

# Physics-Informed Learning of Aerosol Microphysics

---

Paula Harder

# Content

Motivation

Data & Model

Physics-Informing

Results

---

Work done with:  
Duncan-Watson Parris, Philip  
Stier, Janis Keuper, Dominik  
Strassel and Nico Gauger

# Motivation



# What are aerosols?

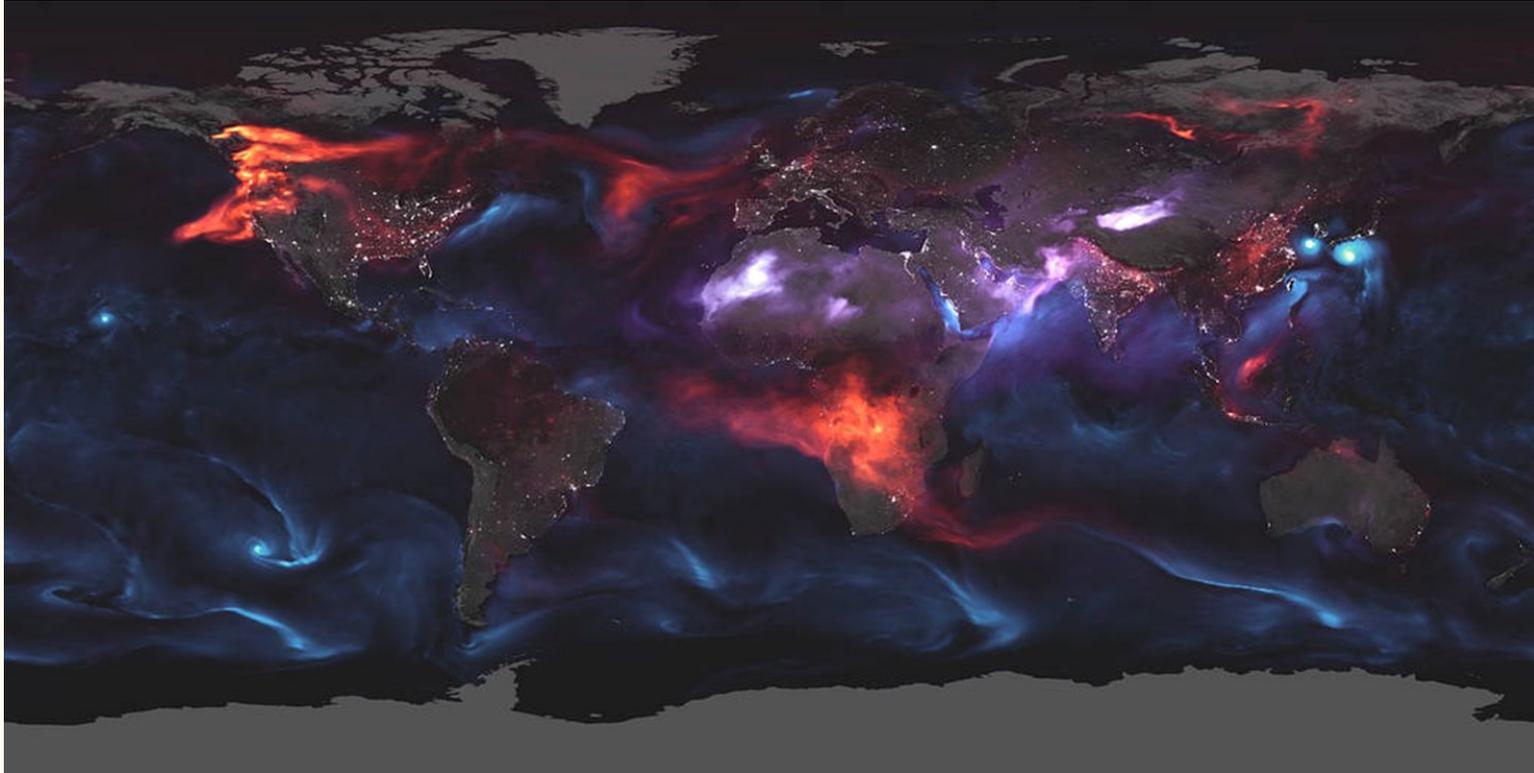
An aerosol is a suspension of fine solid particles or liquid droplets in air or another gas

Important atmospheric aerosols: Dust, sea salt, black carbon, organic carbon, sulphates

Natural and anthropogenic sources: Volcanic eruptions, forest fires, fossil fuel burning

