



Karlsruhe Institute of Technology
Chair of Statistics and Econometrics

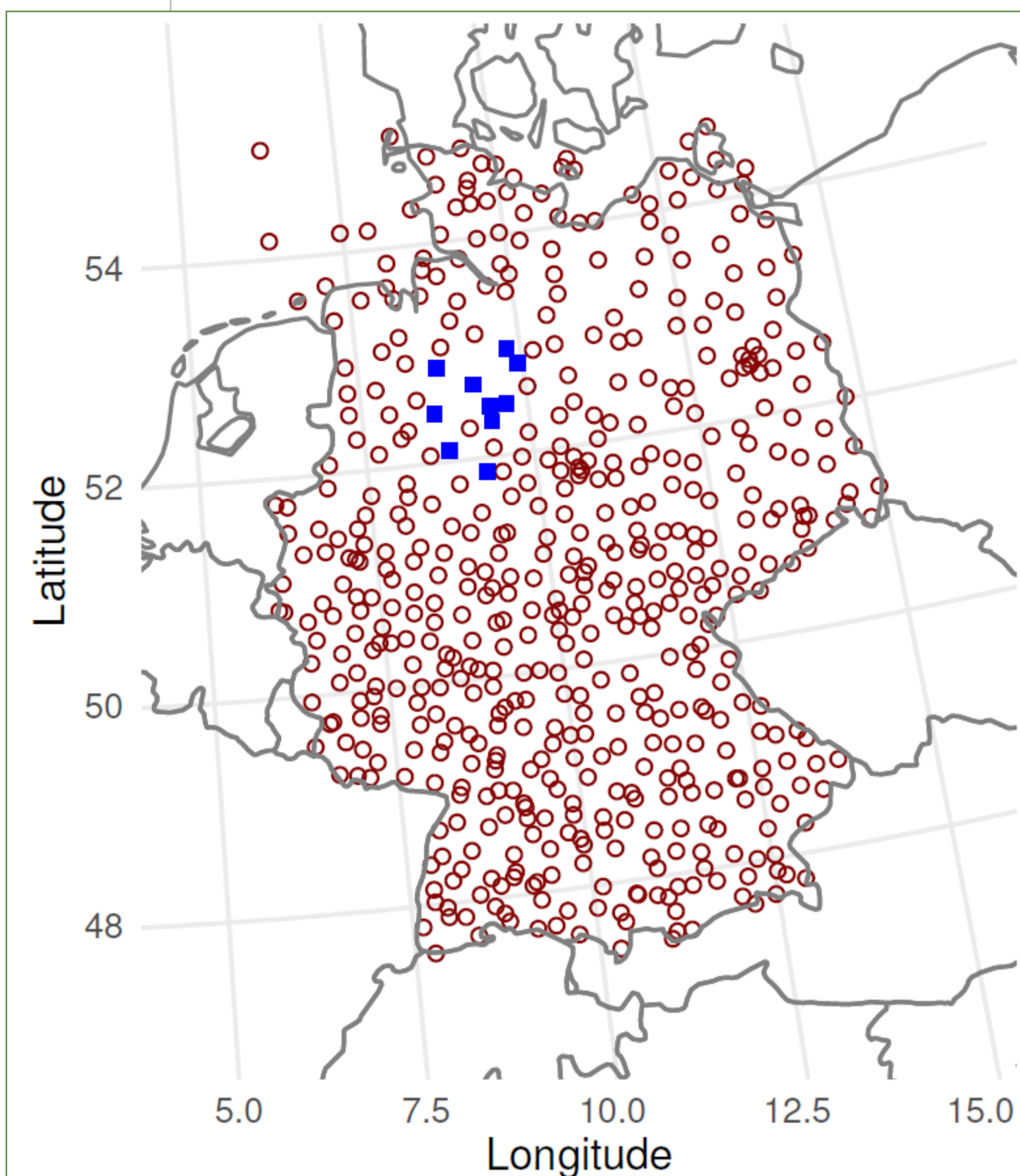


Fig. 1: Locations of weather stations in the dataset; Spatial dependence between 10 nearby stations of temperature forecast is considered in this study.

