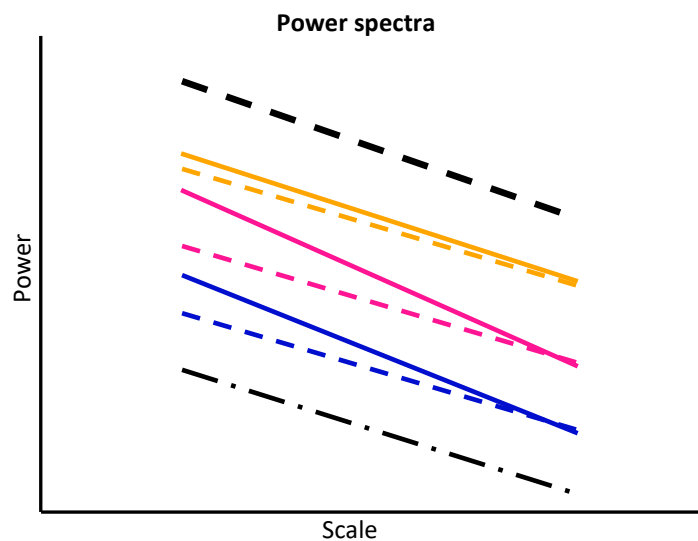
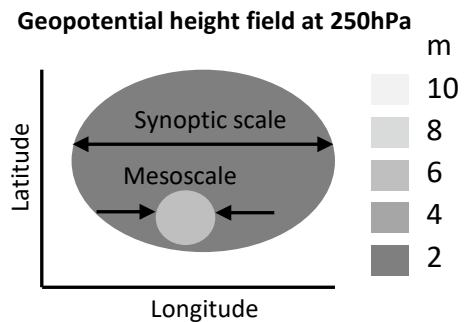
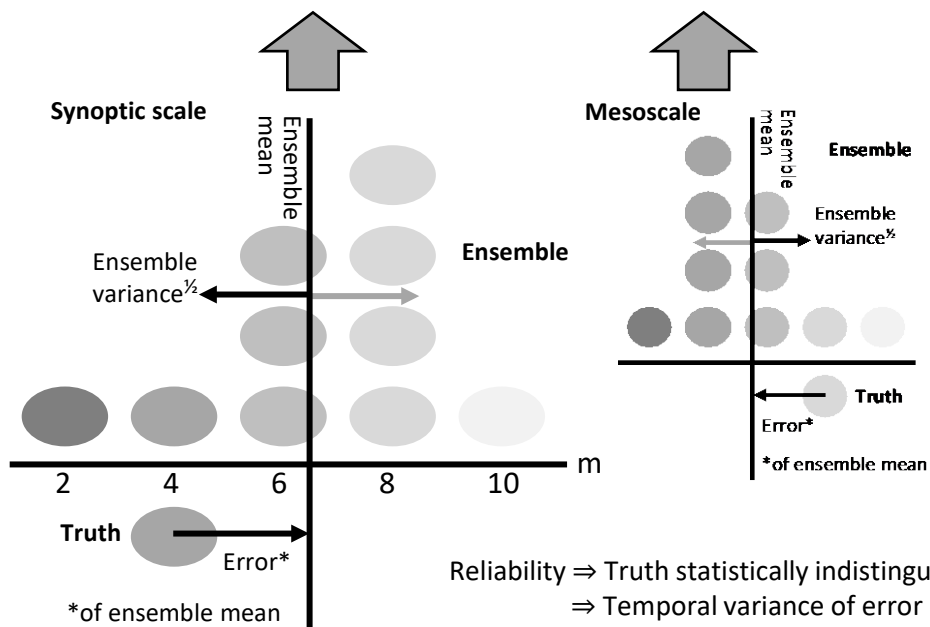


Creating power spectra to show the spatiotemporal evolution of ensemble spread and error



