

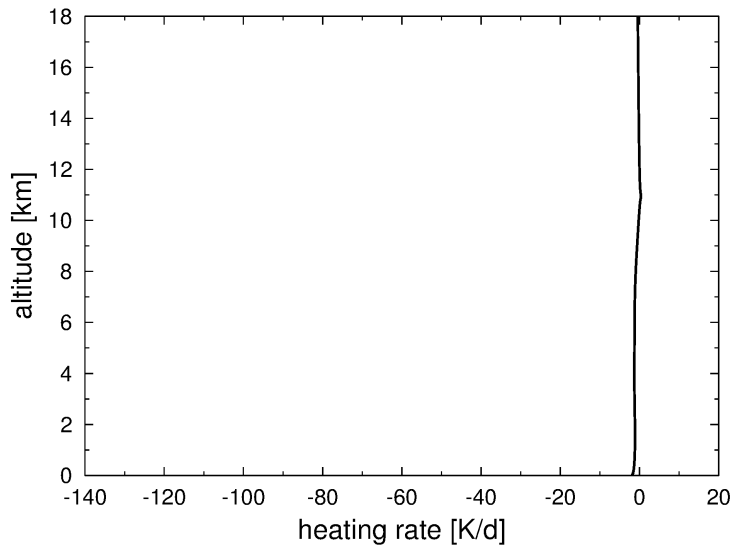
# A Dynamic Approach to 3D Radiative Transfer in NWP Models

Bernhard Mayer, Richard Maier, Fabian Jakub

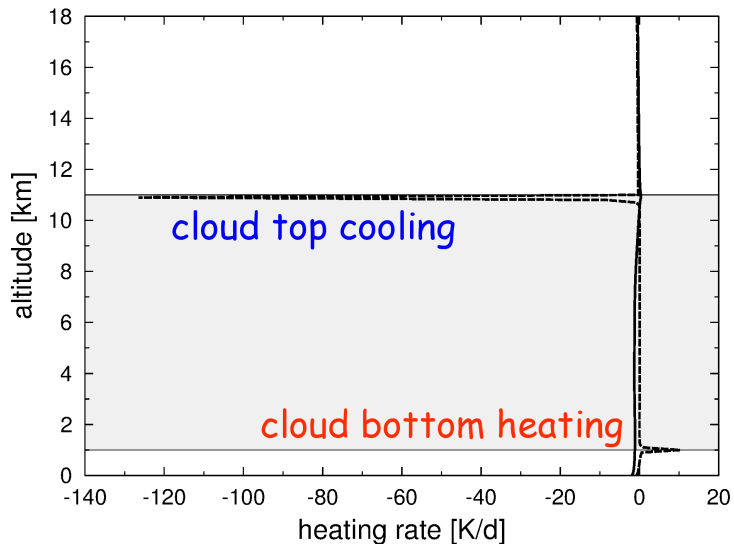
Ludwig-Maximilians-Universität (LMU)  
Theresienstrasse 37, 80333 München, Germany

September 14, 2022

# Radiative Heating and Cooling: Thermal (1D)



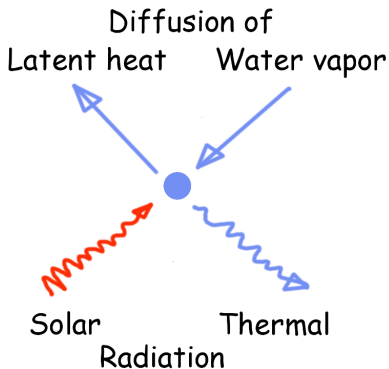
# Radiative Heating and Cooling: Thermal (1D)



# Potential Effects of Radiation on Clouds

- Droplet growth affected by absorption/emission of radiation
- Effect of heating/cooling rates on dynamics
- Differential heating of the surface (cloud shadows)

# Radiative Heating and Cooling: Microscopic View



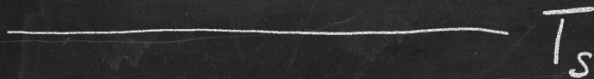
# Analytical 3D Thermal Heating and Cooling Rates

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no atmosphere!  
("vac")

# Analytical 3D Thermal Heating and Cooling Rates





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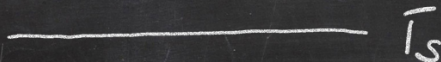