Multivariate post-processing techniques are developed to retain the spatial, temporal, or inter-variable dependencies that univariate post-processing fails to preserve.

- Forecast data from ECMWF, with 50 ensemble members; The same dataset as has been used in Rasp and Lerch (2018)¹.
- 10 years of data available, splitting into training (2007–2014), validation (2015), and test (2016) sets.
- Focusing on preserving the **spatial** dependency (multiple locations) of **temperature** forecast in multivariate post-processing.
- Auxiliary weather variables: 'd2m', 'cape', 'q_pl850', 'sp', 'tcc', 'u_pl500', 'u_pl850', 'v_pl500', 'v_pl850', 'gh_pl500', 'u10', 'ssr', 'v10', 'str', 'sshf', 'slhf'.

Standard approaches for multivariate post-processing:

- Copula-based, two-step methods;
 - First post-process ensemble forecasts univariately;
 - Then reorder post-processed samples to reintroduce multi-dimensional dependencies, based on the rank order structure learned from
 - raw ensemble members (**ensemble copula coupling², ECC**),
 - or a set of historical observations (**Schaake shuffle³, SSh**),
 - or a fitted Gaussian copula (**Gaussian copula approach⁴, GCA**).

Generative machine learning models

[build upon the work of Janke and Steinke (2020)⁵]

- Conceptually simpler, new class of data-driven multivariate distributional regression models;
- Multivariate probabilistic forecasts are directly obtained as output, bypassing the copula-based two-step approaches;
- Allows generation of unlimited number of post-processed samples;
- Enables incorporating additional weather variable information into the multivariate post-processing;

Inputs: mean and variance of target variable x and auxiliary variables $a_i (i = 1, 2, \dots)$

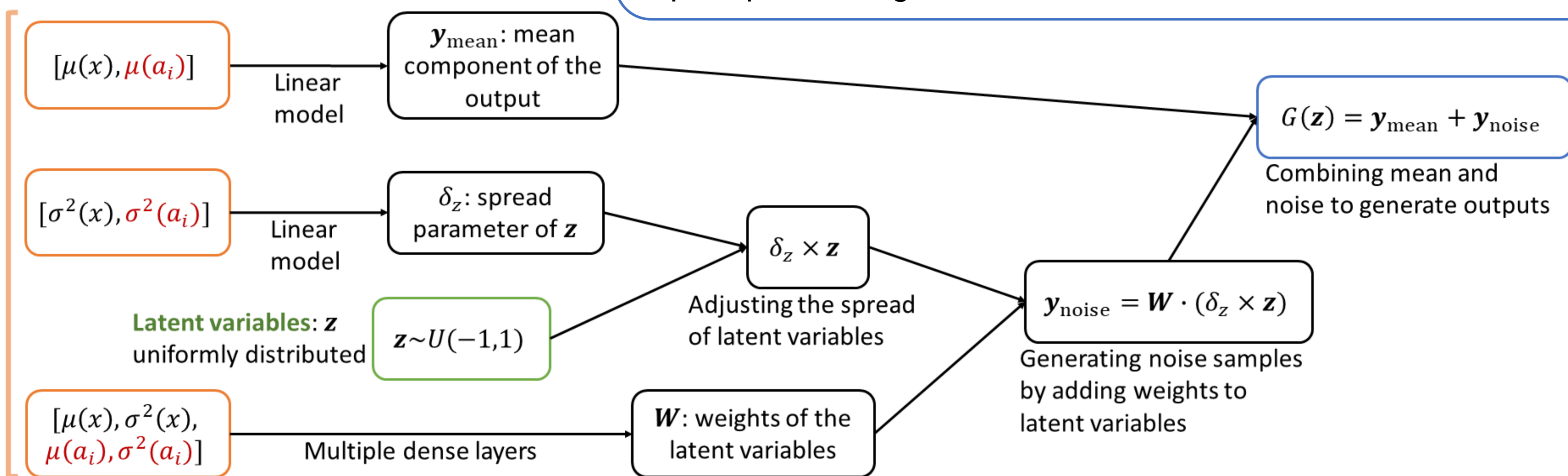


Fig. 2: Structure of the generative machine learning model for multivariate post-processing; The model is trained to minimize the energy score using stochastic gradient descent methods.