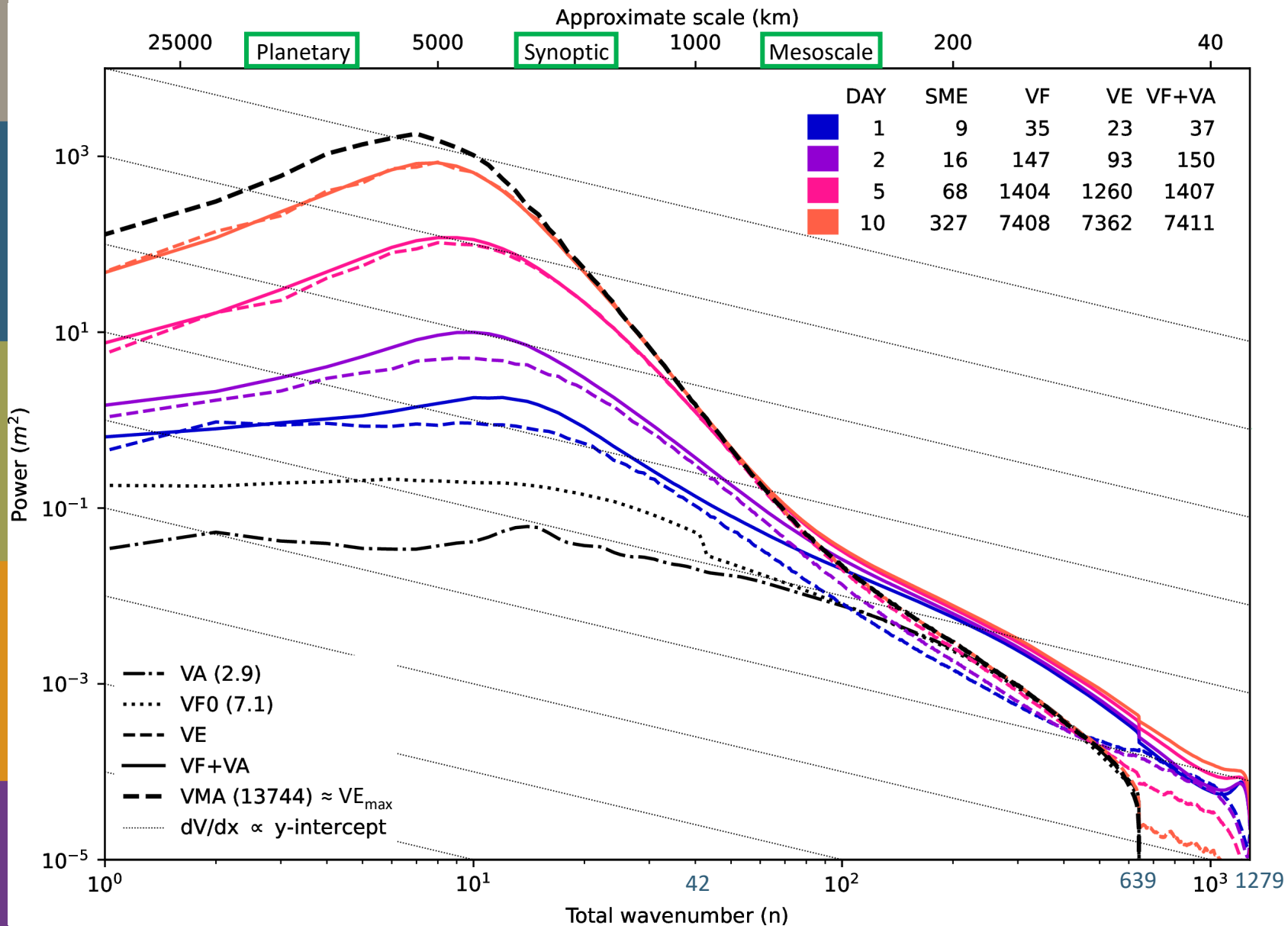
		Sum over all scales			
DAY	SME	VF	VE	VF+VA	
1	4	34	25	37	
2	10	148	104	151	
5	50	1410	1407	1413	
10	327	7367	7522	7370	
15	580	11670	11215	11673	
20	714	13317	12865	13319	
40	794	14302	13600	14305	

- VA = Mean ensemble variance of analysis
- VE = Temporal variance of ensemble-mean error
- VF+VA = Mean variance of forecast + mean variance of verifying analysis
- VMA = Temporal variance of mean analysis ($\approx VE_{max}$)
- SME = Squared temporal-mean of error ("squared bias")



Reliability \Rightarrow Truth statistically indistinguishable from an ensemble member
 \Rightarrow Temporal variance of error (VE) = mean variance of forecast (VF) { + mean variance of verifying analysis (VA) }

Operations: Z250 power spectra of medium-range ensemble: Dec 2023 – Feb 2024 (DJF24)



Log-log plot

- Wavenumbers (n) more tightly packed towards right
- Diagonal contours indicate contribution to total variance per unit linear distance on x-axis
- Contour value is proportional to the y-intercept

EDA

- Maximum variance contribution at scales $\approx 1000\text{km}$
- Global average total variance = 2.9m^2
- Spectral resolution $n = 639$ ($\approx 60\text{km}$), 50 members
- Curious wobbles at synoptic scales

ENS initial conditions

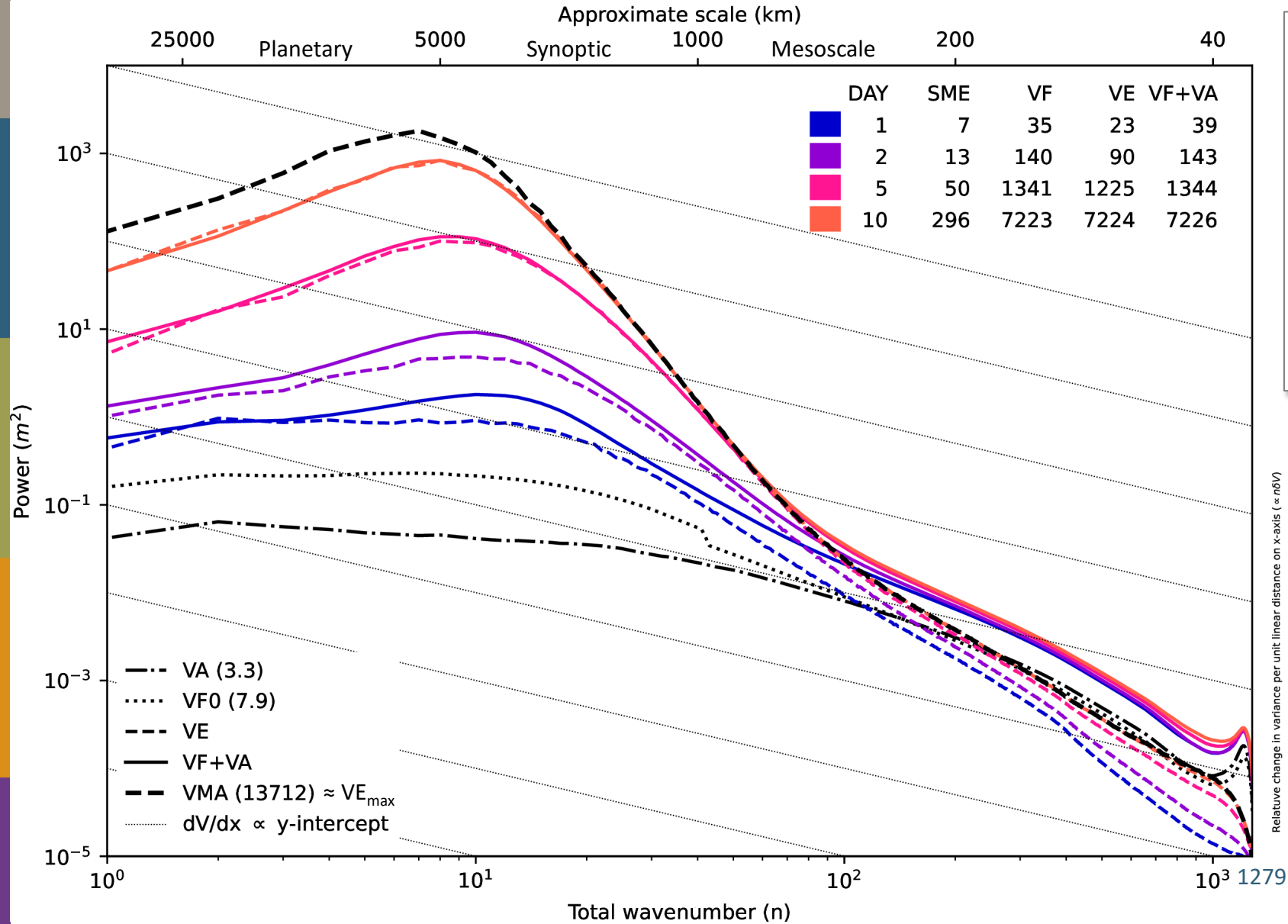
- A few hours forecast variance growth
- Singular vector (SV) perturbations at $n \leq 42$
- Maximum Variance Contribution at $\approx 2000\text{km}$