# Analytical 3D Thermal Heating and Cooling Rates

Let's assume a convex cloud:



cloud surface area  
 $A_0$



$\bar{T}_s$

# Analytical 3D Thermal Heating and Cooling Rates

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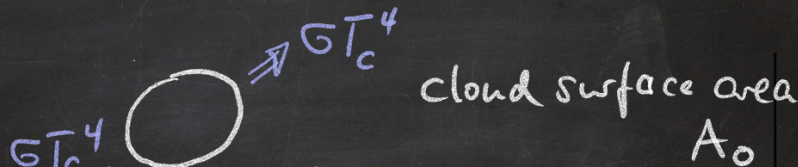


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$$\dot{Q}_{em, vac} = A_0 \cdot \sigma T_c^4$$

# Analytical 3D Thermal Heating and Cooling Rates

Let's assume a convex cloud:



$$\dot{Q}_{em, vac} = A_0 \cdot \sigma T_c^4$$

$$\dot{Q}_{abs, rec} = \frac{1}{2} A_0 \sigma T_s^4 \text{ (only from below)}$$

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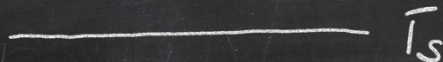
$$\dot{Q}_{rad, vac} = \dot{Q}_{abs, vac} - \dot{Q}_{em, vac} = A_0 \sigma \left( \frac{1}{2} T_s^4 - T_c^4 \right)$$

# Analytical 3D Thermal Heating and Cooling Rates

And now: 1D (independent column approximation)

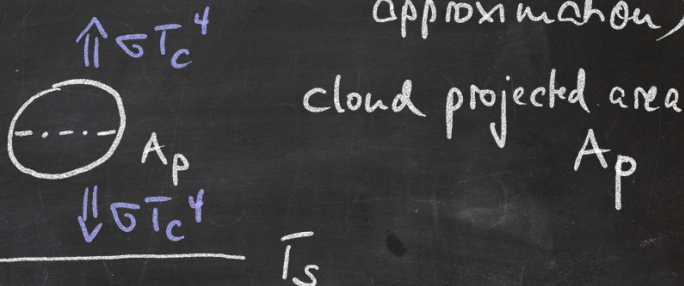


cloud projected area  
 $A_p$



# Analytical 3D Thermal Heating and Cooling Rates

And now: 1D (independent column approximation)



$$\dot{Q}_{em, vac, 1D} = 2 \cdot A_p \cdot \sigma T_c^4$$



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# Analytical 3D Thermal Heating and Cooling Rates

And now: 1D (independent column approximation)



$$\dot{Q}_{em, vac, 1D} = 2 \cdot A_p \cdot \sigma T_c^4$$

$$\dot{Q}_{abs, vac, 1D} = A_p \cdot \sigma \cdot T_s^4$$

$$\dot{Q}_{rad, vac, 1D} = A_p \cdot \sigma \cdot (T_s^4 - 2T_c^4)$$

# Analytical 3D Thermal Heating and Cooling Rates

For example: Cube with length  $d$ :

$$A_o = 6d^2$$

$$A_p = d^2 = \frac{1}{6} A_o$$



$$\Rightarrow \underline{\dot{Q}_{\text{rad}, 3D} = 3 \cdot \dot{Q}_{\text{rad}, 1D} !}$$

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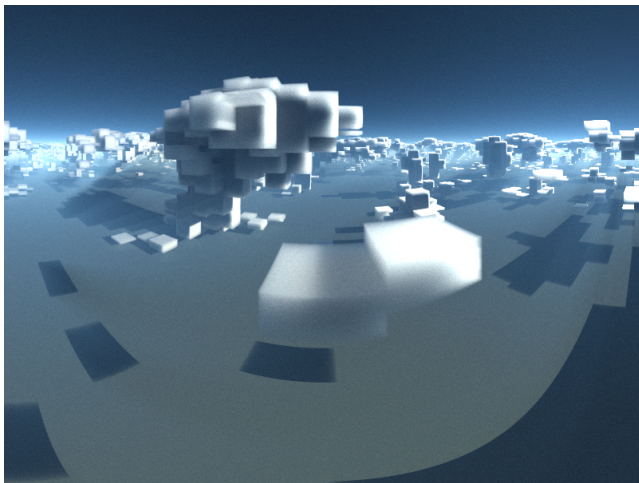


$$\Rightarrow \underline{\dot{Q}_{\text{rad}, 3D} = 3 \cdot \dot{Q}_{\text{rad}, 1D} !}$$