Affecting the climate by aerosol-cloud and aerosol-radiation interactions

# Aerosols



Red - black carbon, purple - dust, blue - sea salt

# Motivation

Most climate models do not include aerosols in detail and if they are included the computational costs do make long-term high-resolution runs impossible

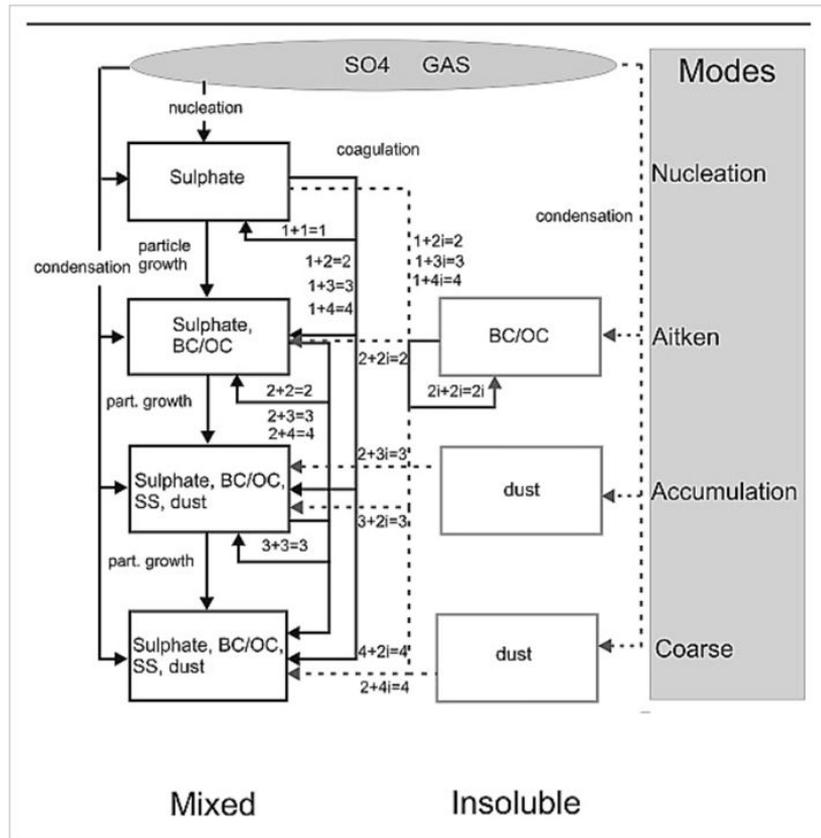
Idea: Replace original computationally expensive model with cheap ML model = Emulation

The machine learning model is trained once offline and we benefit from fast inference time online

# Data & Model



# Aerosol Microphysics Model M7



Aerosol microphysics model by  
Vignati et al. 2004

Different aerosol types modeled with  
size bins

M7: An efficient size-resolved aerosol microphysics module for  
large-scale aerosol transport models, Vignati et al. 2004

# Data generation

Input data generated from runs of global aerosol-climate model ECHAM-HAM

Output data generated with M7 aerosol microphysics box model

~5.5M data points for training, ~3M for validation, ~3M for testing, each from different days spread out through the year

# Data

Idea: Same input and output as traditional model, e.g. no spatial information

Predict one time step for fixed time step length, here 450s

32 input and 30 output variables

Input/Output: 26 values for masses and numbers of different aerosol types

Input only: Atmospheric variables, temperature, pressure, RH, ...

Output only: Water content of aerosols

# Data challenges

Changes in variables are small to full variables → we model changes and evaluate on changes

Changes themselves are exponentially distributed

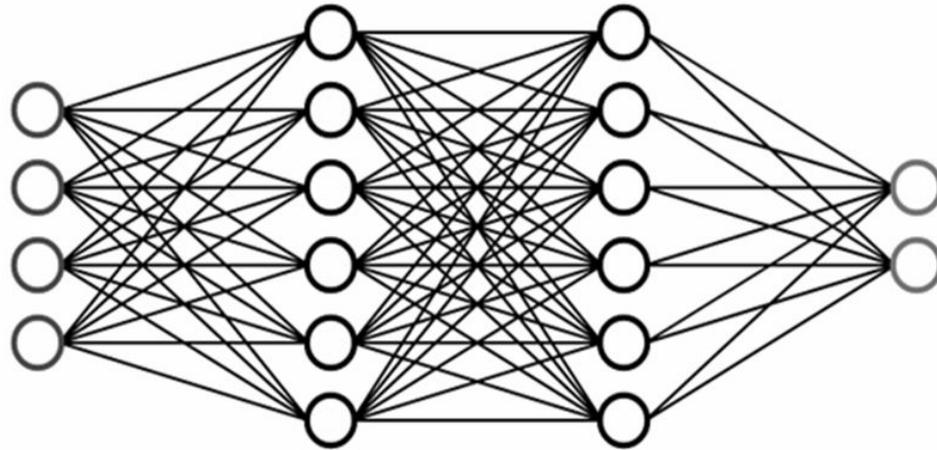
We compare using logarithmically transformed and just standardized variables