ENS days 1–10

- Spectral resolution $n = 1279$ ($\approx 30\text{km}$), 50 members
 - Synoptic scales*
 - Dominate medium-range variance (role of SVs?)
 - Over-dispersive (in stormtracks) at days 1,2
 - Better reliability at days 5,10
 - Maximum error not reached by day 10
 - Smaller scales*
 - Errors quickly converge to theoretical maximum
 - Forecast variance saturates at higher level
 - Assumptions in spectral error-spread rel^n less valid?
 - Disregard error and reliability for $n > 639$ as no EDA

Results based on OUTC runs only for compatibility with experimental system

New IFS cycle: Z250 power spectra of the medium-range ensemble: DJF24 0Z



EDA

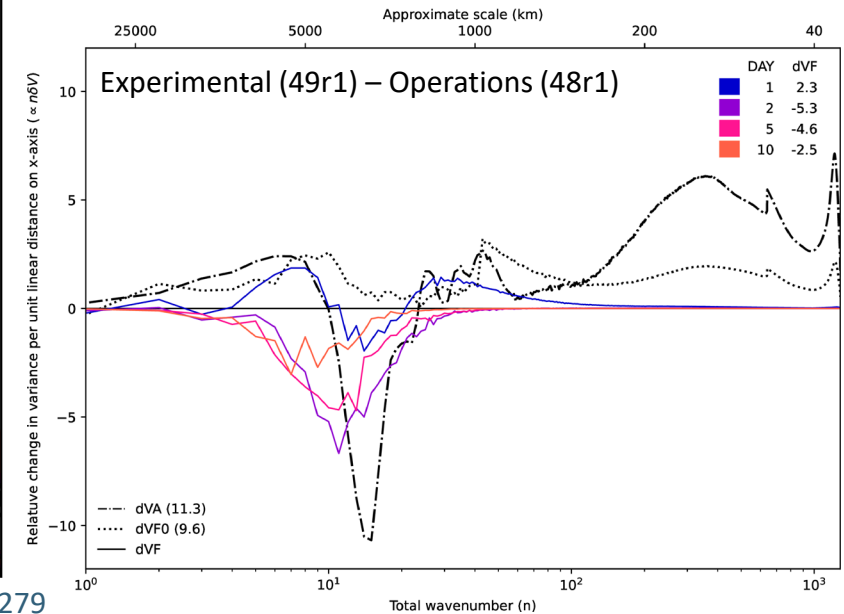
- The higher resolution EDA looks much better
- Reduced synoptic-scale wobbles
- Less drop-off in variance at scales 300 – 40 km

ENS initial conditions

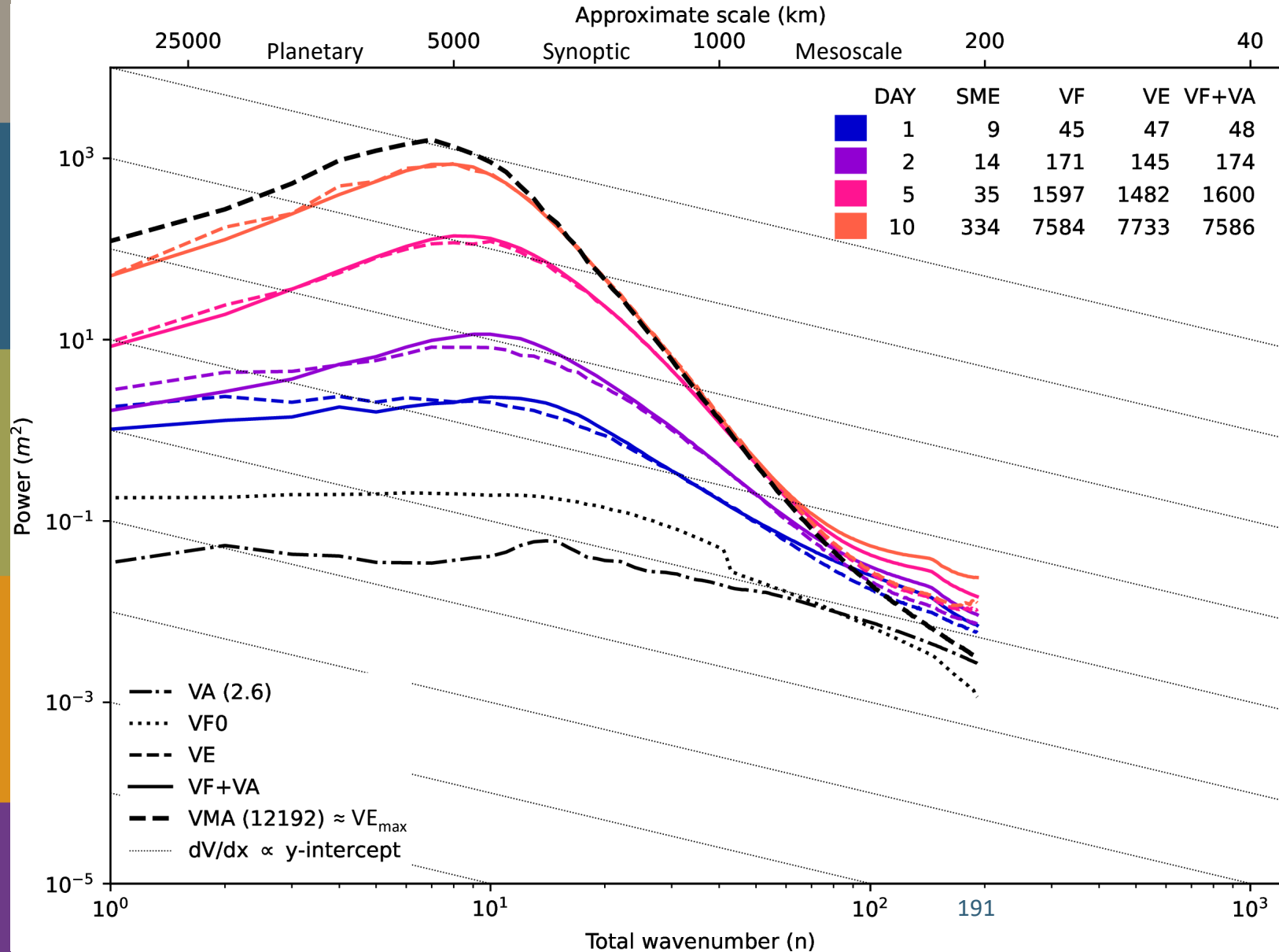
- Initialisation adds slightly more variance