Sphere instead of cube:

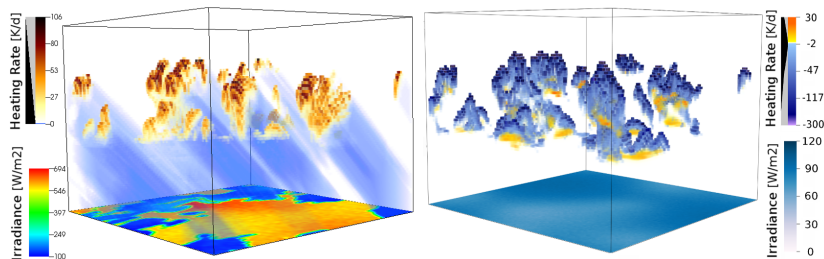
Factor 2 instead of 3

# Model clouds are often cubes!



MYSTIC visualization of 2km “convection-permitting” model output

# Of course we can do much better than that!

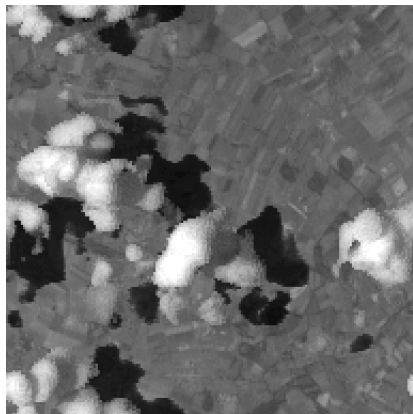


MYSTIC simulation: Carolin Klinger, Fabian Jakub, HD(CP)2  
*Monte Carlo Code for the physically correct tracing of photons  
in cloudy atmospheres, e.g. Mayer, 2009*



## Monte carlo code for the phySically correct Tracing of photons In Cloudy atmospheres

*Mayer, 2009; Buras, Emde, Klinger, ...*



# Effects: Cloud Streets (Jakub and Mayer, 2017)



**Figure 1.** Virtual photograph of LES simulations at a cruising altitude of 15 km. Top panel: cloud formation of a simulation driven by 3D radiation (TenStream with **sun in the east, i.e. right** ( $\varphi = 90^\circ$ )). Lower-panel: cloud formation of a simulation which was performed with 1D radiation (Two-stream). The specific model setup is the same as referenced in fig. 2 i.e., no background wind and a continental land surface. The simulations differ with respect to cloud size distributions and the organization in cloud streets, the cloud fraction though is the same (27%). The visualization was performed with a physically correct rendering with MYSTIC (MonteCarlo solver in libRadtran (Mayer, 2009, Emde et al. 2015)). **SZA = 60°**



# Effects: Cloud Organization (Klinger et al, 2017)



const.  
cooling



3D avg



3D

Imagine a perfect world !

# Radiative Transfer in NWP Models

High spectral resolution  
(ideally line-by-line)

Imagine a perfect world!

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3D radiative transfer  
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High spectral resolution  
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Imagine a perfect world!

High calling frequency  
(to capture variability  
of clouds)

High spatial resolution  
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# Radiative Transfer in NWP Models

Correlated- $k$   
(few bands)

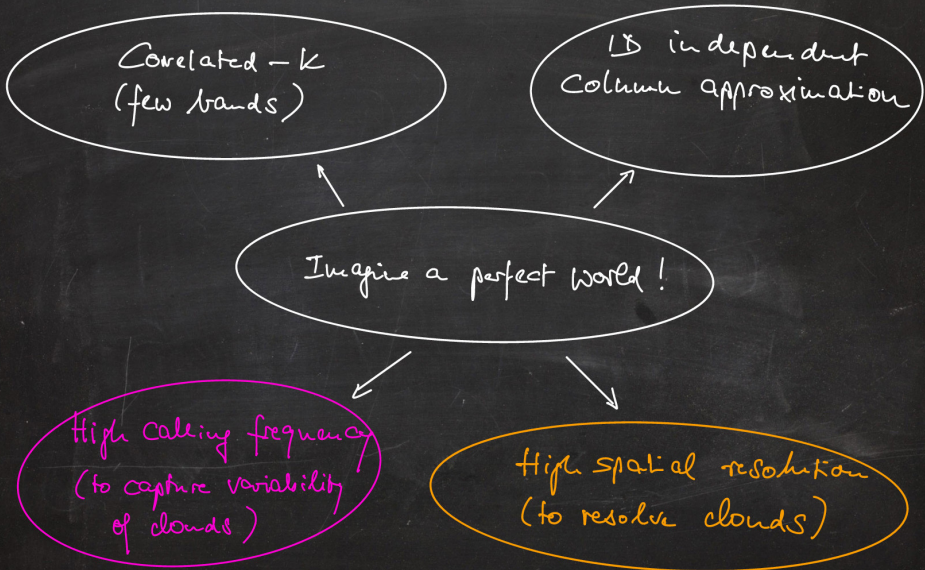
3D radiative transfer  
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Imagine a perfect world!

