

# The transition from practical to intrinsic predictability

## ... and how to diagnose it

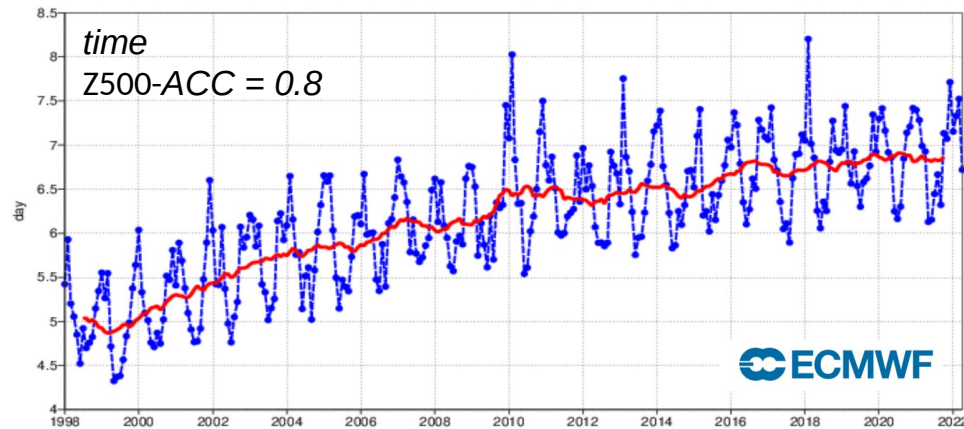
Tobias Selz, Michael Riemer and George Craig




# Practical vs. intrinsic predictability

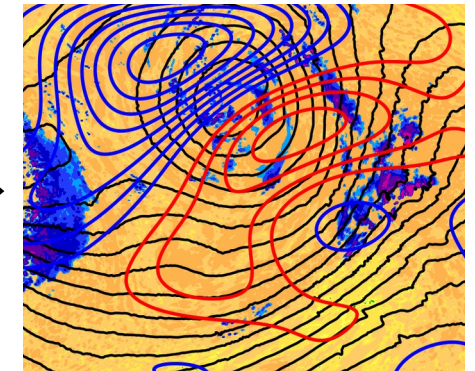
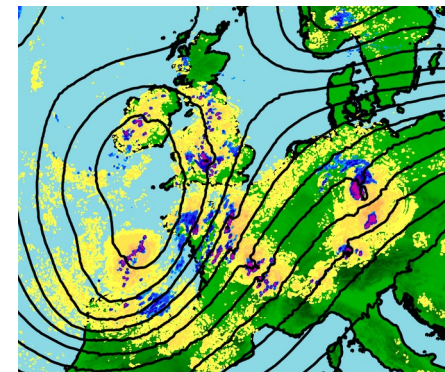
## Practical predictability

- Ability to predict with **current methods**
- Continuously improving over the last decades



## Intrinsic predictability

- Fundamental, physical limit 
- Caused by scale interactions (“**Butterfly effect**”)



(Selz and Craig, 2015)

Where are we right now?

How much **improvement potential**?

How **can we diagnose**?

# Experimental design

ECMWF  
Analysis

Initial condition uncertainty  
(ECMWF EDA-system)

**ICON-simulations** (R2B6, 40km)  
with stochastic convection scheme (Plant-Craig)

12 cases  
(Oct 16 – Sep 17)

+  
+  
+  
+  
+

pert. 1

pert. 2

pert. 3

pert. 4

pert. 5



run with seed 1

run with seed 2

run with seed 3

run with seed 4

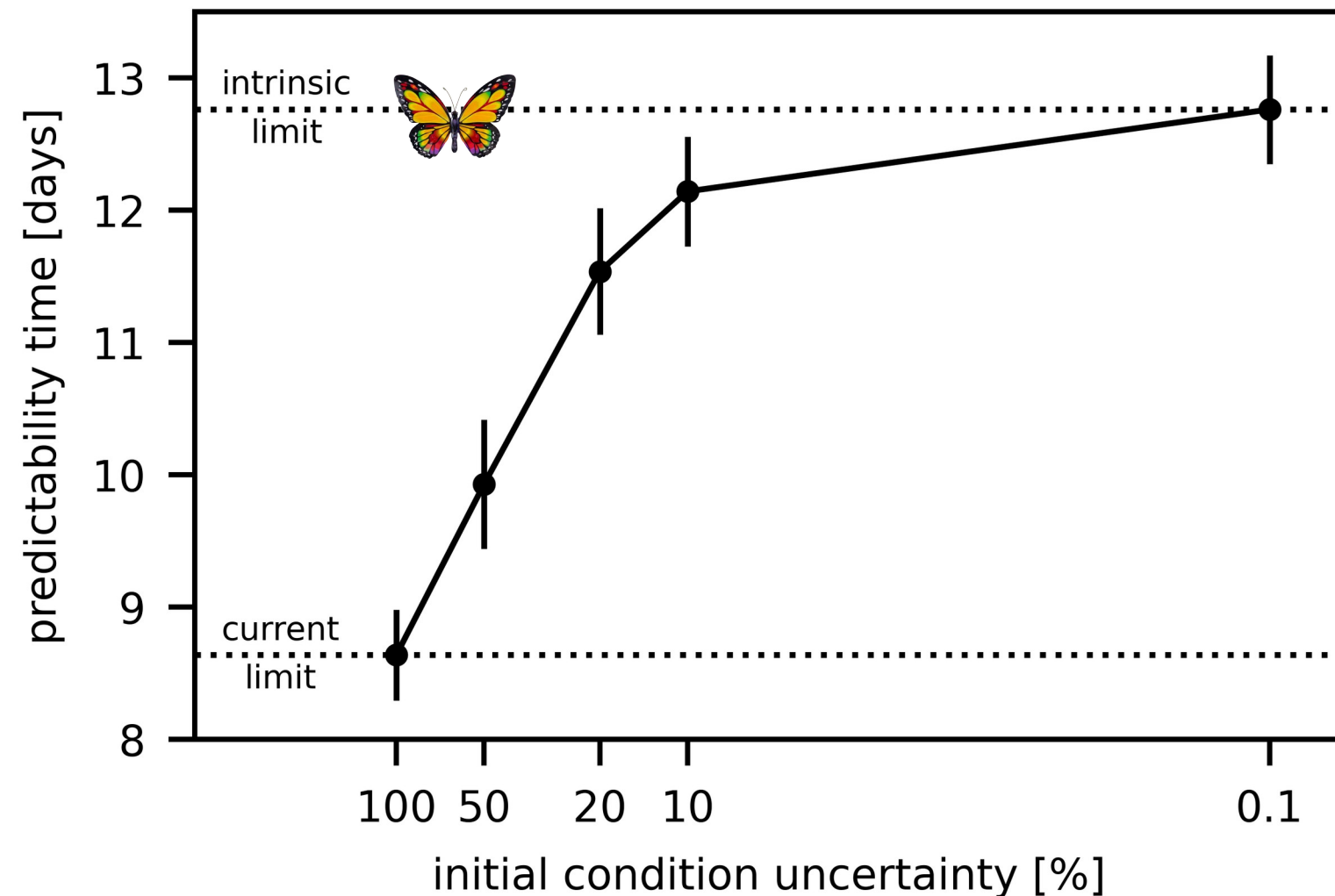
run with seed 5

rescaled to:  
**100%, 50%, 20%,  
10%, 0.1%**

Stochastic convection scheme to better represent  
uncertainty growth from unresolved convective motions

