

Flow dependence of error-growth mechanisms: PV diagnostics and feature framework

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JG|U

Why diagnose error-growth mechanisms?

- The intrinsic limit of predictability is characterized by a distinct sequence of error-growth mechanisms (presentation by Tobias Selz on Monday).
- Representation of error-growth mechanisms in numerical (ensemble) models determines representation of forecast uncertainty.

Why diagnose flow dependence?

- may indicate flow situations, in which intrinsic limit is already reached
- enables more focused model verification and development
- aids in recognizing model error wrt. representation of uncertainty, a limitation of current ML models*

* (e.g., Selz, T., & Craig, G. C. (2023). Can artificial intelligence-based weather prediction models simulate the butterfly effect?. *GRL*, 50(20))

The background is a dark, monochromatic painting of a tropical scene. It features several palm trees with long, slender trunks and large, feathery fronds. In the foreground, there are the silhouettes of buildings with gabled roofs. The overall tone is dark and atmospheric, with a focus on the shapes and textures of the tropical elements.

Potential-vorticity diagnostic for error-growth mechanisms

Why potential vorticity (PV)?

A single scalar quantity – PV – subsumes the balanced state of the atmosphere.

☐ PV is a key quantity of atmospheric dynamics

Upscale error growth eventually affects the balanced state.



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$$\frac{\partial PV}{\partial t} =$$

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Why potential vorticity (PV)?

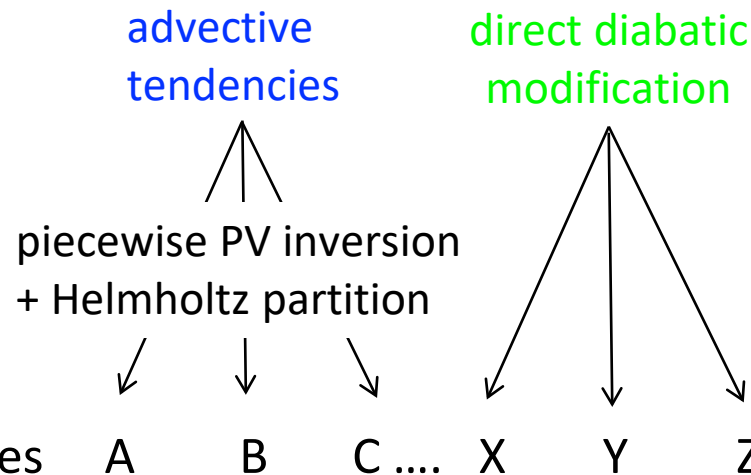
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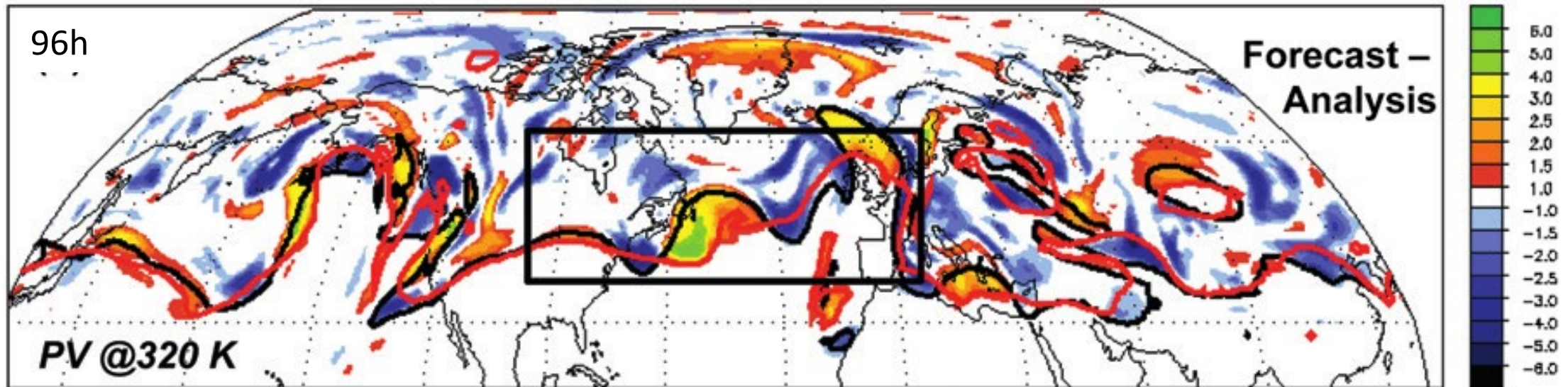


Piecewise PV tendency framework

☐ Mechanistic understanding

PV perspective on forecast errors

(Davies and Didone 2013, Fig. 1b)



2 PVU contour: — forecast — analysis

Davies and Didone (2013):

- PV errors maximize near the tropopause; displacement of the tropopause
- PV-error tendency equation

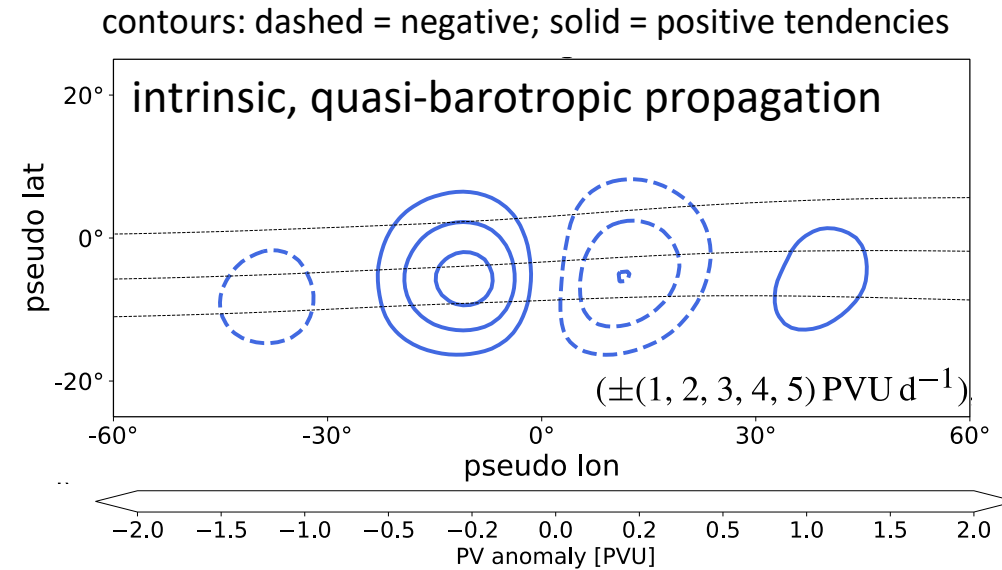
Baumgart et al. (2018, 2019); Baumgart and Riemer (2019):

Piecewise PV-error tendencies = quantification of *individual* contributions to error/ spread growth

Piecewise PV tendencies: Illustration

- Dynamics of Rossby wave packets
- Upper-level perspective on isentropes that intersect the midlatitude tropopause
- Composites over ERA-5 period

(Teubler and Riemer 2021, Fig. 3, modified)



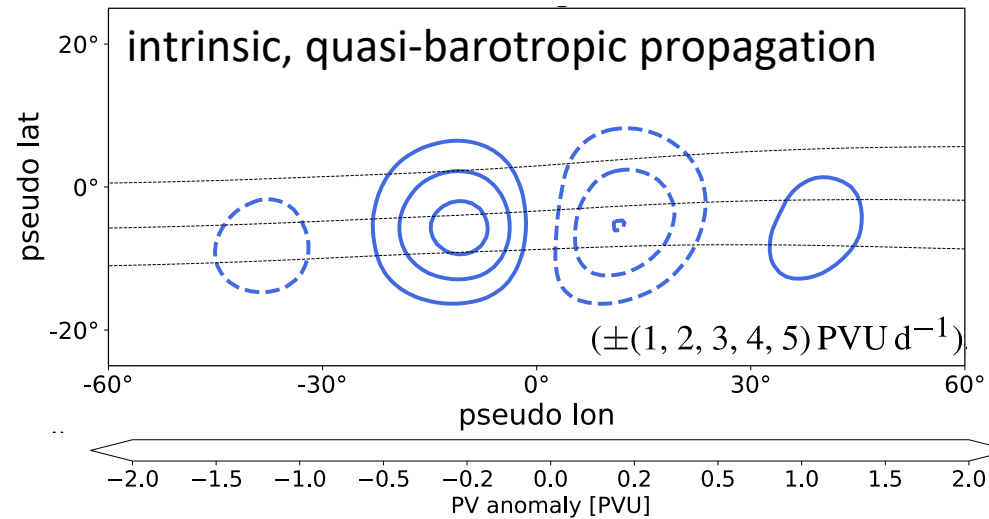
includes
nonlinear
tropopause
dynamics

Piecewise PV tendencies: Illustration

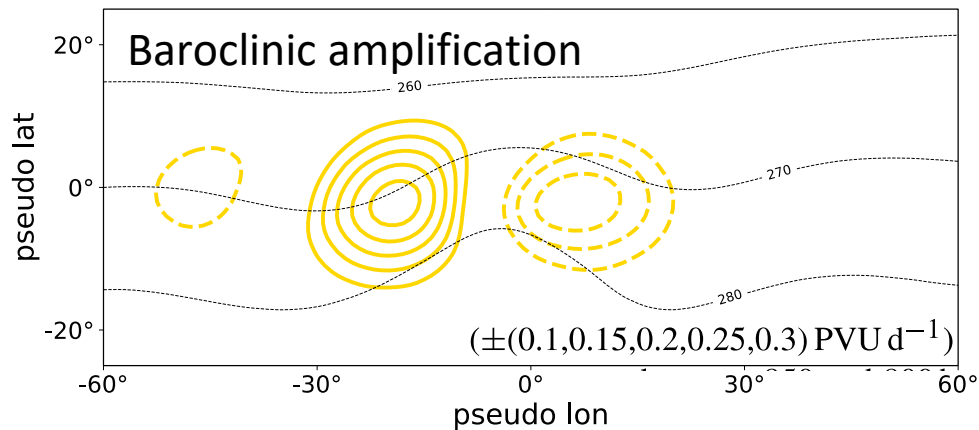
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contours: dashed = negative; solid = positive tendencies



