



**Case Study Of Error-  
growth From  
Mesoscale  
Convection Near The  
Intrinsic Limit:  
Combining Potential  
Vorticity Error  
Growth Tendencies  
With Ensemble  
Sensitivity Analysis**



Edward Groot (previously Johannes Gutenberg University, Mainz, Germany; currently University of Oxford, UK)

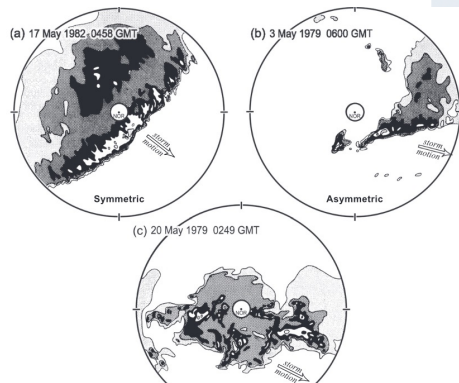
Collaborators: Michael Riemer, Tobias Selz

September 12, ECMWF, Reading

# Why variability of deep moist convection?

Since Lorenz' works we have been chasing "butterflies"

- **Convective instability** as important instability
- Lorenz (1963, 1969) "deterministic chaos" & finite predictability horizon
- Convective organisation and outflow affecting weather predictability (Rodwell et al. 2013, Baumgart et al. 2019)



- Do the "butterflies" actually exist as such? (Durrán & Gingrich, 2014, Lorenz 1969)

➔ Investigate error cascade and its spread evolution!!



"Pre-Lorenz" processes??

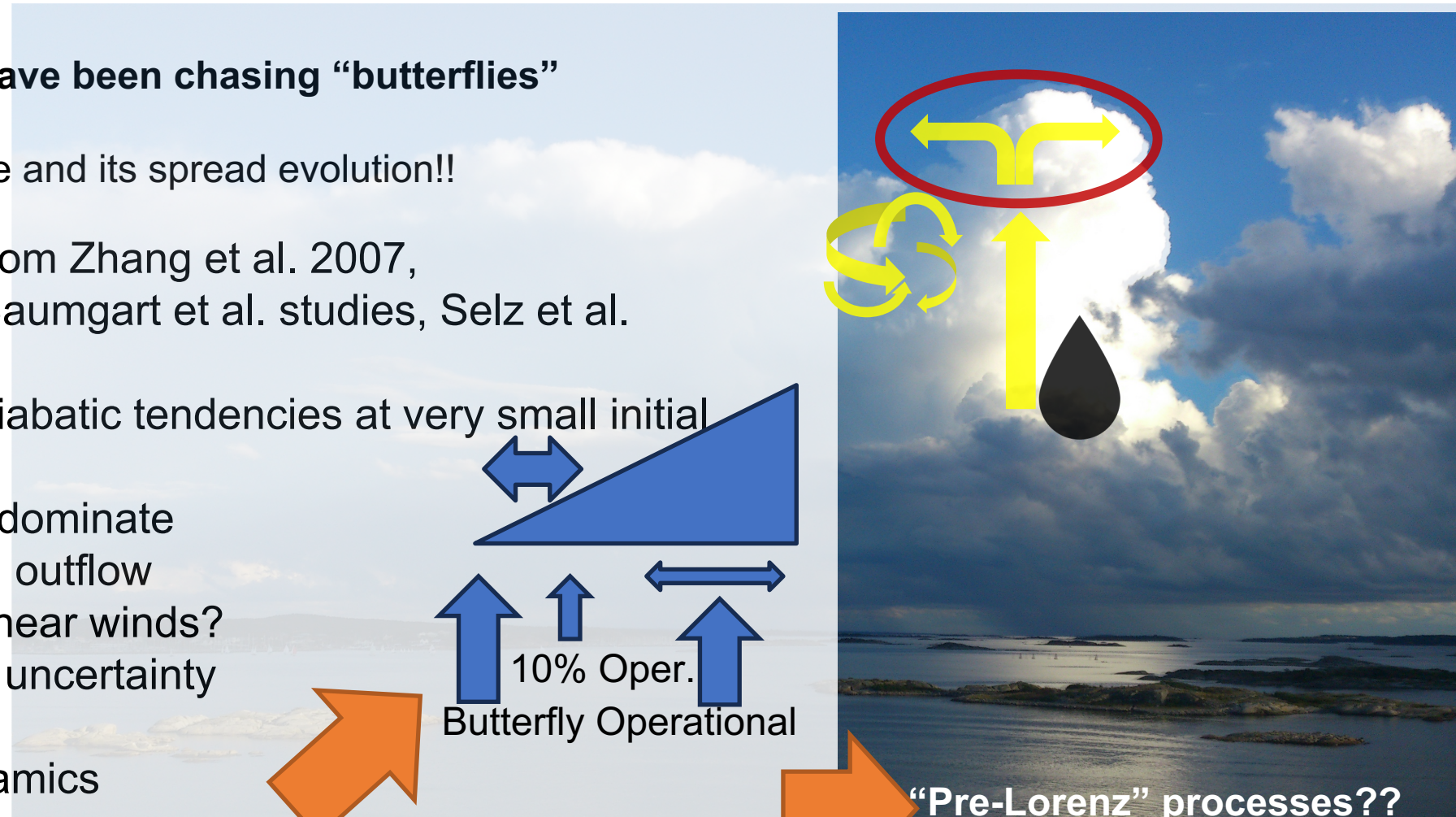
# Why variability of deep moist convection?

Since Lorenz' works we have been chasing "butterflies"

→ Investigate error cascade and its spread evolution!!

1. Error-growth stages from Zhang et al. 2007,
2. Mean evolution from Baumgart et al. studies, Selz et al. 2022/Tobias' talk:

- Spread growth from diabatic tendencies at very small initial condition uncertainty
- Convection seems to dominate
- Convective heating → outflow  
→ DIV pert → non-linear winds?
- < 10-20% operational uncertainty
- Dominant days 1 & 2
- Near-tropopause dynamics



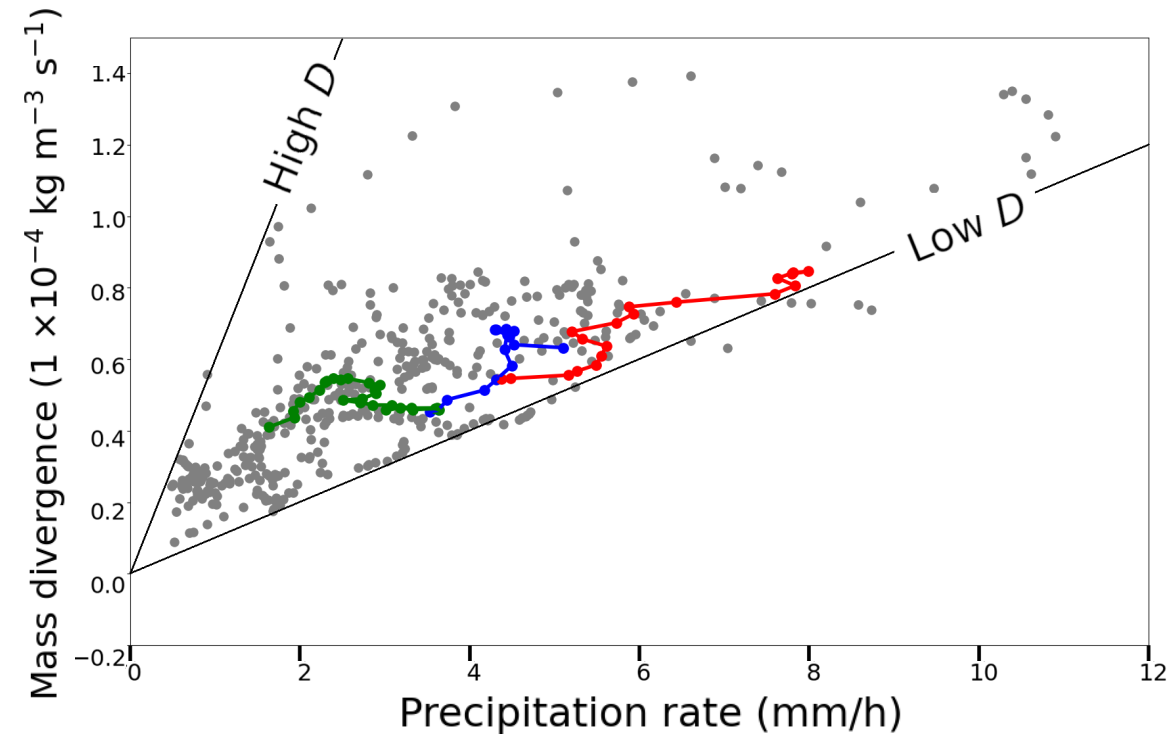
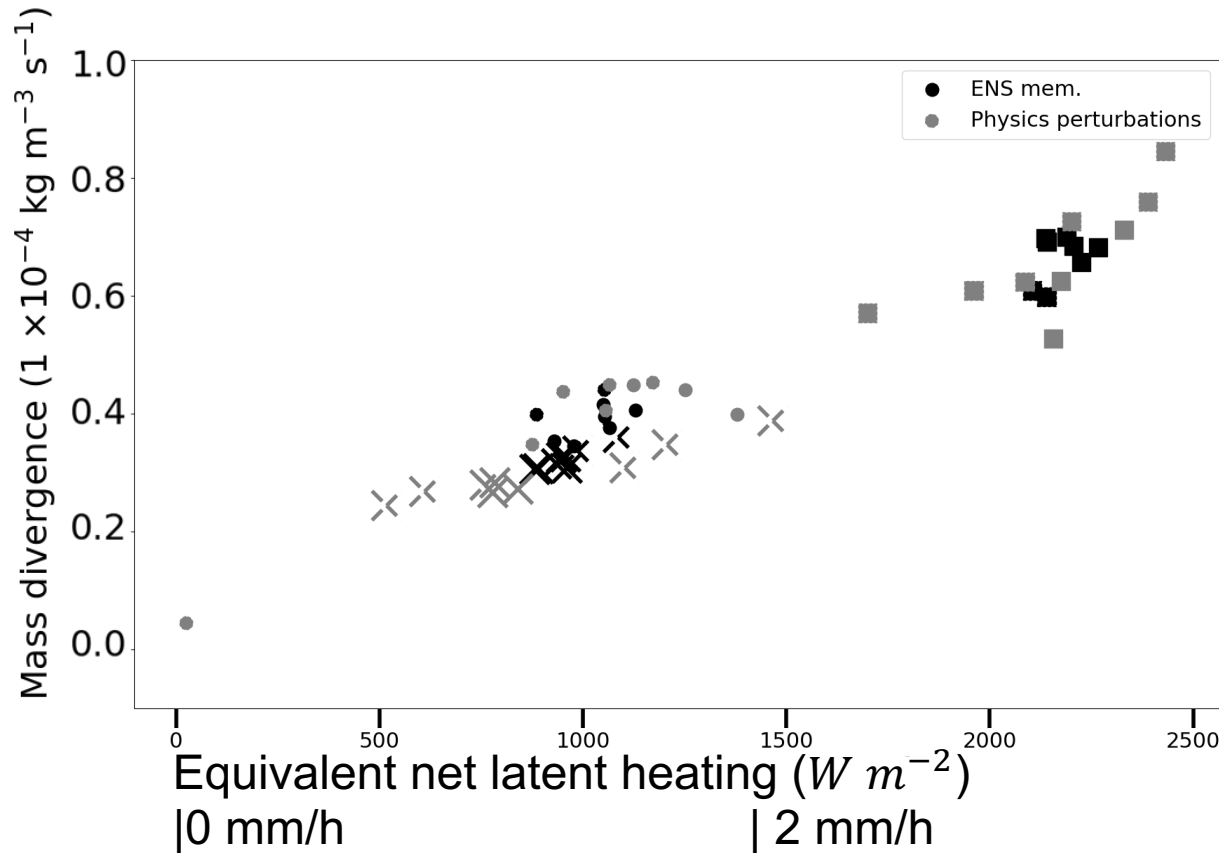
What about case-to-case variability and individual cases?

"Pre-Lorenz" processes??

# Handy "tool" from earlier work...

13 km parameterized deep conv.

| 1 km conv.-permitting



# Summary earlier work on convective outflow

## Upper tropospheric divergent outflow in ICON depends

### Parameterised set-up (13 km)

- ⚡ Linearly on (net) latent heating
- ✖ Weak variation around linear relation

### Convection-permitting set-up (1 km)

- ⚡ On (net) latent heating
- ⚡ On convective aggregation
- ❓ Possibly on outflow dimensionality

LES-study, CM1



← This ICON-study



# Large-scale sensitivity to the outflows

Hypothesis: convective systems of event can induce a subsequent jet stream shift in a much underdispersed ensemble\*

\*(Rescaled initial uncertainty  $\rightarrow\rightarrow$  Lorenz' "butterflies",  $n = 50$ )

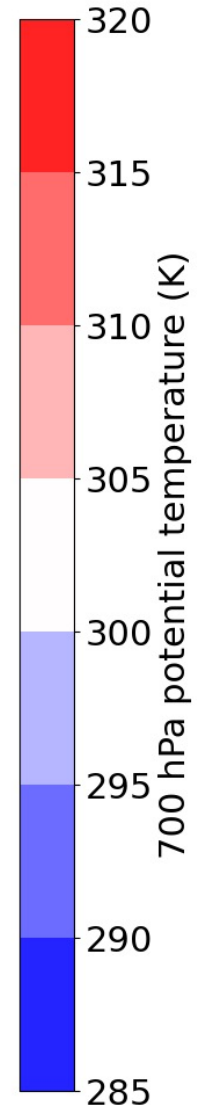
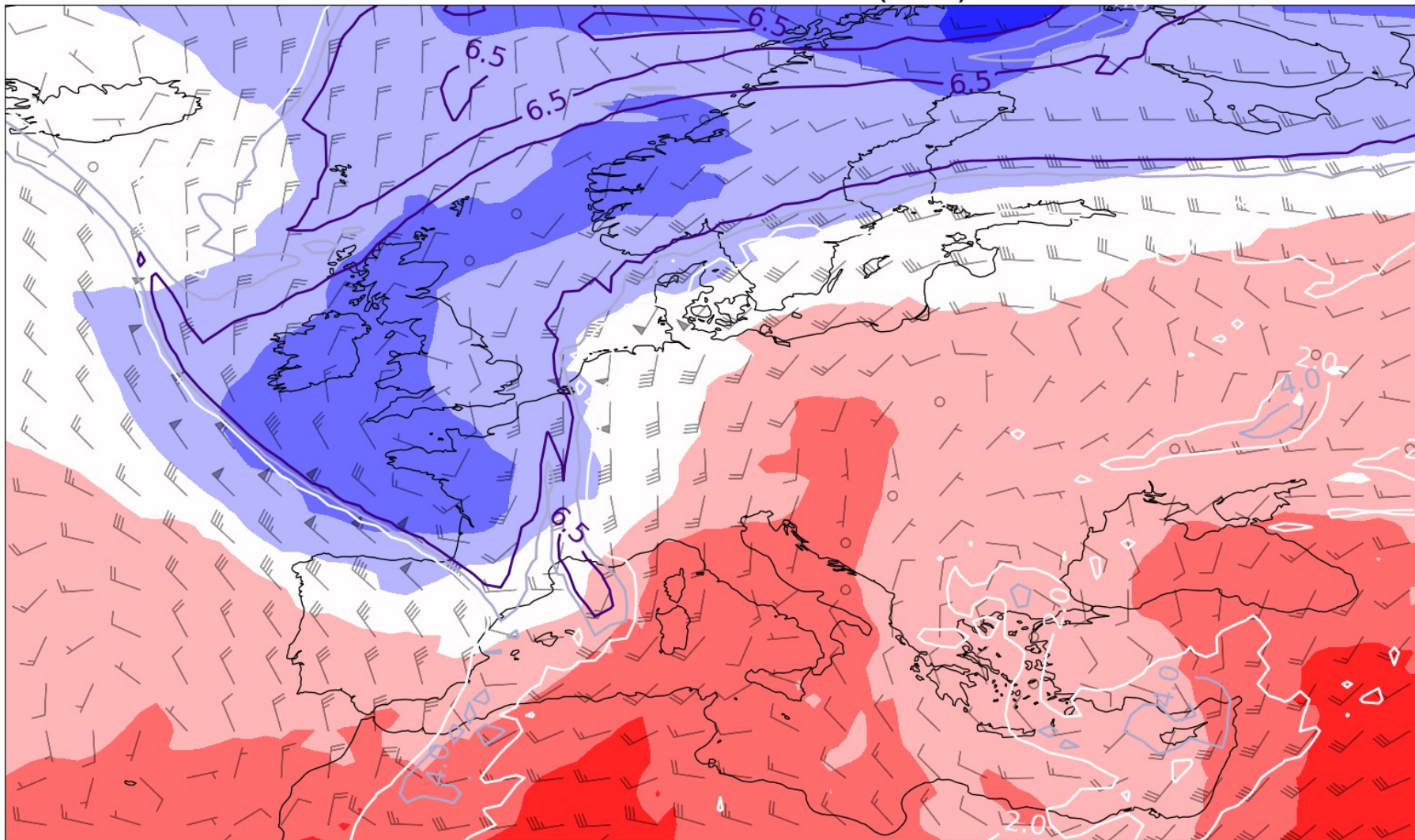
Methods:

1. Ensemble sensitivity analysis (regression)
2. Spread growth diagnostics for attribution (Selz et al. 2022; Baumgart et al. 2019)

A convective event

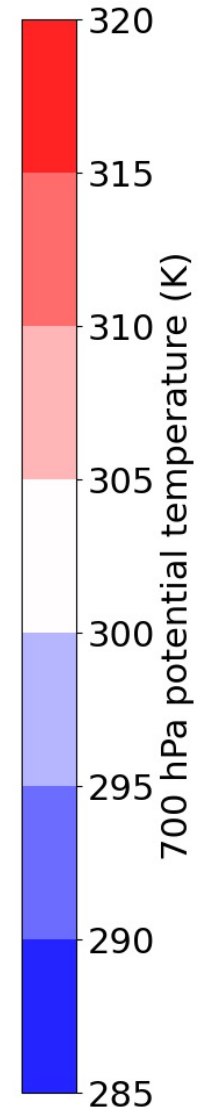
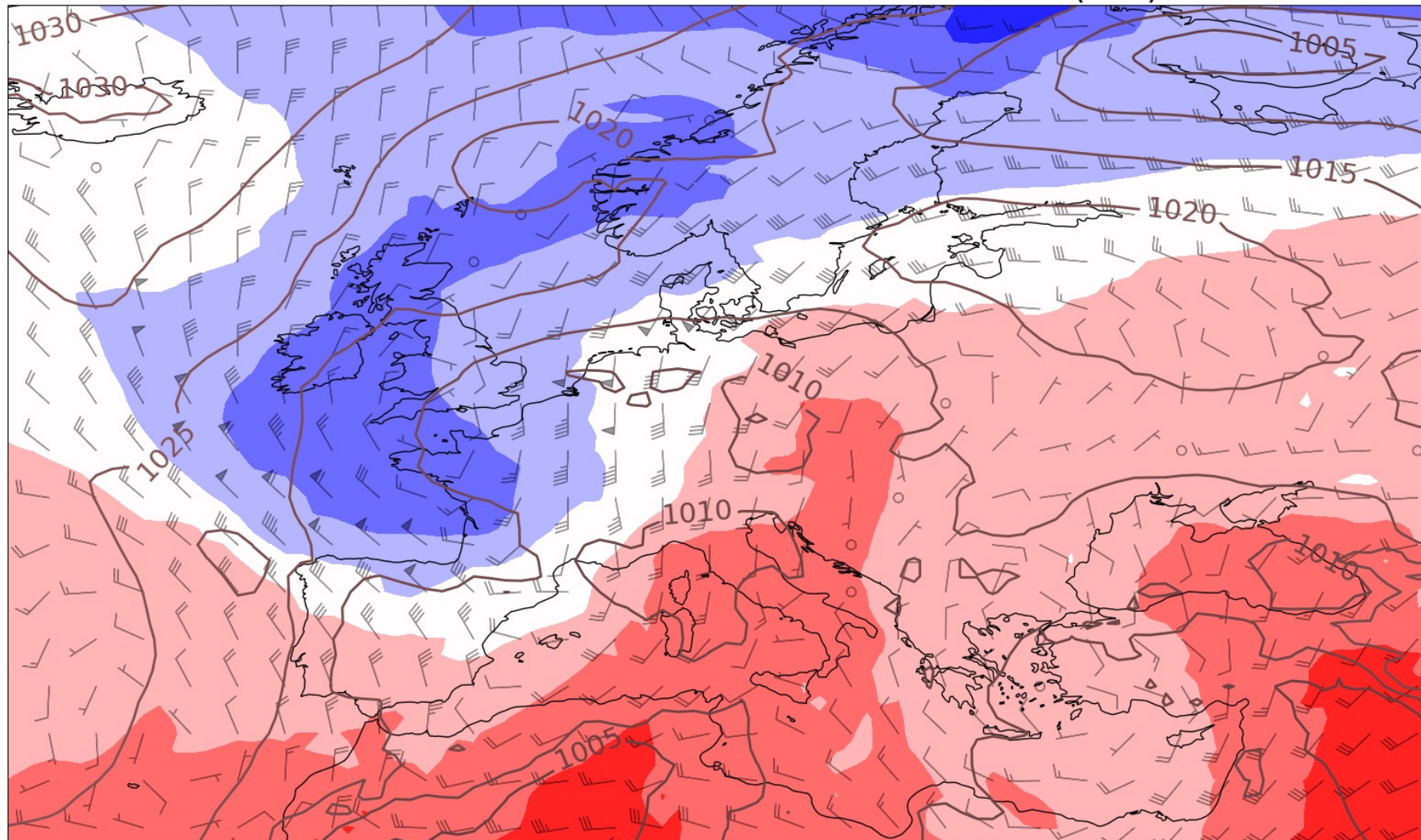
# Synoptic setting