# Predictability time

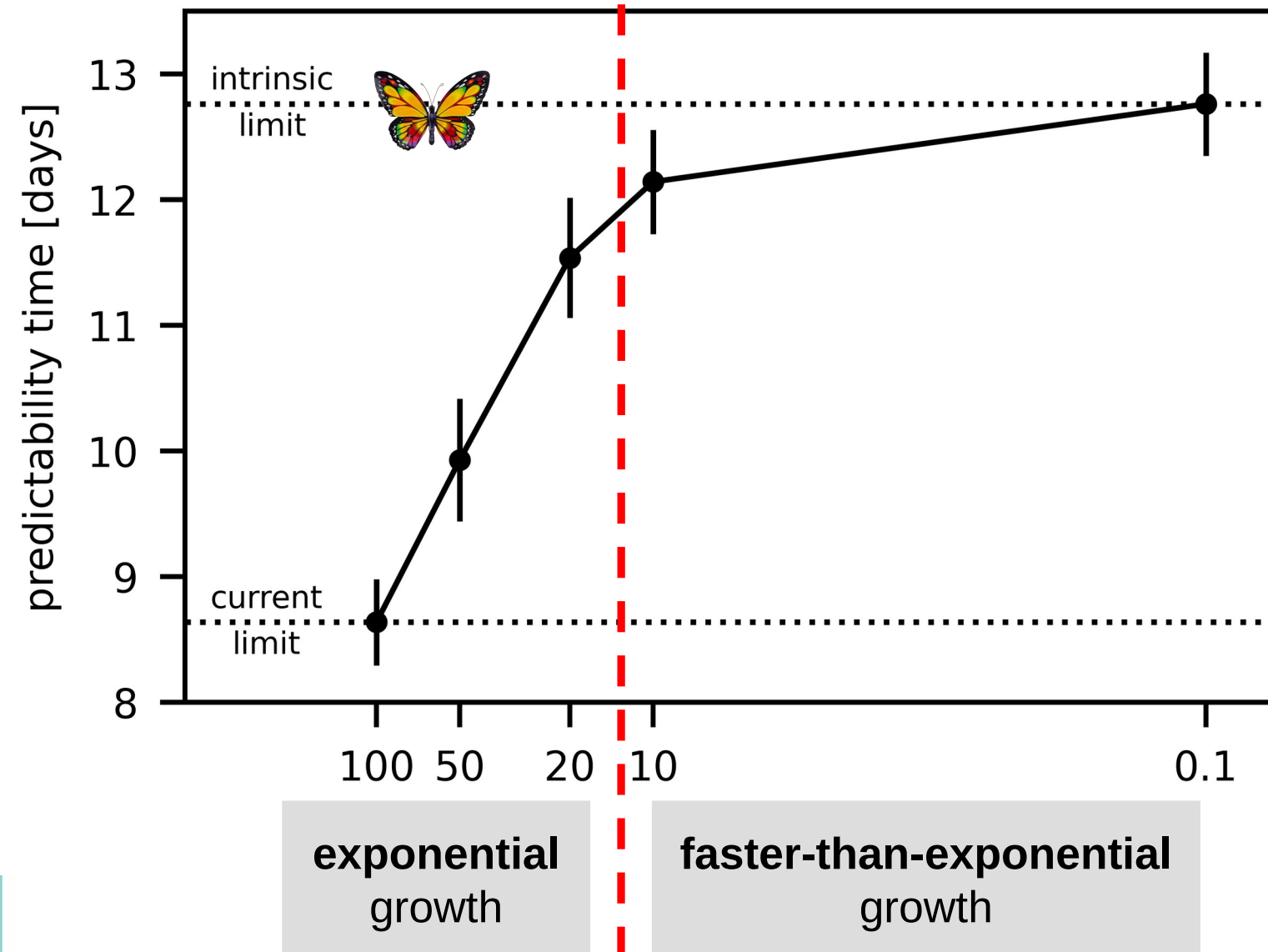
time to reach 50% of clim. Variance of 300hPa DKE



- Possible gain through initial condition-perfection: ca. **4-5 days**
- Can be achieved with **≈ 90% reduction** of initial condition uncertainty
- Further improvement will show **little additional benefit**

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# Potential vorticity diagnostics

PV tendency equation on isentropic levels

$$\partial_t \pi = -\mathbf{v} \cdot \nabla \pi + N$$

Prognostic equation for the ensemble variance

$$\partial_t \text{var}(\pi) = \frac{2}{n-1} \sum_{i=1}^n \left[ -\delta\pi_i \delta\mathbf{v}_i \cdot \nabla \bar{\pi} + \frac{\delta\pi_i^2}{2} \nabla \cdot \mathbf{v}_i + \delta\pi_i \delta N_i \right]$$

Separation of processes

$$\mathbf{v} = \sum_j \mathbf{v}^{(j)},$$

$$N = \sum_j N^{(j)}$$

Here:

$\mathbf{v} \rightarrow \text{div, rot}$

$N \rightarrow \text{convection, gridsc. prec., lw-radiation}$

Spatial integration over midlatitudes (40°-60°) at tropopause (2PVU)

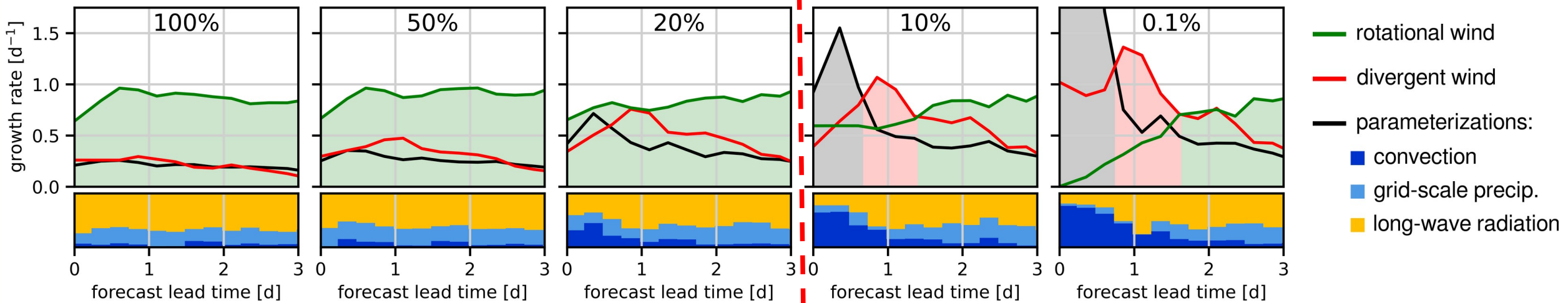


# Potential vorticity diagnostics

initial condition uncertainty:

current estimates

“butterflies”



**Large-scale** uncertainty growth  
in **dry, balanced** flow

**Upscale** uncertainty growth  
from **moist convection**

# Summary and conclusions I



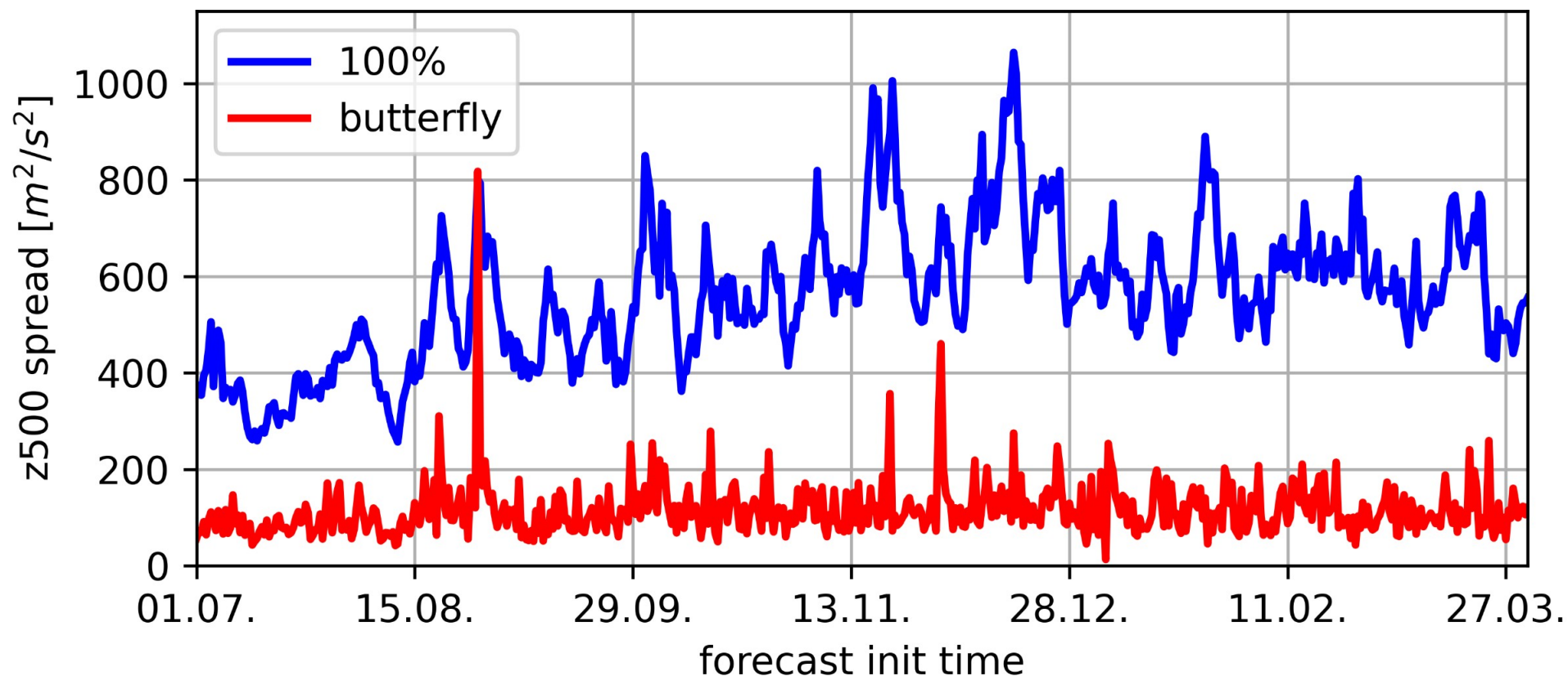
- Possible gain through initial condition-perfection: **4-5 days** (model improvement excluded)
- **Reduction** of current initial condition uncertainty **by 90%** is required
- **Practically predictability** is mostly limited by uncertainty growth in **balanced 2D dry** motions
- **Intrinsic predictability** is limited by **diabatically-driven** uncertainty growth on **convective scales** and subsequent upscale interactions
- The predictability “regime” can be identified with the **PV-diagonals**