Log-transformation requires an additional network to classify whether a change is positive or negative

# Network architecture

Neural network with 2 hidden layers, 256 nodes per hidden layer, ReLU activation

Inputs:  
Temperature, RH,  
pressure,...  
Aerosol masses  
Aerosol number



Outputs:  
Change in aerosol  
masses  
Change in aerosol  
numbers  
Water content

# Physics-Constraining

—

# Equality and inequality constraints

Let  $x$  be the NN's input and  $y$  the output,  $h, g$  (linear) functions

**Equality constraints:**

$$h(x, y) = 0$$

**Inequality constraints:**

$$g(x, y) \geq 0$$

# Soft vs. Constraining

Let  $\tilde{y}$  be the target

**Soft constraining:** The NN's loss  $L$  is extended by additional terms

$$L(y, \tilde{y}) := \|y - \tilde{y}\|^2 + \lambda \text{ Penalizer term}$$

**Hard constraining:** Enforce constraints in additional network layer



# Soft Constraints

$$L(x, y, \tilde{y}) := \|y - \tilde{y}\|^2 + \underbrace{\lambda \|h(x, y)\|^2}_{\text{equality constraints}} + \underbrace{\mu \|\text{ReLU}(-g(x, y))\|^2}_{\text{inequality constraints}}$$

**Equality constraints:** Minimizing  $\|h(x, y)\|$  encourages the NN to output  $y$ , such that  $h(x, y)$  is close to  $0$

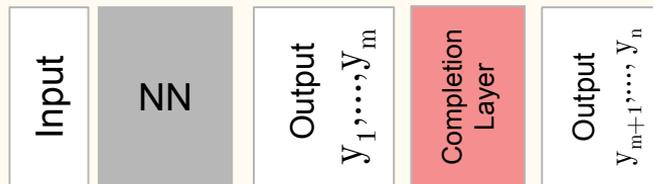
**Inequality constraints:**  $\text{ReLU}(z) = \max(0, z)$ , it sets the negative part to  $0$ .

Minimizing  $\|\text{ReLU}(-g(x, y))\|$  encourages the NN to output  $y$ , such that  $g(x, y)$  is positive

# Hard Constraints

**Equality constraints:** Output partial set  $(y_1, \dots, y_m)$  and then calculate  $(y_{m+1}, \dots, y_n)$ , such that  $h(x,y)=0$

This process is called **completion**



**Inequality constraints:** If  $g(x,y) < 0$  then set  $y$  such that  $g(x, y) \geq 0$

Example: Constraint is that  $y \geq 0$ . If  $y_i < 0$  then set  $y_i = 0$

This process is called **correction**



# Our Constraints

## Mass conservation - Equality constraints

Let  $S = \{\text{SO}_4, \text{DU}, \text{OC}, \text{BC}\}$  be the set of aerosol species. For every  $s \in S$  let  $I_s$  be the indices of our output  $y$  corresponding to value of that species. Mass conservation is given by

$$\sum_{i \in I_s} y_i = 0$$

**Soft constraining:** Add loss term  $\|\sum_{i \in I_s} y_i\|^2$

**Hard constraining:** Choose  $j \in I_s$  and set  $y_j := -\sum_{i \in I_s \setminus \{j\}} y_i$

# Our Constraints

## Mass positivity - Inequality constraints

All predicted masses have to be positive. For our input  $x$  (masses at time 0) and our output  $y$  (change in mass), the constraint is

$$y+x \geq 0$$

**Soft constraining:** Add loss term  $\|\text{ReLU}(-(y+x))\|^2$

**Hard constraining:** Add correction layer  $\{\text{If } y_i+x_i < 0 \text{ then set } y_i = -x_i\}$

# Results



# Results - Log vs Linear

Better performance with log transformed data in log-scale

Transformation	Linear	Log-Scale
R <sup>2</sup>	0.763	0.974
MSE	0.162	0.030

Original units/linear scaling probably more relevant for application

# Results - Mass conservation

Soft constraining with mass loss term decreases mass violation of each aerosol species, but accuracy is decreased too

