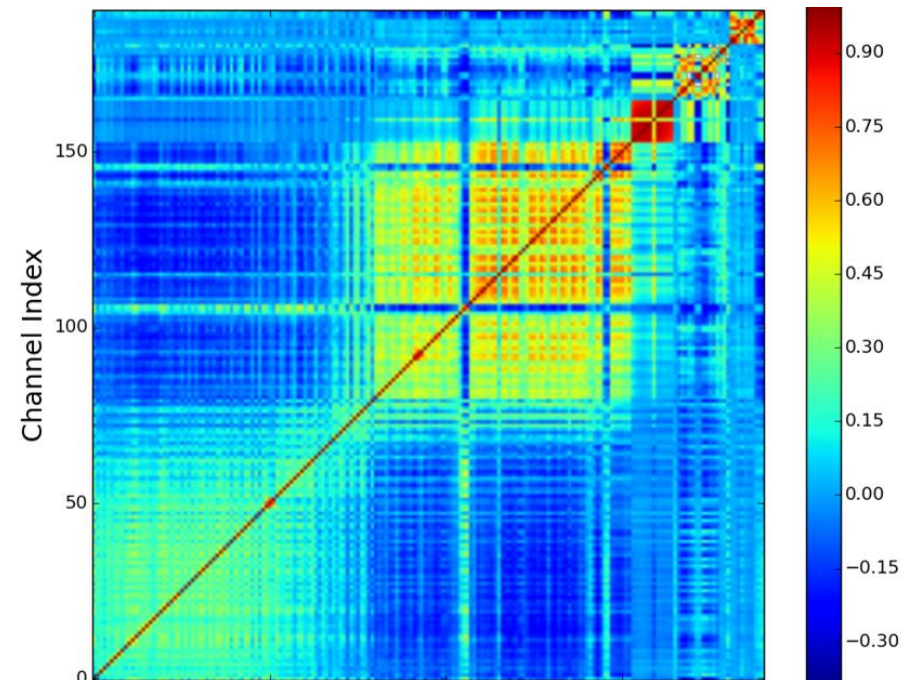
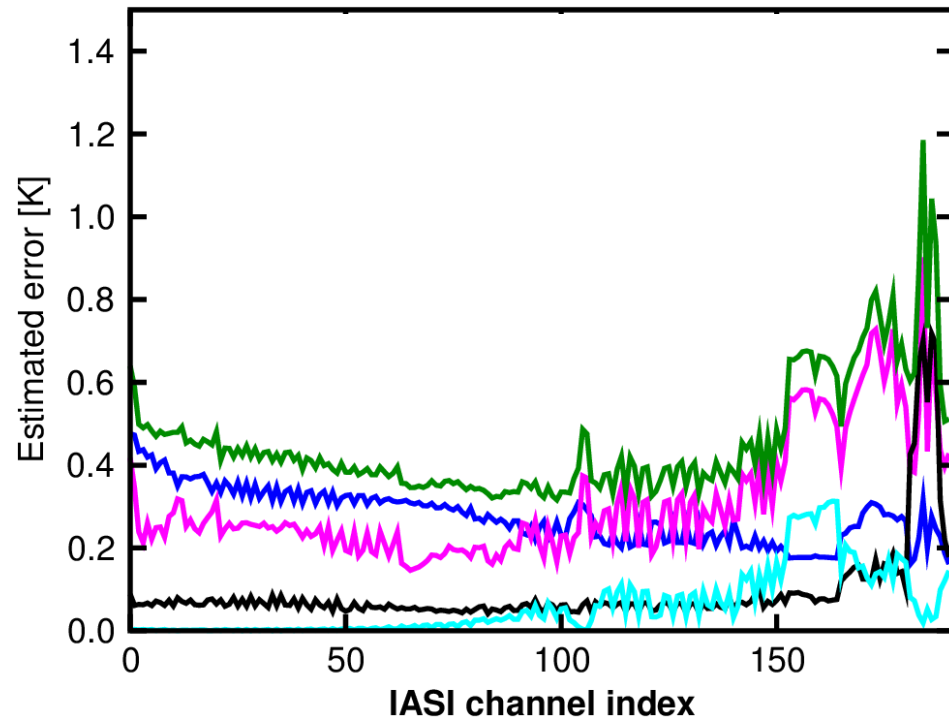
- Idea: Estimate the observation error from **estimates of all uncertainty** contributions.
- Example: error inventory for IASI