ENS days 1–10

- Reduction in synoptic-scale over-dispersion (due to major change in stochastic physics: SPPT \rightarrow SPP?)
- Global budgets: reduced bias, error variance and better match between VE and VF+VA



AIFS: Z250 power spectra of experimental Artificial Intelligence ensemble: DJF24 0/12 Z



AIFS ensemble (experimental; not real-time version)

- Resolution $\sim 1^\circ \rightarrow$ T191 (≈ 210 km)
- Timestep 6h
- Ensemble size = 8
- Trained on ERA5 1979—2017
- Optimisation based on proper scoring (CRPS)
- Retains random component (“stochastic physics”)

ENS days 1—10

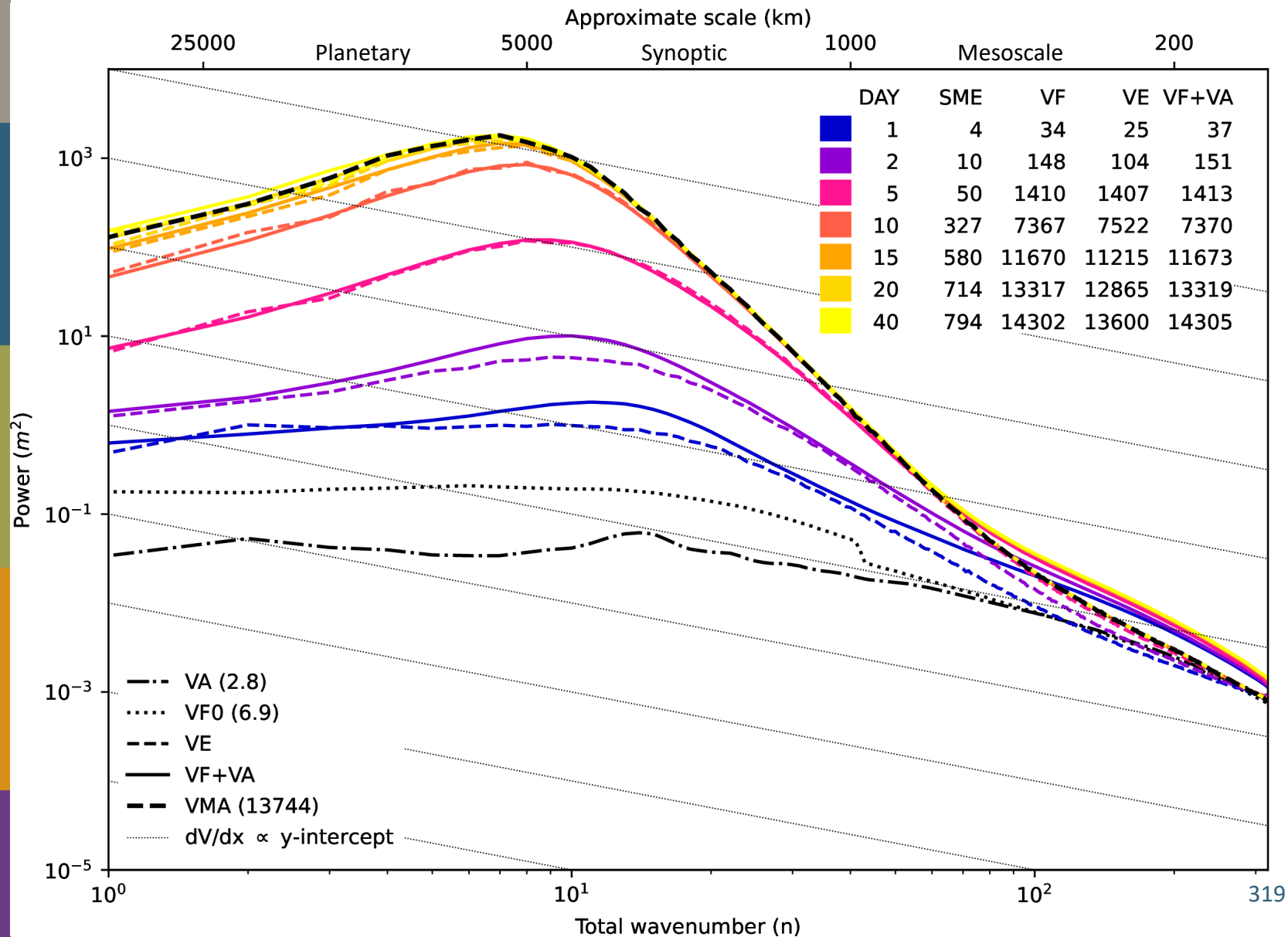
- Planetary scales*
- Under-dispersive at days 1,2 (worse than IFS)
- Synoptic scales*
- Over-dispersive at days 1,2 (better than IFS)
- Smaller scales*
- VE > VE_{max} (as VMF is not negligible)
- All scales*
- AIFS more reliable but at higher variances than IFS