Wind at 250 hPa and PV (PVU)



# Synoptic setting

Wind at 250 hPa and Mean Sea Level Pressure (hPa)



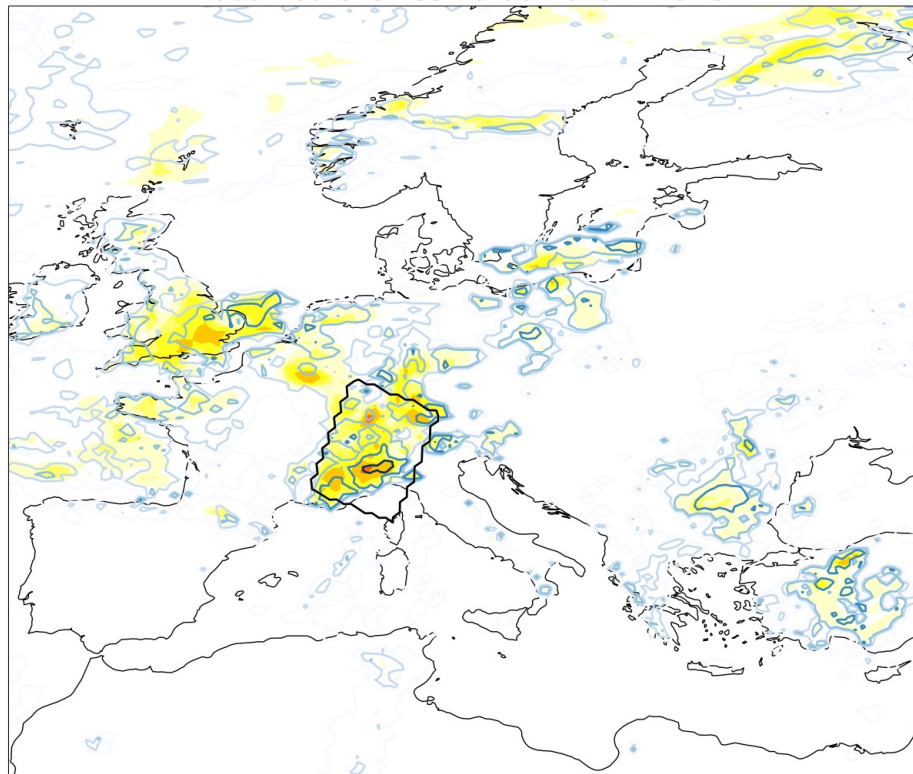


# Convective systems

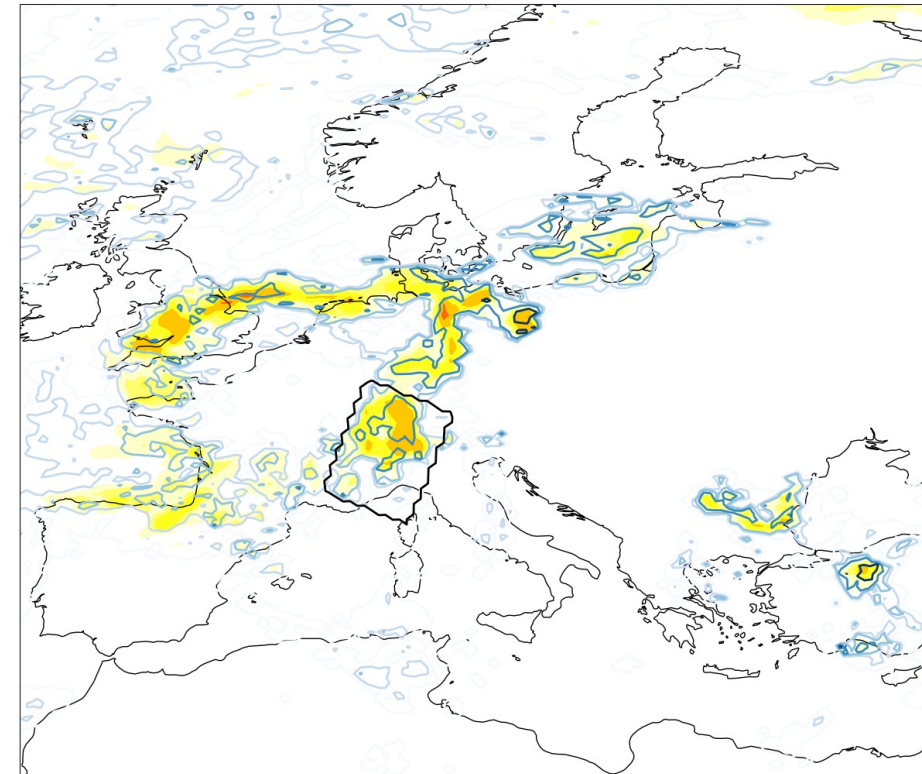
“Alps system”:

2-13 h forecast time

Rescaled IFS-ens, hourly  $\mu_{preciprate}$  and  $\sigma_{preciprate}$   
003 hours since 10-06-2019 12 UTC



Rescaled IFS-ens, hourly  $\mu_{preciprate}$  and  $\sigma_{preciprate}$   
012 hours since 10-06-2019 12 UTC

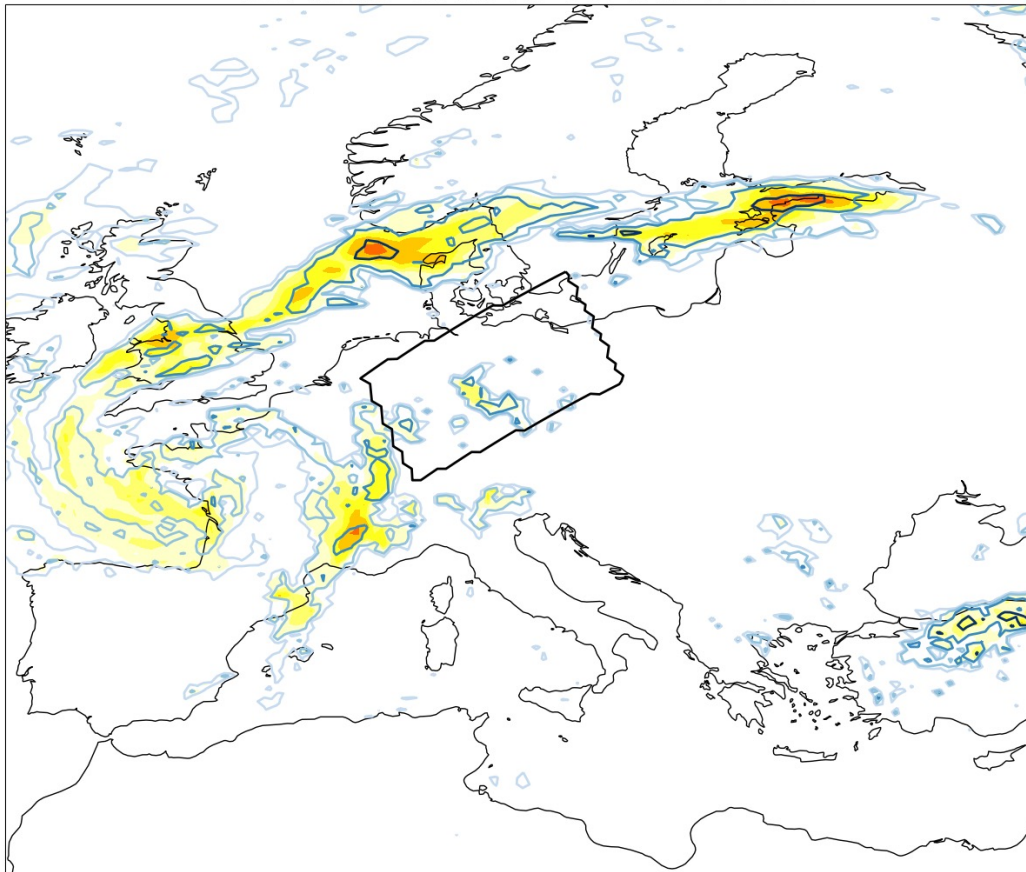


# Convective systems

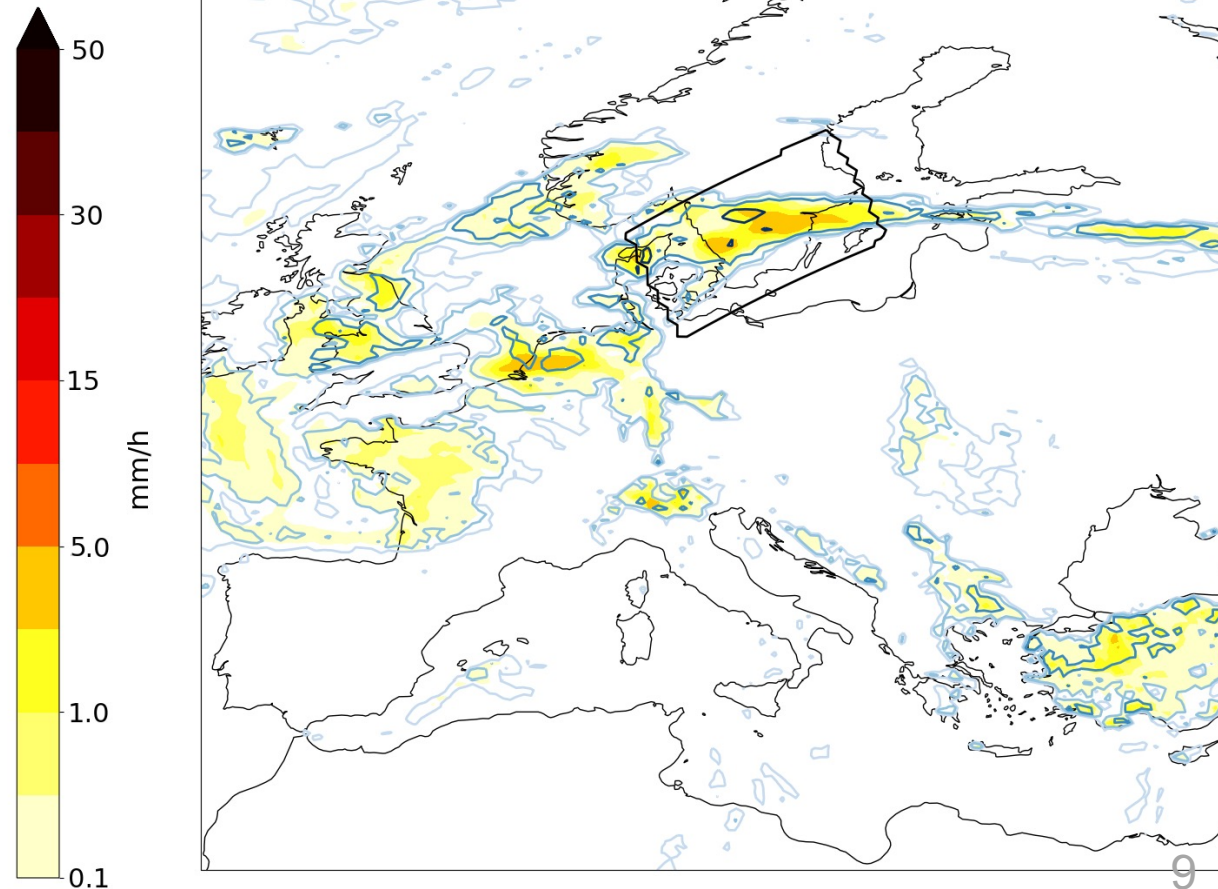
“Day 2” system:

31-46 h forecast time

Rescaled IFS-ens, hourly  $\mu_{preciprate}$  and  $\sigma_{preciprate}$   
031 hours since 10-06-2019 12 UTC



Rescaled IFS-ens, hourly  $\mu_{preciprate}$  and  $\sigma_{preciprate}$   
046 hours since 10-06-2019 12 UTC

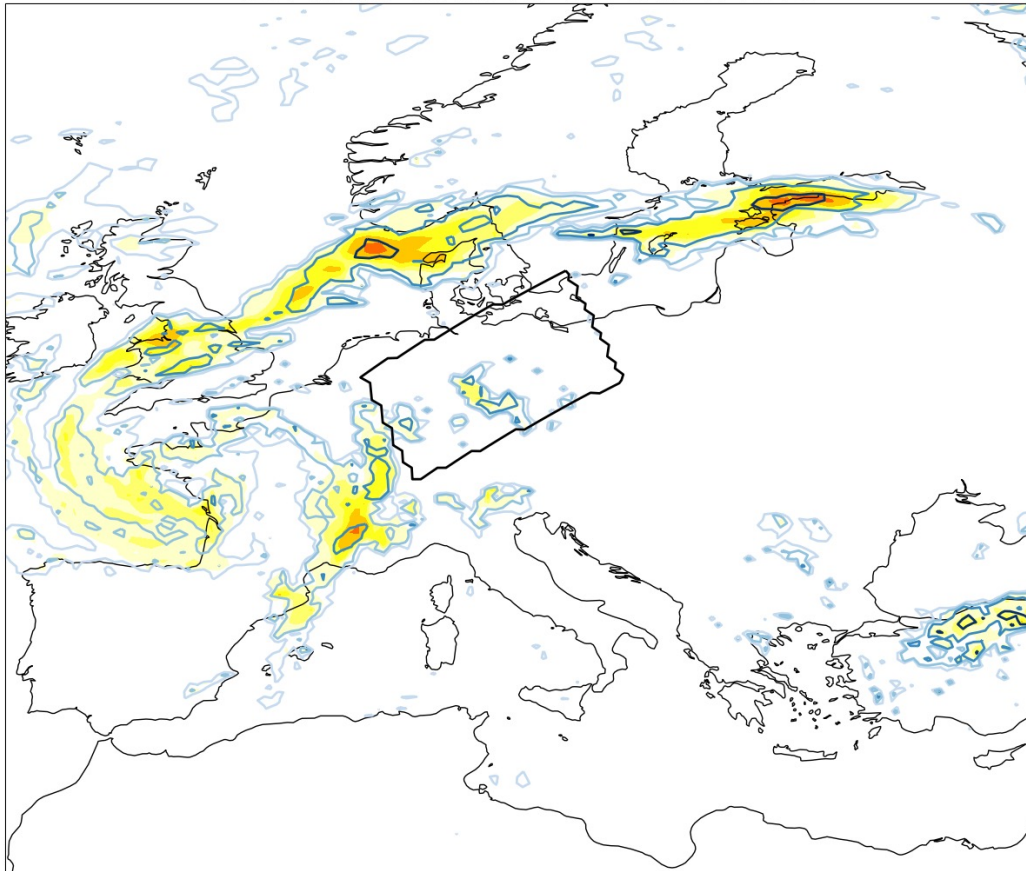


# Convective systems

“Day 2” system:

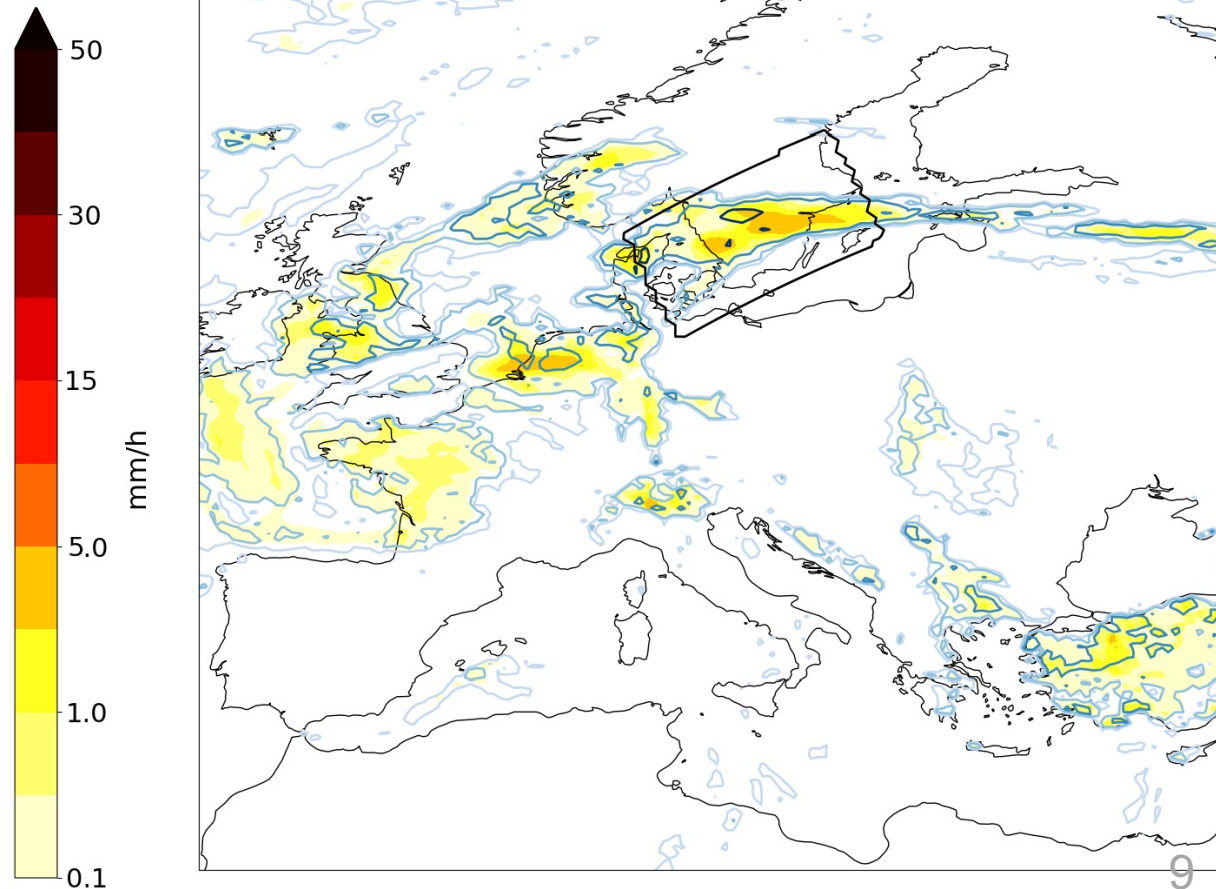
31-46 h forecast time

Rescaled IFS-ens, hourly  $\mu_{preciprate}$  and  $\sigma_{preciprate}$   
031 hours since 10-06-2019 12 UTC



Both convective systems have a total range in area mean precipitation accumulation of roughly 1-10%!