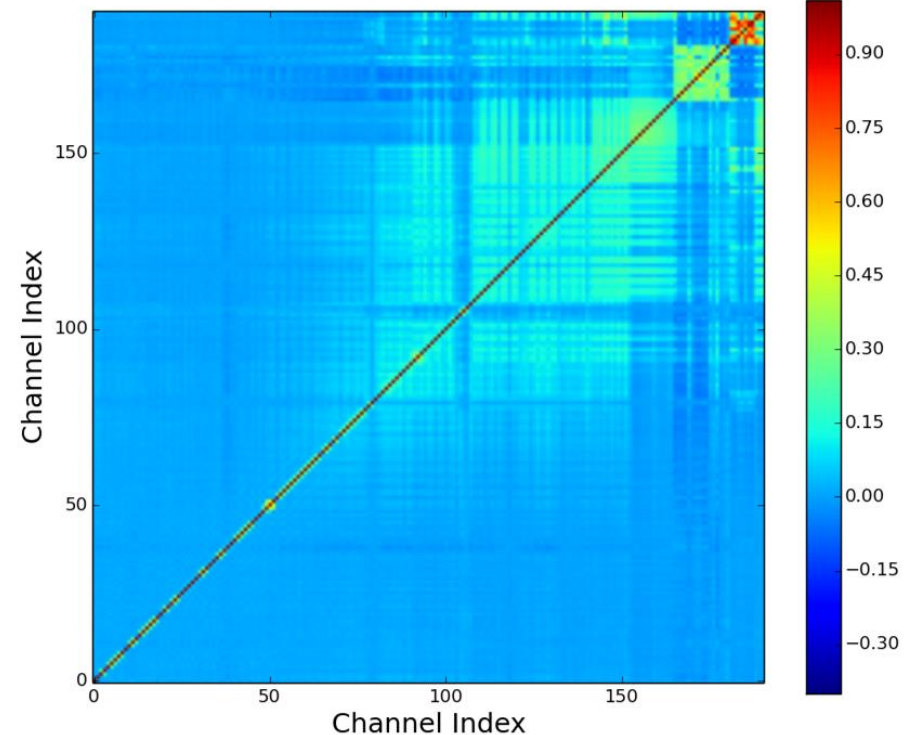
# Error inventory

(e.g., Chun et al 2015)

- Idea: Estimate the observation error from *estimates of all uncertainty* contributions.
- Example: error inventory for IASI