Corresponding table for IFS (truncated to T191)

DAY	SME	VF	VE	VF+VA
1	7	33	23	36
2	15	144	92	146
5	65	1370	1218	1372
10	312	7259	7149	7262

All curves and table values are scaled here to give unbiased estimators for VF

Sub-seasonal ranges: Z250 power spectra of operational ensemble: DJF24 0Z



ENS days 1—40

- Spectral resolution $n = 319$ ($\approx 125\text{km}$), 100 members
- Similar spatiotemporal behaviour to T1279 ENS
- Errors almost completely saturate at VMA by day 40
- T1279 ENS *error* comparison \Rightarrow Resolution matters

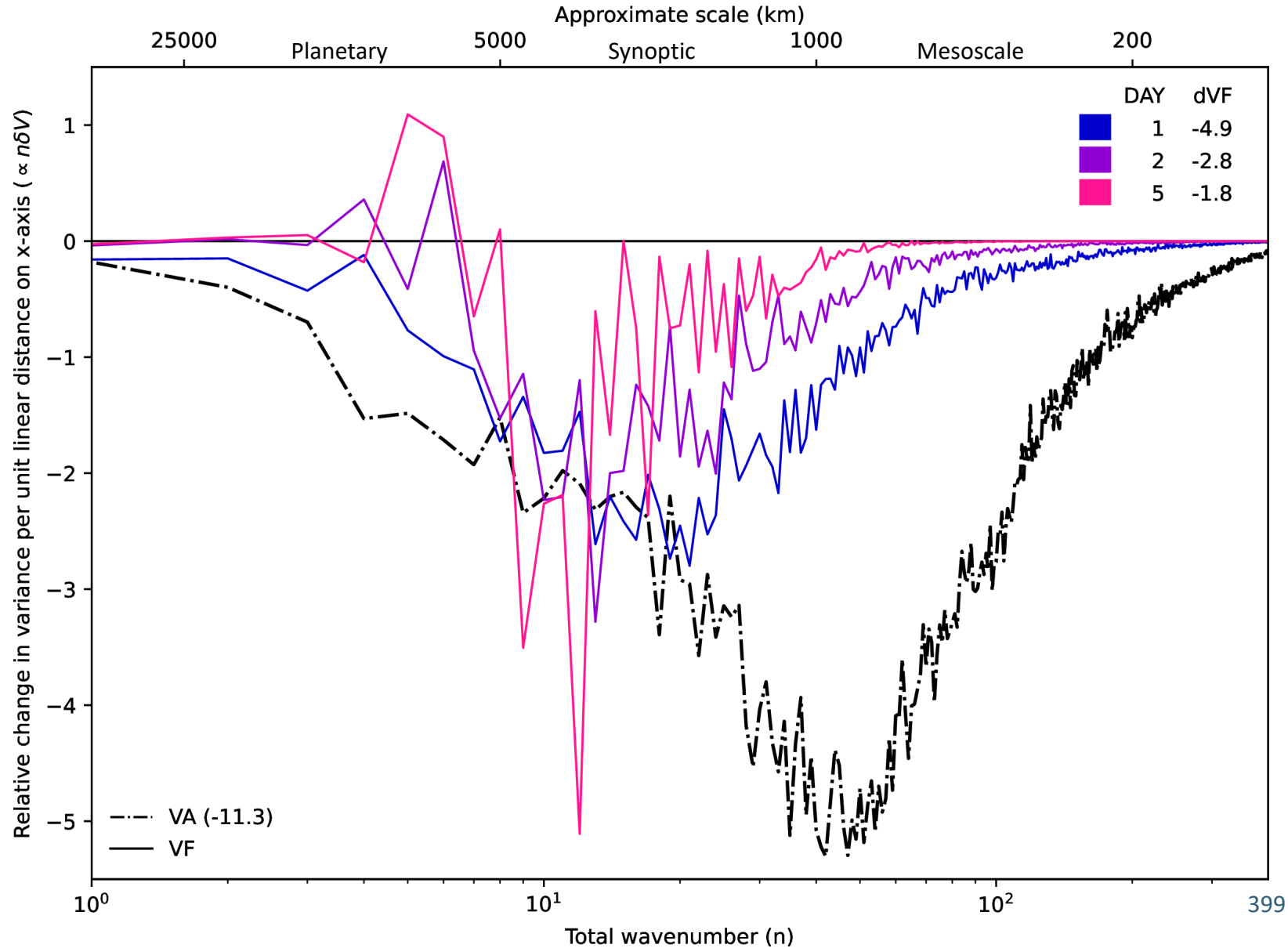
Note that the interhemispheric mode in Z250 displays additional temporal variance associated with the seasonal cycle. This was removed with a quadratic fit. (Just affects Z_1^0 , i.e. wavenumber 1 = 10^0).