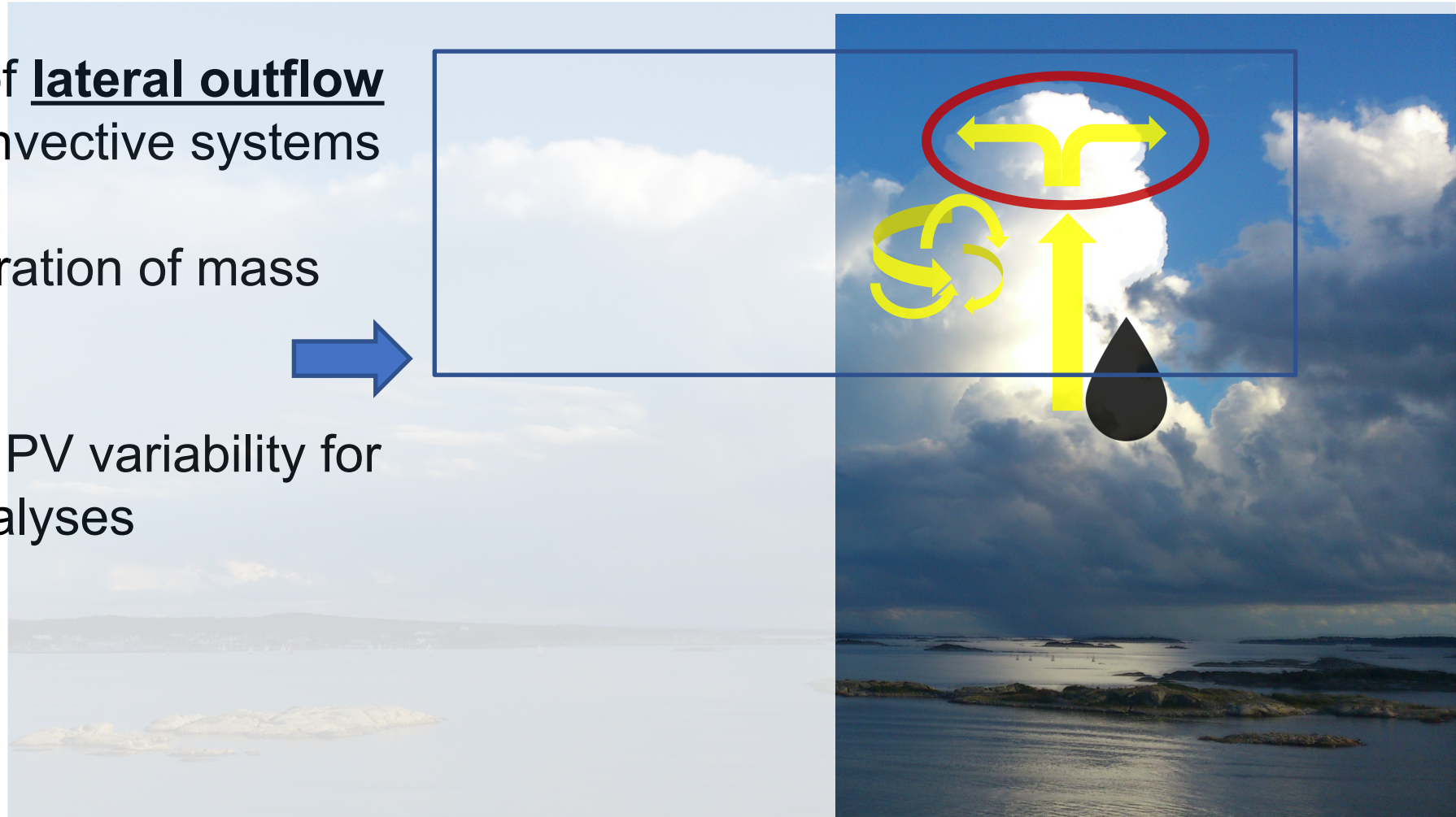
Rescaled IFS-ens, hourly  $\mu_{preciprate}$  and  $\sigma_{preciprate}$   
046 hours since 10-06-2019 12 UTC

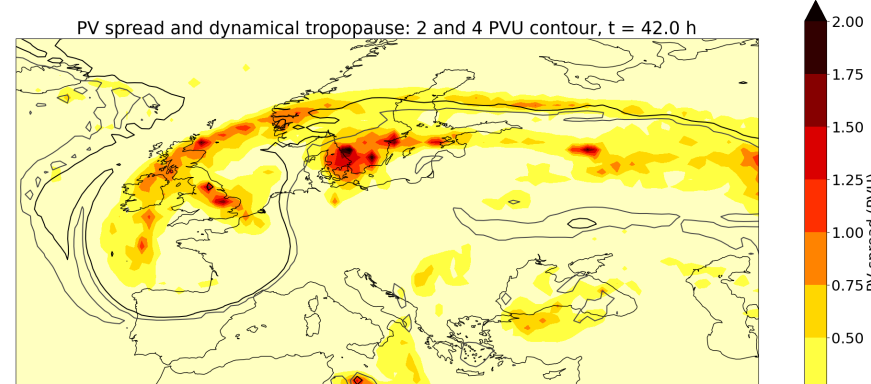
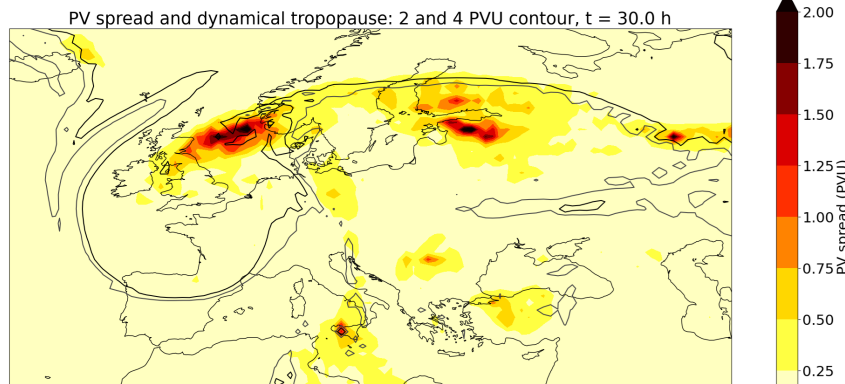
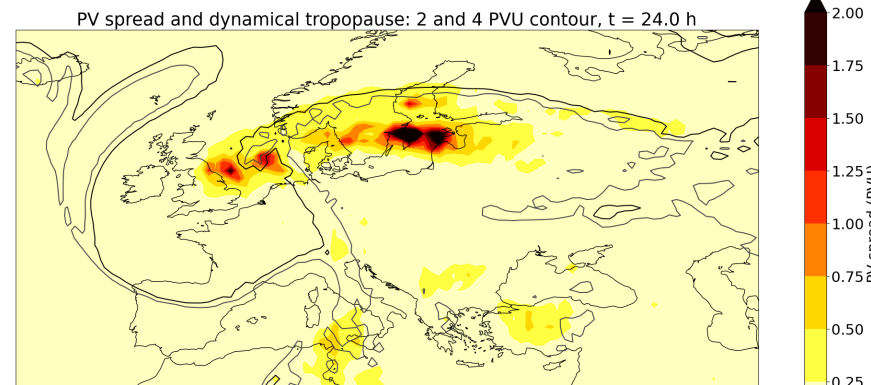
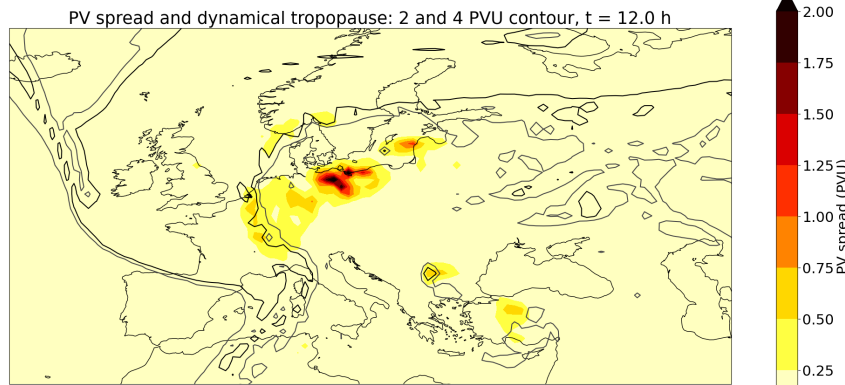
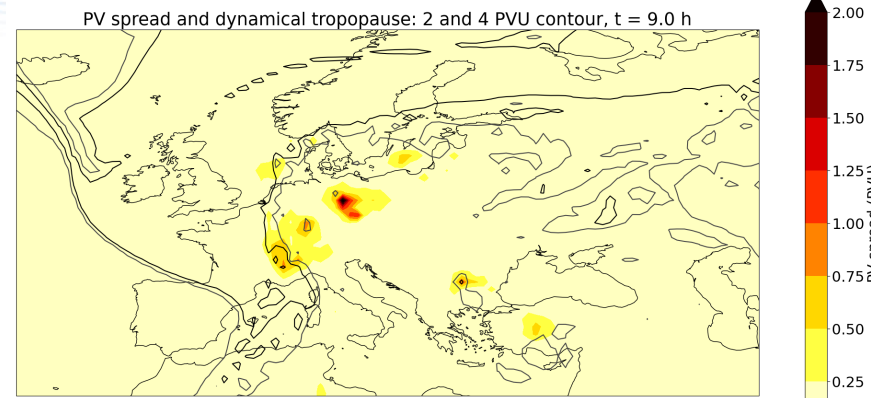
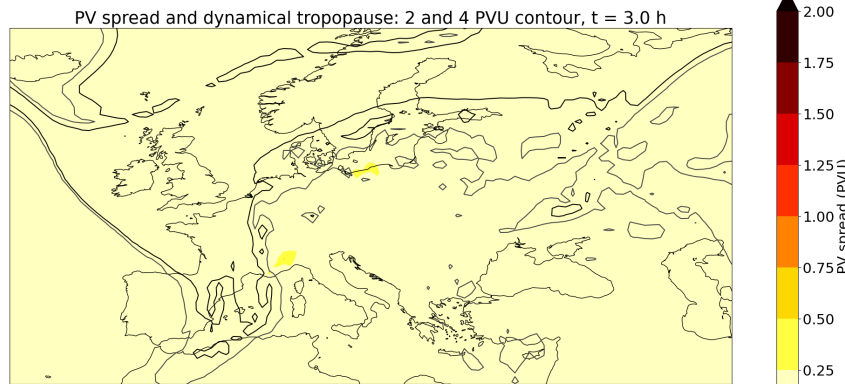


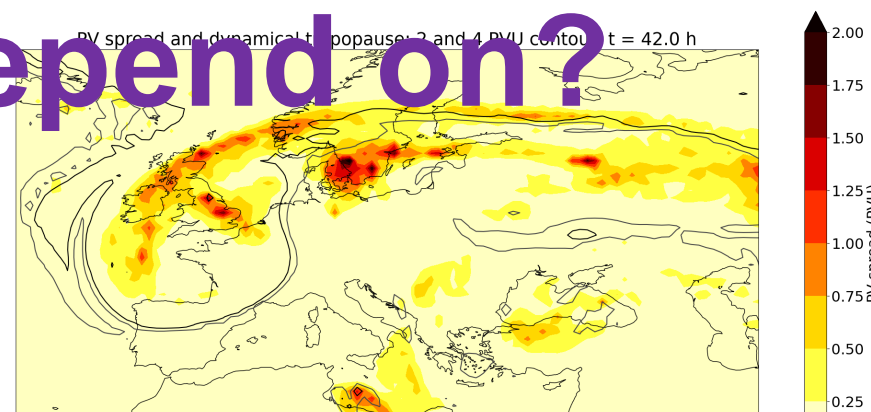
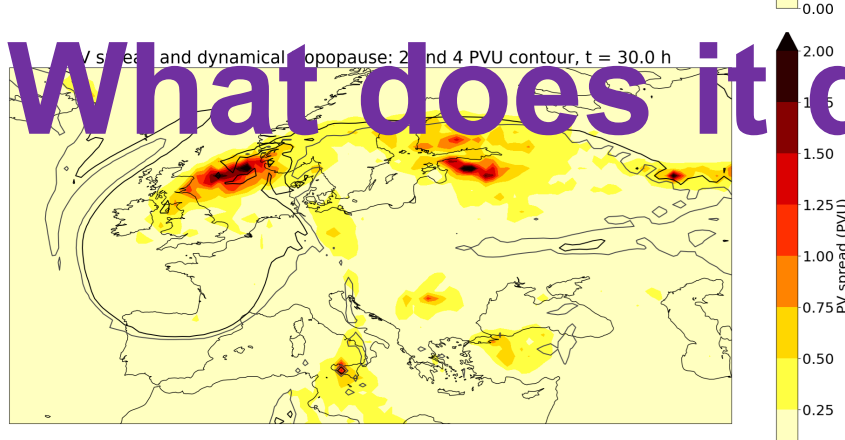
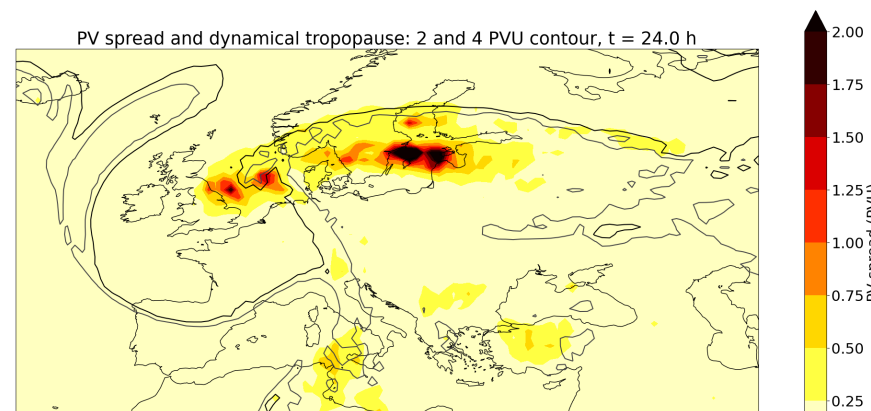
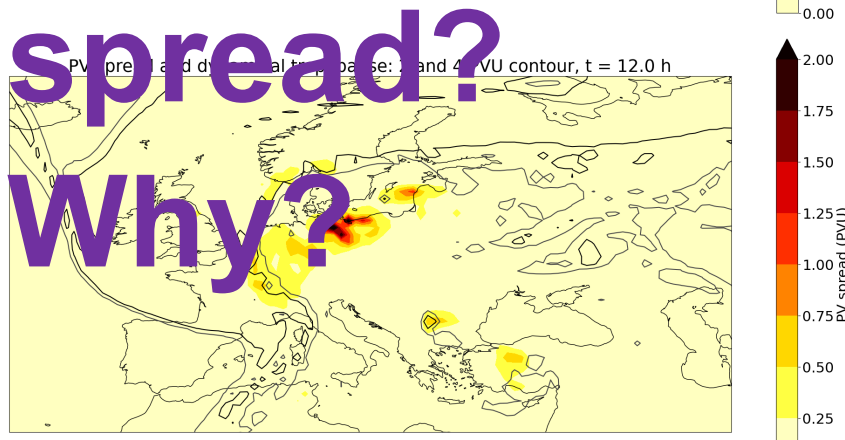
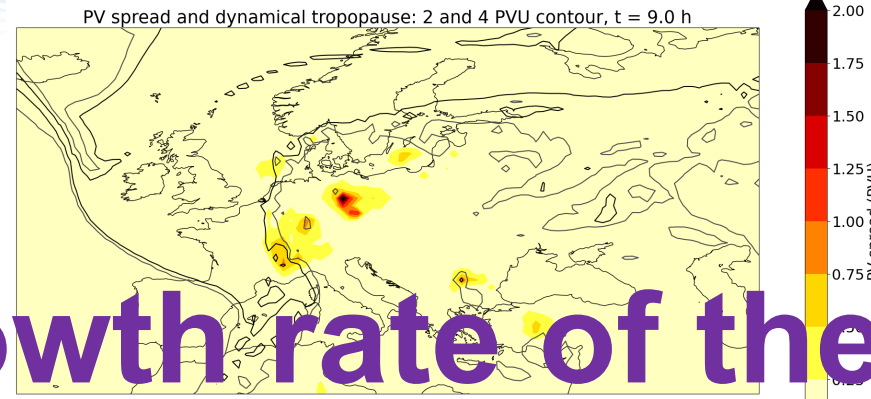
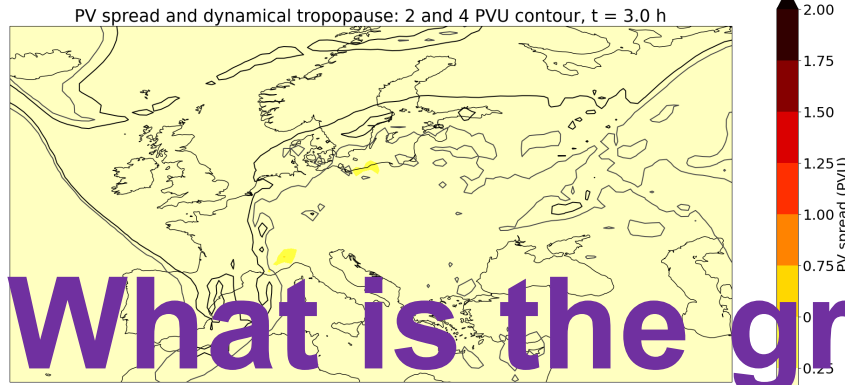
# Methods sensitivity analysis

Quantification of lateral outflow at the top of convective systems

- Volume integration of mass divergence
- Compared to PV variability for sensitivity analyses







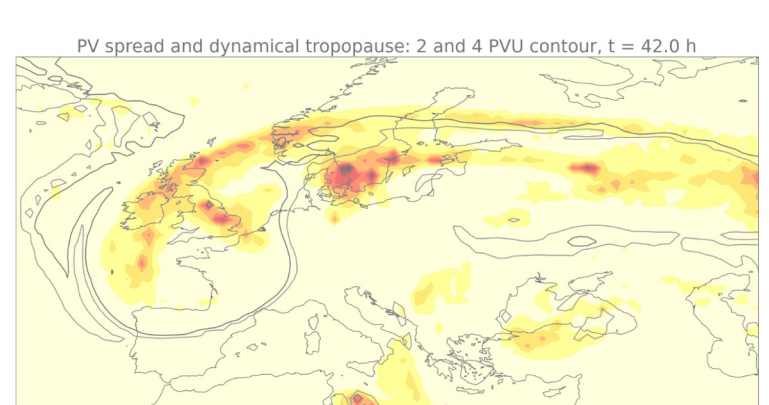
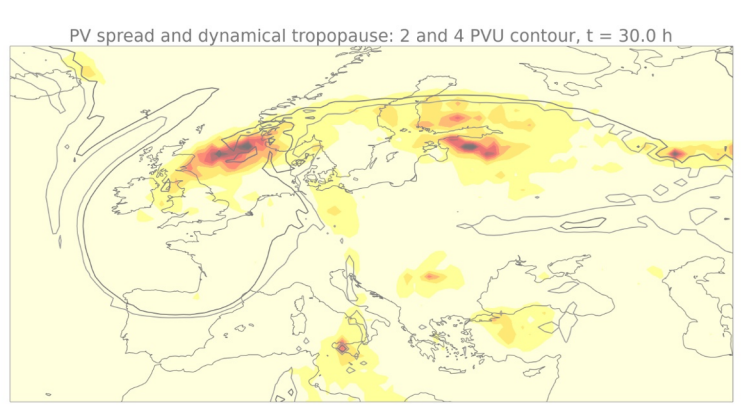
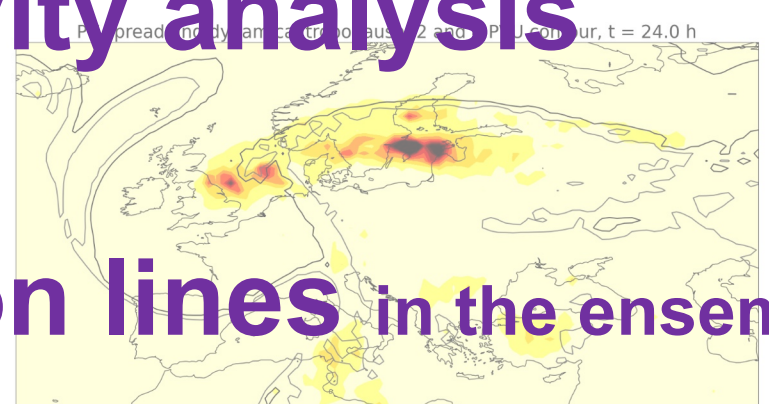
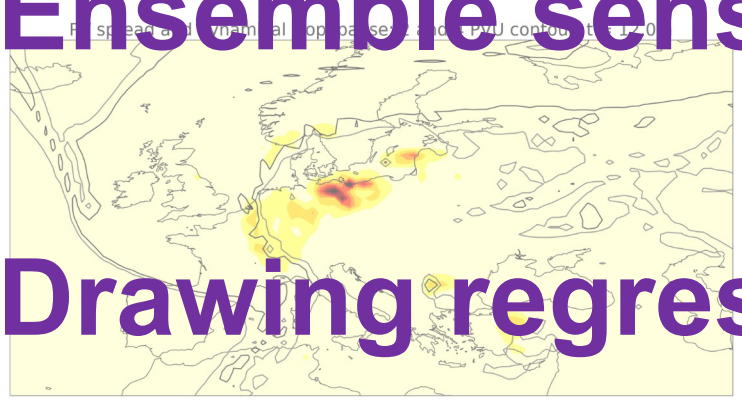
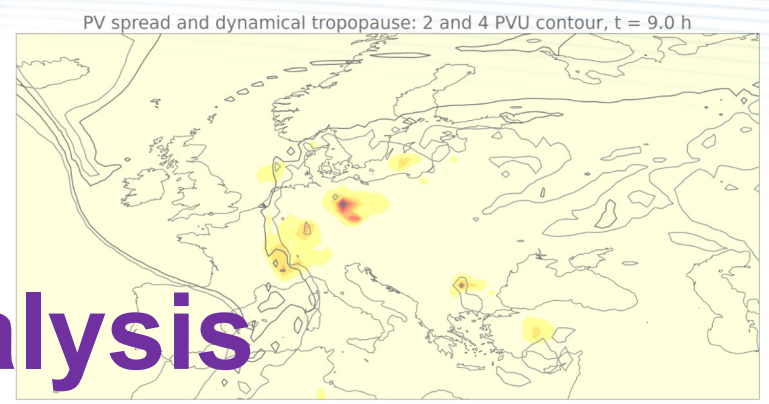
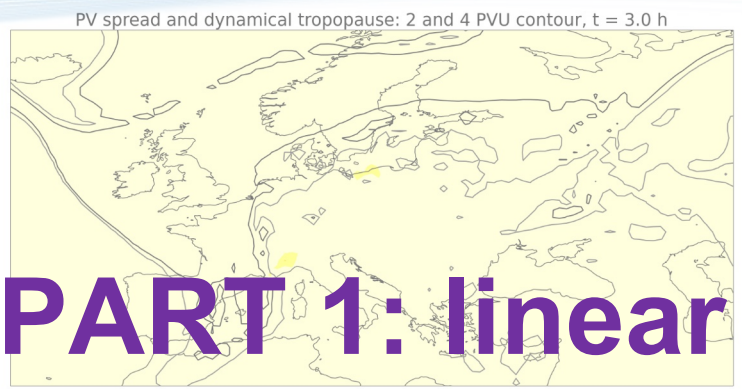
What is the growth rate of the spread?  
Why?