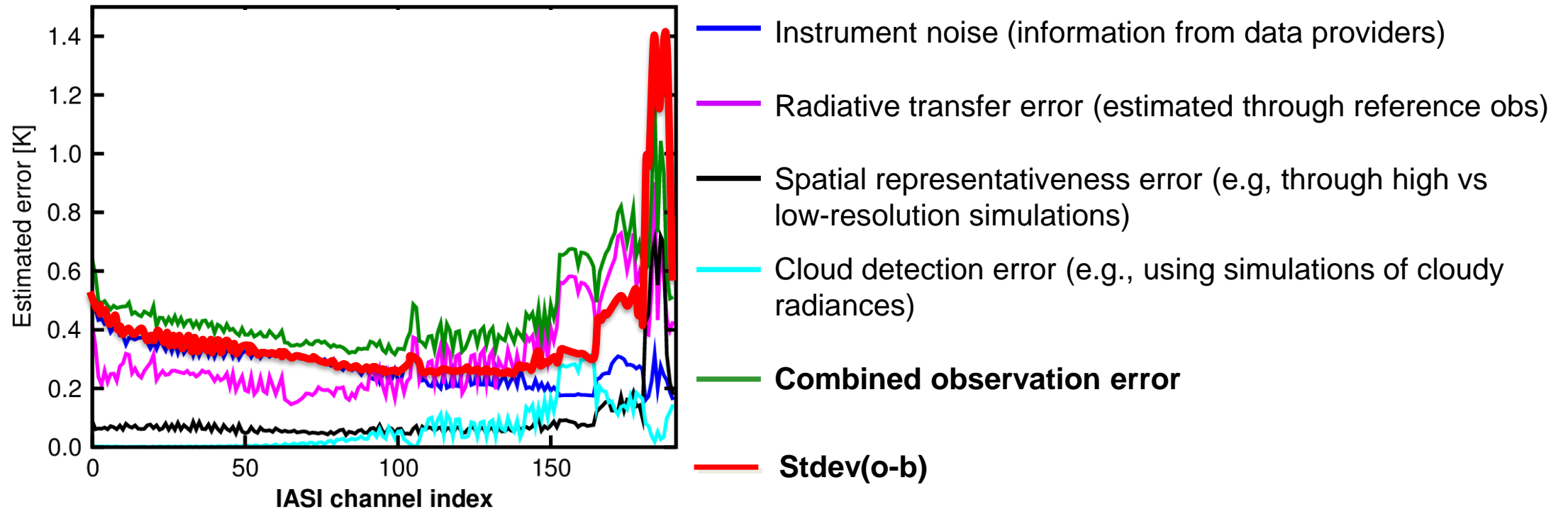
Inventory approach



Diagnosed using Desroziers

## Error inventory ... and closure studies

- How do the separate error estimates compare to the total (observation + background) error estimate from observation departures?
- Here: **Combined observation error estimate alone is (mostly) larger than  $\text{stdev}(\text{o-b})$ .**
  - Overestimation of error contributions?
  - Correlations between background and observation errors (e.g., cloud detection error)?



# Outline

1. Introduction
2. Situation-dependent observation errors
3. Correlated observation errors
4. Error inventories and closure studies
- 5. Summary**

# Summary

- A lot of progress in specifying observation errors in recent years; **more aspects of observation error are being taken into account**.
  - **Situation-dependence** of observation errors increasingly taken into account, based on **physical considerations paired with departure statistics**.
  - **Inter-channel error correlations** are now widely accounted for, using results of **departure-based diagnostics** with some adjustments to specify R.
  - Accounting for **horizontal error correlations** is emerging.
  - Continue to see **significant benefit** for forecast skill from better specifications of observation errors.
- Most sophistications of observation error modelling are based on departure statistics in one way or another.
  - Stdev(o-b), Hollingsworth/Lönnberg, Desroziers, Cov(o-b) – **HBH<sup>T</sup>**; collocated observations/triple collocations
  - All rely on a **range of assumptions**, which may or may not be true.
  - Sometimes **adjustments** are necessary (inflation/reconditioning), sometimes they aren't.
  - **Error inventories** can instead shed light on the dominant sources of error, and they can bring **further independent information** to error modelling.

## Some thoughts for the working groups

- A lot of progress in specifying observation errors in recent years with increased sophistication.
  - But what level of (further) sophistication is useful/desirable?
    - Limitations in the available estimates for specifying R
    - Maintainability of error modelling - responding to changes in the size of error contributions
- What tools do we have to estimate observation errors and how well do they cover our needs?
  - How can we make more use of uncertainty characterisation beyond departure-based diagnostics (e.g., instrument characterisation, metrological approaches, etc)?
- When do observation error correlations matter?
  - Compare, for instance, success of taking inter-channel error correlations into account for hyper-spectral IR vs the diagonal observation error modelling in successful MW all-sky assimilation (where representation error is huge and correlated).
- What aspects of observation error modelling may become more important in the future?
  - E.g., due to higher-resolution analyses; observations with higher temporal resolution; Earth system approaches