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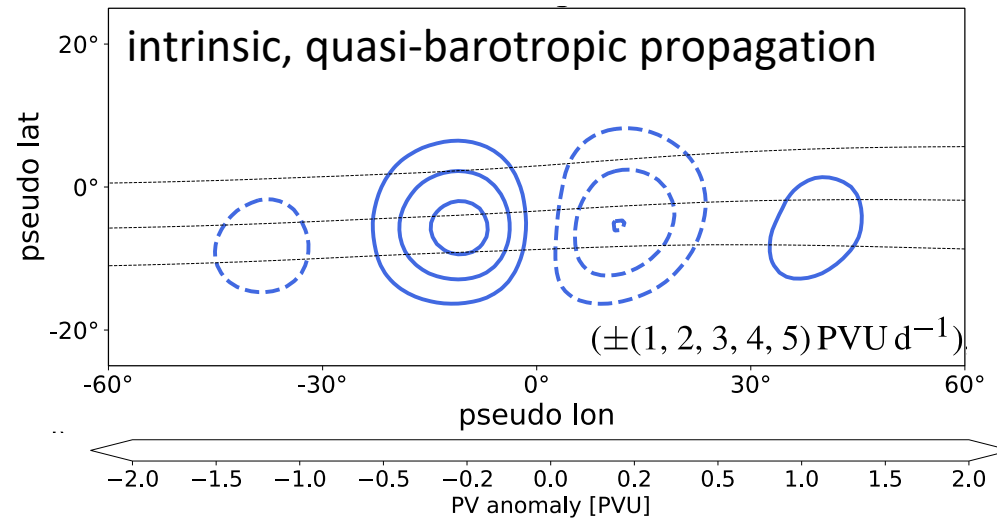


Piecewise PV tendencies: Illustration

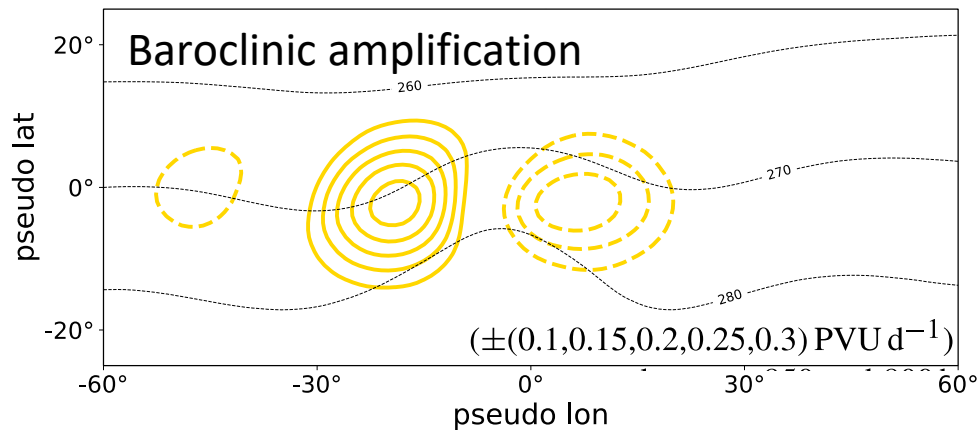
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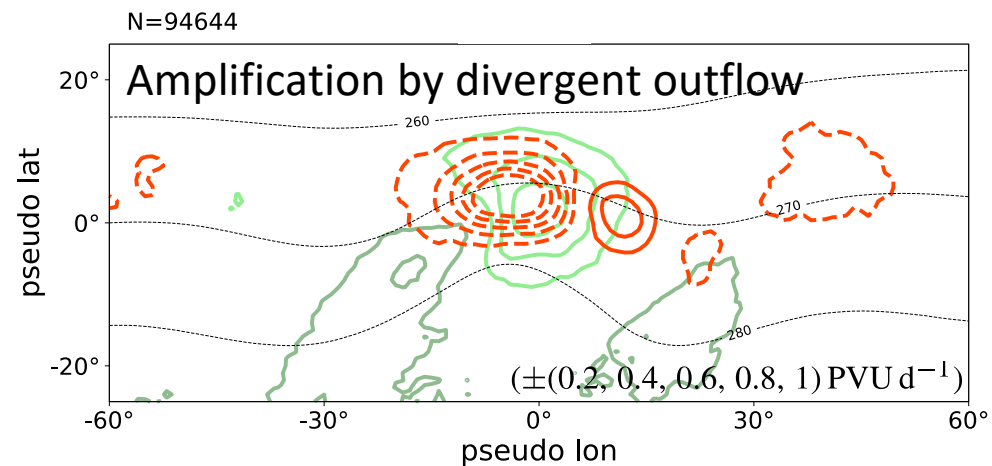
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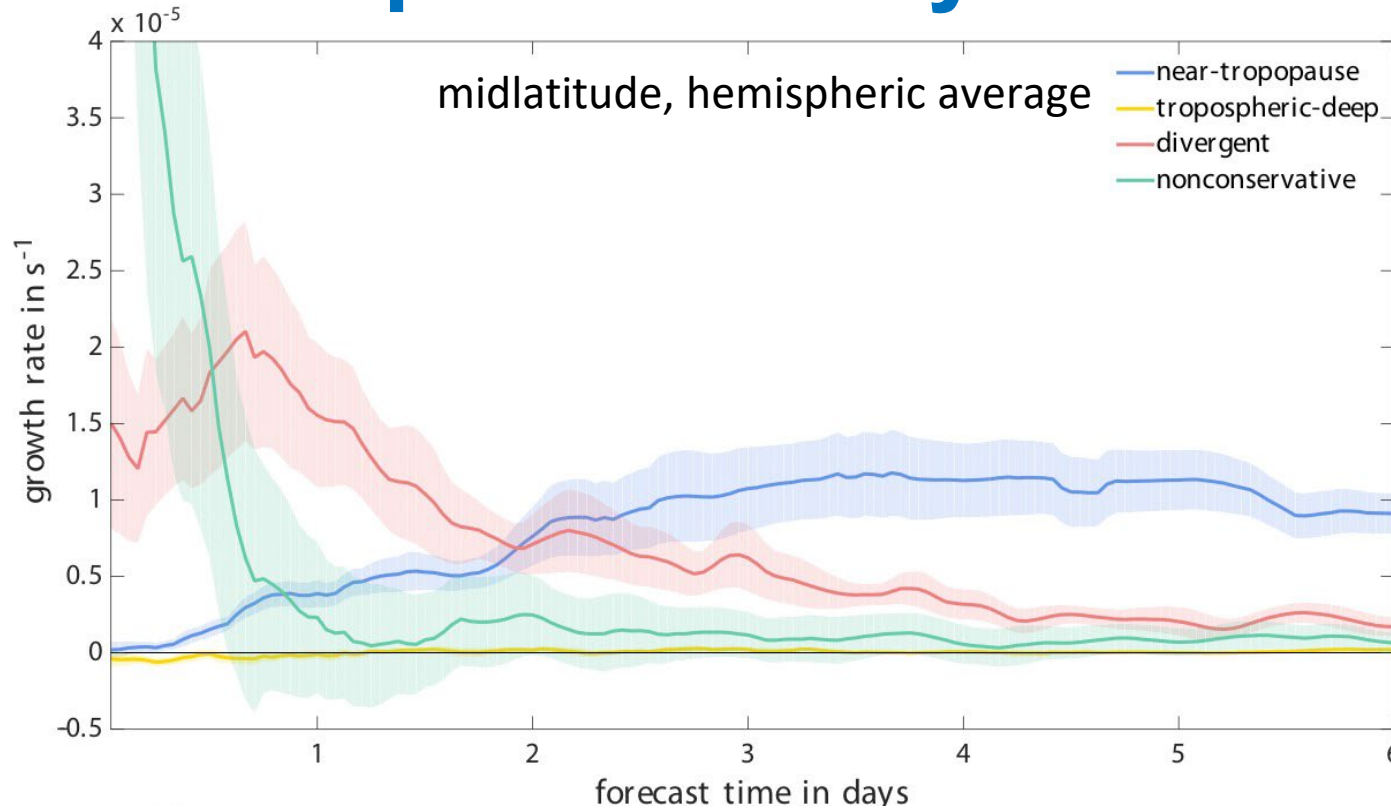
moist-baroclinic development



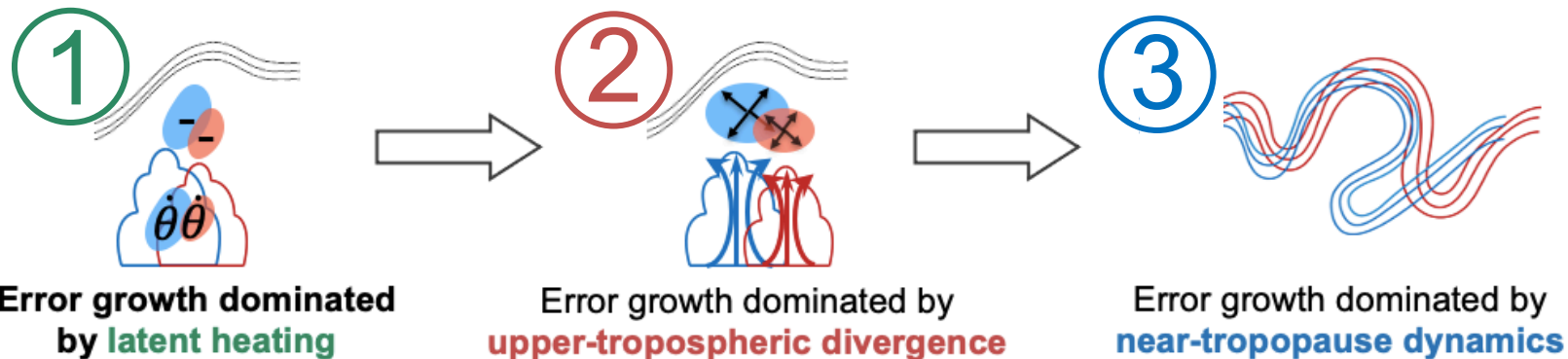
light green: proxy of latent heat release

Same result as presented by Tobias Selz

PV diagnostic applied to error-growth experiment with minimal IC uncertainty (Baumgart et al. 2019)