What does it depend on?

# PART 1: linear analysis

# Ensemble sensitivity analysis

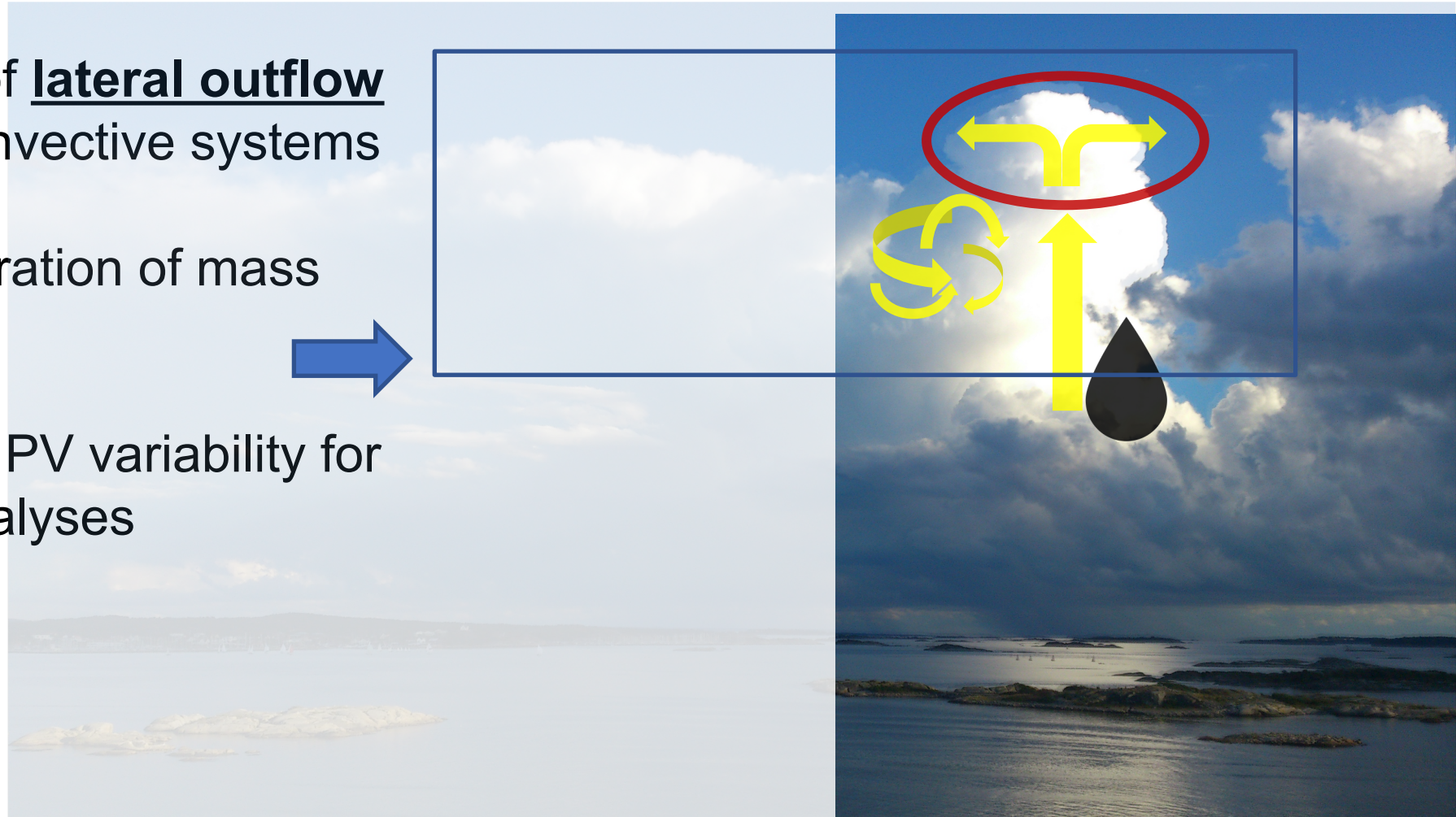
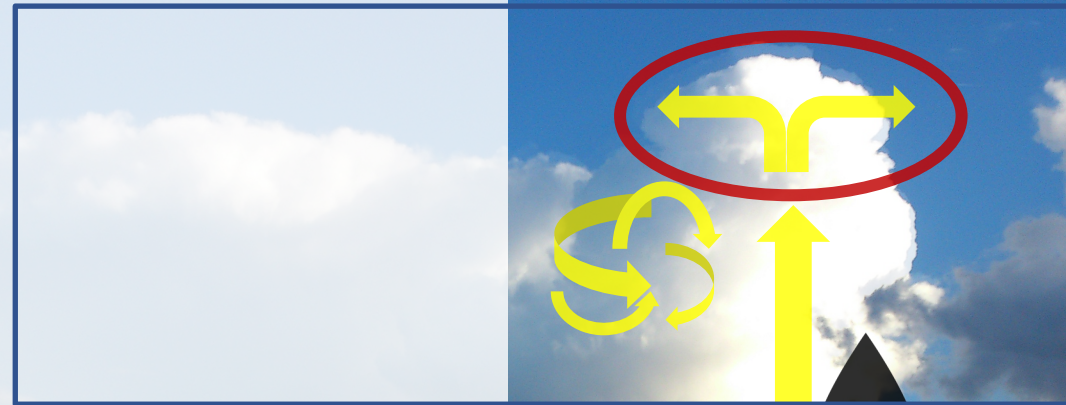
# Drawing regression lines in the ensemble covariance



# Methods sensitivity analysis

Quantification of lateral outflow at the top of convective systems

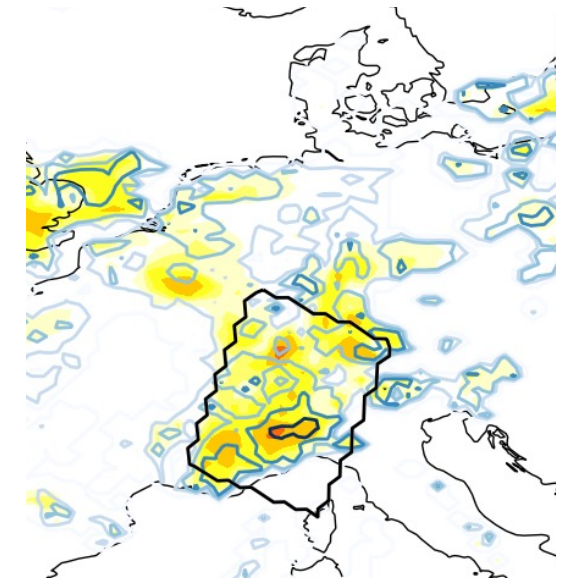
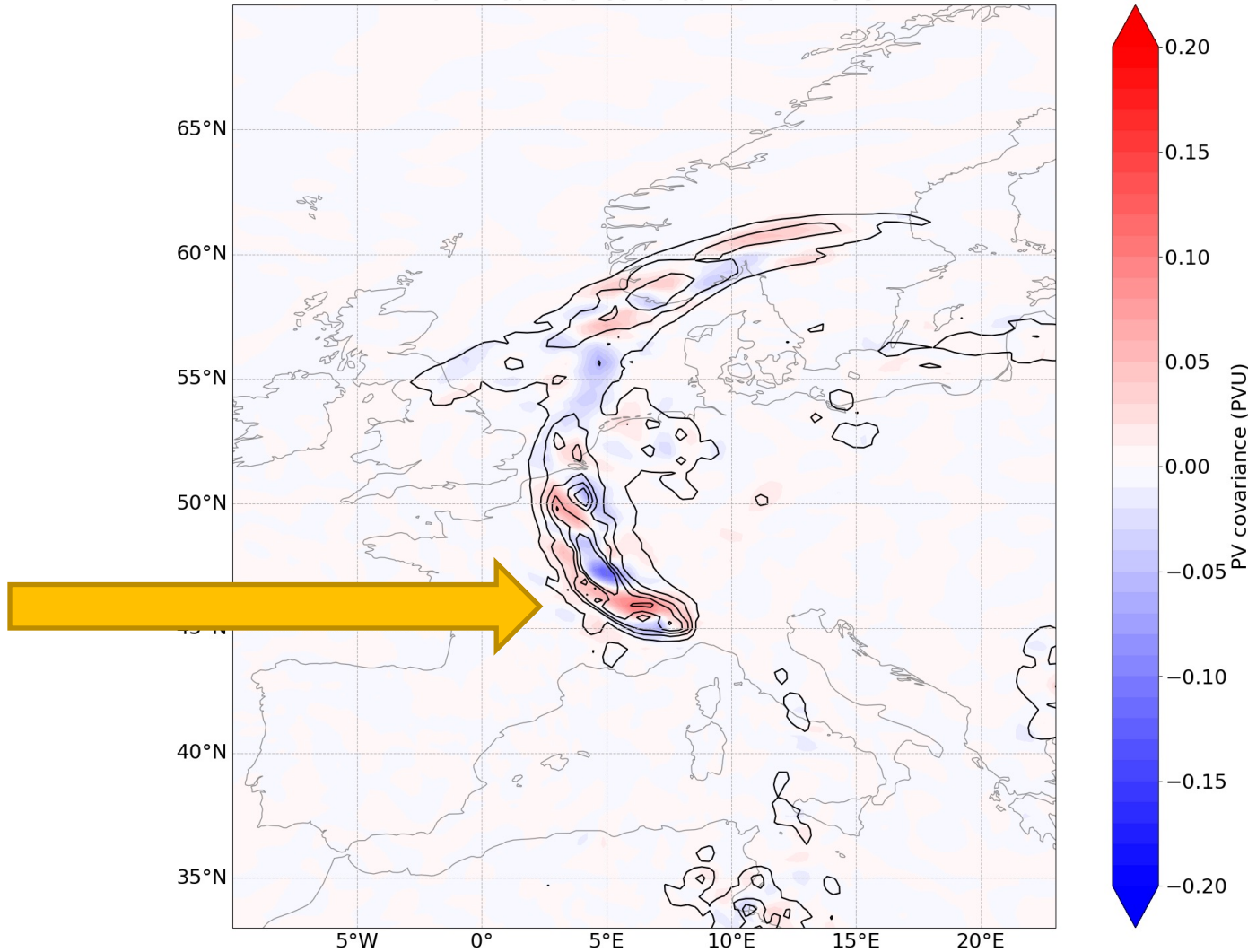
- Volume integration of mass divergence
- Compared to PV variability for sensitivity analyses



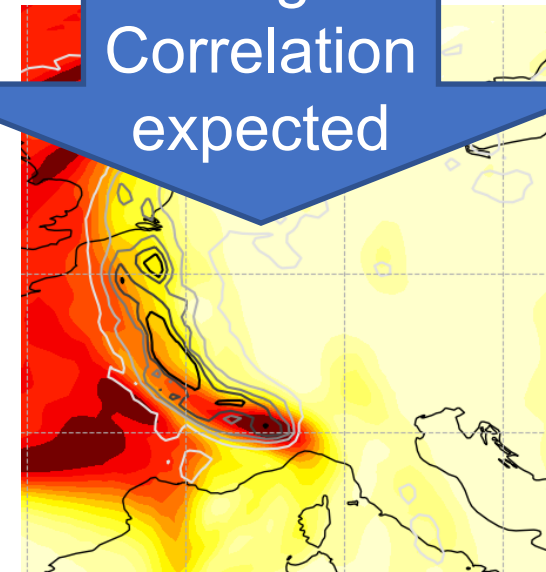


# “Alps system” +12h

ESA: PV sensitivity structure (colours); PV-spread 250 hPa (isolines)  
012 hours since 10-06-2019 12 UTC

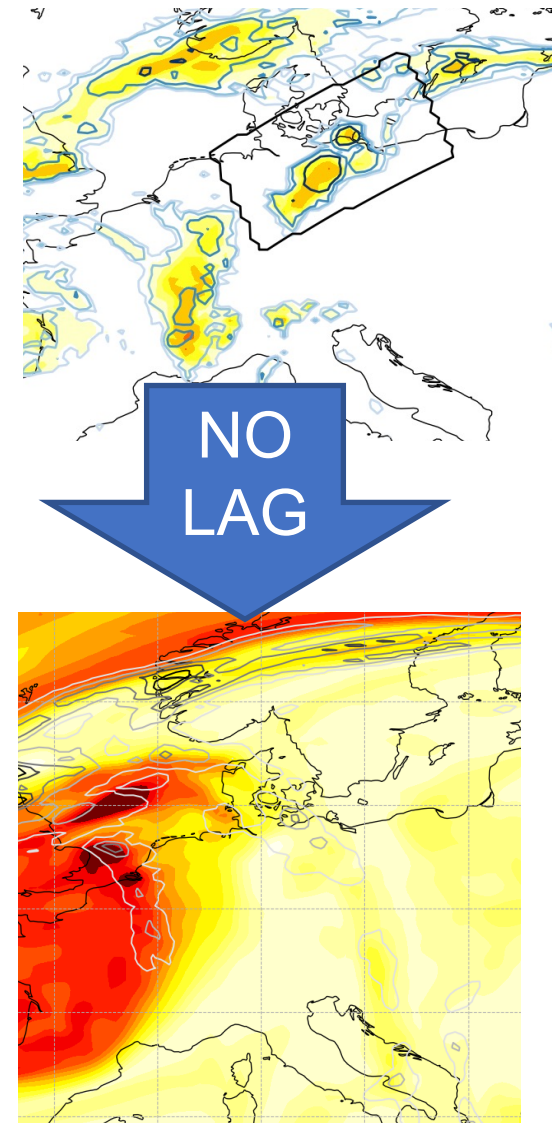
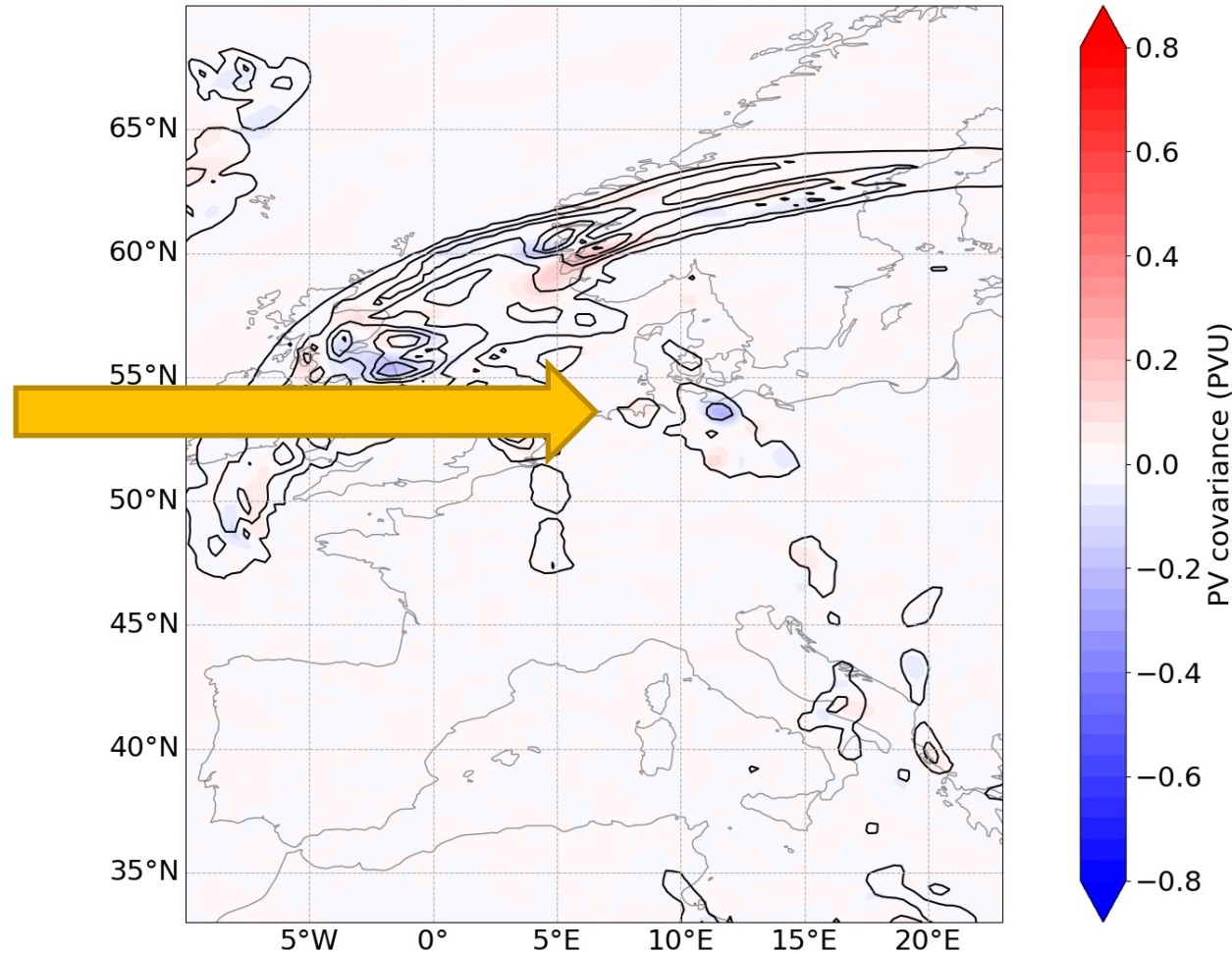