**These results hold on average**



# There may be exceptions ...

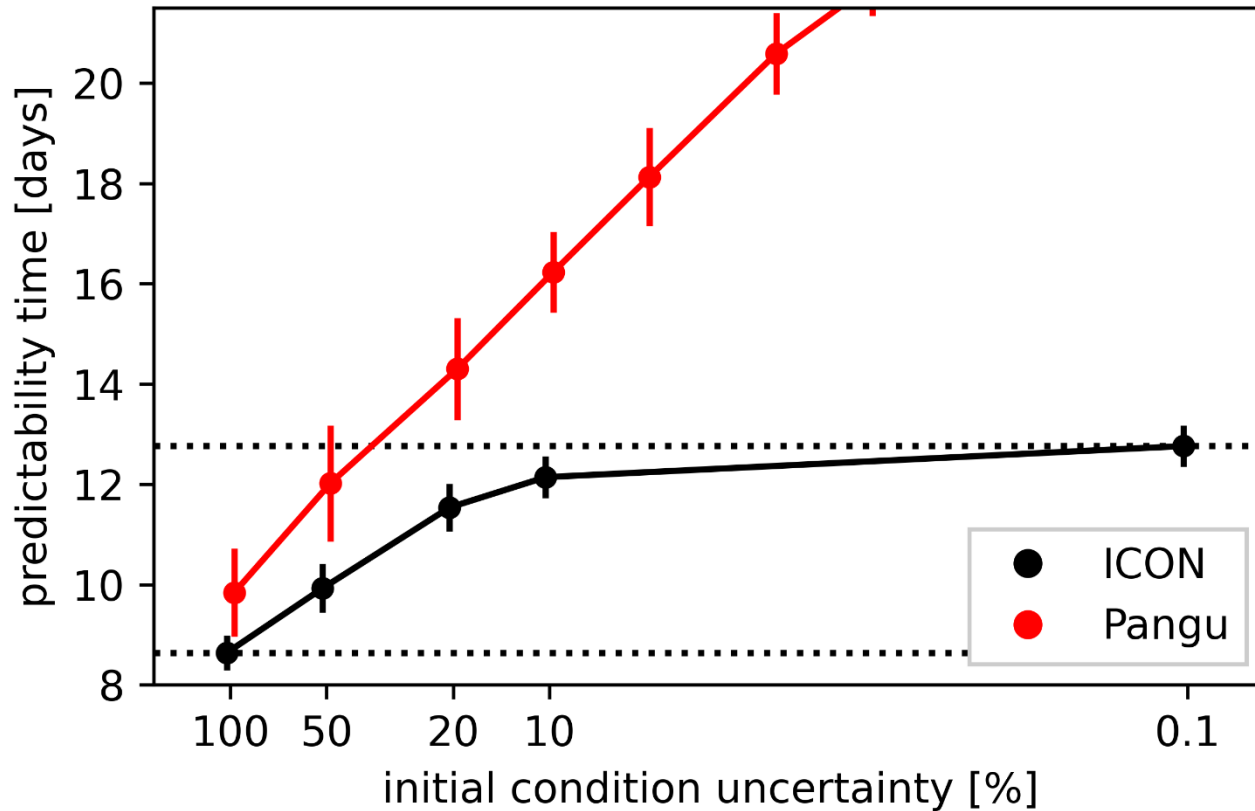
## 7-day ECMWF forecasts for Europe



localized PV-diagnostics required

→ Talk by Michael Riemer on Thursday, 10:00

# Can AI models simulate the “butterfly effect”?

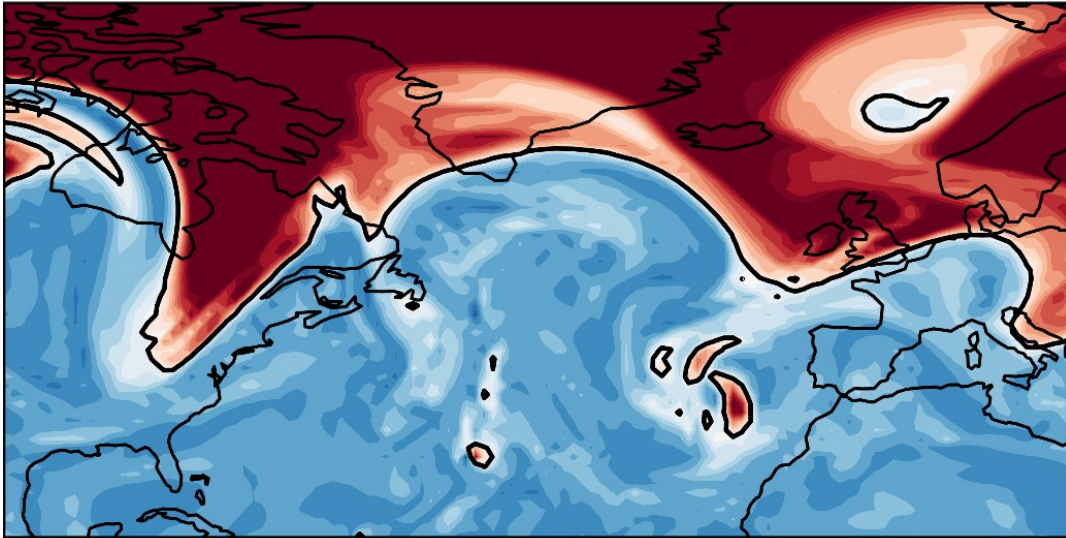


- **AI models**  
*[Pangu, GraphCast, FourCastNet, NeuralGCM]*  
**incorrectly suggest infinite predictability**

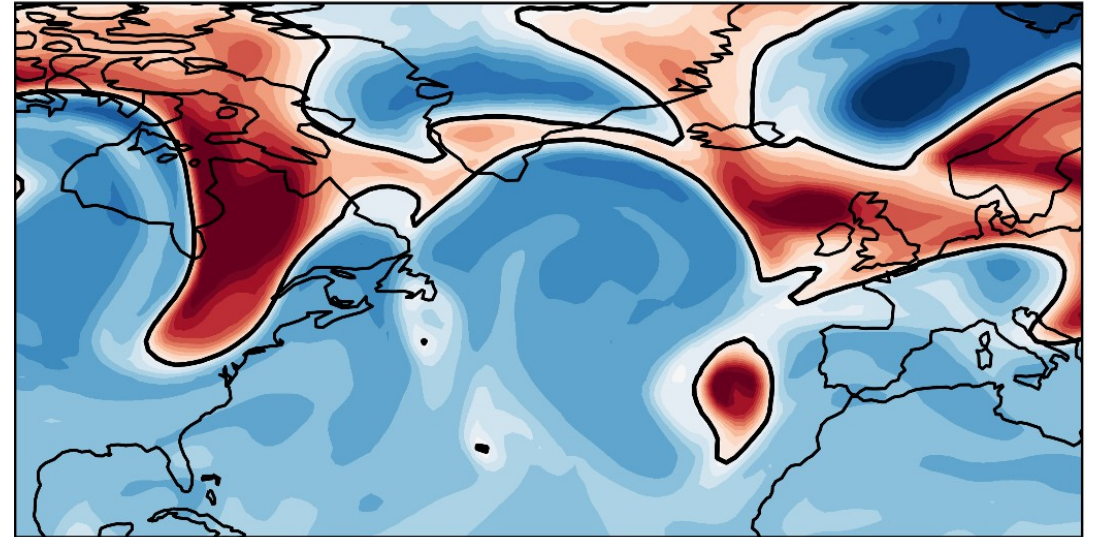
Can we apply the PV diagnostics to AI models?