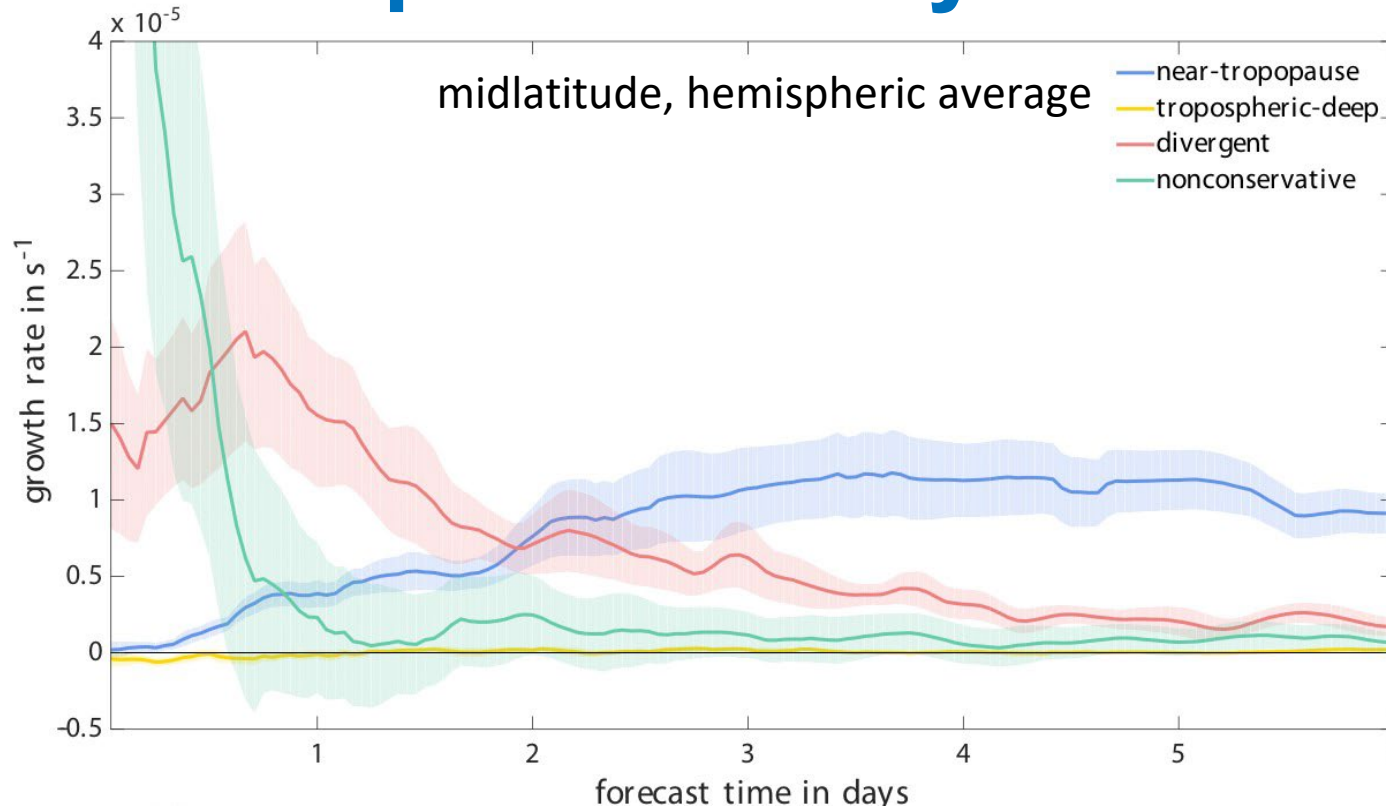


Sequence of dominant error-growth mechanisms (3-stage model)



Same result as presented by Tobias Selz

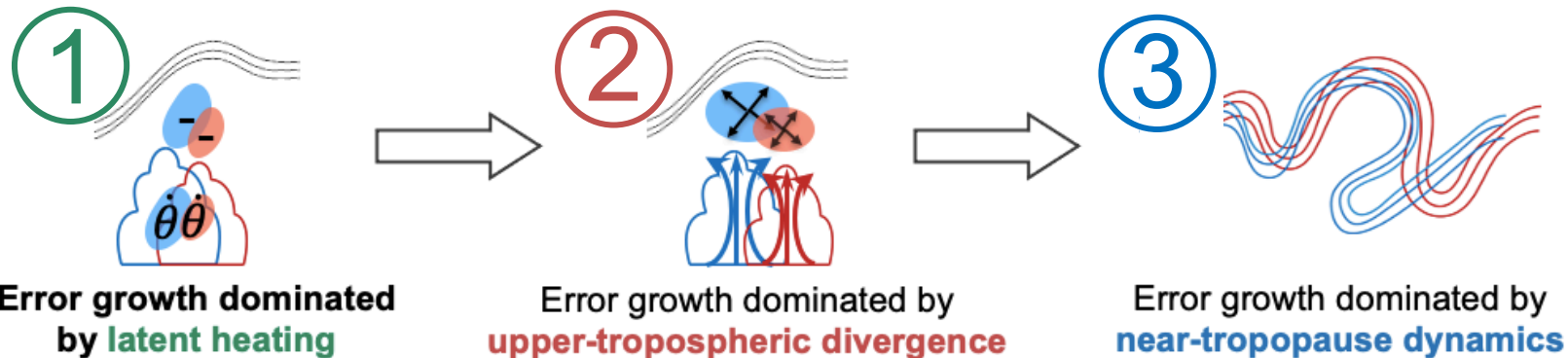
PV diagnostic applied to error-growth experiment with minimal IC uncertainty (Baumgart et al. 2019)



Tropospheric-deep baroclinic growth is *on average* a subordinate error-growth mechanism

(costly piecewise PV inversion for many applications not required)

Sequence of dominant error-growth mechanisms (3-stage model)

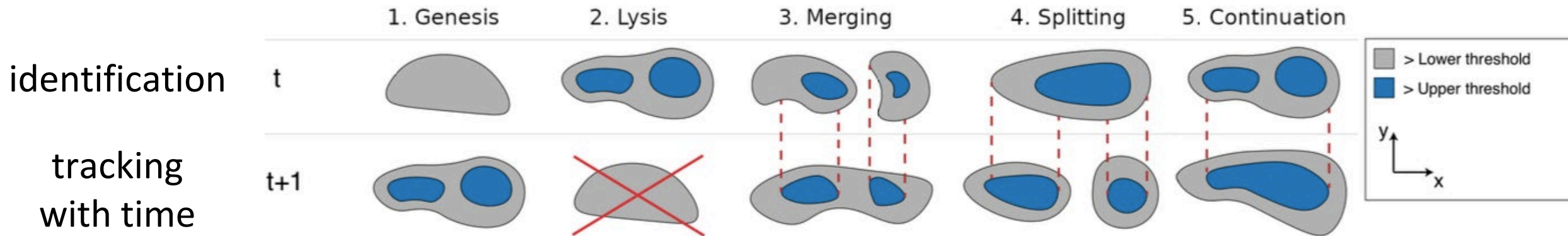


A dark, atmospheric background featuring a tropical scene with palm trees and a building. The text is overlaid in a bright yellow color.

next talk: case study

**Efficient analysis of a large
number of “cases” □
feature-based analysis**

Feature framework

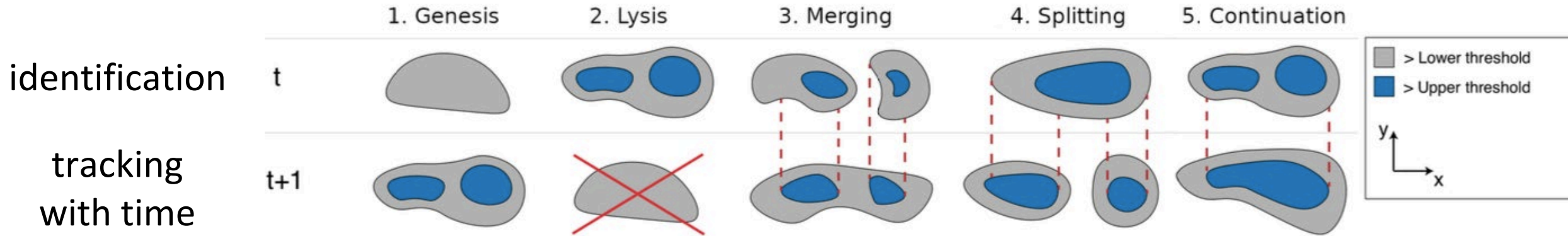


Goal: identify evolution that is coherent in space and *time*

Weather systems (MSC, cyclones, ...)



Feature framework difficult for errors/ spread

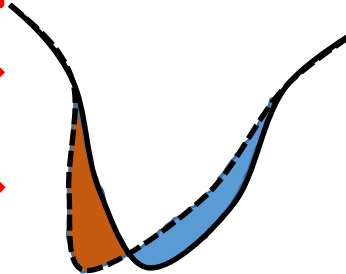


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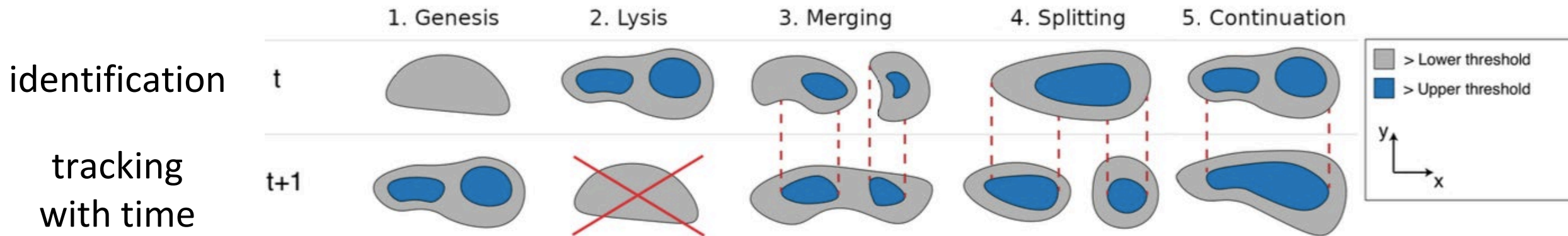
Weather systems (MSC, cyclones, ...)



Forecasts errors/ spread



Feature framework difficult for errors/ spread

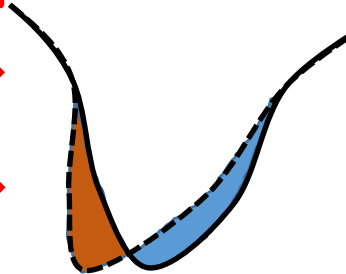


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Forecasts errors/ spread



Splitting and merging is ubiquitous for error features.

Feature framework difficult for errors/ spread



Goal: identify evolution that is coherent in space and *time*

Weather systems (MSC, cyclones, ...)  Forecasts errors/ spread 

Splitting and merging is ubiquitous for error features.
 → non-uniqueness in the temporal evolution of features *or*
 → severe limitation to track features back in time

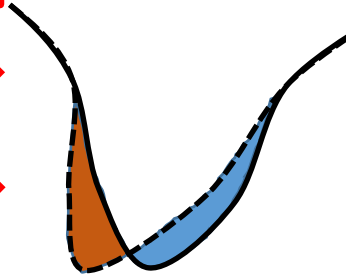
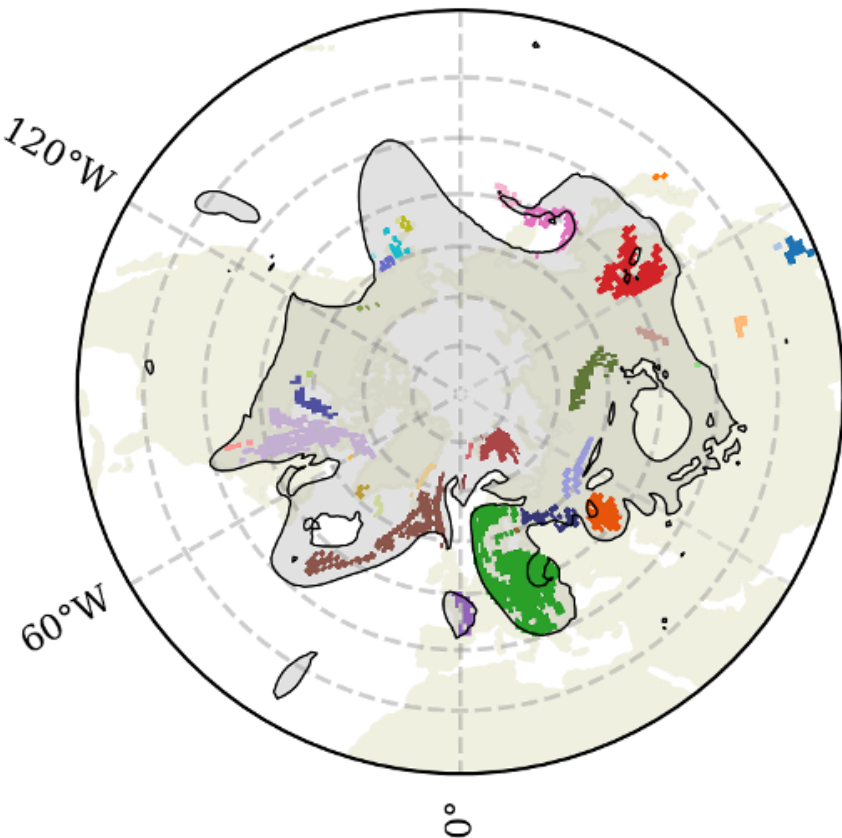