Neg.  
Correlation  
expected



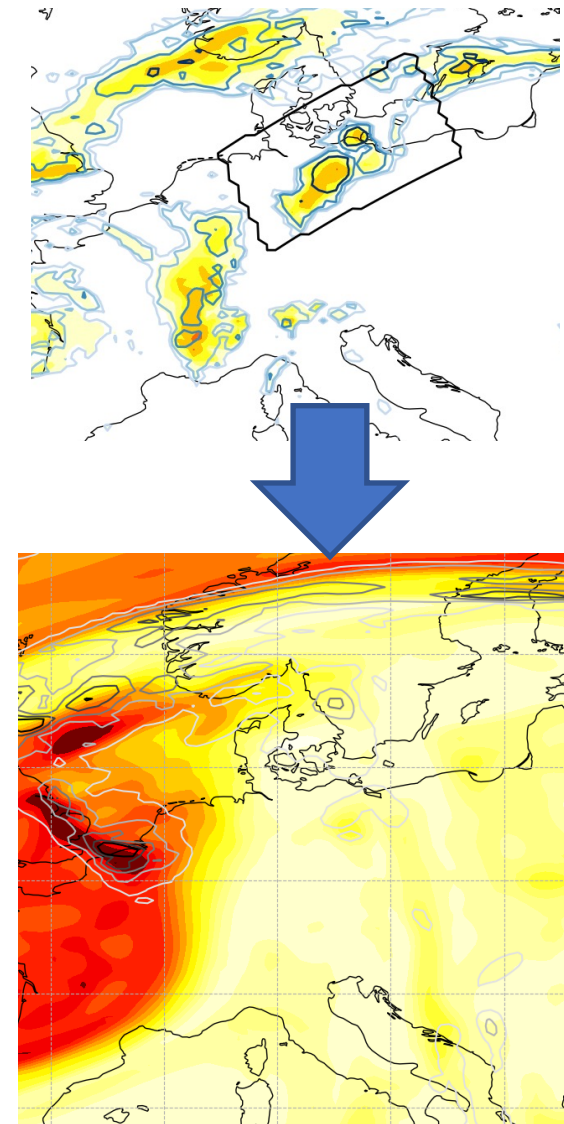
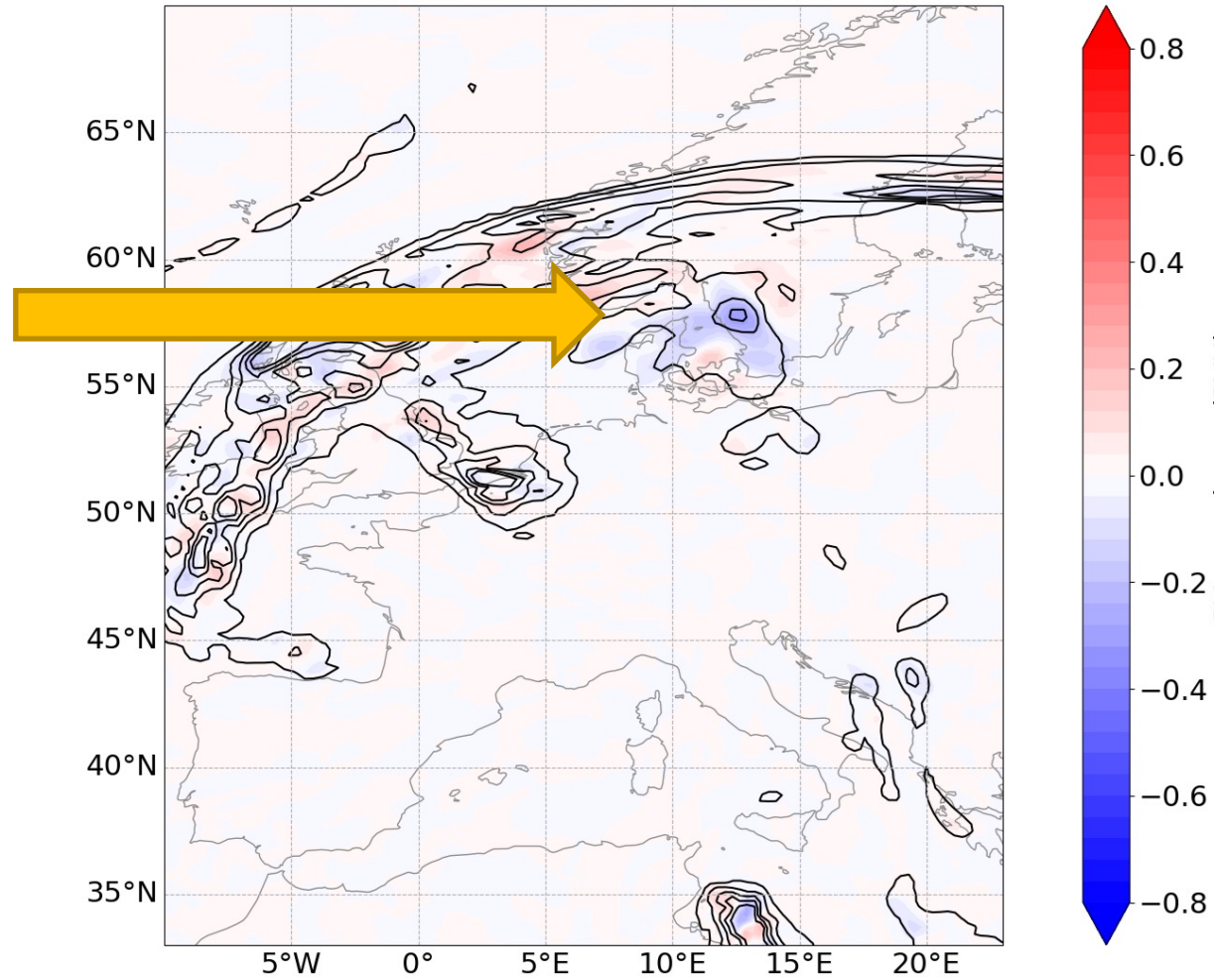
# “Day 2 system” +34h

ESA: PV sensitivity structure (colours); PV-spread 250 hPa (isolines)  
034 hours since 10-06-2019 12 UTC



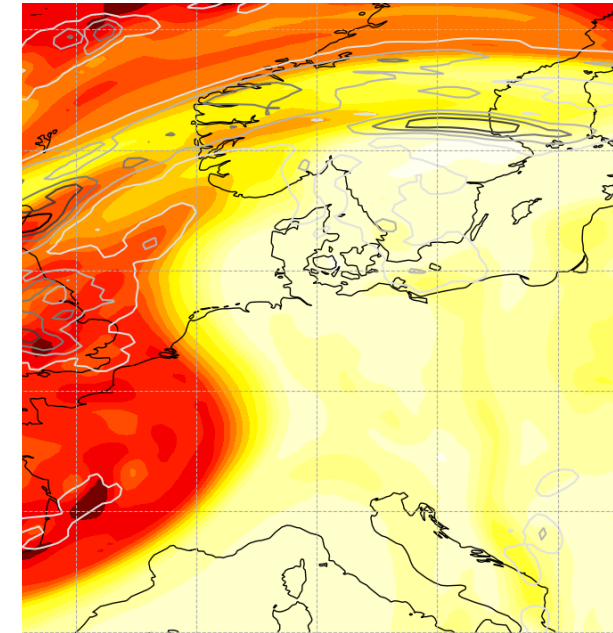
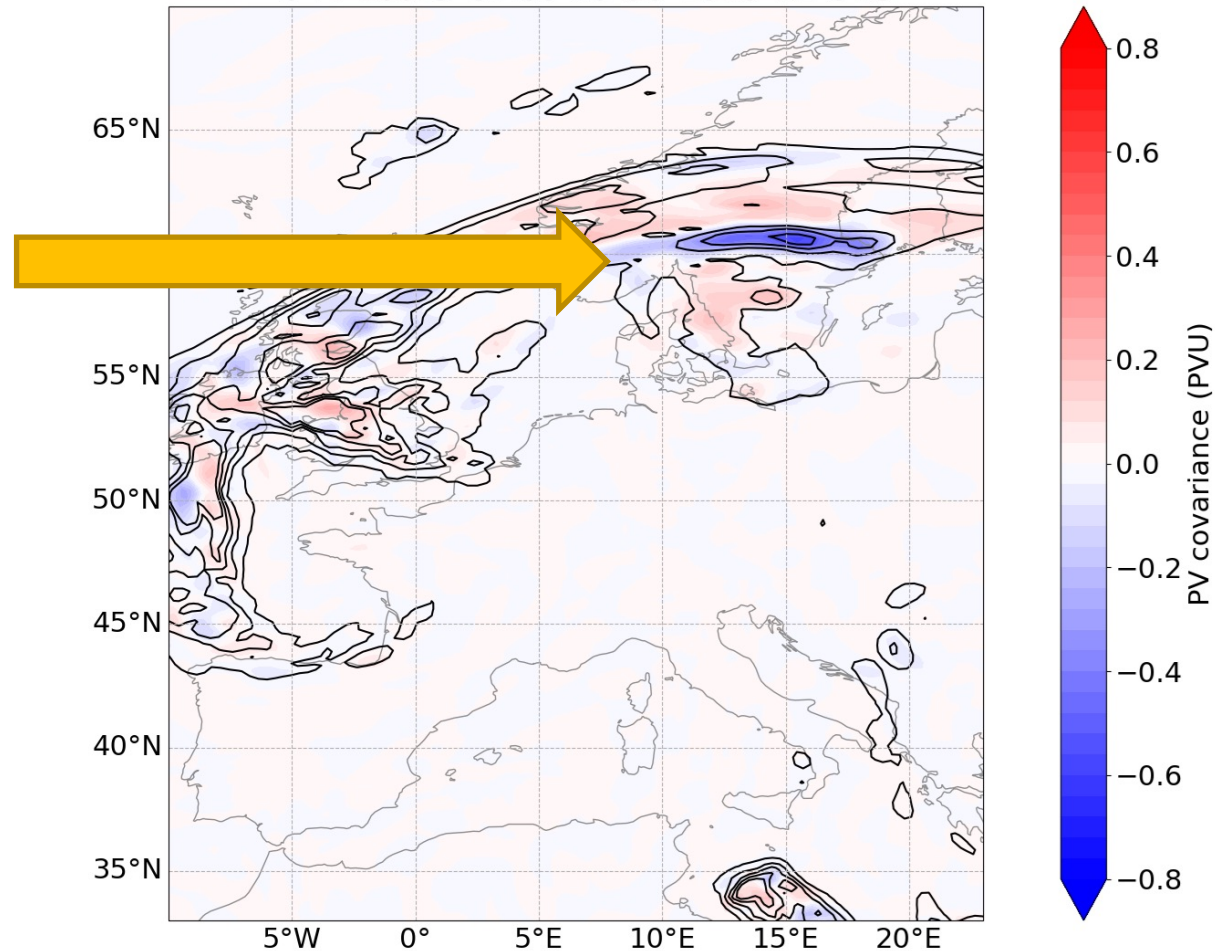
# “Day 2 system” +39 h

ESA: PV sensitivity structure (colours); PV-spread 250 hPa (isolines)  
039 hours since 10-06-2019 12 UTC



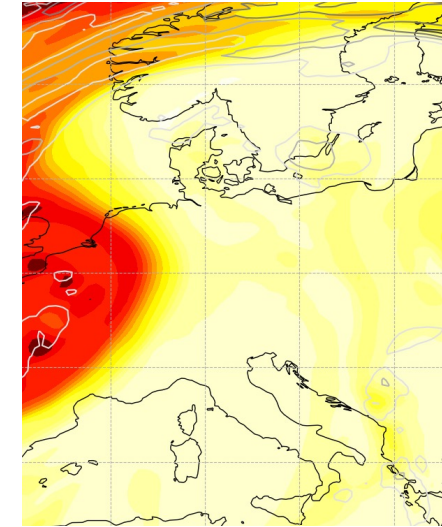
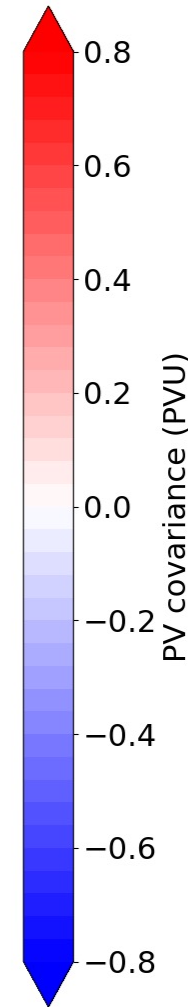
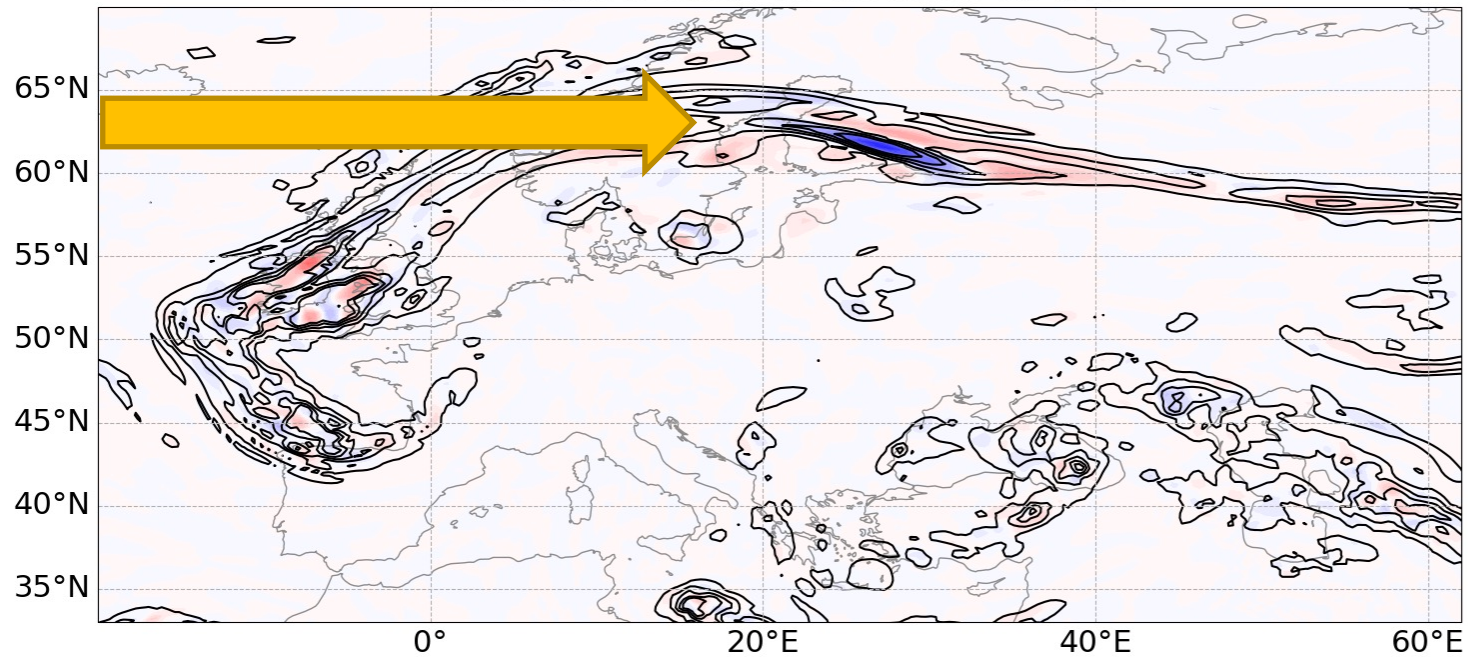
# “Day 2 system” +44 h

ESA: PV sensitivity structure (colours); PV-spread 250 hPa (isolines)  
044 hours since 10-06-2019 12 UTC

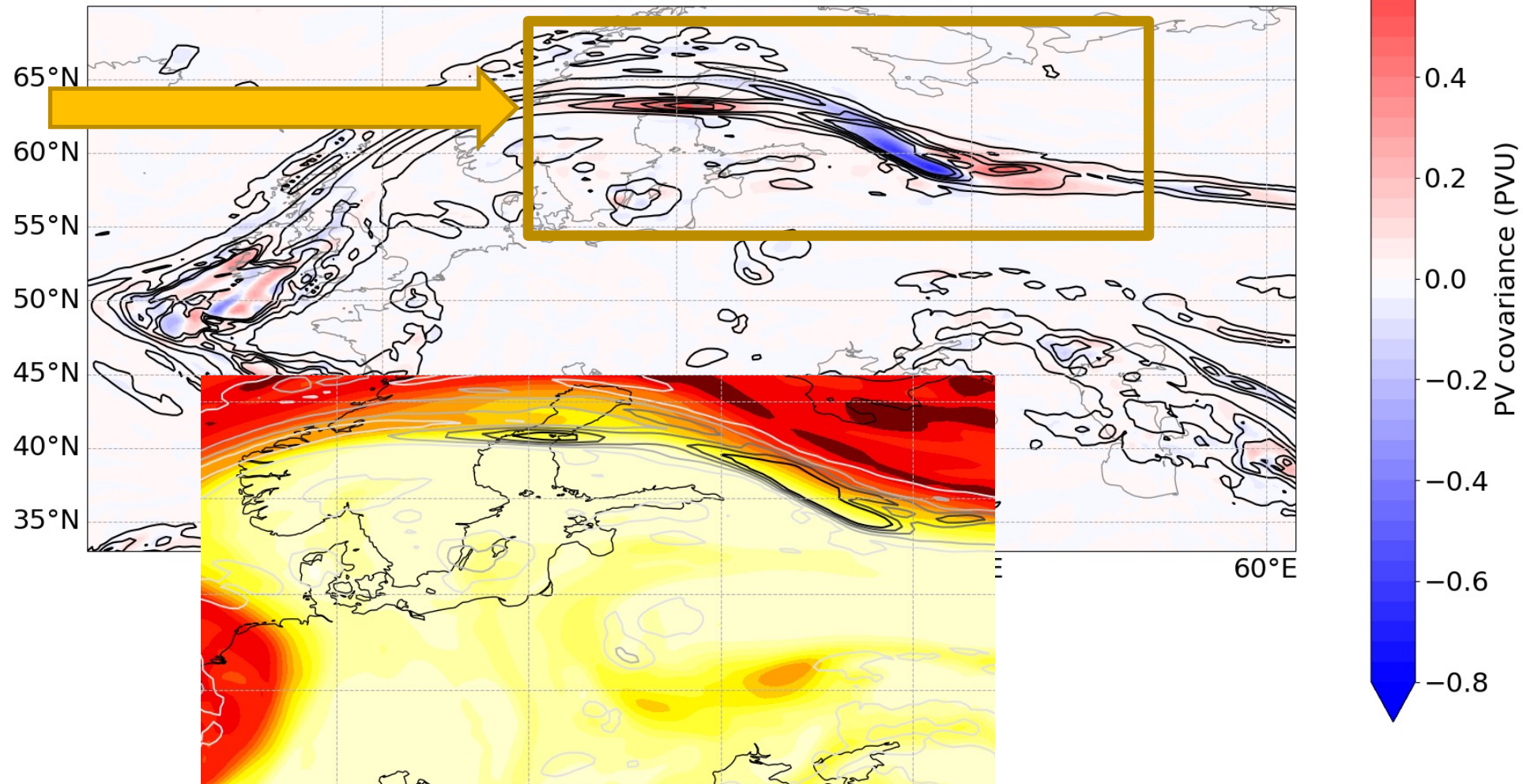


# “Day 2 system” +50 h

ESA: PV sensitivity structure (colours); PV-spread 250 hPa (isolines)  
050 hours since 10-06-2019 12 UTC