Corresponding table for T1279 ENS (truncated to T319)

DAY	SME	VF	VE	VF+VA
1	9	34	23	37
2	16	147	93	150
5	68	1403	1260	1406
10	327	7407	7362	7410
15	625	11733	11286	11735

Errors finally appear to saturate at \sim day 40. Remarkable agreement

Impact of new observations: Z250 % change in power spectra



ENS days 0–5

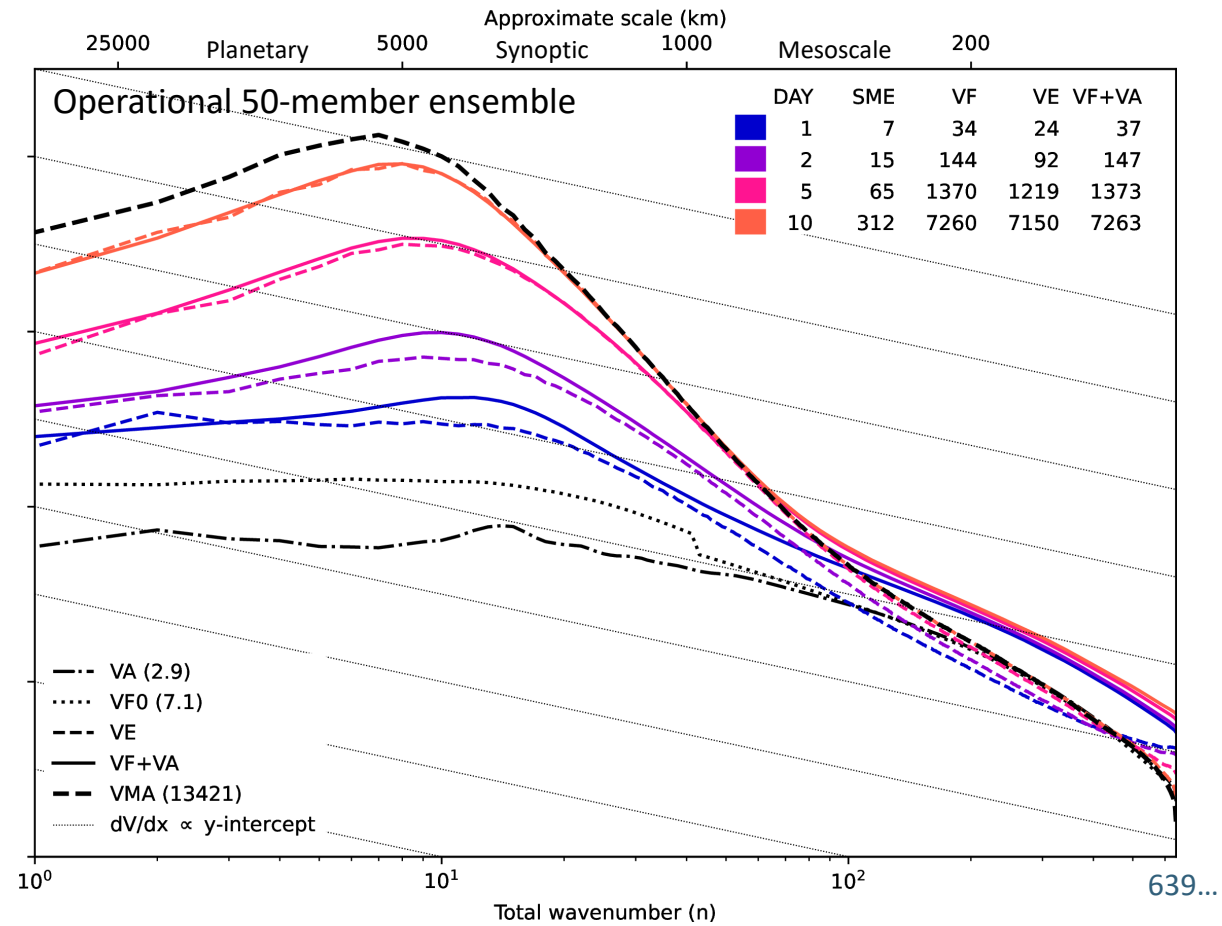
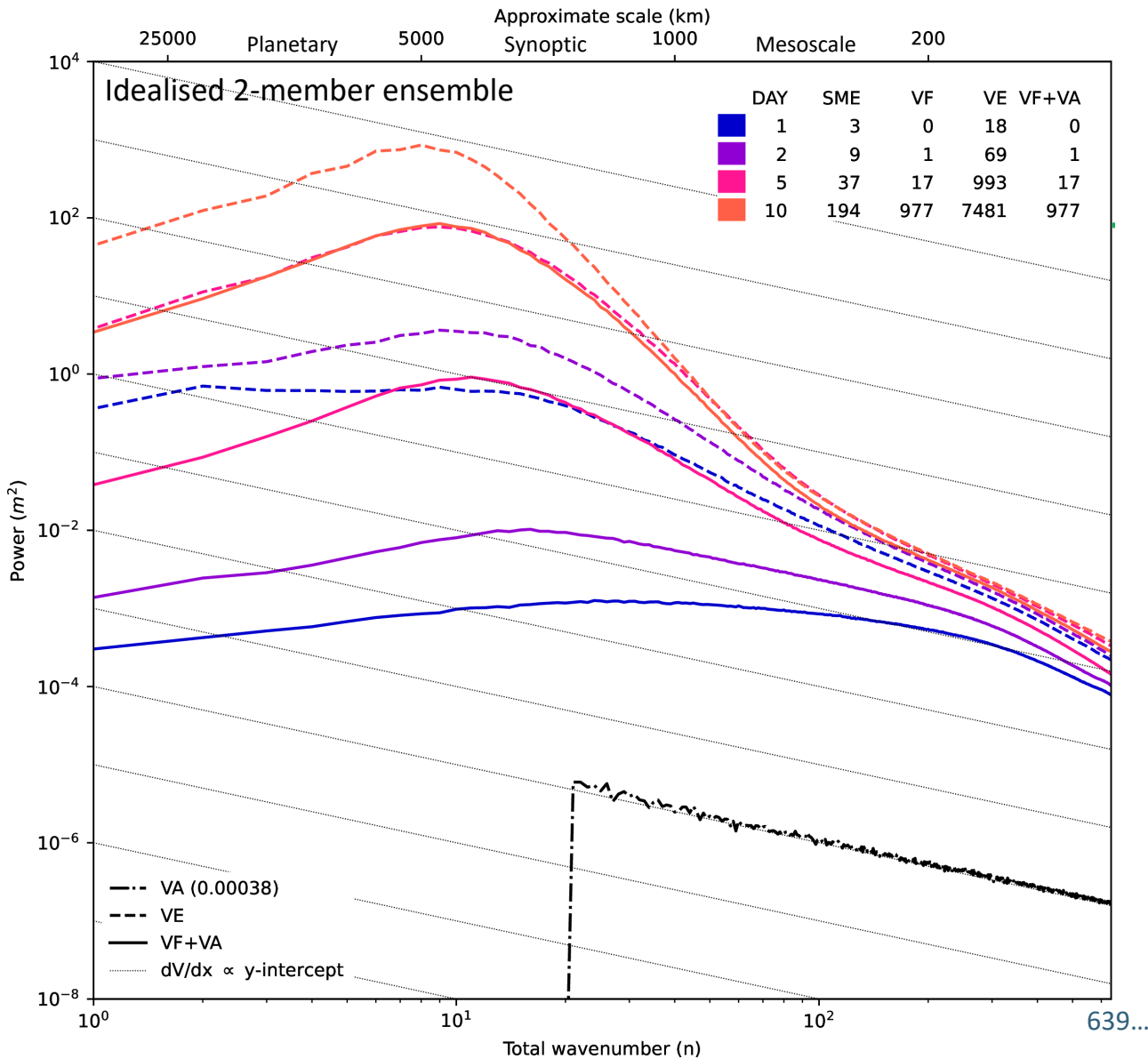
- 30,000 new Radio Occultation observations each analysis cycle (from IROWG ROMEX initiative)
- Error and spread reduced
- Informative to see spatiotemporal impact on ENS
- 11% reduction in EDA variance, centred $\sim 1000\text{km}$
- Biggest impact seen at $\sim 4000\text{km}$ by day 5
- Bigger impact in northern midlatitudes (not shown)