Illustration of problem (grey features)

lead time 72h

unprocessed

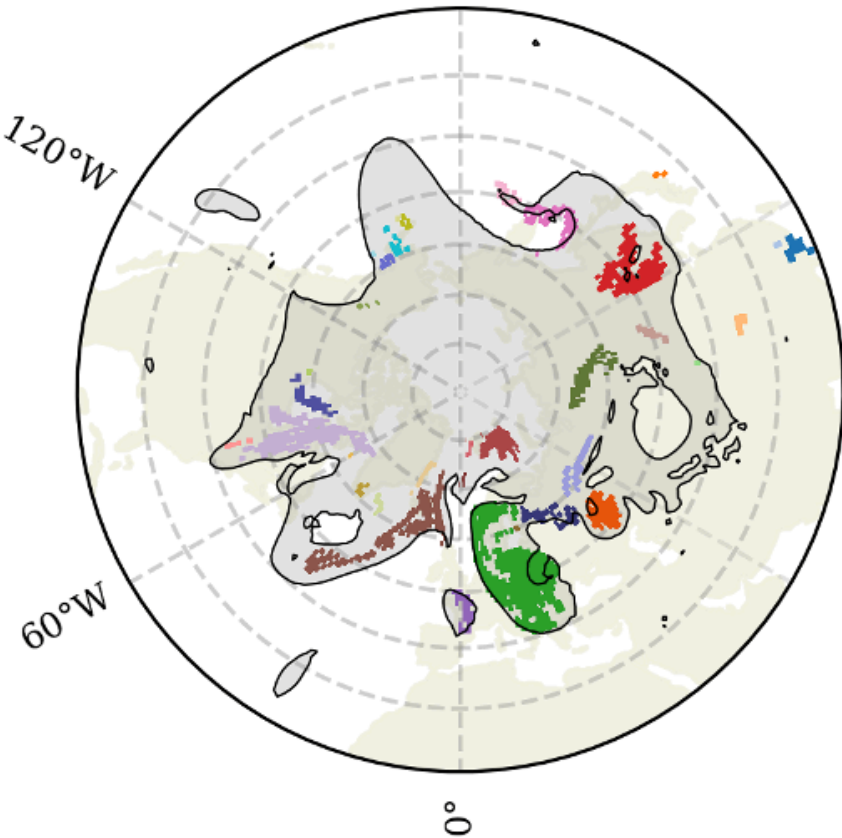


Colors: Features identified at 72h lead time

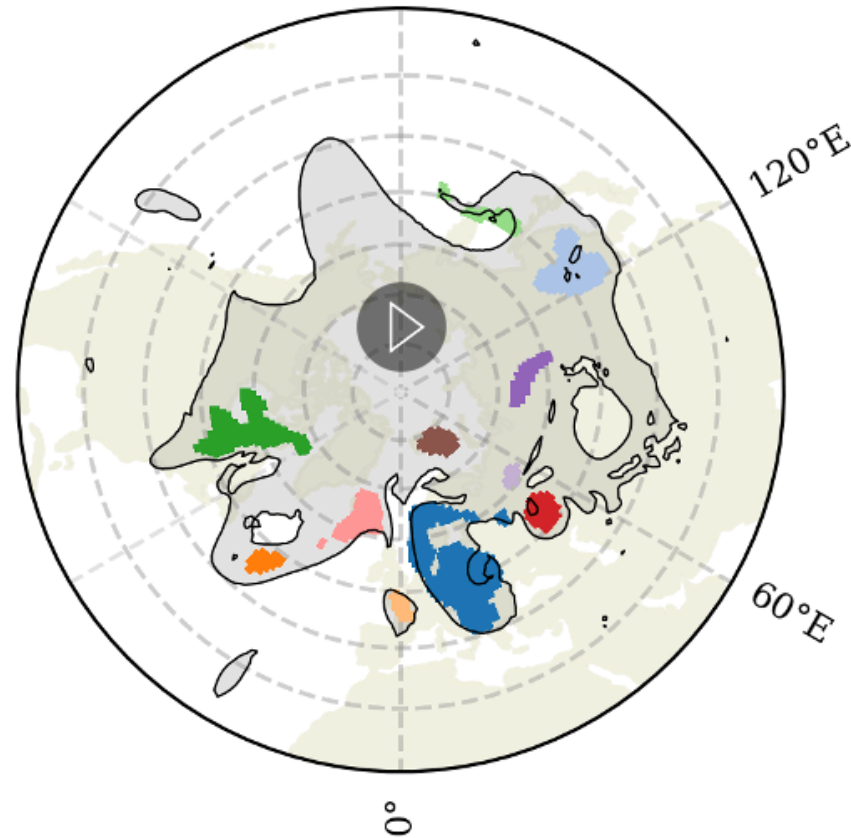
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smoothed

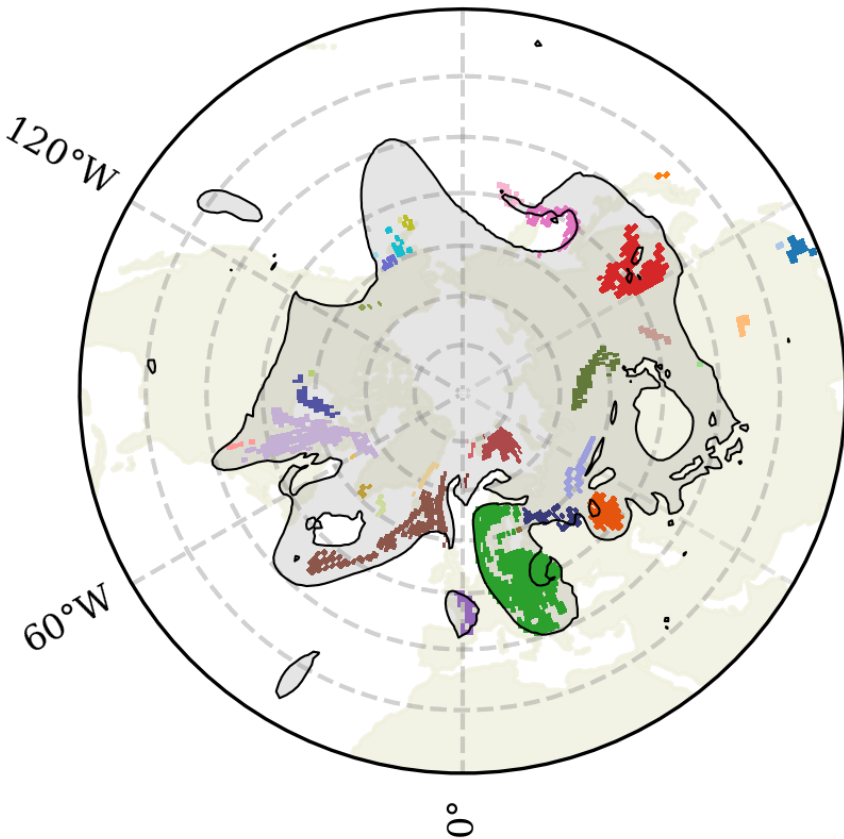


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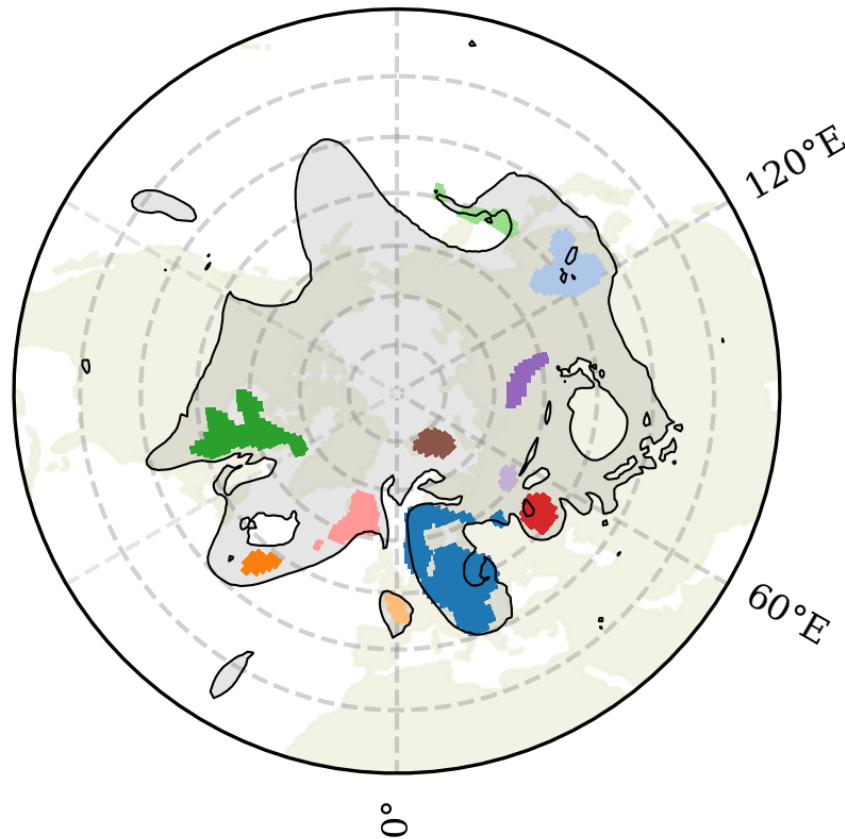
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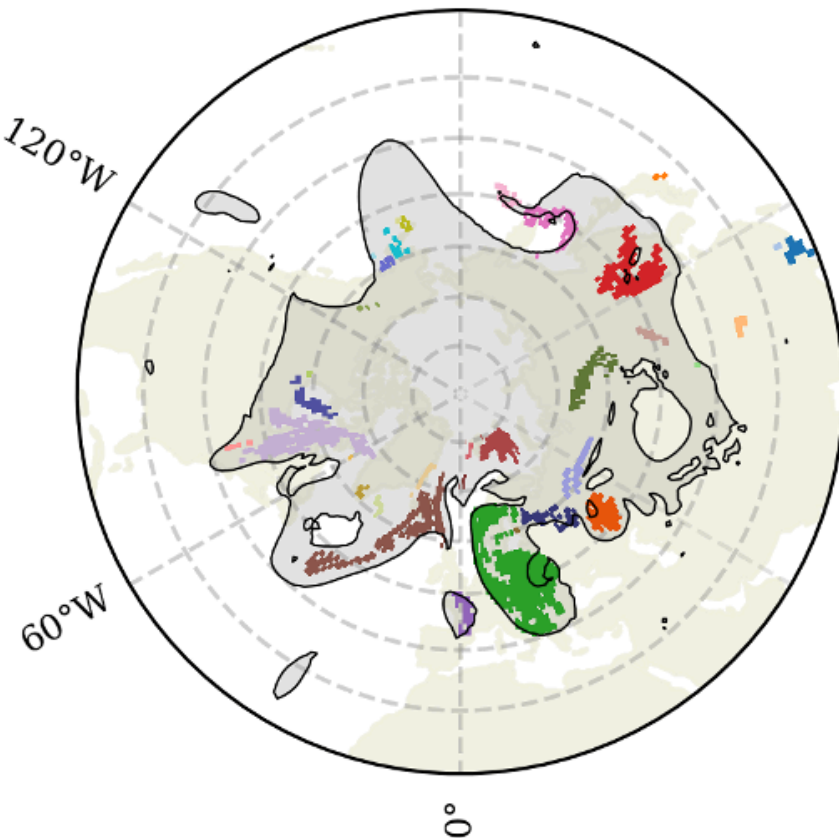
- Smoothing of underlying data and size-filtering of features improves the situation, but
- ... does *not* solve the fundamental problem.
 - ... implies loss of information.