# PV field from an AI model

ICON PV (320K)



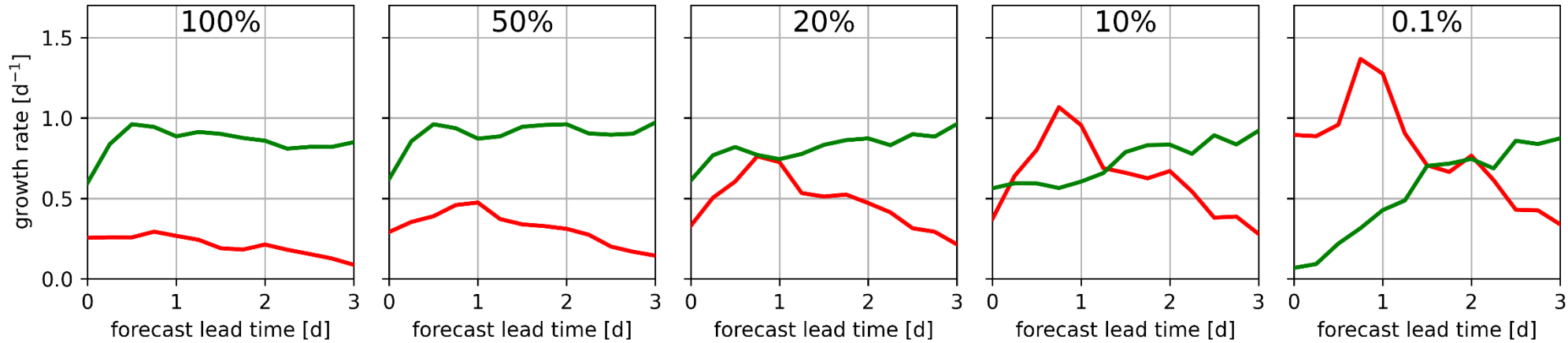
Pangu PV (320K)



- Effective resolution is low
- Troposphere and tropopause look realistic
- Stratospheric stratification is incorrect

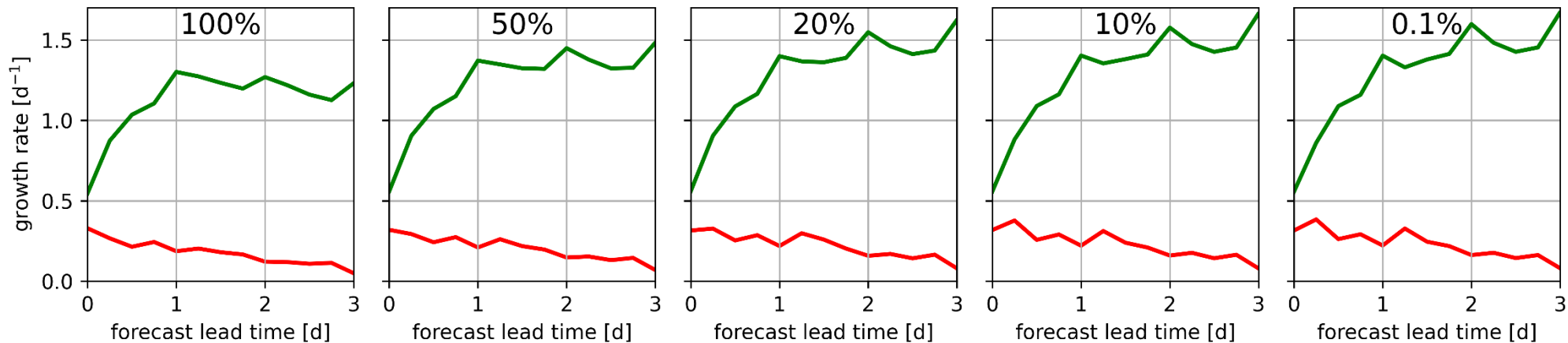
# Simplified PV diagnostic from AI model

## ICON simulations



- rotational wind
- divergent wind

## Pangu simulations





# Summary and conclusions II



- Current **AI models cannot** simulate the “**butterfly effect**”  
*[Pangu, GraphCast, FourCastNet, NeuralGCM]*
- They **incorrectly** suggest **infinite** predictability
- Yet to **test: Generative AI** models
- A **simplified PV diagnostic** could be applied
- **No transition** to the **divergent** component of the flow

# Publications



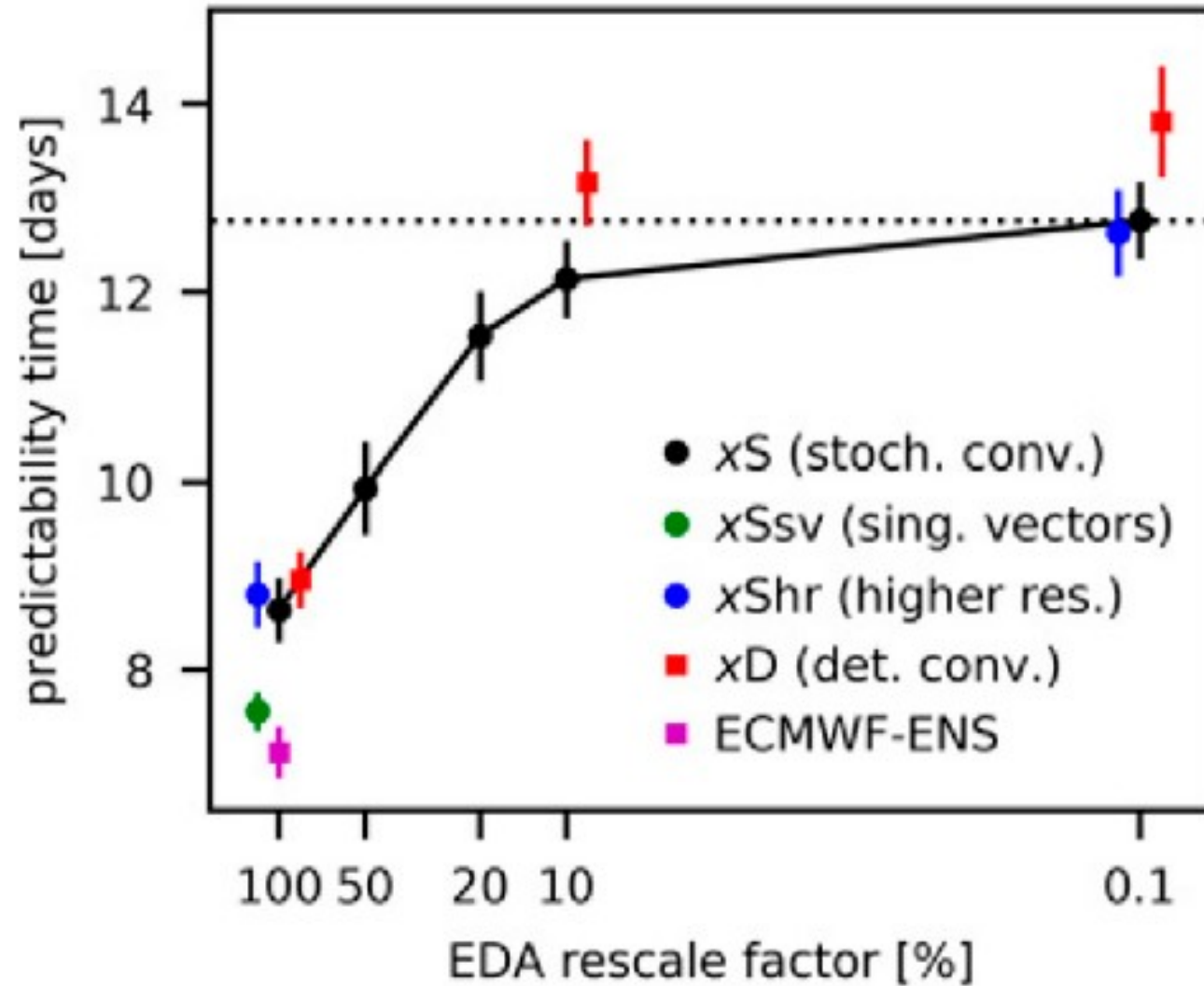
Selz, T., Riemer, M., & Craig, G. C. (2022). The Transition from Practical to Intrinsic Predictability of Midlatitude Weather. *Journal of the Atmospheric Sciences*, 79(8), 2013-2030. <https://doi.org/10.1175/JAS-D-21-0271.1>

Selz, T., & Craig, G. C. (2023). Can artificial intelligence-based weather prediction models simulate the butterfly effect? *Geophysical Research Letters*, 50, e2023GL105747. <https://doi.org/10.1029/2023GL105747>



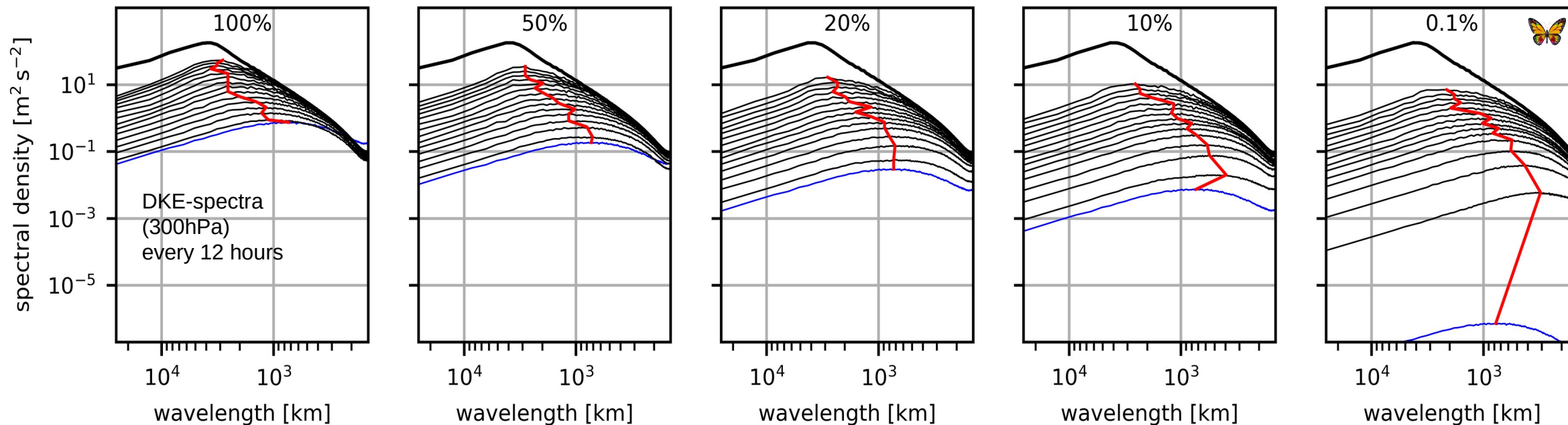
# Extra Slides

Threshold  $\alpha=0.5$  (acc=0.60)