Hard constraining with completion procedure guarantees mass conservation, but also decreases accuracy

Model	Base NN	NN + mass loss	NN + completion
R <sup>2</sup>	0.763	0.730	0.738
Mass Bias SO4	0.000011	0.0000086	0
Mass Bias BC	0.000038	0.000034	0
Mass Bias OC	0.000033	0.000011	0
Mass Bias DU	0.000001	0.00000028	0
Overall Mass Violation	0.00037	0.00014	0

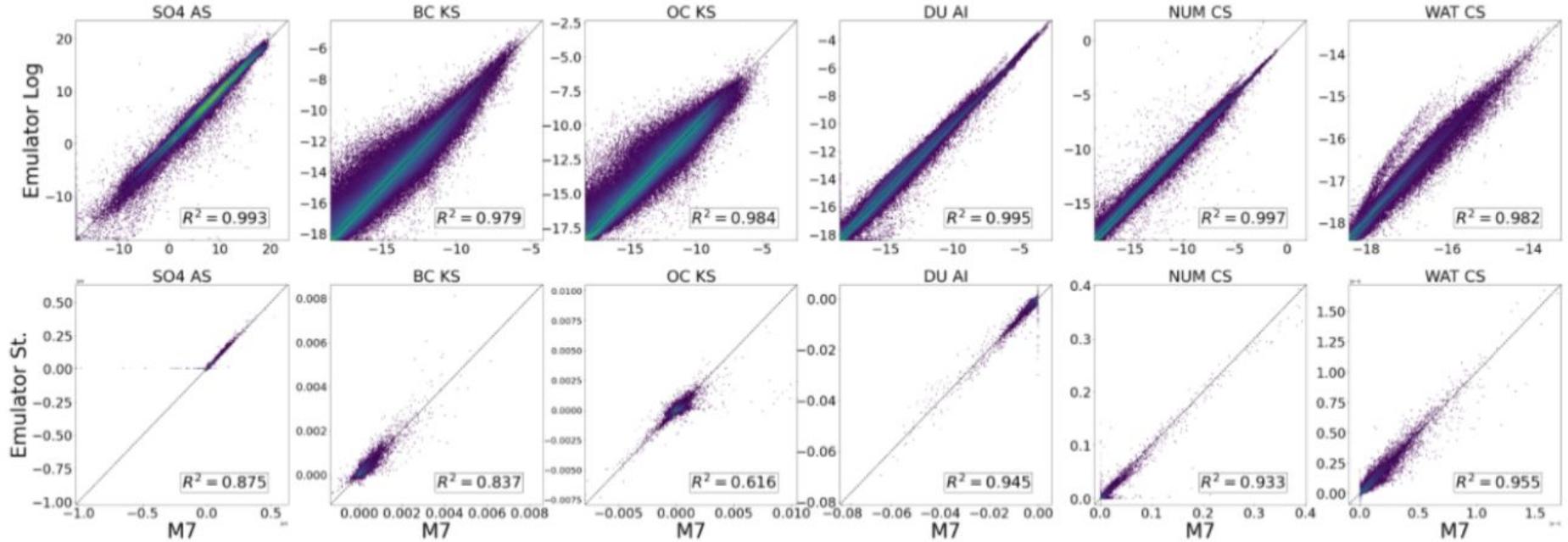
# Results - Positivity

Soft constraining with positivity loss decreases negative fraction and negative mean, but also accuracy

Hard constraining with correction procedure guarantees no negative values and also increases accuracy

Model	NN Base	NN + Positivity Loss	NN + Correction
R <sup>2</sup>	0.763	0.709	0.771
Negative Fraction	0.134	0.0894	0
Negative Mean	0.00151	0.000081	0

# Results - Plots



# Results - Speed-ups

Runtimes for the prediction of one global time step:

Model	M7	NN pure GPU	NN CPU-GPU-CPU	NN CPU
Time (s)	5.781	0.000517	0.0897	2.042
Speed-up	1	11181.8	64.4	2.80

# Summary & Outlook

Neural networks can accurately emulate aerosol microphysics model

We can incorporate physical constraints with hard constraining to make the emulator feasible for a stable global climate model run

A significant speed-up, especially on a GPU can be achieved

Next step: Implement neural network emulator in Fortran and integrate into global climate model

Thanks for your attention!