Addressing the fundamental problem

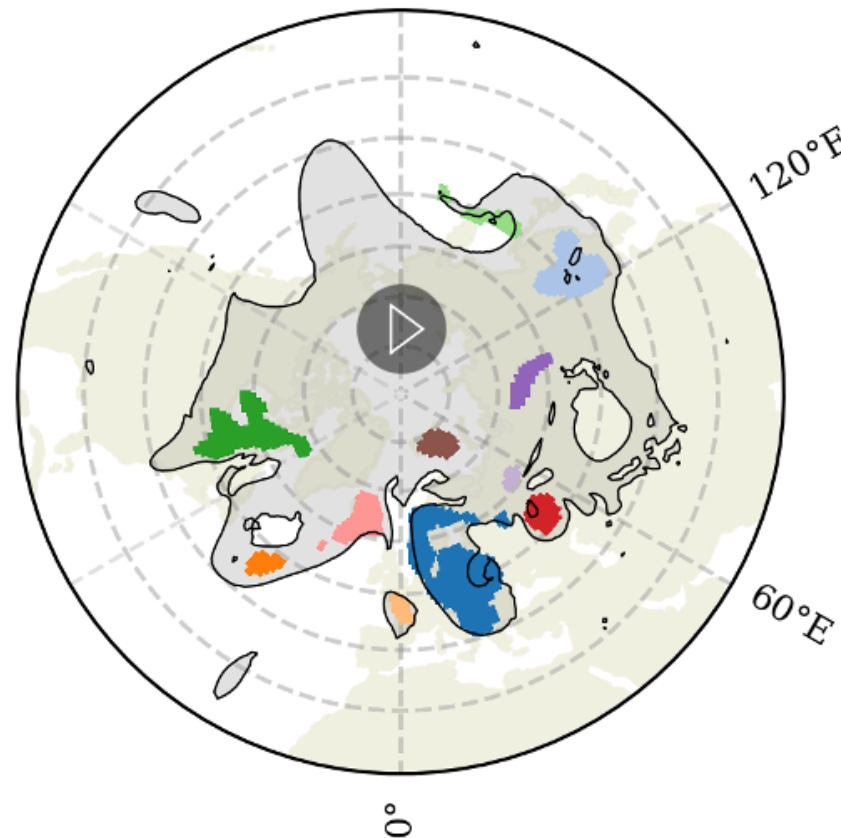
Schmidt, S., et al.: A feature-based framework to investigate atmospheric predictability. *MWR*, in revision

lead time 72h

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smoothed



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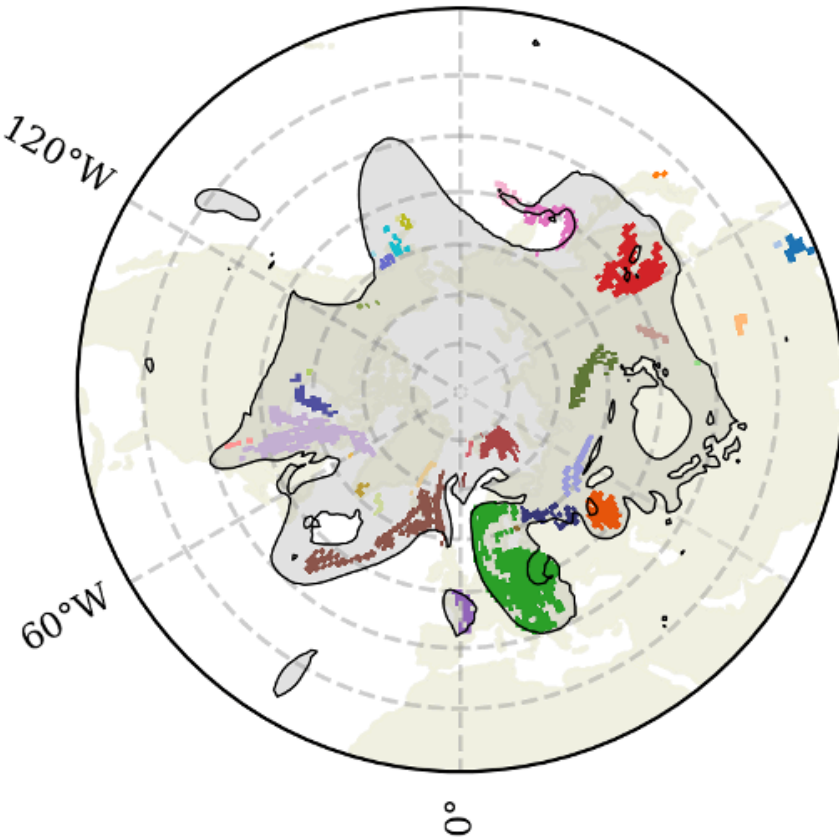
Basic idea:

- Group together features, for which the temporal evolution over a specified period is *not* sufficiently distinct.
- The groups of features define spatio-temporally coherent error patterns with *sufficiently distinct* evolution.