initial condition uncertainty:  
current estimates

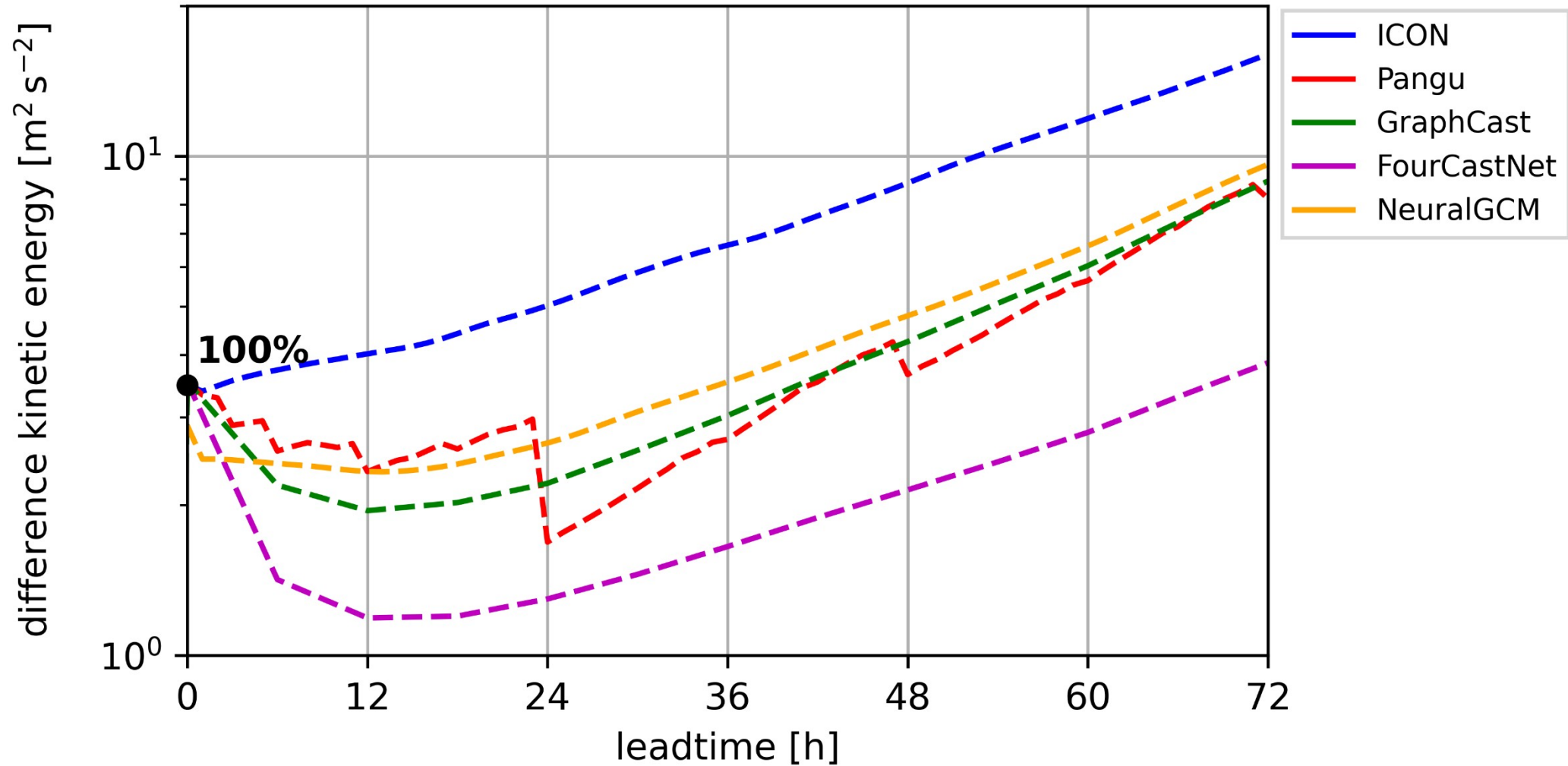
“butterflies”



Basically **constant** error growth

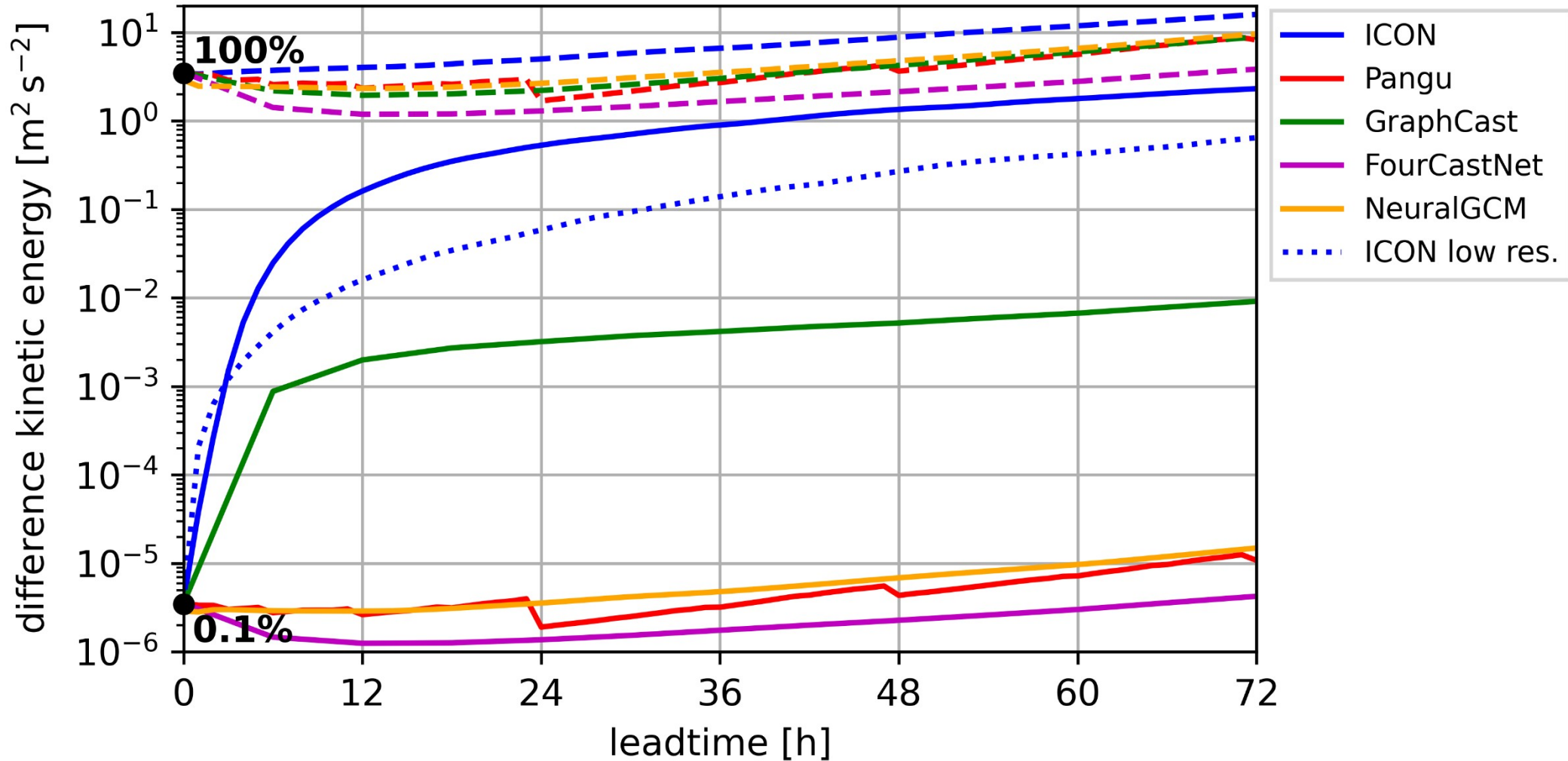
Initial **fast** and **downscale** growth, upscale from there