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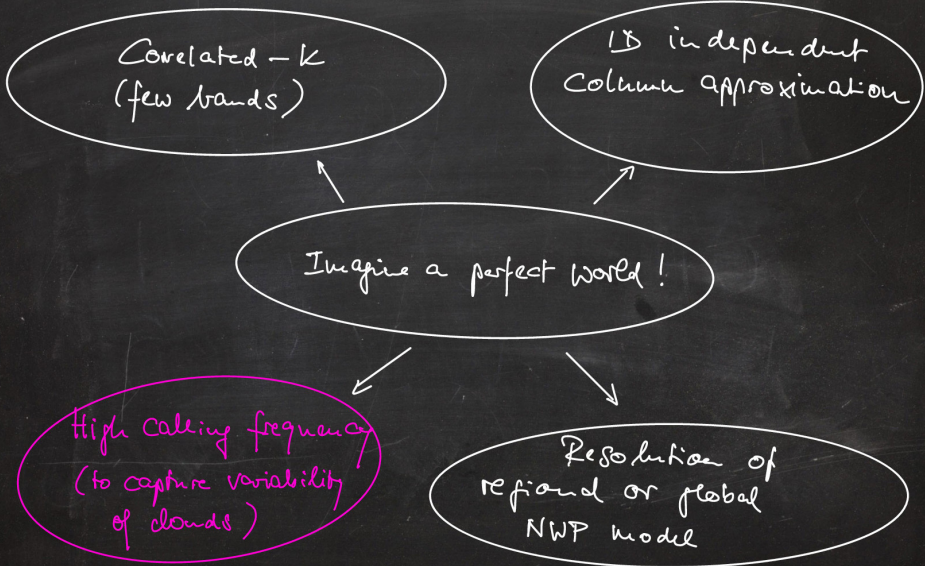
High spatial resolution  
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# Radiative Transfer in NWP Models





# Radiative Transfer in NWP Models



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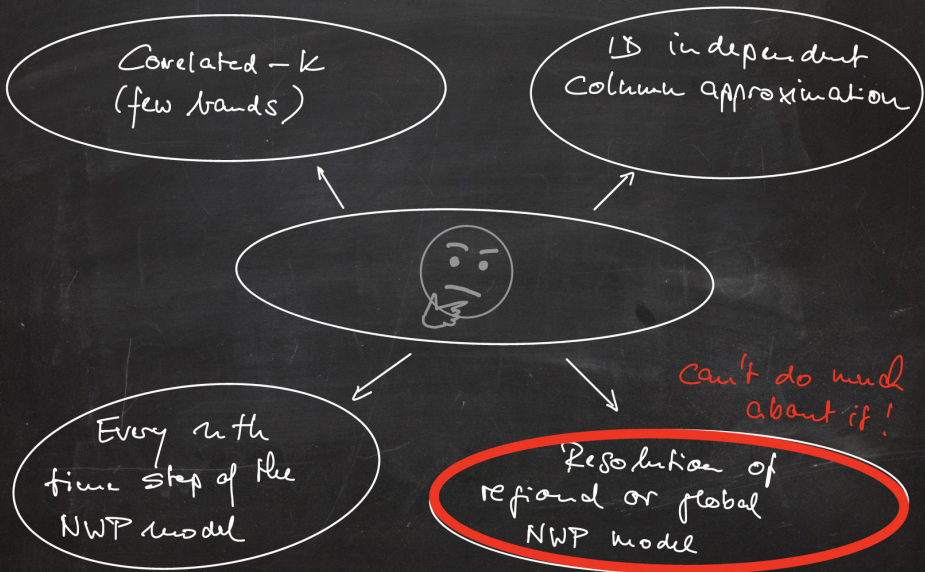
1D independent  
column approximation

Imagine a perfect world!