Error patterns with distinct evolution

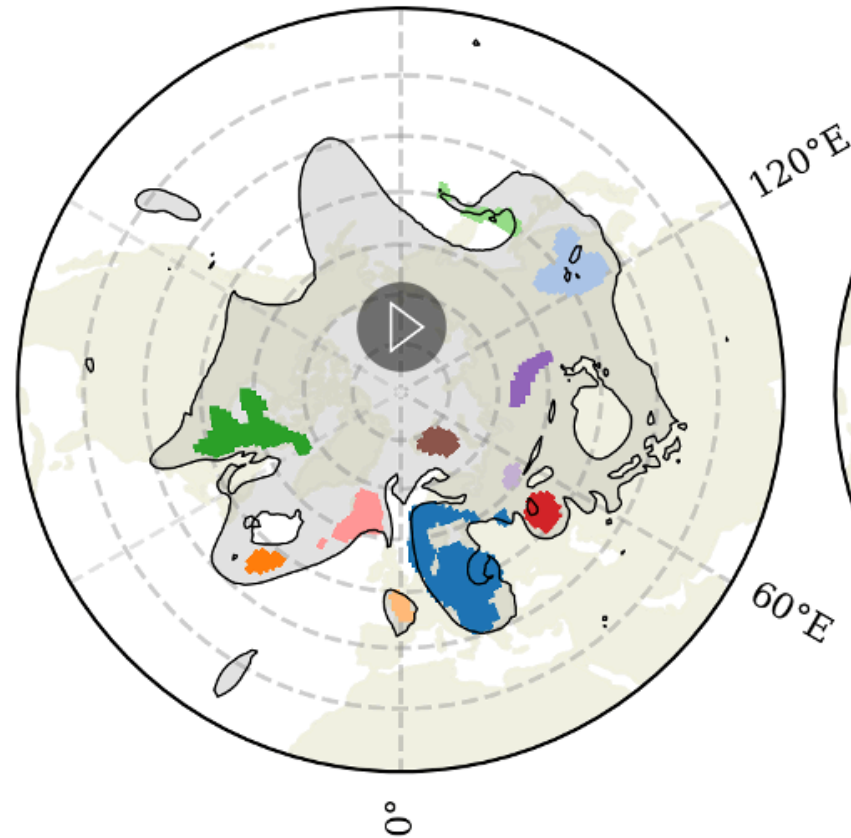
lead time 72h

unprocessed

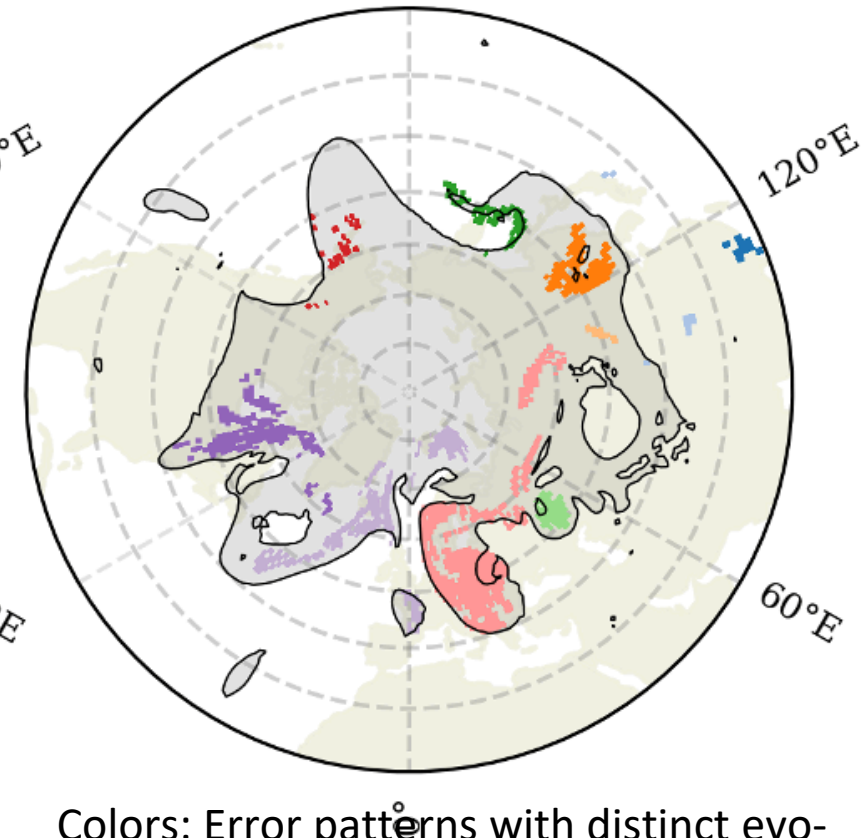


Colors: Features identified at 72h lead time

smoothed



redundancy-filtered

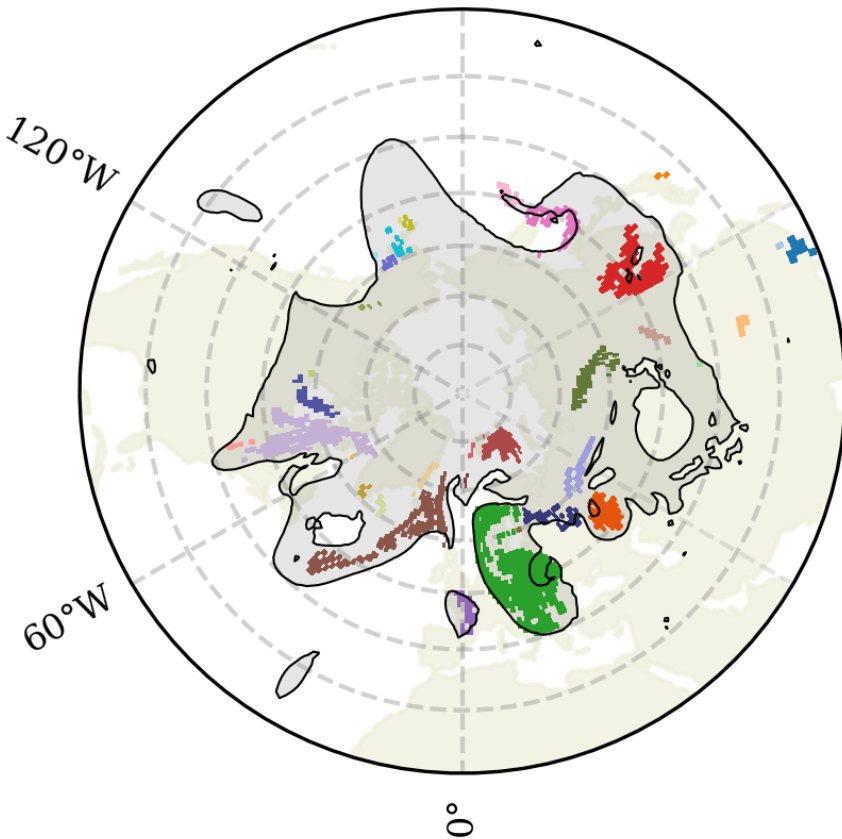


Colors: Error patterns with distinct evolution over specified period (here 48h).