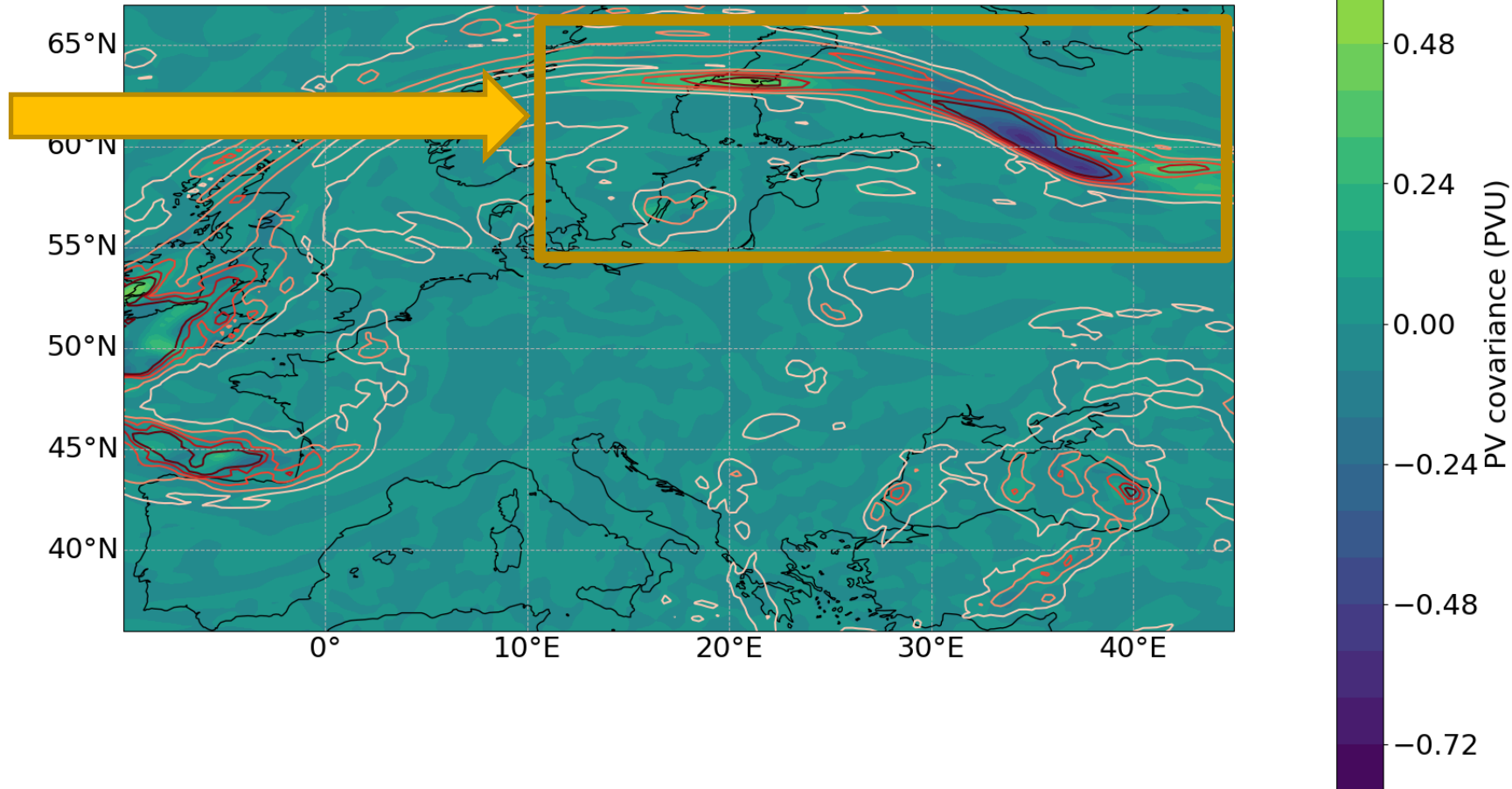


ESA: PV sensitivity structure (colours); PV-spread 250 hPa (isolines)  
054 hours since 10-06-2019 12 UTC

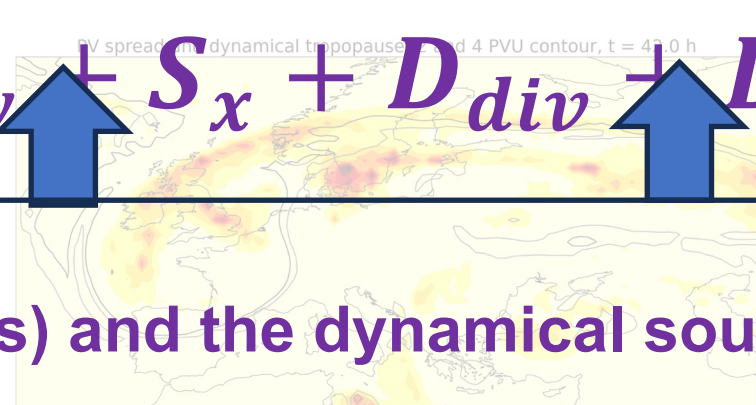
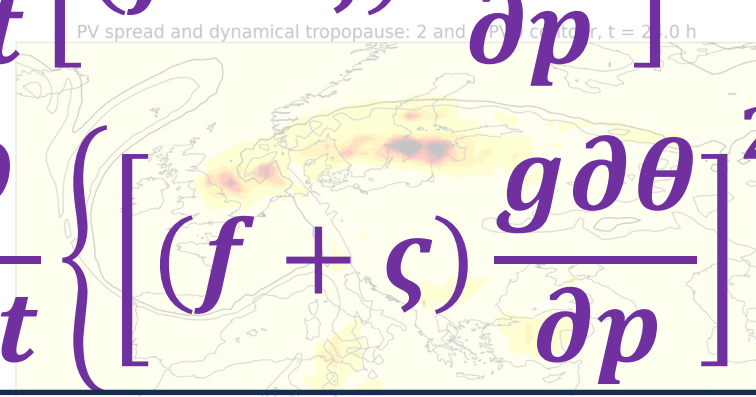
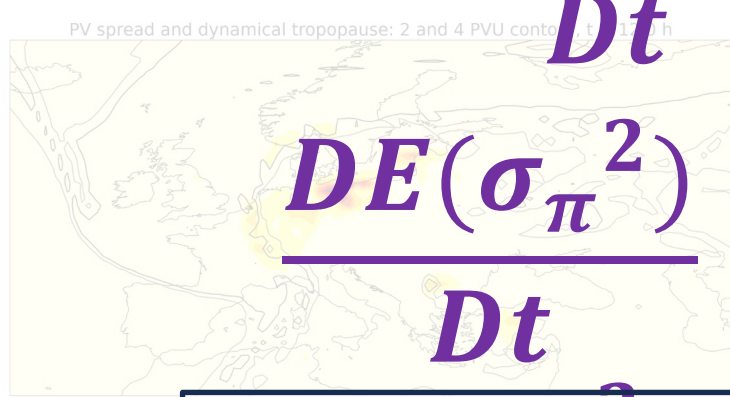


# “Day 2 system” +54 h: precipitation rate

ESA: PV sensitivity structure (colours); PV-variability 250 hPa (isolines)  
054 hours since 10-06-2019 12 UTC



# PART 2: Why does the spread grow?



$$\frac{D\pi}{Dt} = \frac{D}{Dt} \left[ (f + \zeta) \frac{g\partial\theta}{\partial p} \right]$$

$$\frac{DE(\sigma_\pi^2)}{Dt} = \frac{D}{Dt} \left\{ \left[ (f + \zeta) \frac{g\partial\theta}{\partial p} \right]^2 \right\}$$

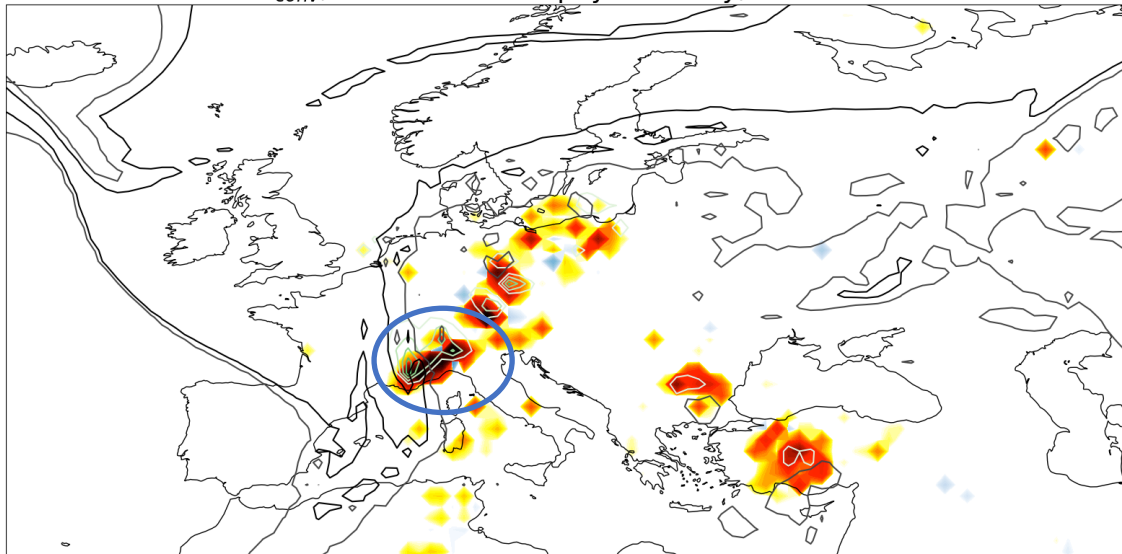
$$\frac{DE(\sigma_\pi^2)}{Dt} = S_y + S_x + D_{div} + D_{rot}$$

The parameterized sources (sinks) and the dynamical sources (sinks)

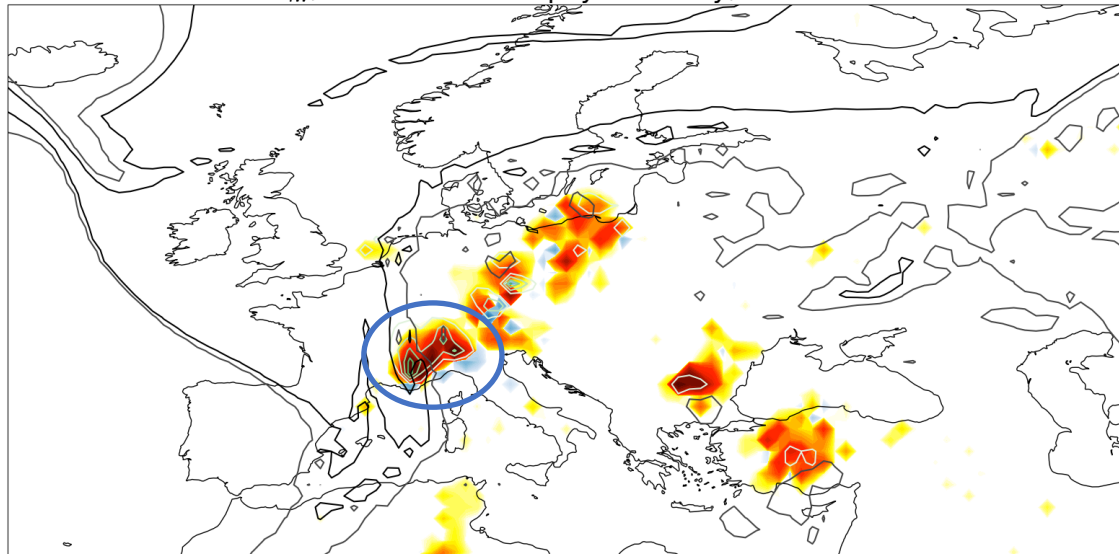
of ensemble spread



$T_{conv}$ , 3hr mean enstrophy tendency,  $t = 6.0$  h

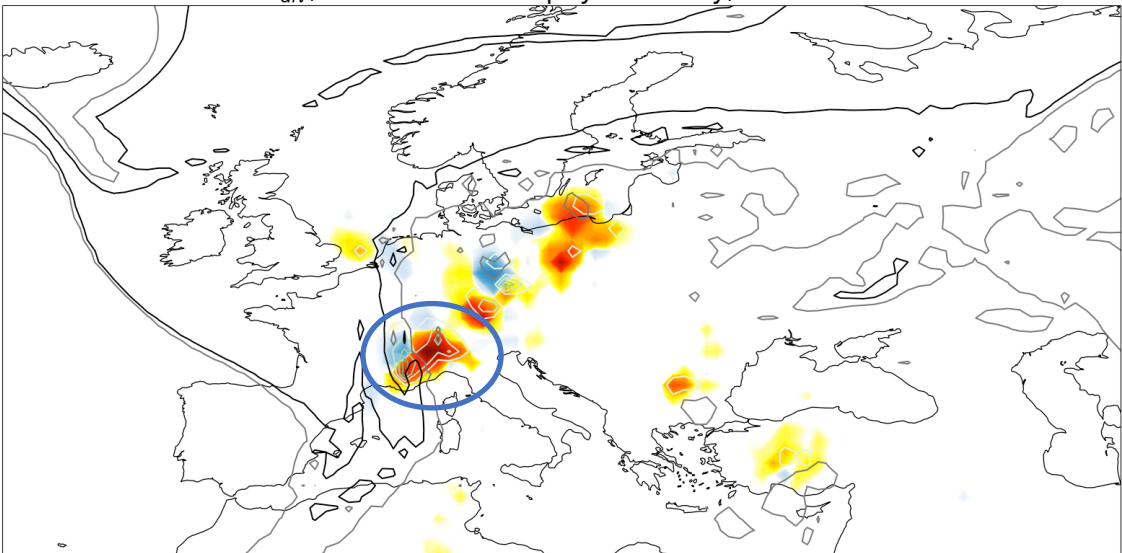


$T_{lw}$ , 3hr mean enstrophy tendency,  $t = 6.0$  h



### Convective heating

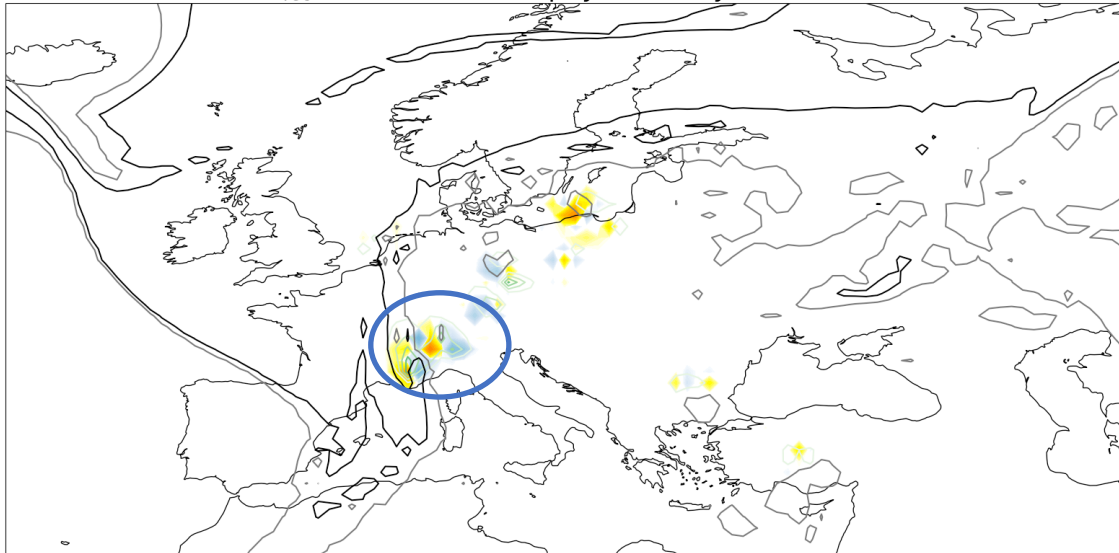
$T_{div}$ , 3hr mean enstrophy tendency,  $t = 6.0$  h



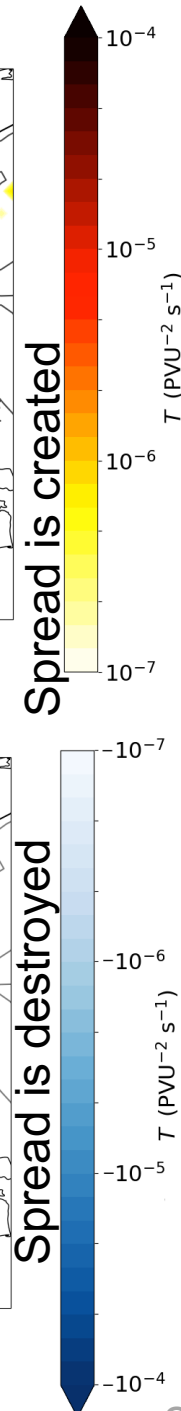
### Divergent advection

### Longwave radiation

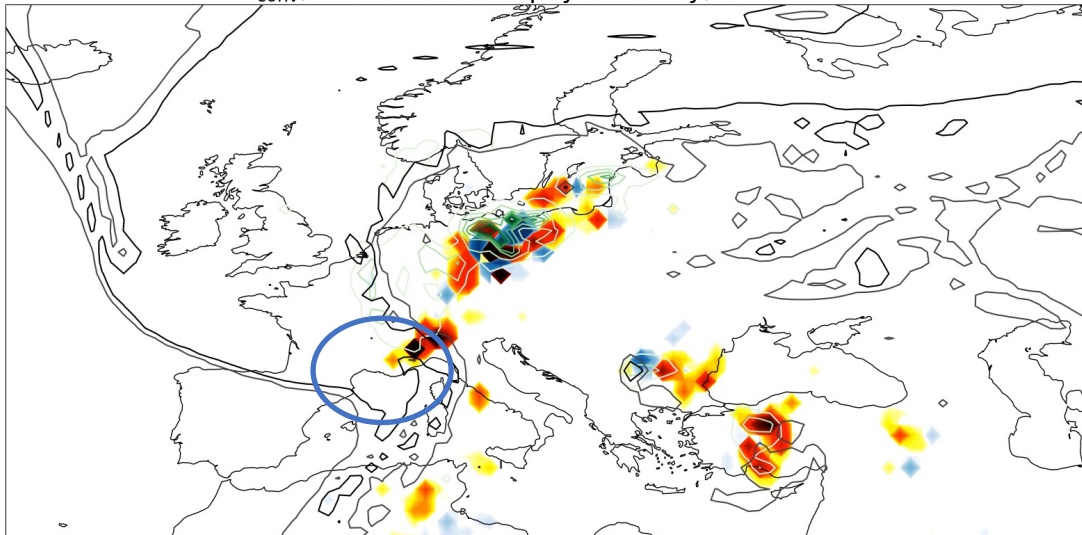
$T_{rot}$ , 3hr mean enstrophy tendency,  $t = 6.0$  h