Every 2th  
time step of the  
NWP model

Resolution of  
regional or global  
NWP model

# Radiative Transfer in NWP Models



# Radiative Transfer in NWP Models

Correlated -k  
(few bands)

1D independent  
column approximation

need even less!



Every nth  
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Resolution of  
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can't do much  
about it!

# Radiative Transfer in NWP Models

Correlated -k  
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1D independent  
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*need even less!*

Every nth  
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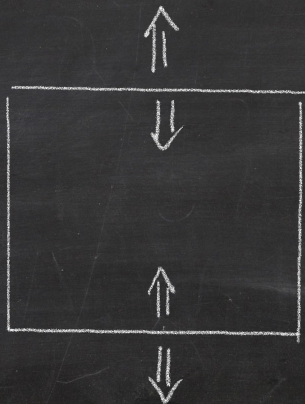
*can't do much  
about it!*

Resolution of  
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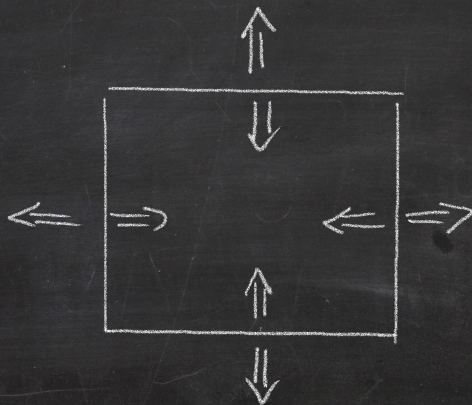
# The Tenstream Solver (Mayer and Jakub, 2015 a,b)



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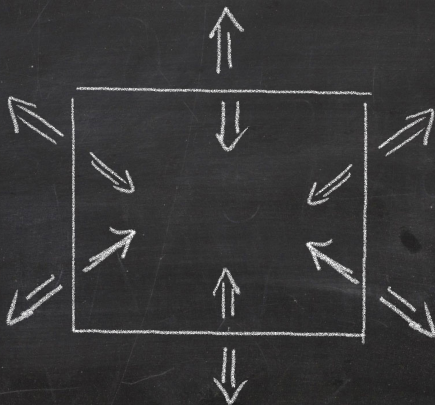


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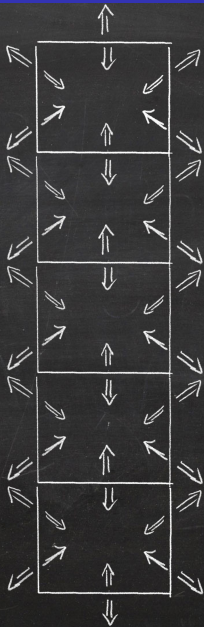




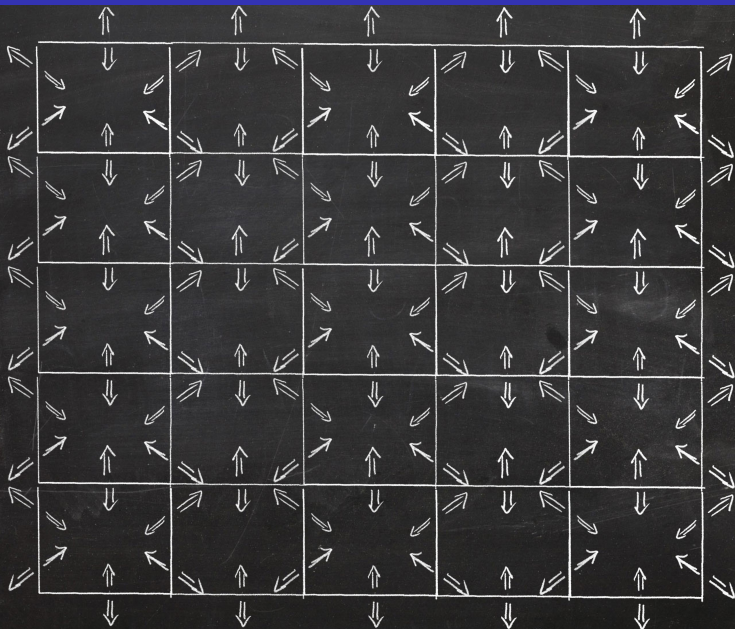
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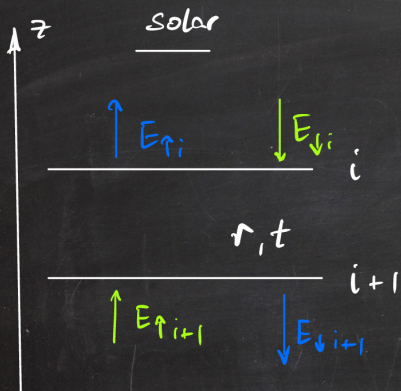
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# "Dynamic RT"