Error patterns with distinct evolution

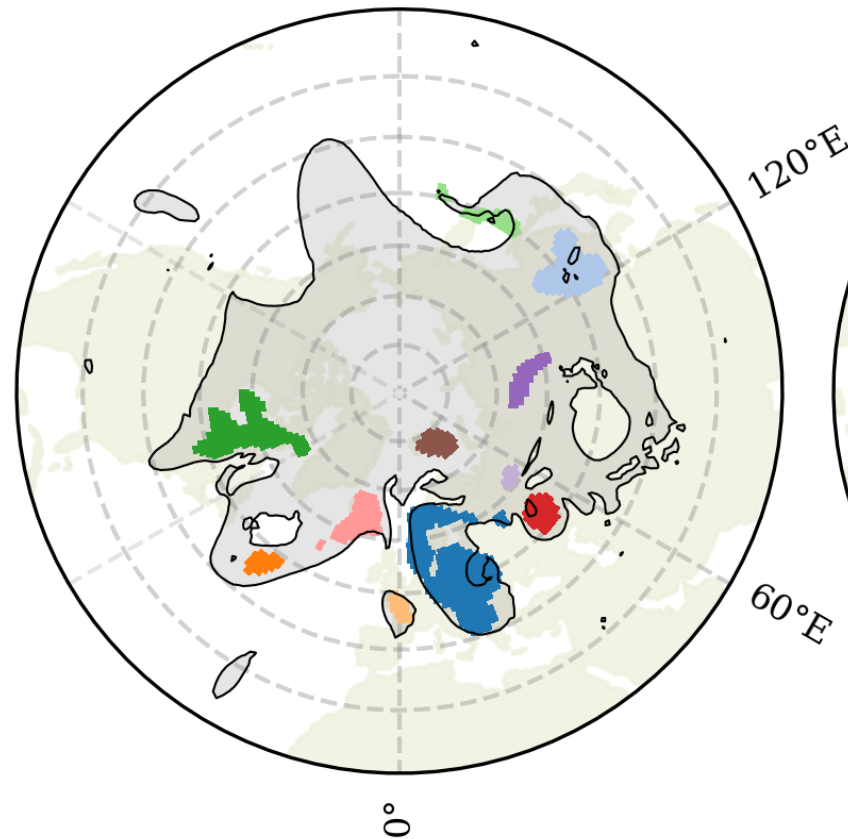
lead time 72h

unprocessed

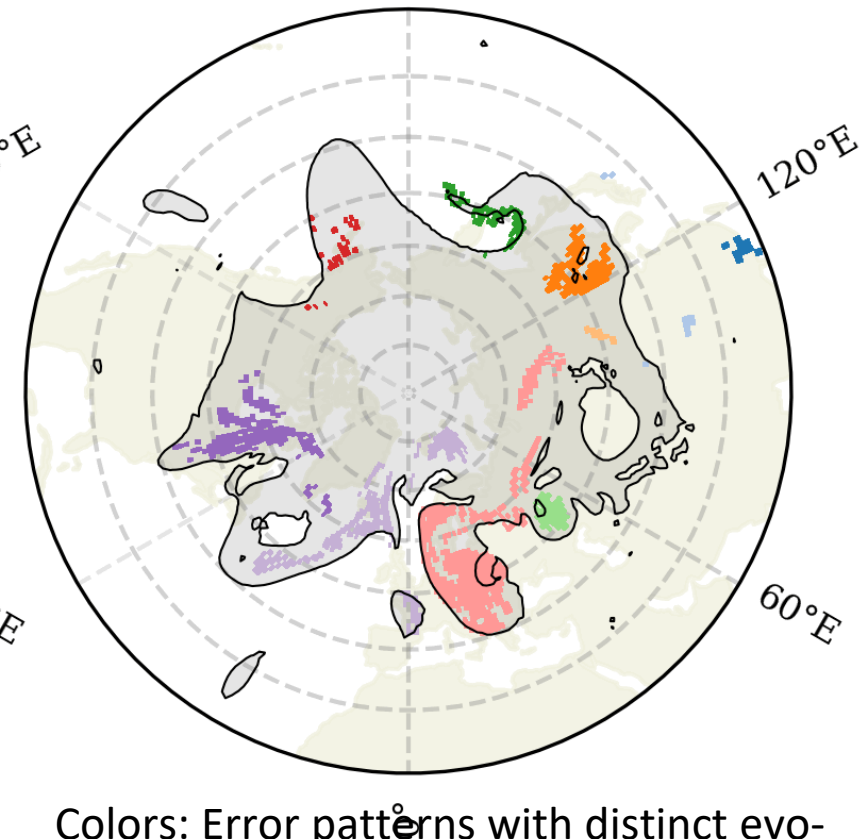


Colors: Features identified at 72h lead time


smoothed



redundancy-filtered

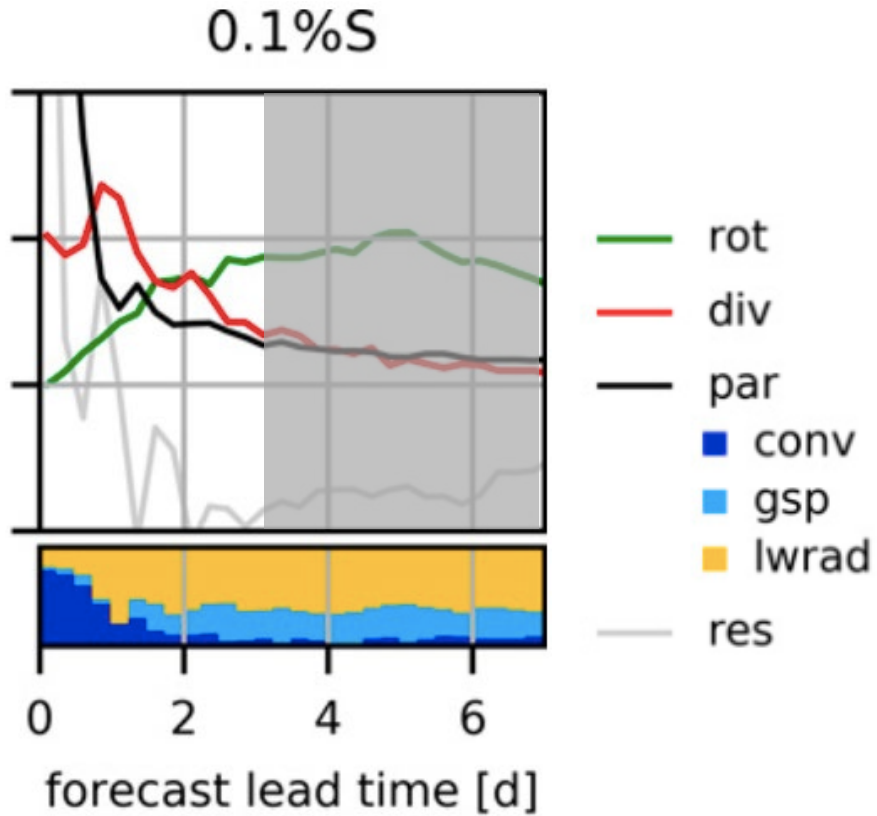


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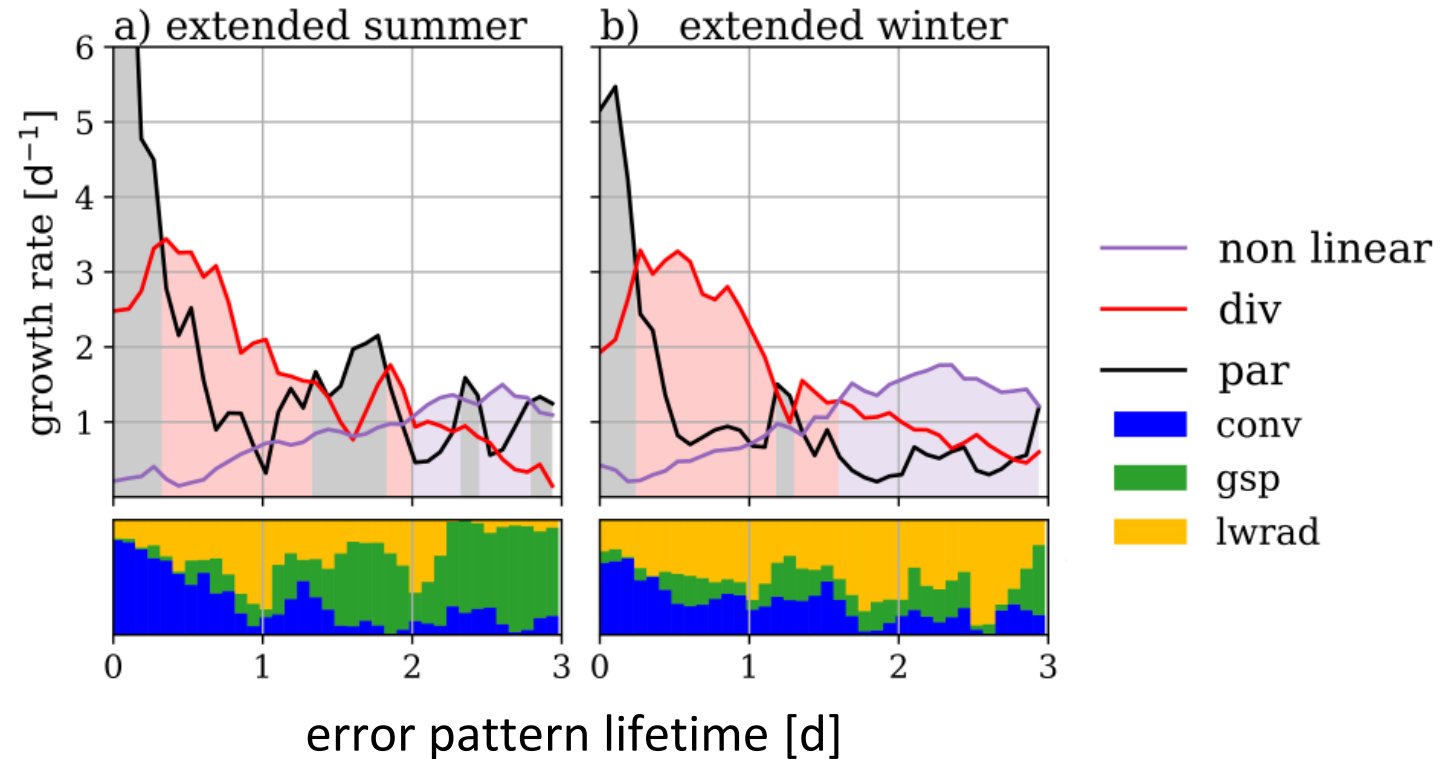
The background is a dark, atmospheric painting of a tropical scene. It features several palm trees with long, slender trunks and large, feathery fronds. In the foreground, the roof of a building is visible, with a small red object, possibly a pot or a vase, sitting on it. The overall color palette is muted and dark, with shades of grey, black, and brown, creating a somber and mysterious mood. The text is overlaid in a bright yellow color, providing a strong contrast against the dark background.

**Identify flow configurations
that will first reach the
intrinsic limit
(one application; preliminary results)**

Average picture reproduced



Selz et al. (2022)



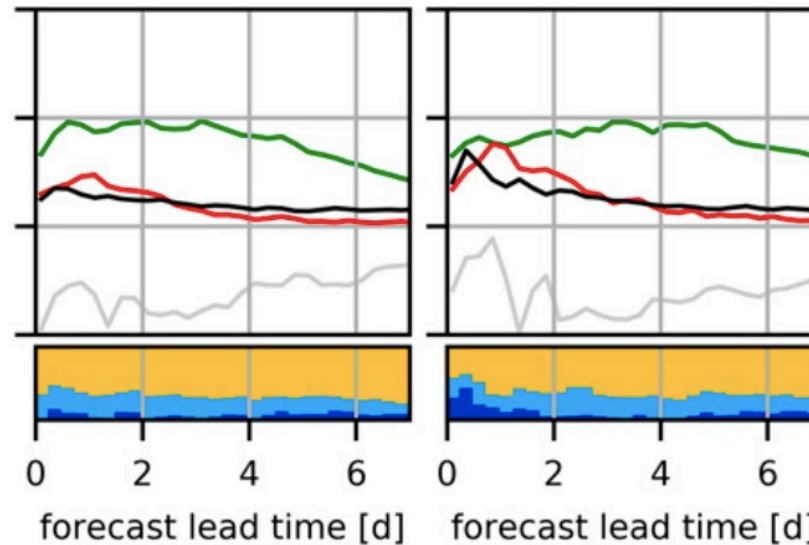
Schmidt et al. (2024)

Contrasting error-growth regimes

hemispheric mean (from Selz et al. 2022)

50%S

20%S



Most error patterns exhibit 'operational' characteristics.

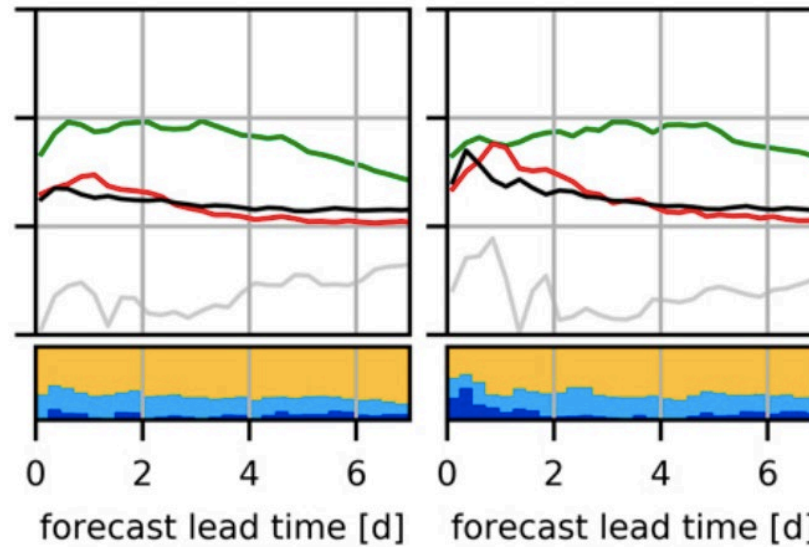
Most error patterns exhibit 'upscale' characteristics.

Contrasting error-growth regimes

hemispheric mean (from Selz et al. 2022)

50%S

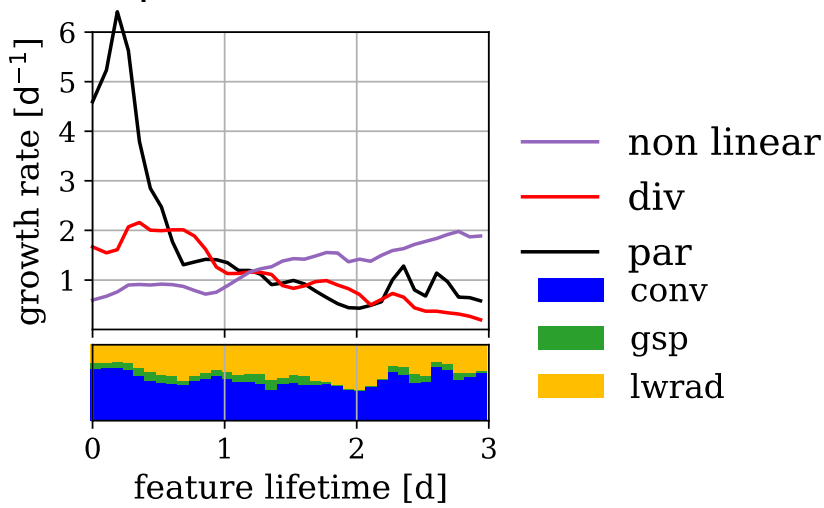
20%S



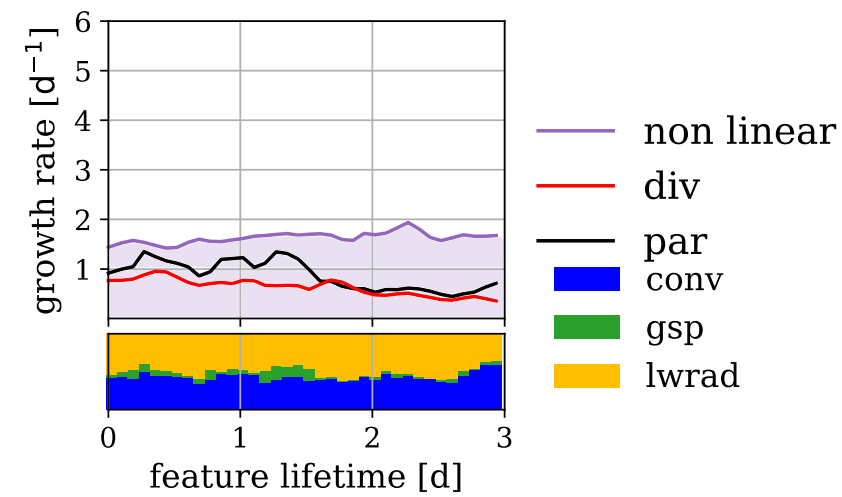
Most error patterns exhibit 'operational' characteristics.

Most error patterns exhibit 'upscale' characteristics.

Select cases that exhibit 'upscale' characteristics.



Select cases that exhibit 'operational' characteristics.