### Rotational advection

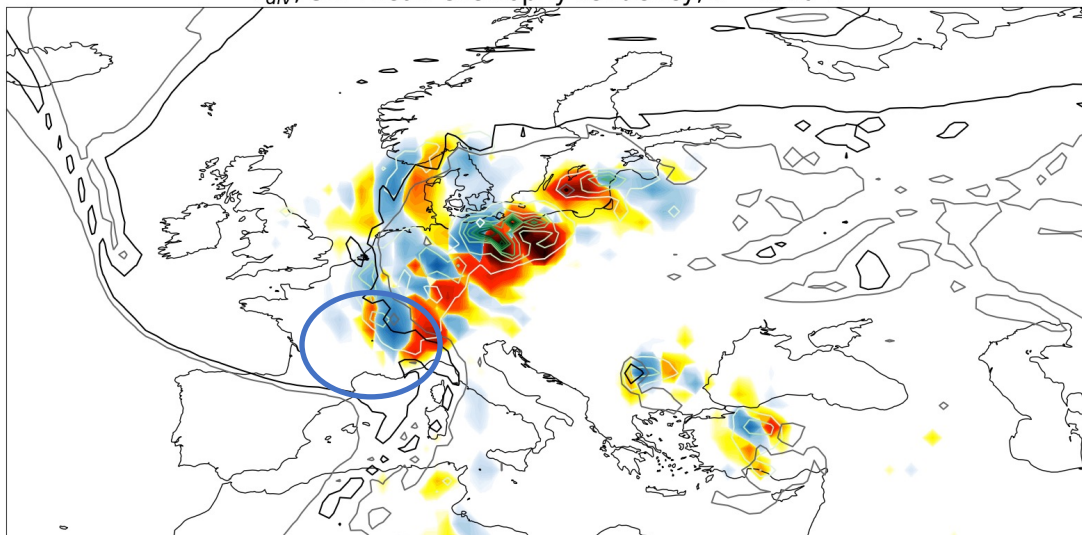


$T_{conv}$ , 3hr mean entrophy tendency, t = 12.0 h



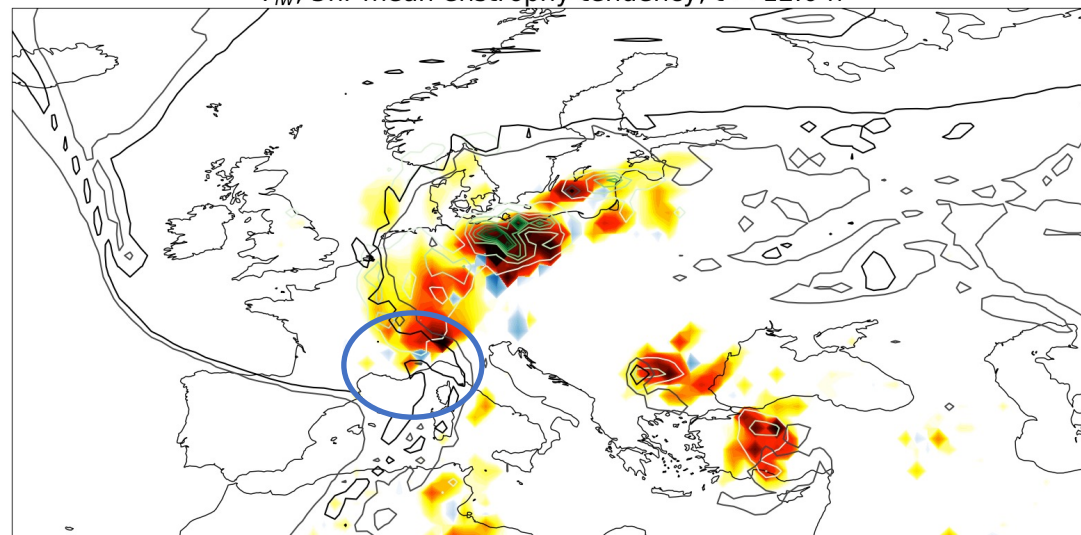
Convective heating

$T_{div}$ , 3hr mean entrophy tendency, t = 12.0 h



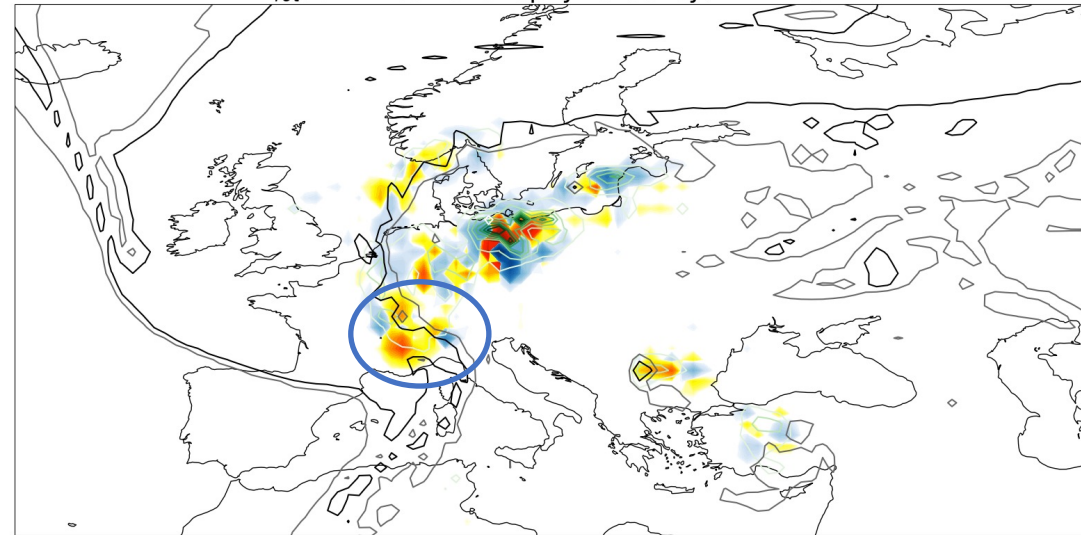
Divergent advection

$T_{lw}$ , 3hr mean entrophy tendency, t = 12.0 h

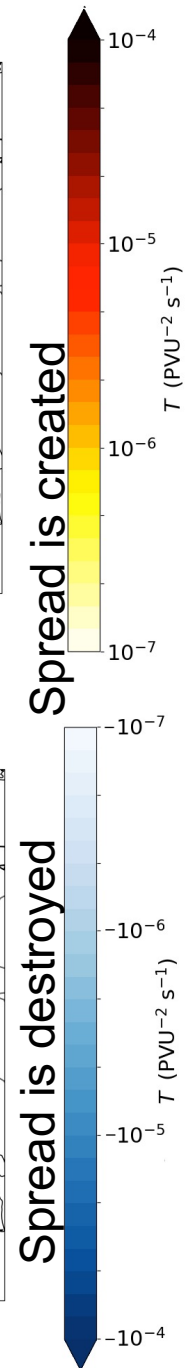


Longwave radiation

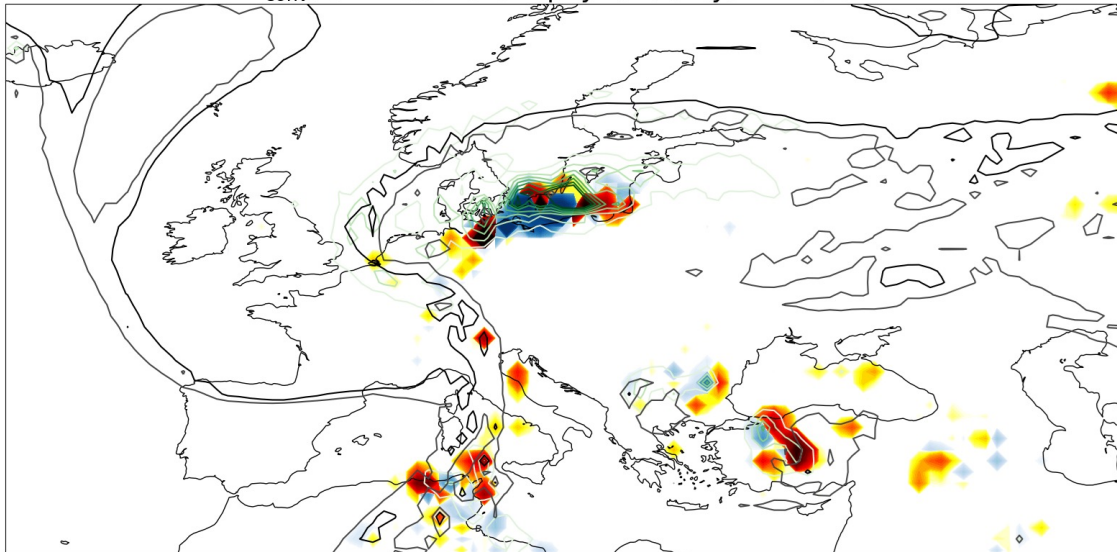
$T_{rot}$ , 3hr mean entrophy tendency, t = 12.0 h



Rotational advection

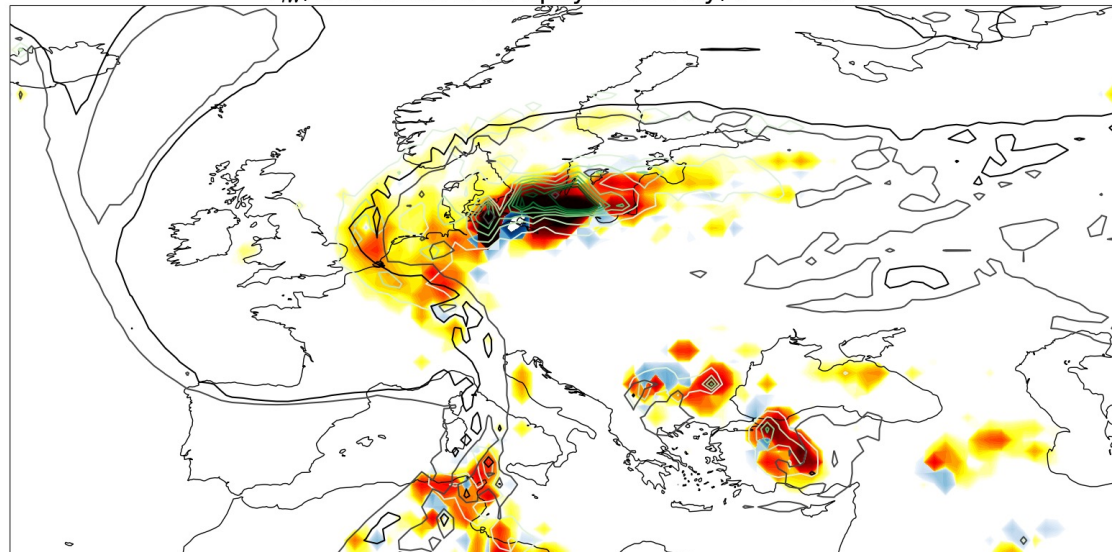


$T_{conv}$ , 3hr mean enstrophy tendency, t = 18.0 h



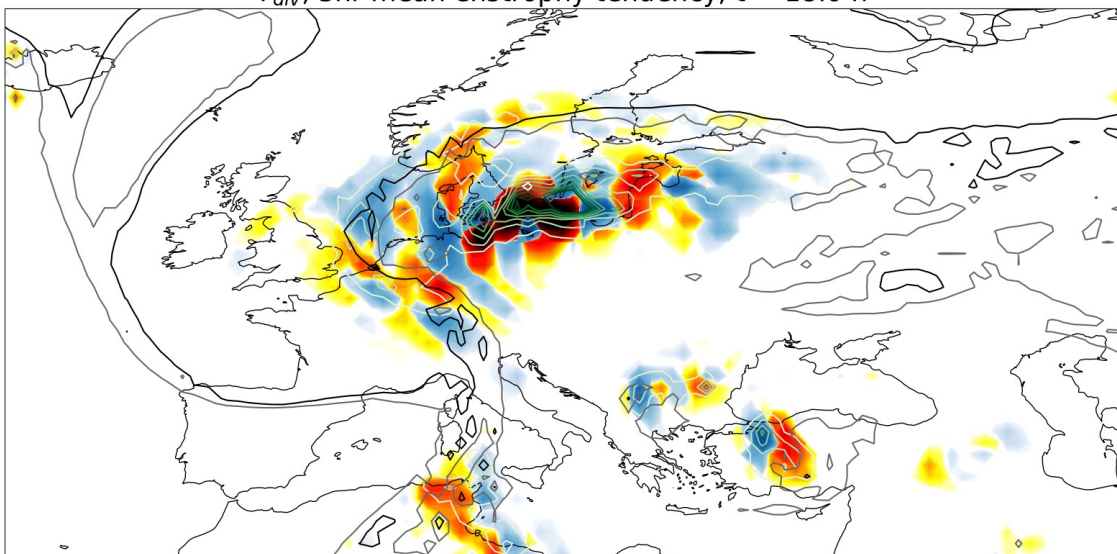
Convective heating

$T_{lw}$ , 3hr mean enstrophy tendency, t = 18.0 h



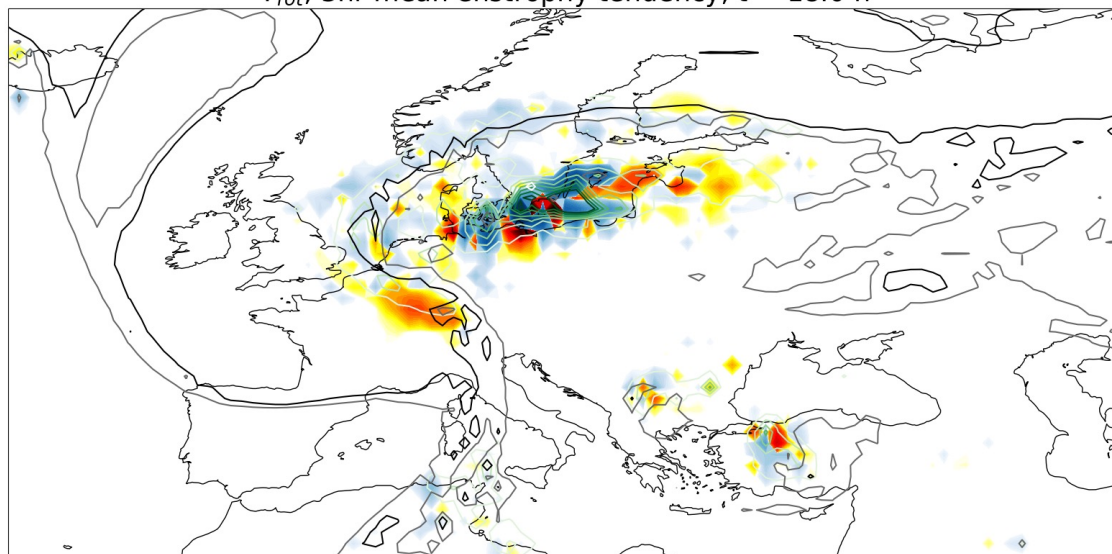
Longwave radiation

$T_{div}$ , 3hr mean enstrophy tendency, t = 18.0 h

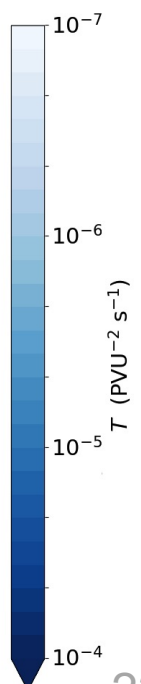
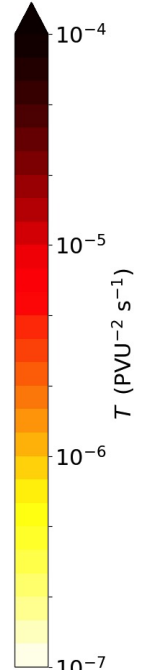


Divergent advection

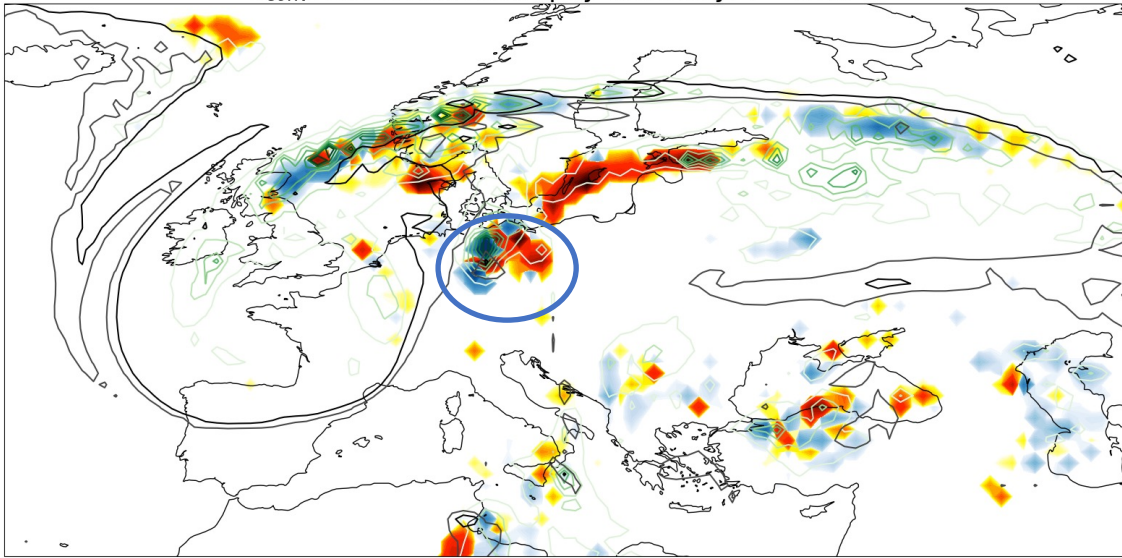
$T_{rot}$ , 3hr mean enstrophy tendency, t = 18.0 h



Rotational advection

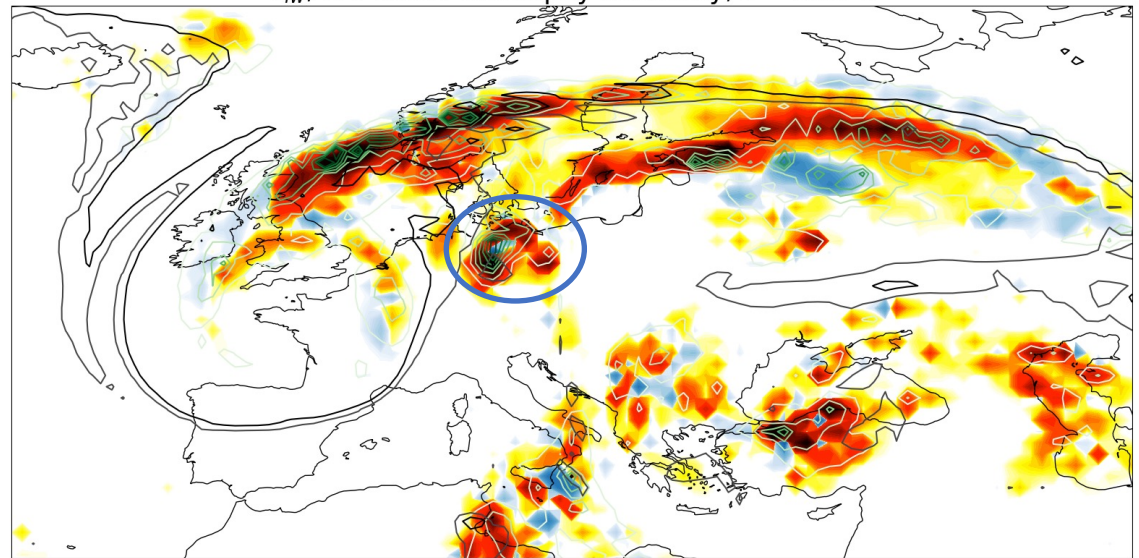


$T_{conv}$ , 3hr mean enstrophy tendency, t = 36.0 h



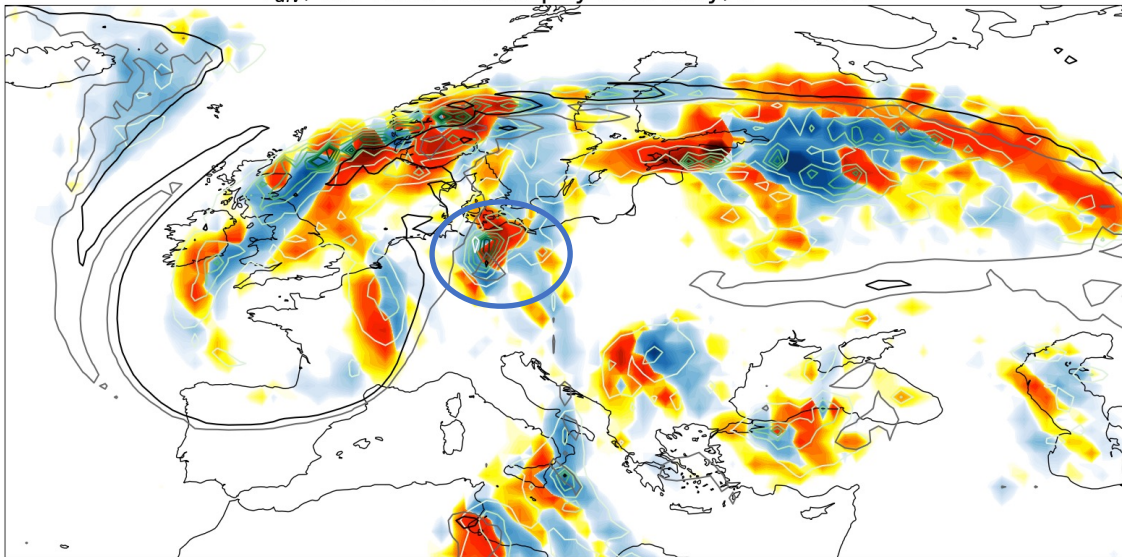
Convective heating

$T_{lw}$ , 3hr mean enstrophy tendency, t = 36.0 h



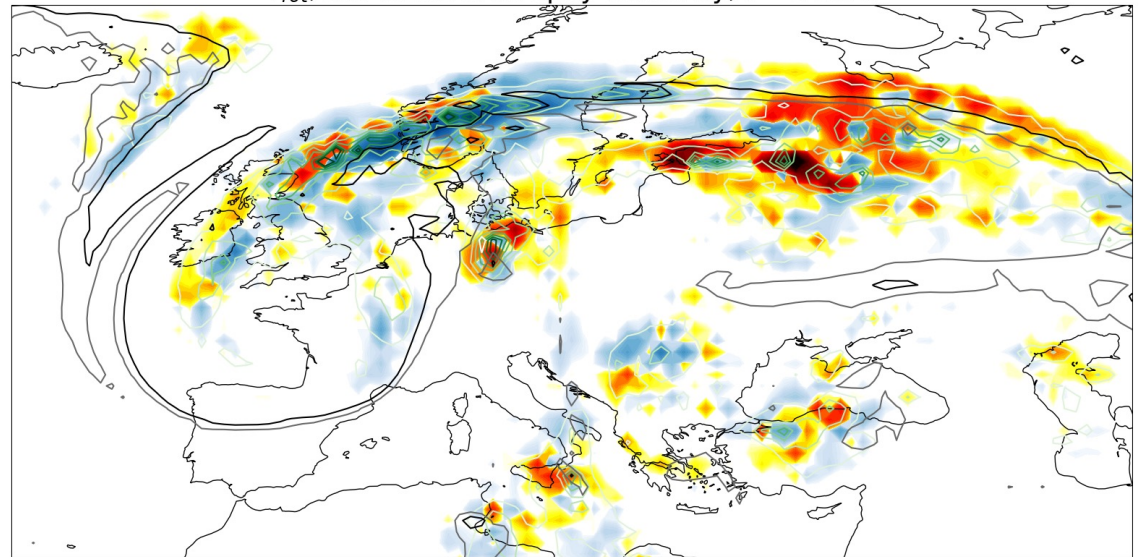
Longwave radiation

$T_{div}$ , 3hr mean enstrophy tendency, t = 36.0 h

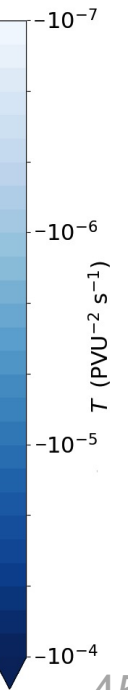
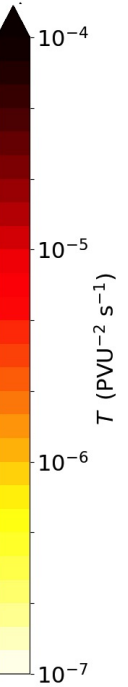