# Uncertainty growth rates (global DKE 300hPa)



# Uncertainty growth rates

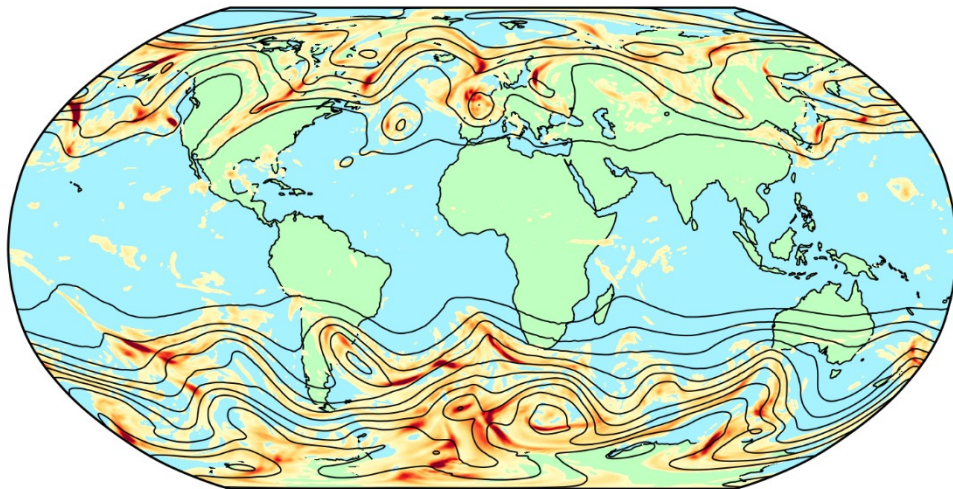
(global DKE 300hPa)