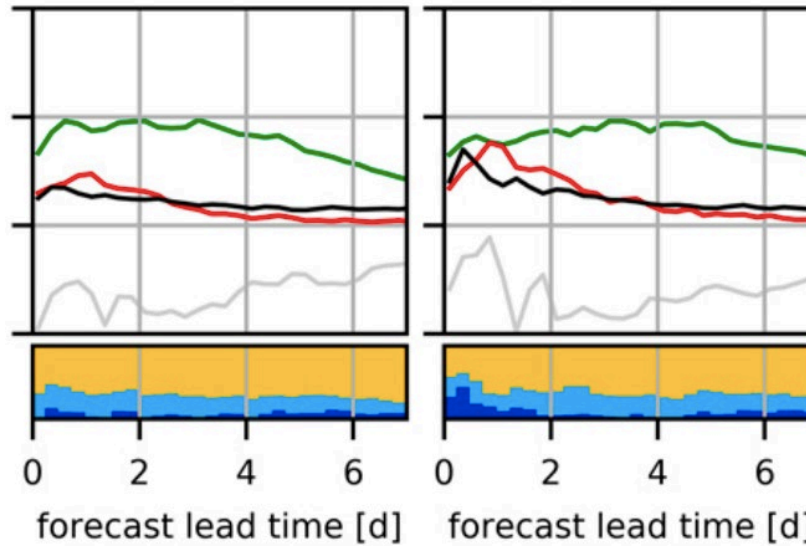


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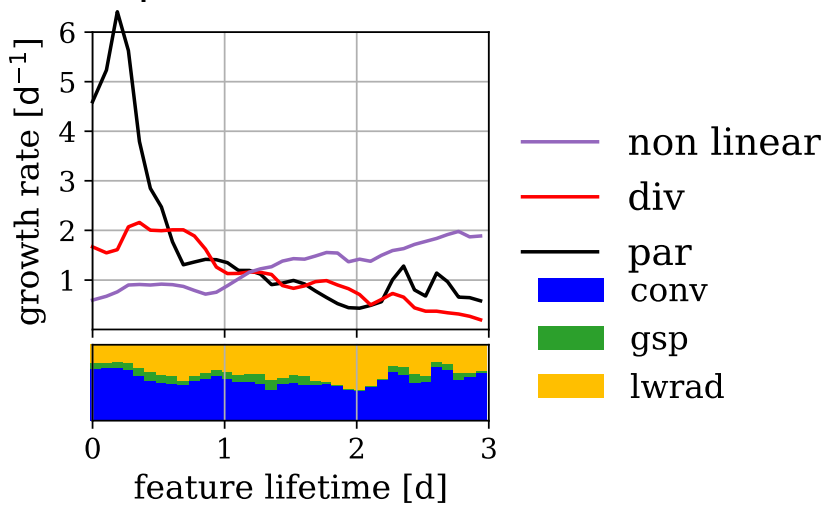
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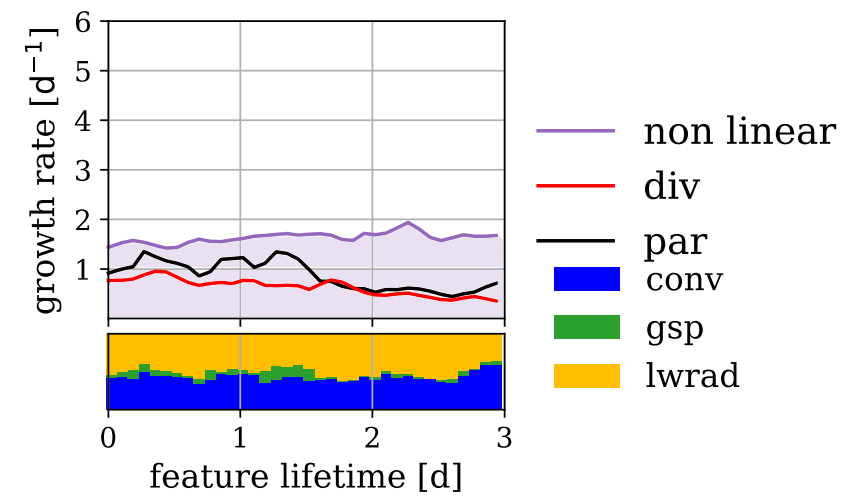
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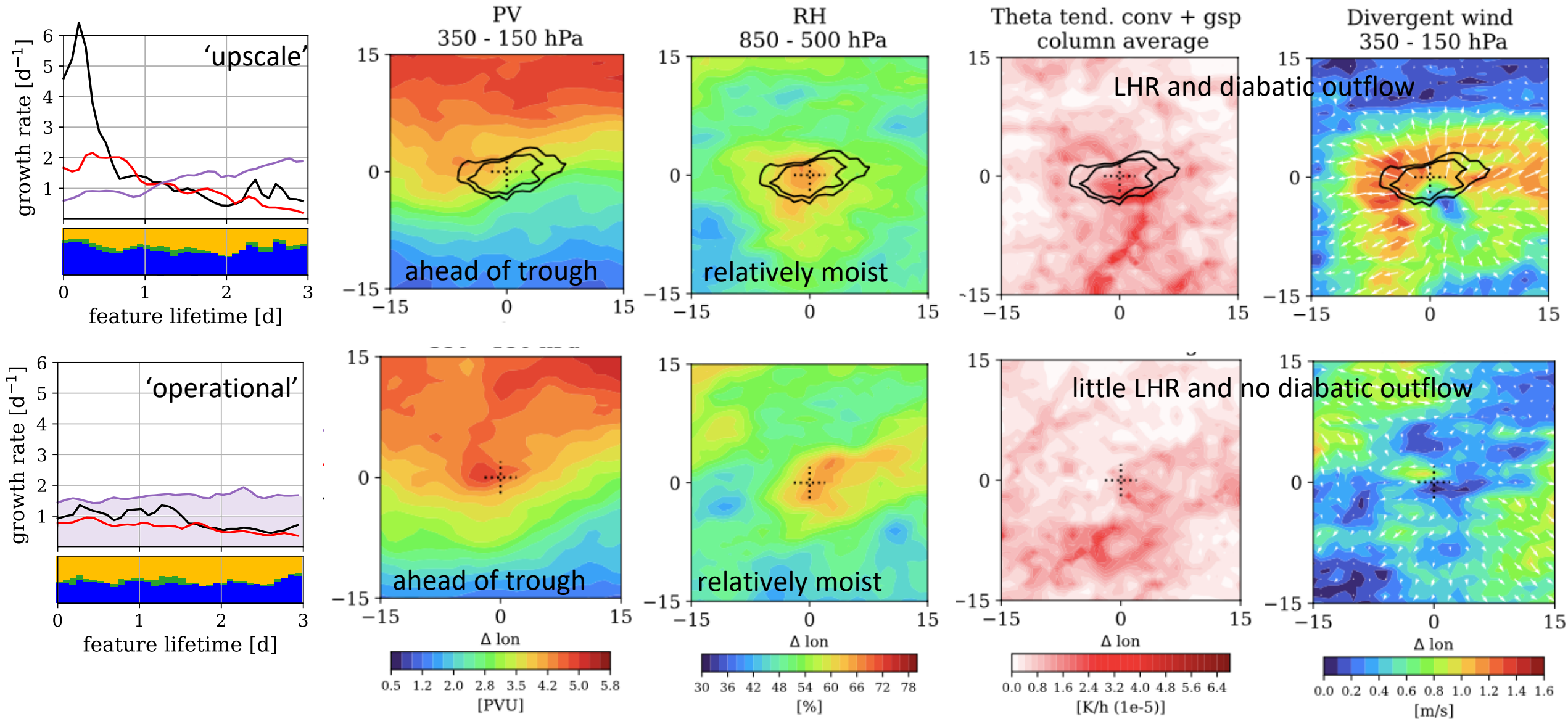
Select cases that exhibit 'operational' characteristics.



50 error patterns each
 2 years of experiments,
 Initialized every 4 days,
 extended summer

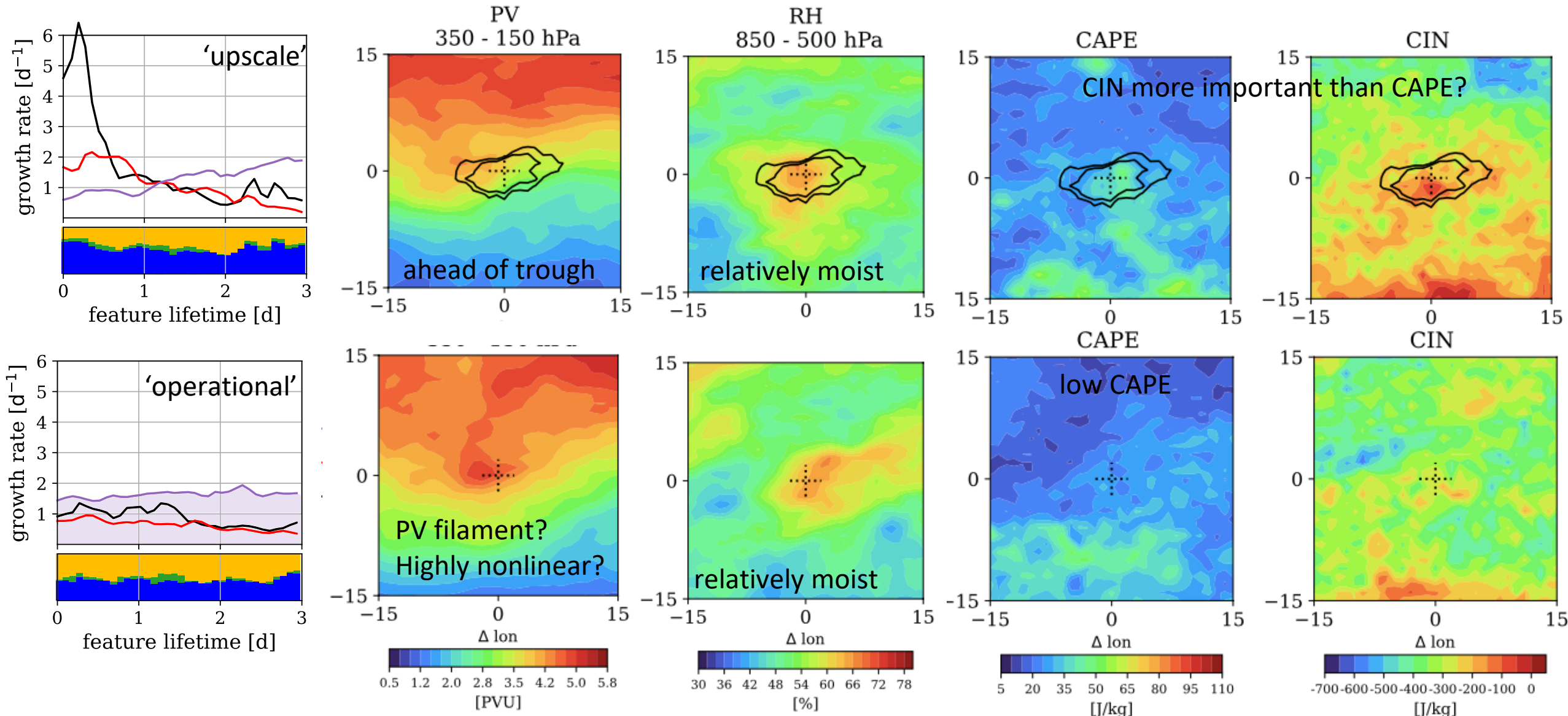
preliminary – preliminary – preliminary

Contrasting regimes: environmental conditions



preliminary – preliminary – preliminary

Contrasting regimes: environmental conditions



Summary

- Piecewise PV-tendency framework quantifies (upscale) error growth mechanisms (midlatitude tropopause region).
- Error-feature framework enables efficient analysis of many ‘cases’.

preliminary:

- Intrinsic limit of predictability may first be reached in high-CIN convective situation ahead of a trough.
- Highly nonlinear tropopause evolution with little LHR may benefit most from reduction in initial condition uncertainty.

References:

Baumgart et al. 2018: Potential vorticity dynamics of forecast errors: A quantitative case study. *MWR*, 146, 1405-1425.

Baumgart et al. 2019: Quantitative view on the processes governing the upscale error growth ... using a stochastic convection scheme. *MWR*, 147, 1713-1731.

Baumgart and Riemer 2019: Processes governing the amplification of ensemble spread in a medium-range forecast *QJRMS*, 145, 3252-3270.

Schmidt et al. 2024: A feature-based framework to investigate atmospheric predictability. *MWR*, in revision

Selz et al. 2022: The transition from practical to intrinsic predictability of midlatitude weather. *JAS*, 79, 2013-2030.