Neural networks for post-processing ensemble weather forecasts

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Post-processing with distributional regression models

NWP ensemble forecasts exhibit systematic errors (biases, lack of calibration, . . . ) that require correction via post-processing.

This is achieved via distributional regression models for statistical post-processing which produce forecast distributions.

Example: EMOS for temperature forecasting

Using ensemble predictions of temperature as input the post-processed forecast takes the form of a Gaussian distribution.

\[ y \mid X^{t2m} \sim \mathcal{N}(\mu, \sigma), \]

\[ \mu = a + b \cdot \text{mean}(X^{t2m}) \]

\[ \sigma = c + d \cdot \text{sd}(X^{t2m}) \]
Parametric distributional regression models

Model probability distribution of target variable $y$ given input predictors $X$ by a parametric distribution $F_\theta$,

$$y \mid X \sim F_\theta, \quad \text{where} \quad \theta = g(X)$$

with a link function $g : \mathcal{X} \rightarrow \Theta$ connecting predictors $X$ and distribution parameters $\theta$.

Limitations of fully parametric approaches:

- requires choice of link function $g$
  - difficult to specify functional form of dependencies if many possible predictors are available
- requires estimation of parameters of $g$
  - global (using all training data) or local (location-specific) models?
- requires choice of parametric model $F_\theta$
Neural networks for distributional regression

**Novel semi-parametric approach** to distributional regression: Estimate distribution parameters $\theta$ directly as output of a **neural network** designed to

- learn arbitrary nonlinear relations between predictors and distribution parameters in an automated, data-driven manner,
- generate local adaptivity in globally estimated models,
- gain meteorological insight from trained models.


Data

- 10 years of forecasts and observations (2007–2016)
- 48 hours-ahead ECMWF 50-member ensemble forecasts of temperature (and 17 other variables)
- Station observations at 537 locations
- Data from 2016 used as evaluation set
Neural networks for distributional regression

▶ Input: Predictor variables (NWP quantities, station characteristics).
▶ Output: Distribution parameters $\theta$
▶ Embeddings generate local adaptivity.

Training via CRPS minimization (mathematically principled non-standard choice).
Advanced benchmark methods

- **Gradient boosting** for EMOS (Messner et al., 2017): Let $F_\theta = \mathcal{N}(\mu, \sigma)$ and

\[
(\mu, \sigma) = (x^T \beta, \exp(x^T \gamma)) ,
\]

and iteratively update coefficient vector entries improving the current model fit most.

- **Quantile regression forest** (Meinshausen, 2006; Taillardat et al., 2016): Nonparametric quantile regression based on random forests. Quantile estimates are obtained from an ensemble of decision trees.

Have to be implemented as local models to achieve good forecasts.
## Overview of results

**CRPS**: Continuous ranked probability score, lower is better

<table>
<thead>
<tr>
<th>Model</th>
<th>Mean CRPS for training period</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>2015</td>
</tr>
<tr>
<td>Raw ensemble</td>
<td>1.16</td>
</tr>
</tbody>
</table>

**Benchmark post-processing methods**

<table>
<thead>
<tr>
<th>Model</th>
<th>2015</th>
<th>2007–2015</th>
</tr>
</thead>
<tbody>
<tr>
<td>Global EMOS</td>
<td>1.01</td>
<td>1.00</td>
</tr>
<tr>
<td>Local EMOS</td>
<td>0.90</td>
<td>0.90</td>
</tr>
<tr>
<td>Local EMOS with boosting</td>
<td>0.85</td>
<td>0.80</td>
</tr>
<tr>
<td>Local quantile regression forest</td>
<td>0.95</td>
<td>0.81</td>
</tr>
</tbody>
</table>

**Neural network models**

<table>
<thead>
<tr>
<th>Model</th>
<th>2015</th>
<th>2007–2015</th>
</tr>
</thead>
<tbody>
<tr>
<td>Neural network with auxiliary predictors and station embeddings</td>
<td><strong>0.82</strong></td>
<td><strong>0.78</strong></td>
</tr>
</tbody>
</table>
Station-specific comparison of NN and benchmark models

Station-specific best model is a NN model / benchmark model

NN models perform best at more than 80% of the stations.

Differences are statistically significant at a large fraction of stations.
Meteorological interpretation of neural network models

Change in mean CRPS after permuting a single input variable according to a random permutation across stations and dates.
Incorporating spatial information

Ensemble forecasts are gridded 2D fields of forecasts of weather variables. Thus far, those were interpolated to station locations.

Gridded ECMWF forecasts over Europe (0.5° resolution, 81 × 81 pixels)

However, large-scale spatial structure and predictability information (e.g., ‘weather regimes’) get lost in the interpolation step.
Ensemble information

Ensemble members provide 50 physically coherent forecasts of weather variables. Thus far, only mean and standard deviation of (interpolated) ensemble forecasts were used.

Possibly important uncertainty information might get lost by the use of summary statistics.
Deep autoencoders for dimensionality reduction

Specific NN architectures to learn a compact representation of inputs (unsupervised) by

- training the network to re-create its own inputs
- creating a bottleneck by using fewer hidden units than inputs

- latent information from spatial forecast fields encoded in hidden layer can be used as an additional input to the NN model for distributional regression
Projections of ensemble forecasts (temperature)

Left: Example input forecast fields from two days. 
Middle: Ensemble members in projected space (blue: top, red: bottom). 
Right: Reconstructed fields.
Projections of ensemble forecasts (cloud cover)

Left: Example input forecast fields from two days.
Middle: Ensemble members in projected space (blue: top, red: bottom).
Right: Reconstructed fields.
Autoencoder representations as additional NN-input

1. Autoencoder neural networks for nonlinear dimensionality reduction of spatial input fields

2. Latent representations as additional model input for post-processing

Preliminary results suggest improvements in mean CRPS.
Ongoing joint work with Kai Polsterer.
Neural networks for post-processing ensemble weather forecasts

Summary

- flexible, automated and data-driven modelling of **nonlinear relations** between predictors and distribution parameters
- perform better than **state of the art approaches**
- surprisingly **computationally efficient** and scale well
- gain **meteorological insight** from trained models