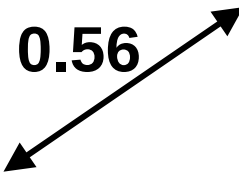


# Uncertainty patterns 100% (DKE, 3 days)

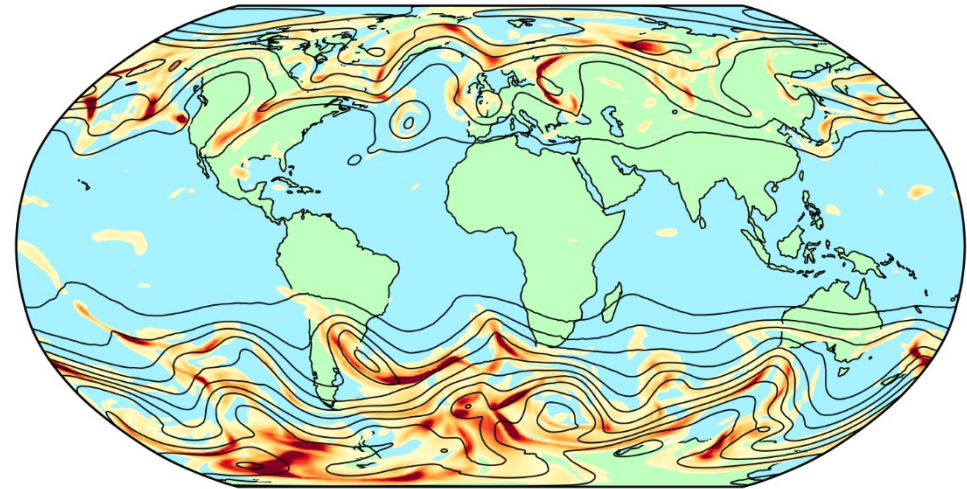
ICON 100%



0.56



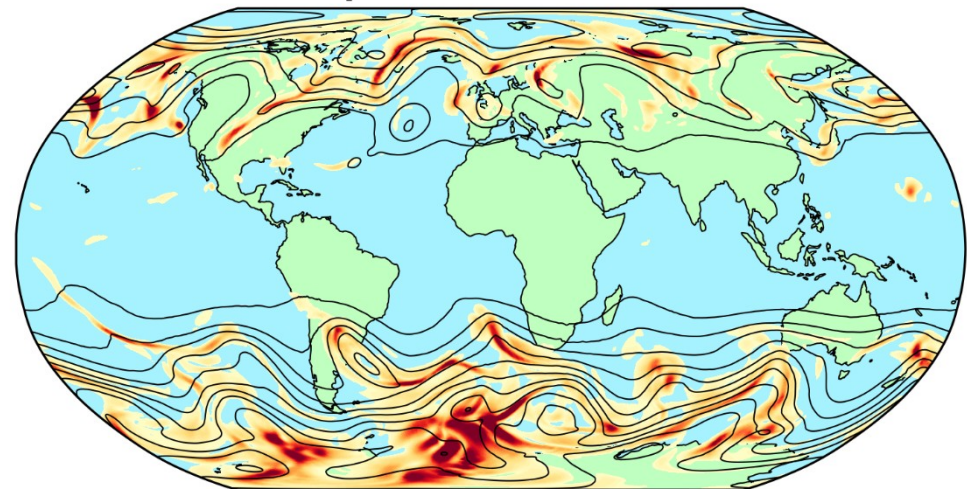
Pangu 100%



0.57



GraphCast 100%

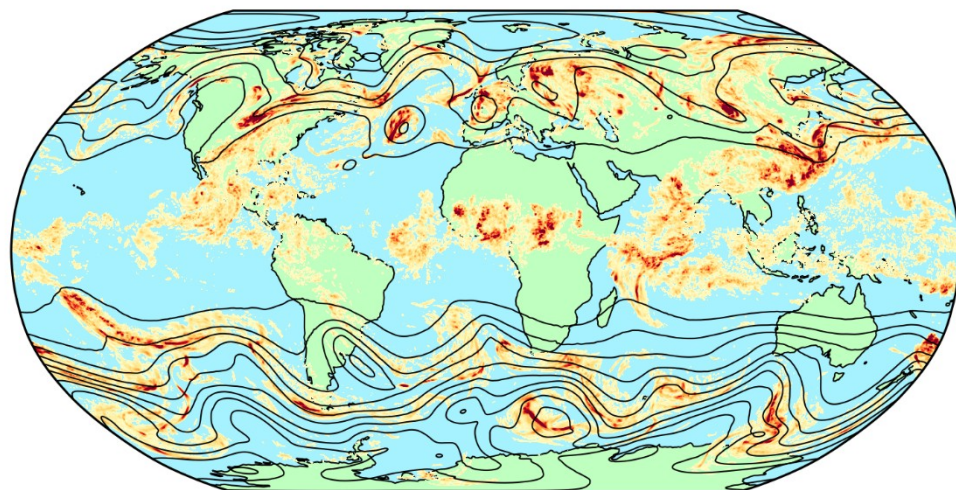




# Uncertainty patterns 0.1% (DKE, 3 days)



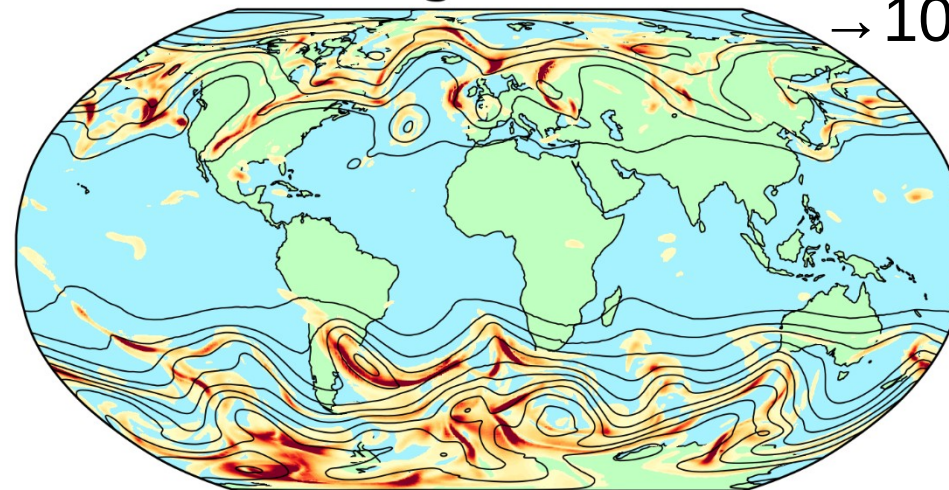
ICON 0.1%



→ 100%: **0.14**

0.05

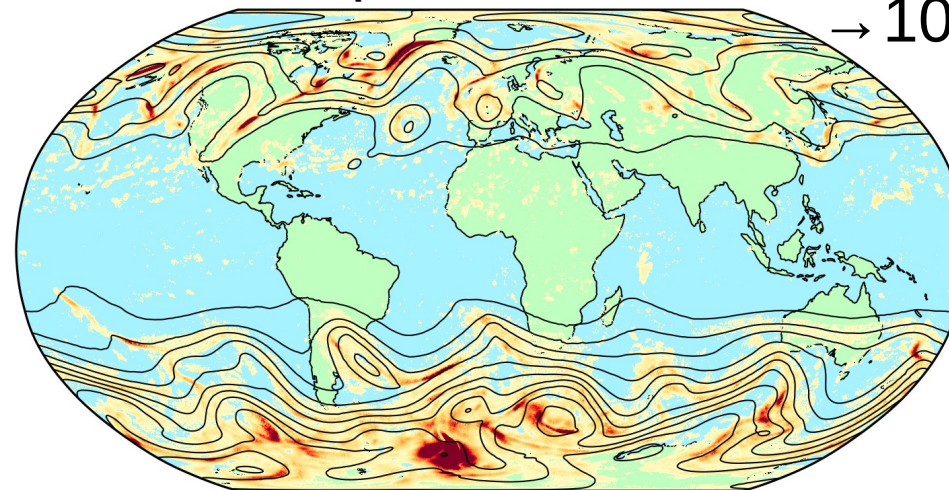
Pangu 0.1%



→ 100%: **0.74**

0.04

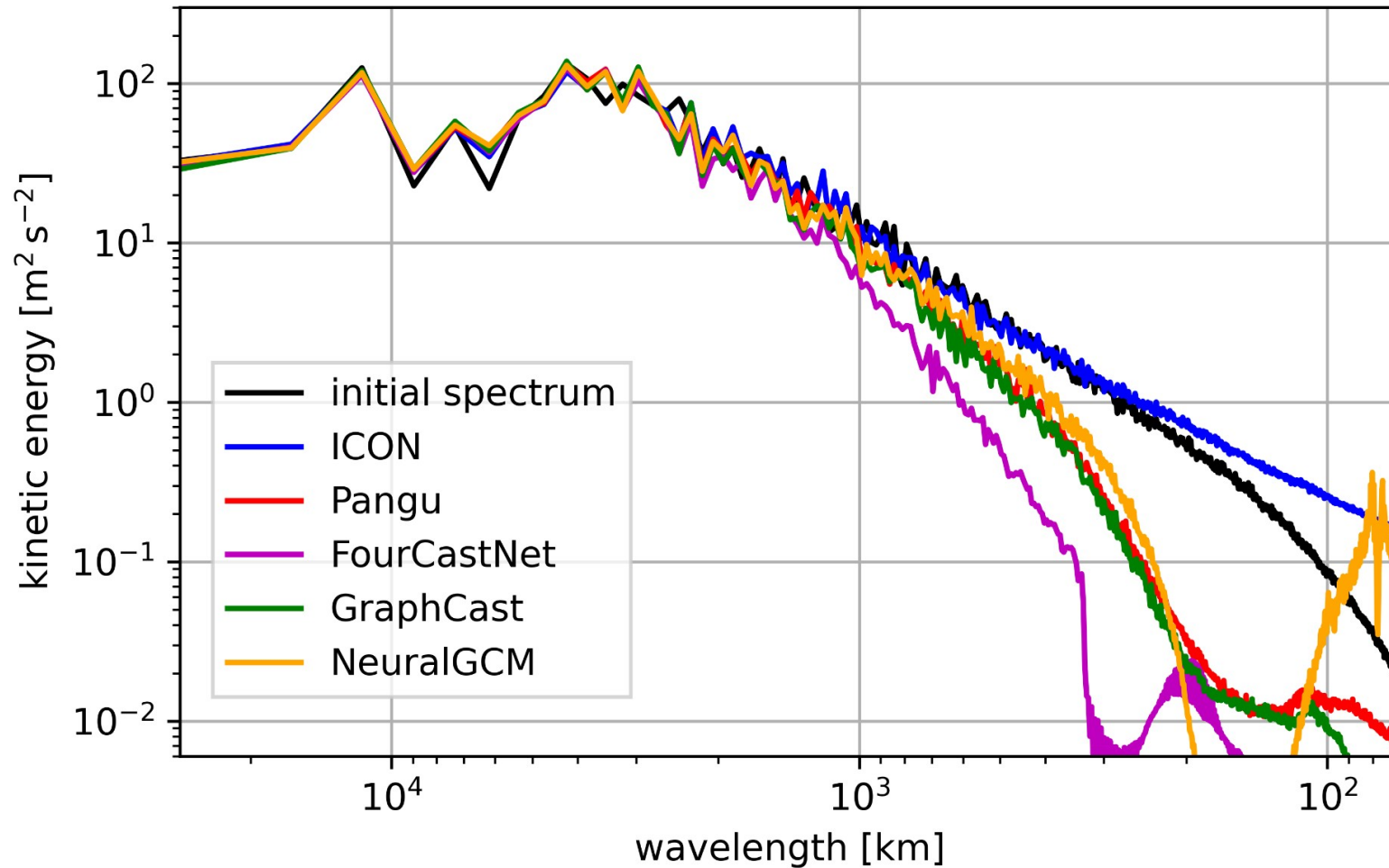
GraphCast 0.1%



→ 100%: **0.54**

**FourCastNet and NeuralGCM similar**

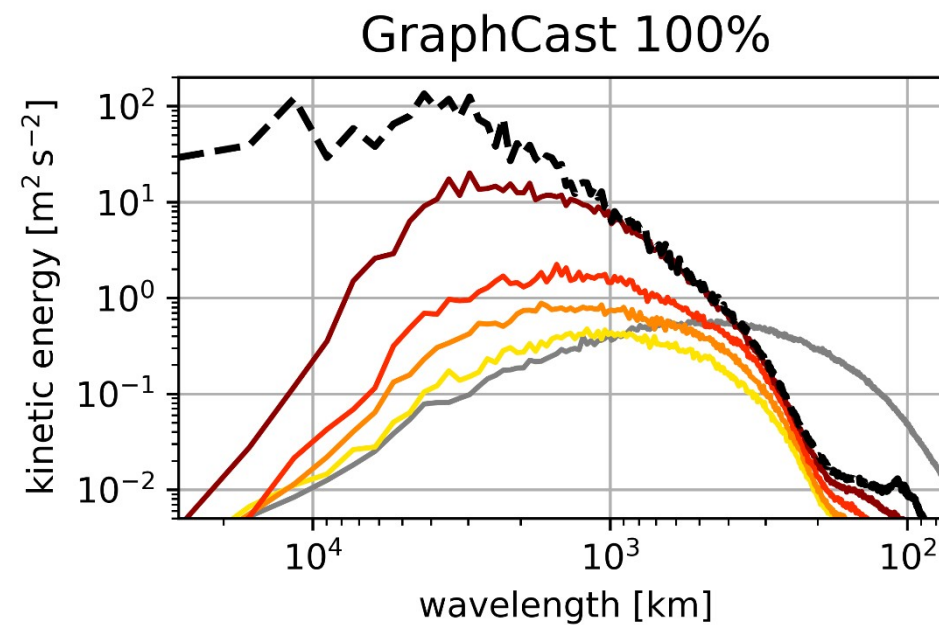
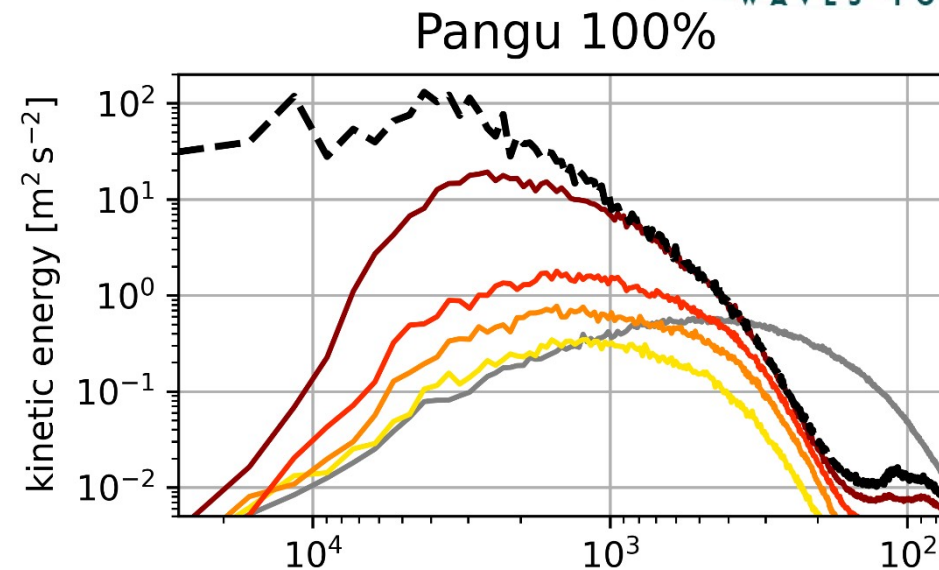
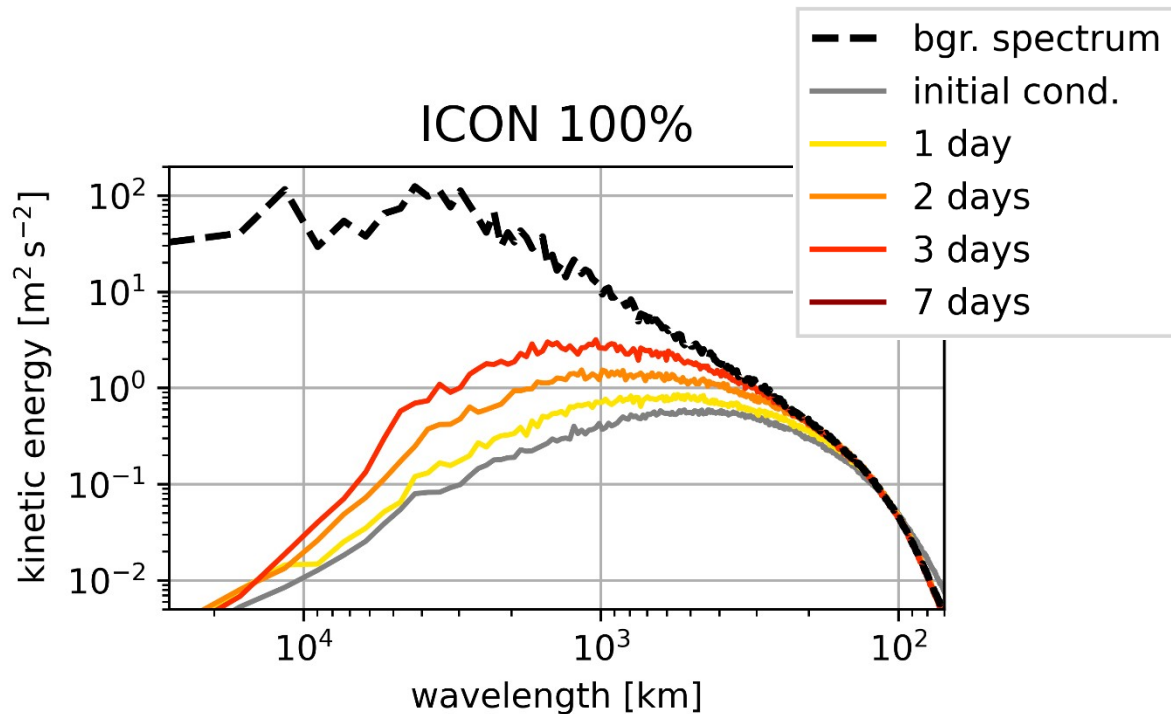
# Kinetic energy spectra (300hPa, 3days)