$$E_{\uparrow i} = r \cdot E_{\downarrow i} + t \cdot E_{\uparrow i+1}$$

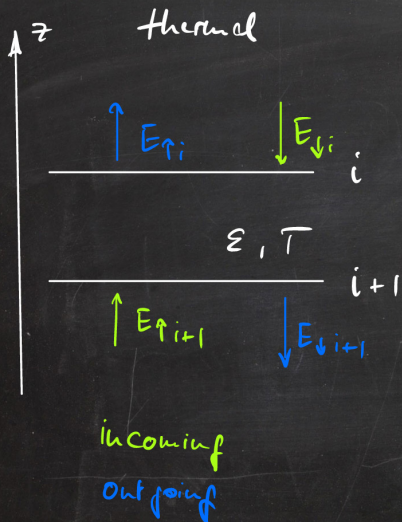
$$E_{\downarrow i+1} = t \cdot E_{\downarrow i} + r \cdot E_{\uparrow i+1}$$

for  $n$  model layers  
→ linear equation system

alternatively iterative  
solution = "dynamic RT"

incoming  
outgoing

# "Dynamic RT"



$$E_{\uparrow i} = (1-\varepsilon)E_{\uparrow i+1} + \varepsilon\sigma T^4$$

$$E_{\downarrow i+1} = (1-\varepsilon)E_{\downarrow i} + \varepsilon\sigma T^4$$

for  $n$  model layers:

upward/downward recurrence

≡ iterative solution

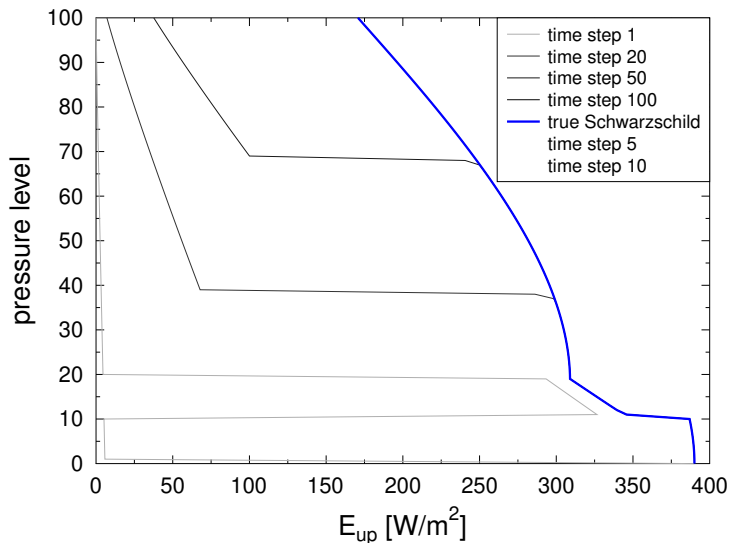
= "dynamic RT"

"Gauss-Seidel"