Divergent advection

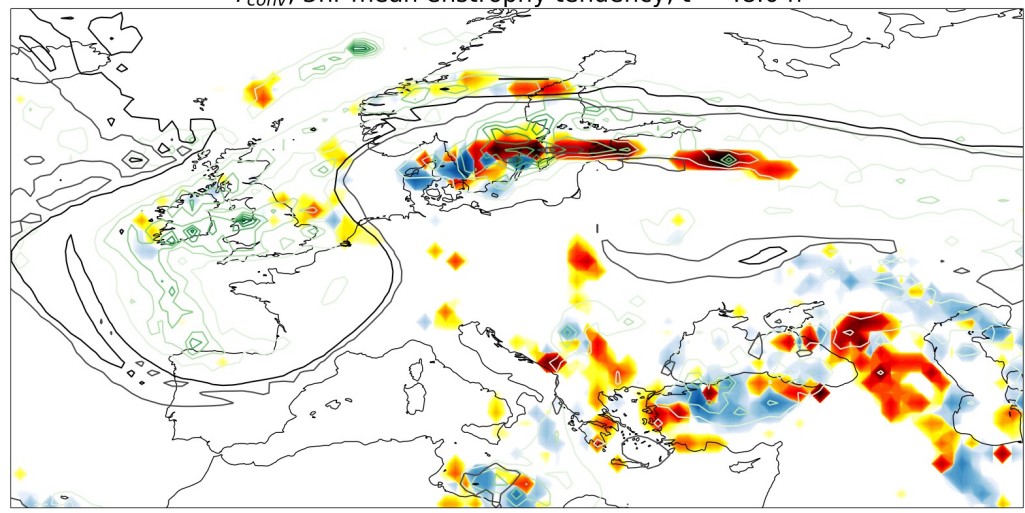
$T_{rot}$ , 3hr mean enstrophy tendency, t = 36.0 h



Rotational advection

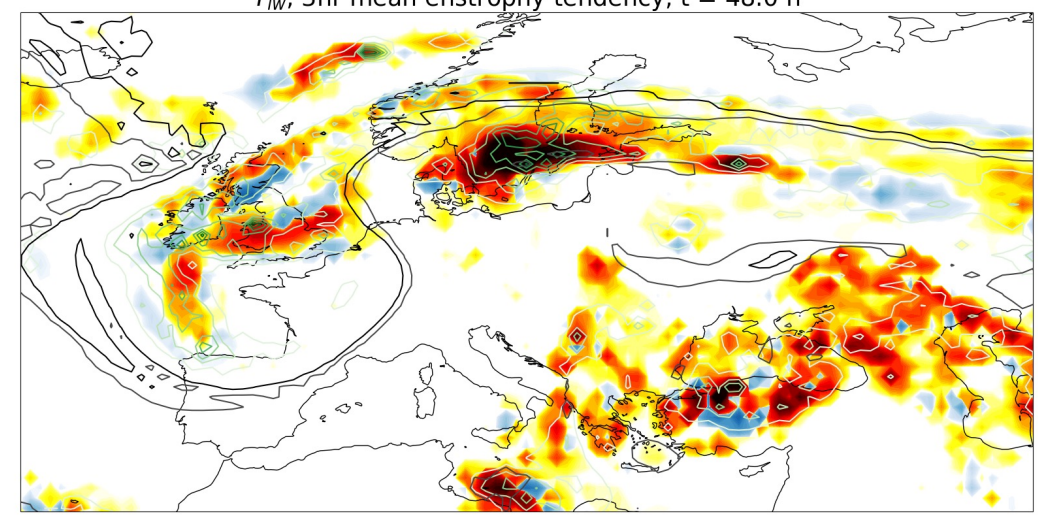


$T_{conv}$ , 3hr mean enstrophy tendency,  $t = 48.0$  h



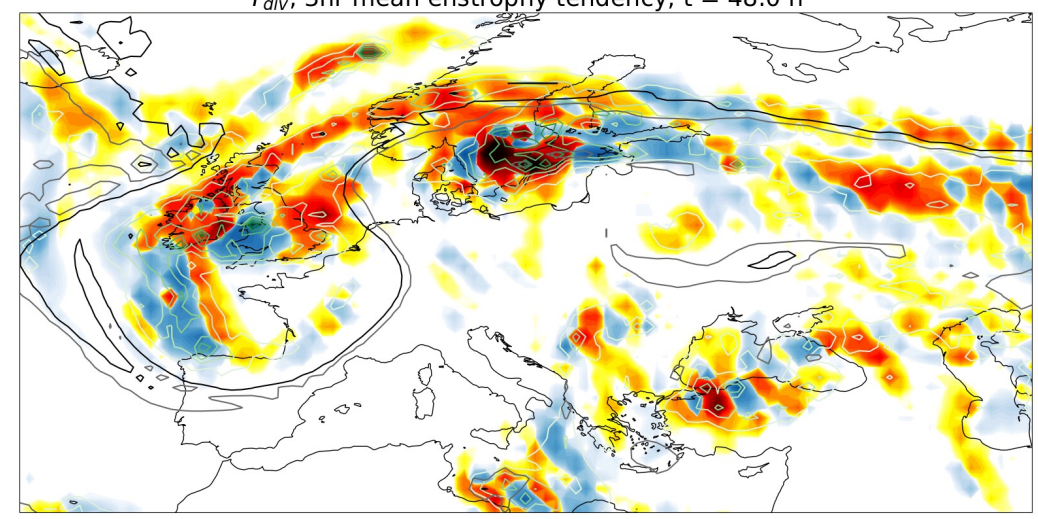
Convective heating

$T_{lw}$ , 3hr mean enstrophy tendency,  $t = 48.0$  h



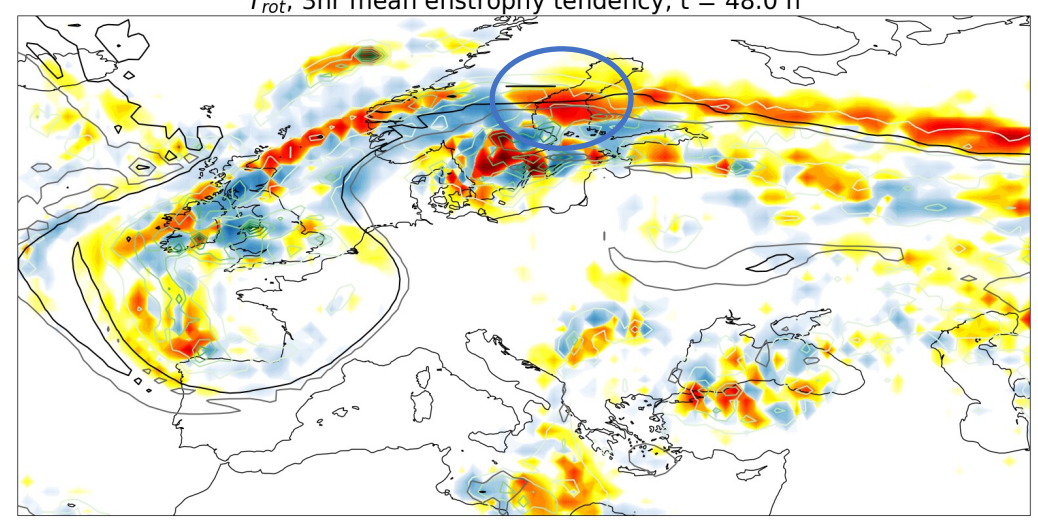
Longwave radiation

$T_{div}$ , 3hr mean enstrophy tendency,  $t = 48.0$  h

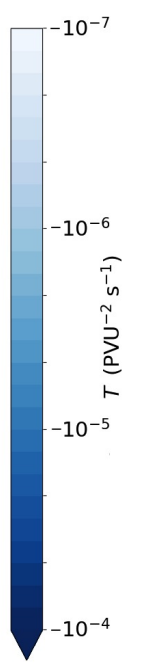
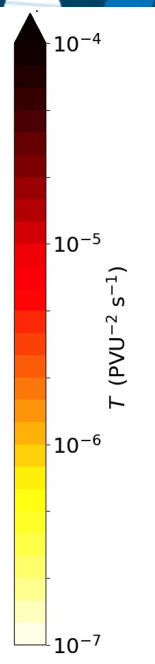


Divergent advection

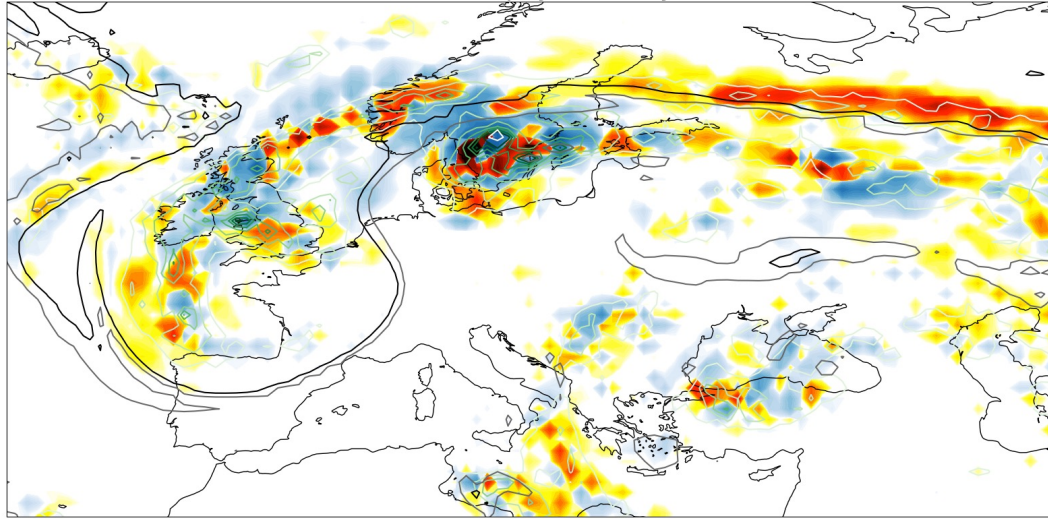
$T_{rot}$ , 3hr mean enstrophy tendency,  $t = 48.0$  h



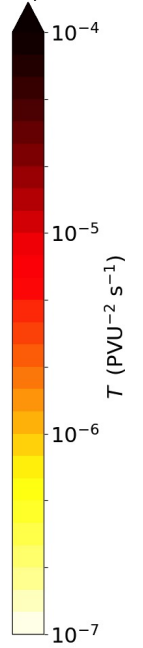
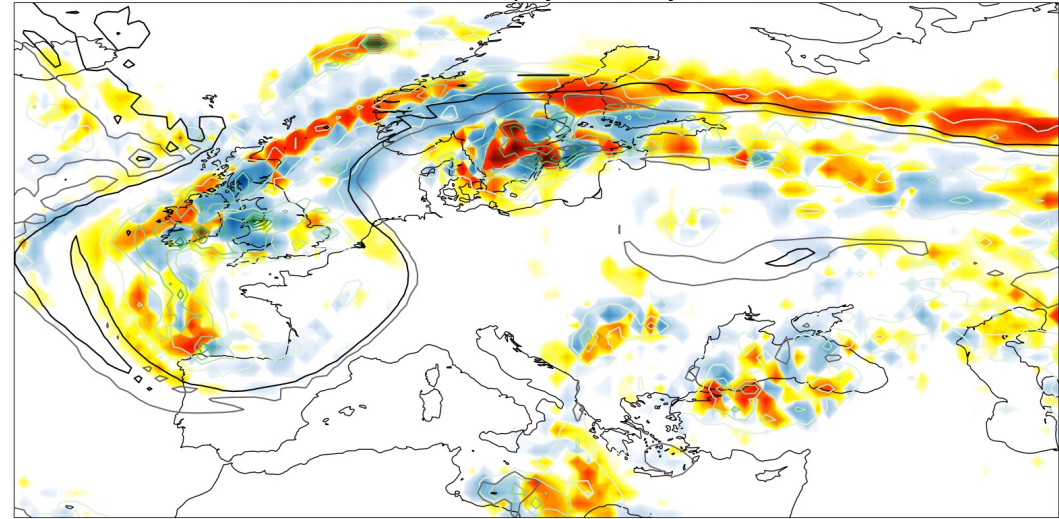
Rotational advection



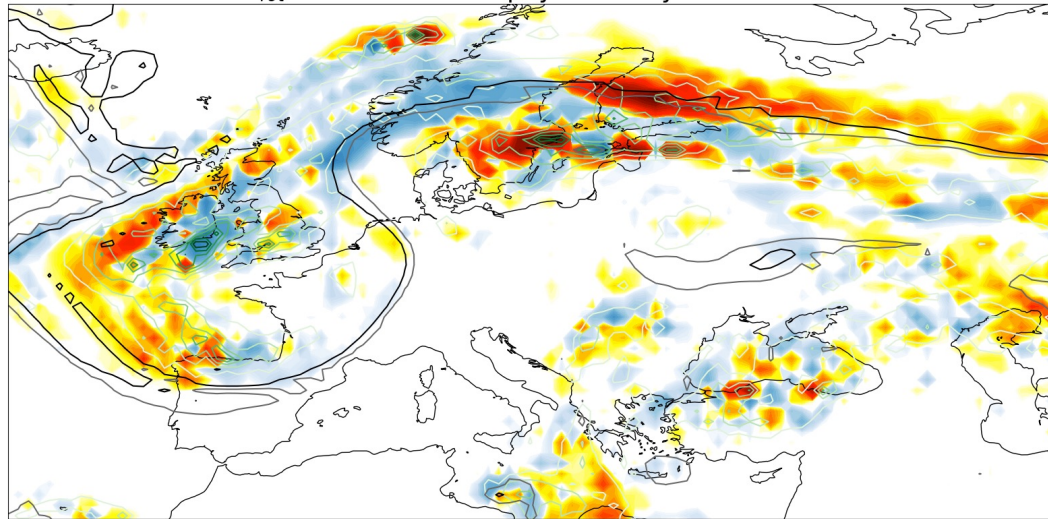
$T_{rot}$ , 3hr mean enstrophy tendency, t = 45.0 h



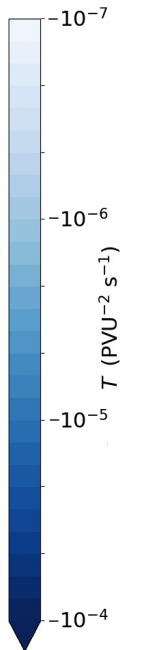
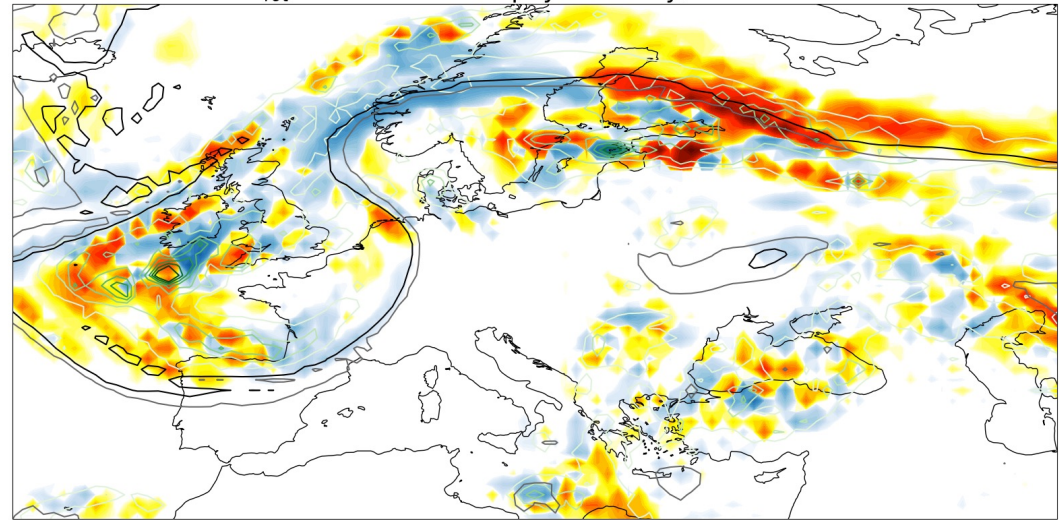
$T_{rot}$ , 3hr mean enstrophy tendency, t = 48.0 h



$T_{rot}$ , 3hr mean enstrophy tendency, t = 51.0 h



$T_{rot}$ , 3hr mean enstrophy tendency, t = 54.0 h



# Summary & conclusions II

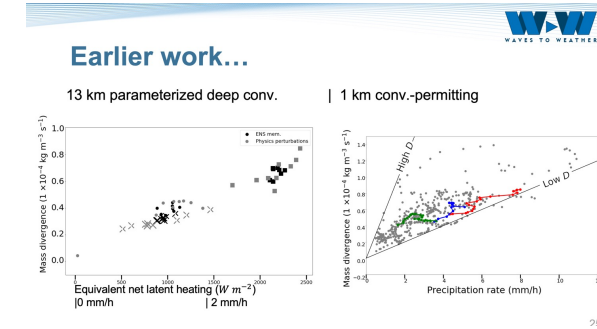
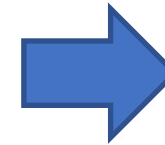
Jet stream winds in an underdispersed ensemble are sensitive to convective variability, where

- Small uncertainties in precipitation can rapidly induce forecast uncertainty downstream
- Convective latent heating/mass divergence variability can but does not always propagate downstream and upscale
- Combining two methods enables us to quantify and attribute forecast uncertainty

# Take home messages

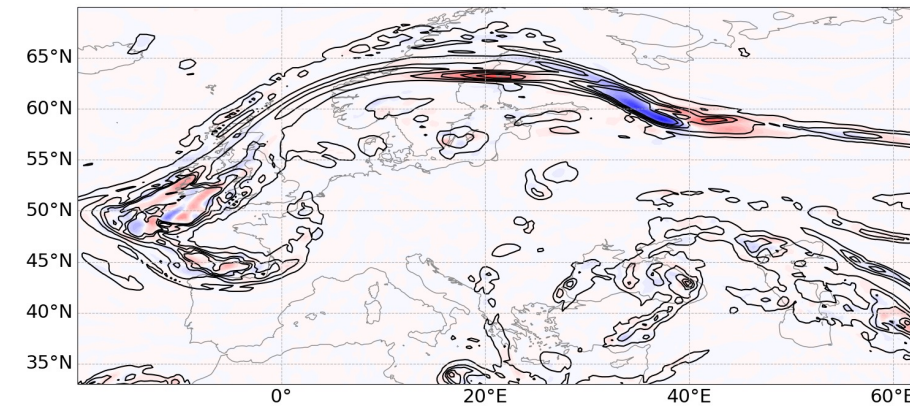
## Modelling of deep convection

- Representation of convective outflow variability is more advanced at higher resolution

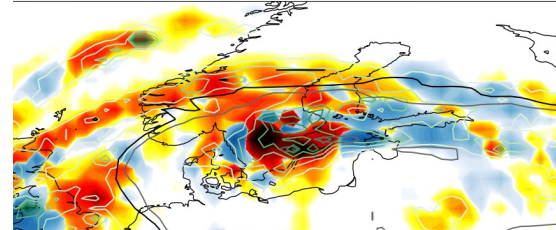


## Downstream effect of deep convection

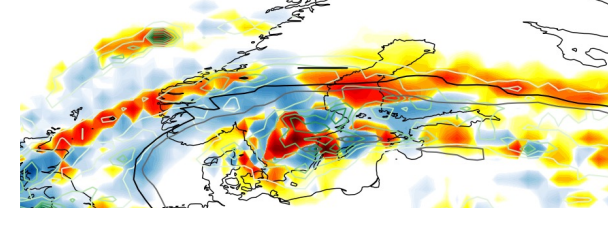
- Convective variability can but does not always propagate downstream and upscale



$T_{div}$ , 3hr mean enstrophy tendency,  $t = 48.0 \text{ h}$



$T_{rot}$ , 3hr mean enstrophy tendency,  $t = 48.0 \text{ h}$





# Thank you for your attention!