AI models have a pretty **low effective resolution** (ca.  $40 \Delta x$ ; 1000km)



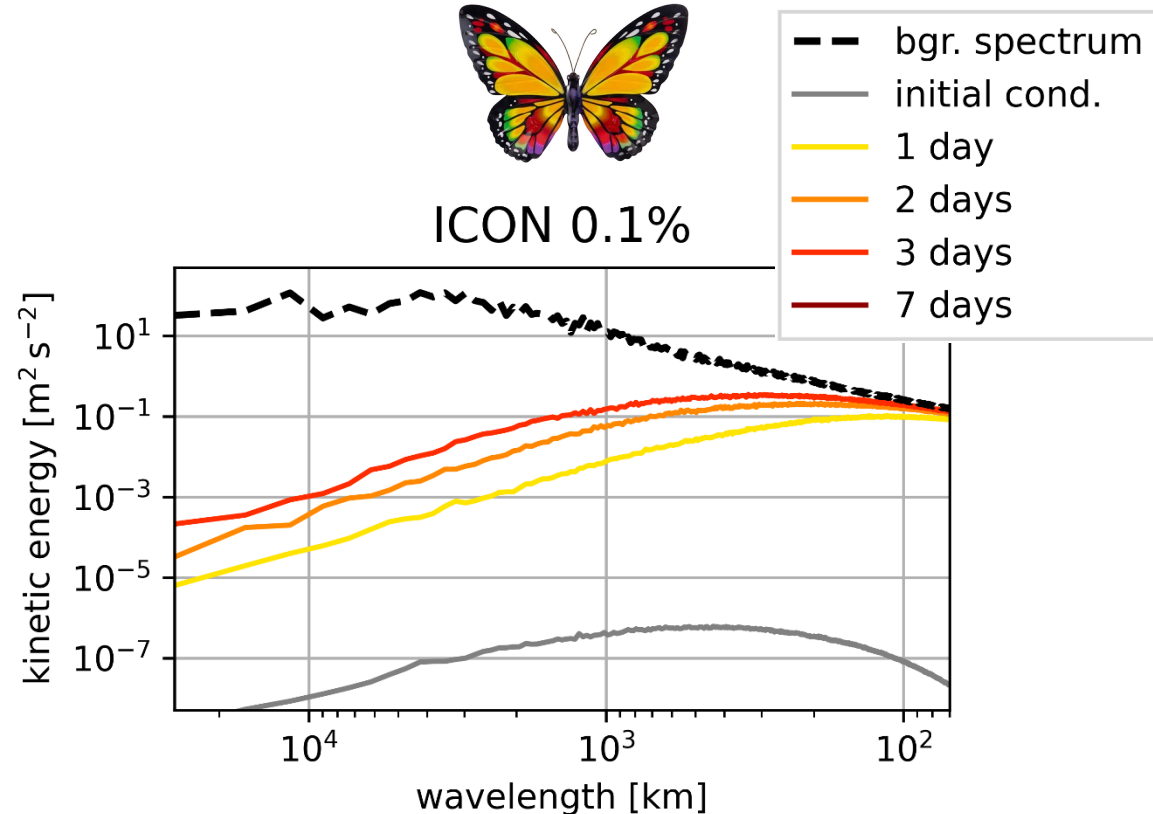
# Uncertainty spectra 100% (DKE 300hPa)



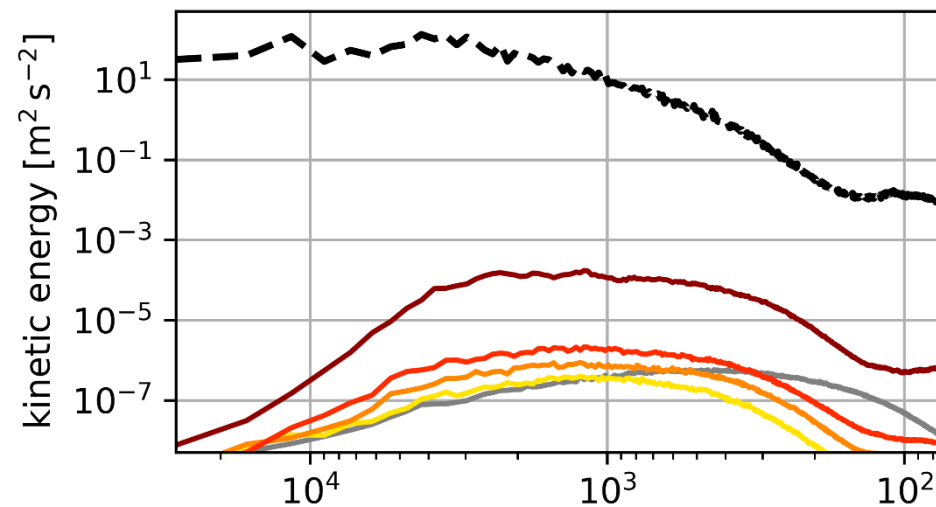
# Uncertainty spectra 0.1% (DKE, 300hPa)



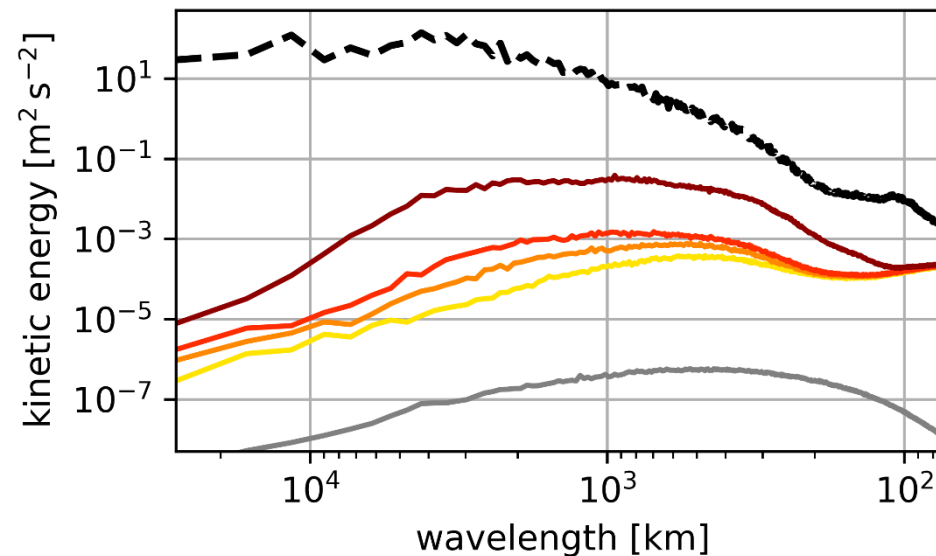
ICON 0.1%



Pangu 0.1%



GraphCast 0.1%



**FourCastNet and NeuralGCM**  
similar to Pangu