# “Dynamic RT” – 1D , static cloud, upward flux

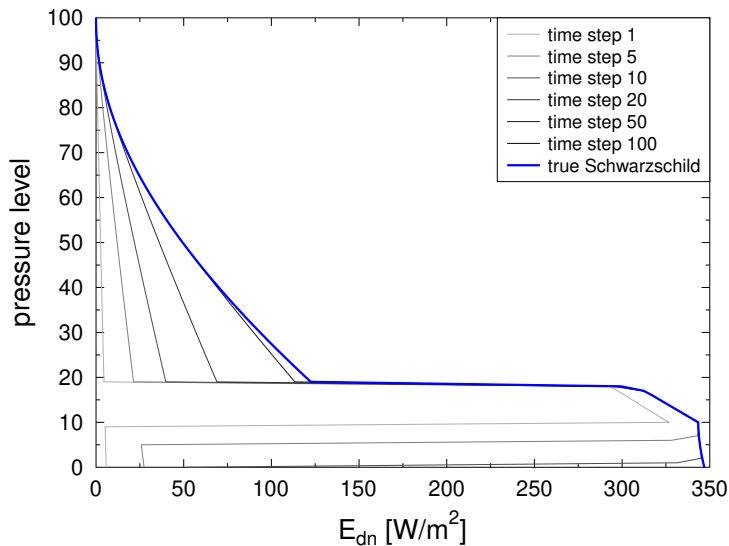
# “Dynamic RT” – 1D, static cloud, downward flux

# Dynamic RT – if the movies won't work





# Dynamic RT – if the movies won't work



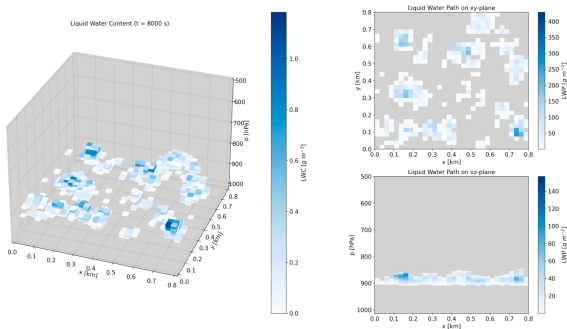
# “Dynamic RT” – 1D , variable cloud, upward flux

# “Dynamic RT” – 1D , variable cloud, downward flux

# Dynamic RT – how good is it?

## Cloud and Model Setup

100 time steps of a precomputed LES cloud field with a temporal resolution of 10 s

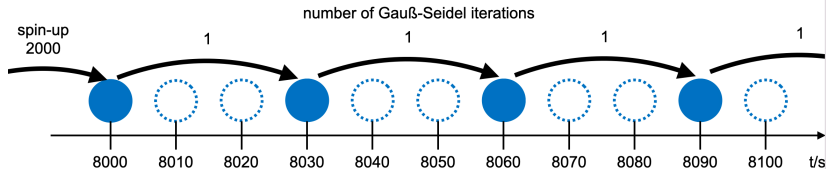


- shallow cumulus cloud field
- 149 vertical layers, 32 x 32 grid boxes in the horizontal
- grid boxes have the same shape and LWC as in the original 256 x 256 domain

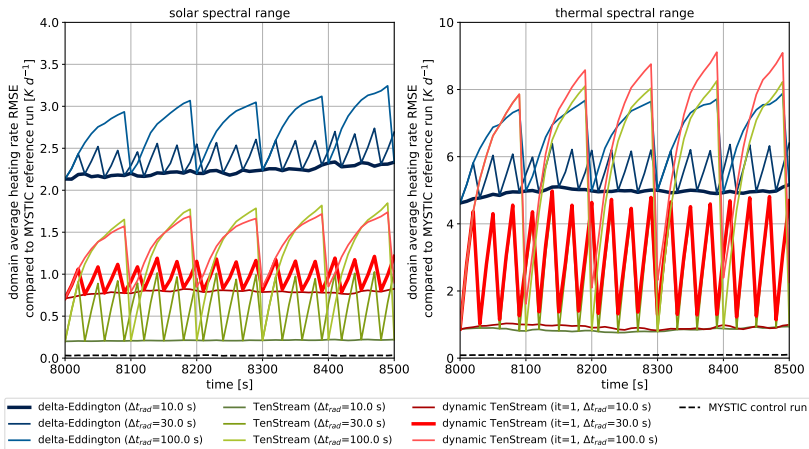
## Evaluation of the New Solver

### Domain Average Solver Performance

Example: setup for  $\Delta t_{\text{rad}} = 30$  s (about as expensive as a 1D delta Eddington-solver)



# Dynamic RT – how good is it?



- Considerable differences between 3D and 1D heating rates in high resolution radiative transfer and cloud models
- Effect on clouds in high resolution models demonstrated
- There is hope for fast (dynamic) parameterizations of 3D radiation
- Even 1 km resolution is grey zone for radiation models!