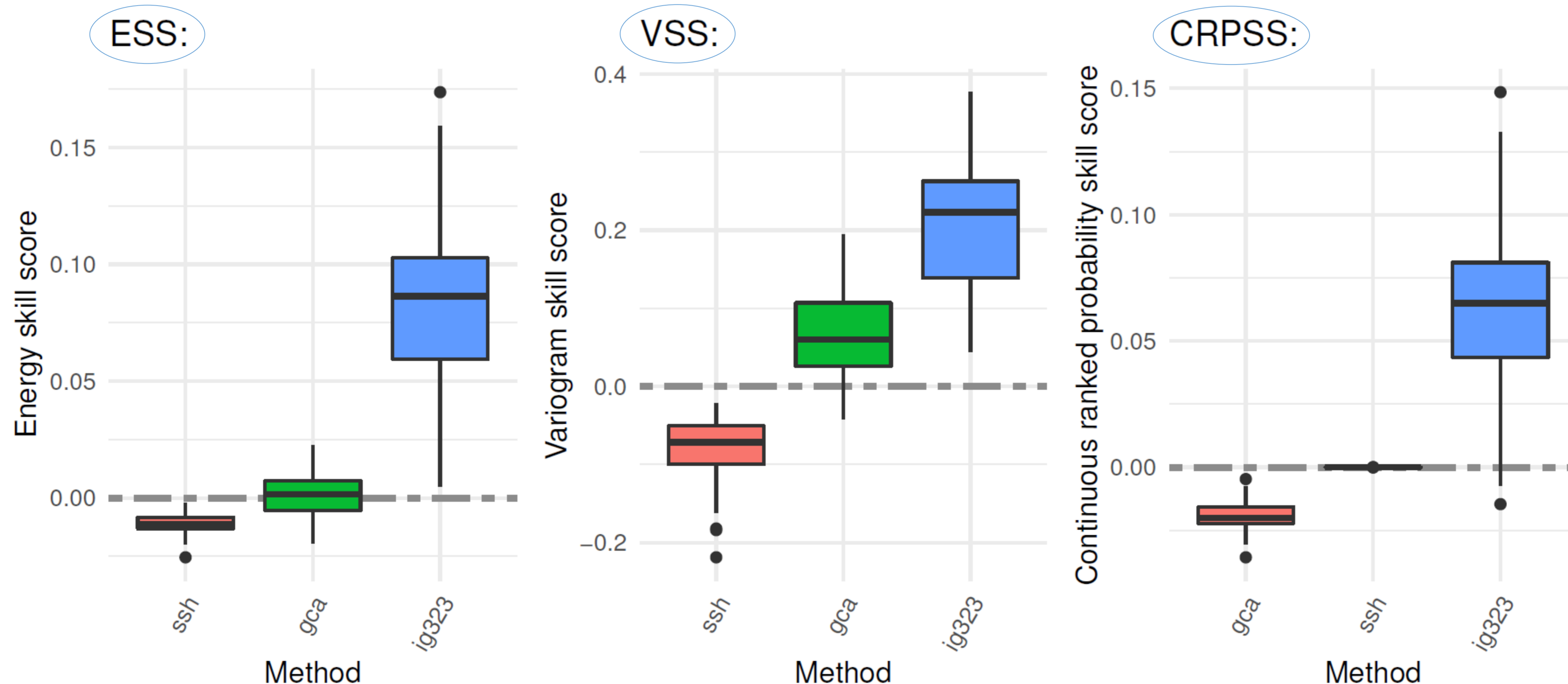


Fig. 3: Boxplots of skill scores for different multivariate post-processing approaches; Comparison between Schaake shuffle ('ssh'), Gaussian copula approach ('gca'), and the generative ML model ('ig323'); All skill scores are computed taking ECC as the reference forecast, using energy score, variogram score, and continuous ranked probability score.

References:

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