Experimental details

- Cycle 48r1
- Spectral resolution $n = 399$ ($\approx 100\text{km}$), 10 members
- No initialisation step
- Sept 2022

IROWG=International Radio Occultation Working Group
ROMEX=Radio Occultation Modeling Experiment

Predictability study: power spectra of idealised ensemble with tiny initial condition uncertainty



- ENS Cntl & “HRES” have identical resolution with tiny initial condition differences
 - Opportunity for a 2-member predictability experiment
 - Idealised day 10 VF < Operational day 5 VF. 48r1 model \Rightarrow +5 days possible
 - Initial conditions are very unreliable, so VE \gg VF+VA
 - Validity of potential gain? Model is approxⁿ (& lacks stochastic physics)
- All curves and table values are scaled here to give unbiased estimators for VF

DJF24 0/12Z

Suggestion for a further 5 days predictability – How model-dependent is this?

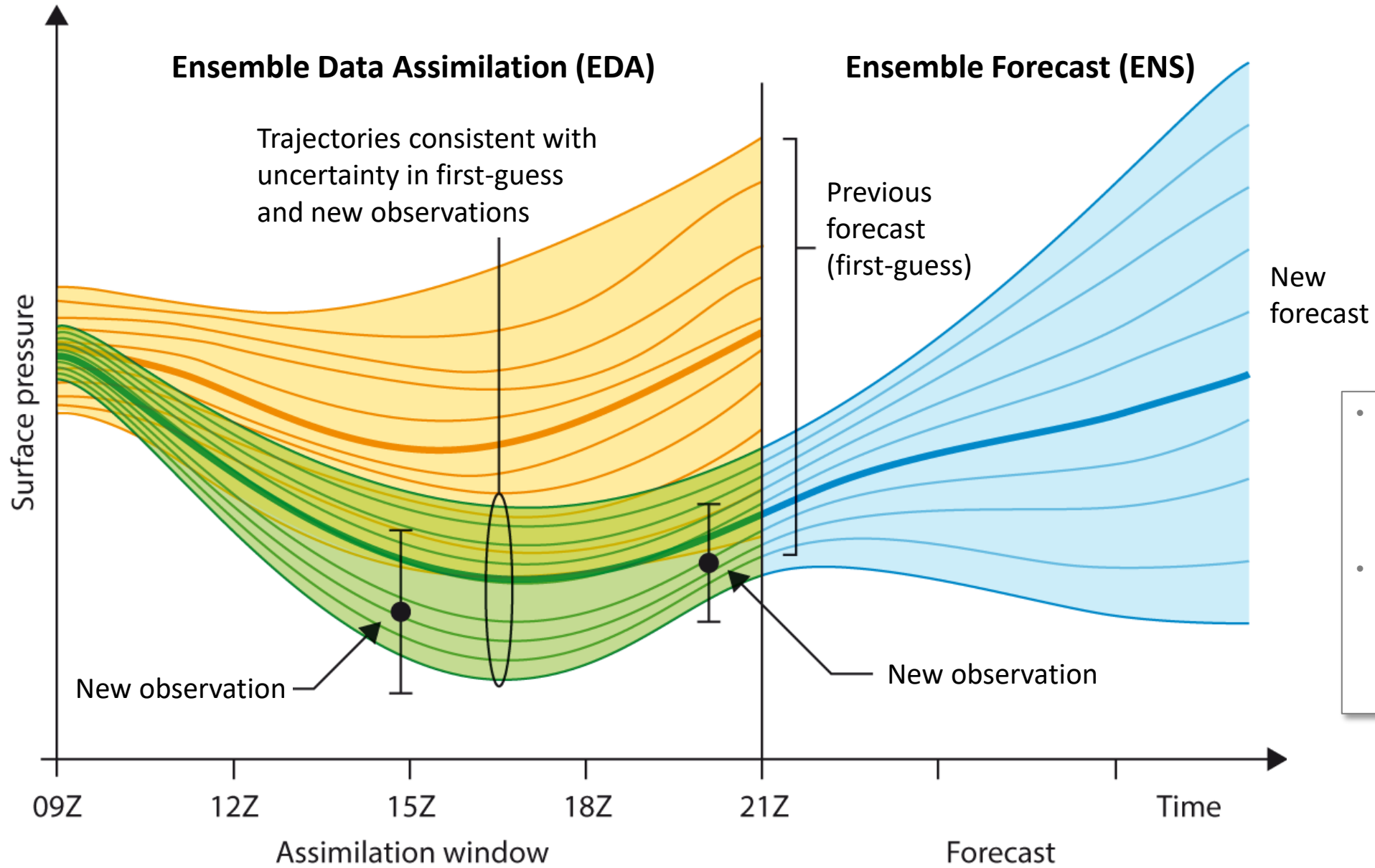
Can:

- Examine spatiotemporal evolution of the ensemble forecast
- Quantify predictive skill as a function of scale
- Chart impact of a new model cycle
- Chart impact of new observations
- Compare ensembles run at different resolutions (inc. AI)

5 more days ...?

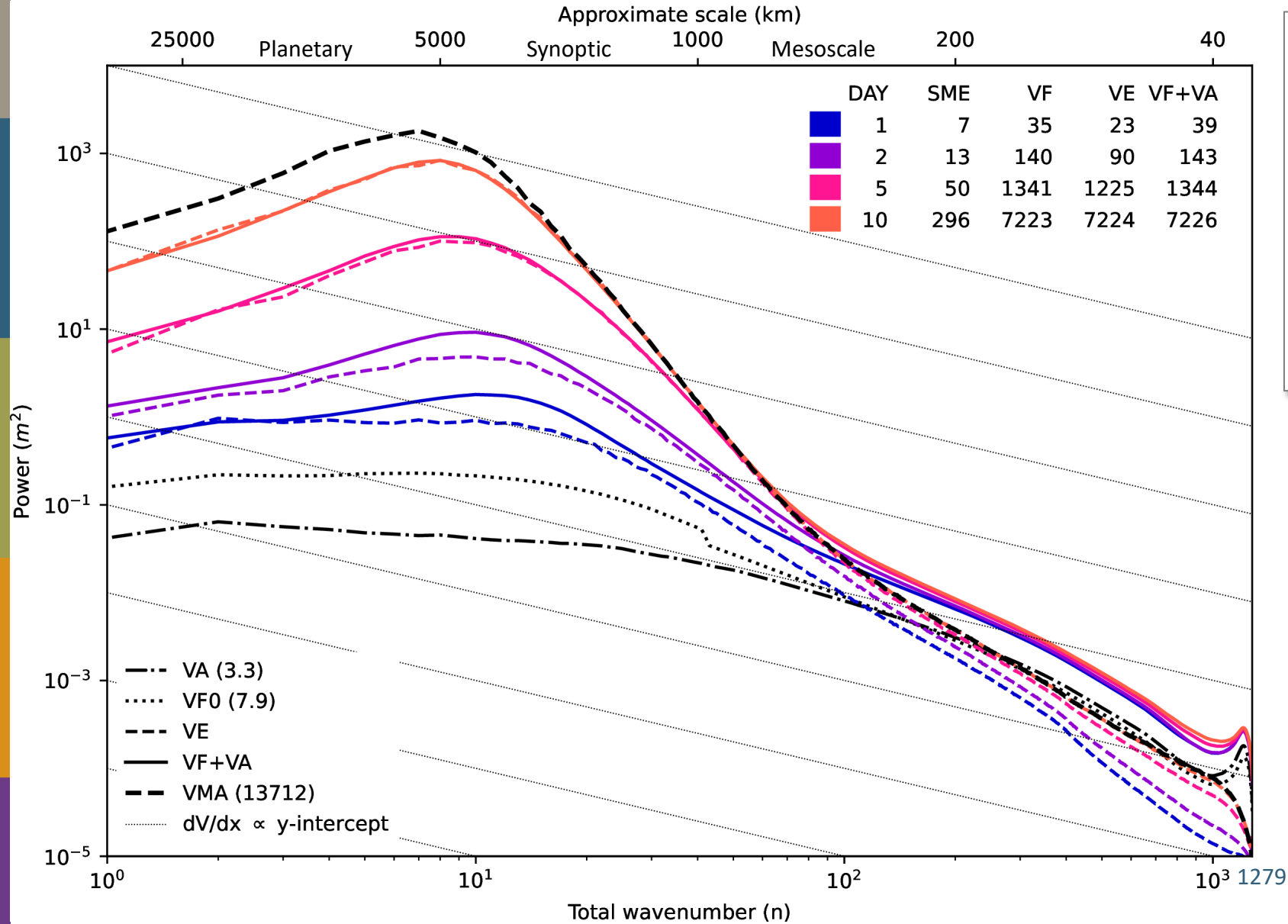
... We just need to make it reliable!

Ensemble Weather Prediction (ECMWF)



- ECMWF's Integrated Forecast System (IFS) includes a global ensemble, which is run with a variety of numbers of members and resolutions.
- The Ensemble of (4D Var) Data Assimilations (EDA) ingests millions of observations each assimilation cycle.

New IFS cycle: Z250 power spectra of the medium-range ensemble: DJF24 0Z



EDA

- The higher resolution EDA looks much better
- Reduced synoptic-scale wobbles
- Less drop-off in variance at scales 200 – 40 km)

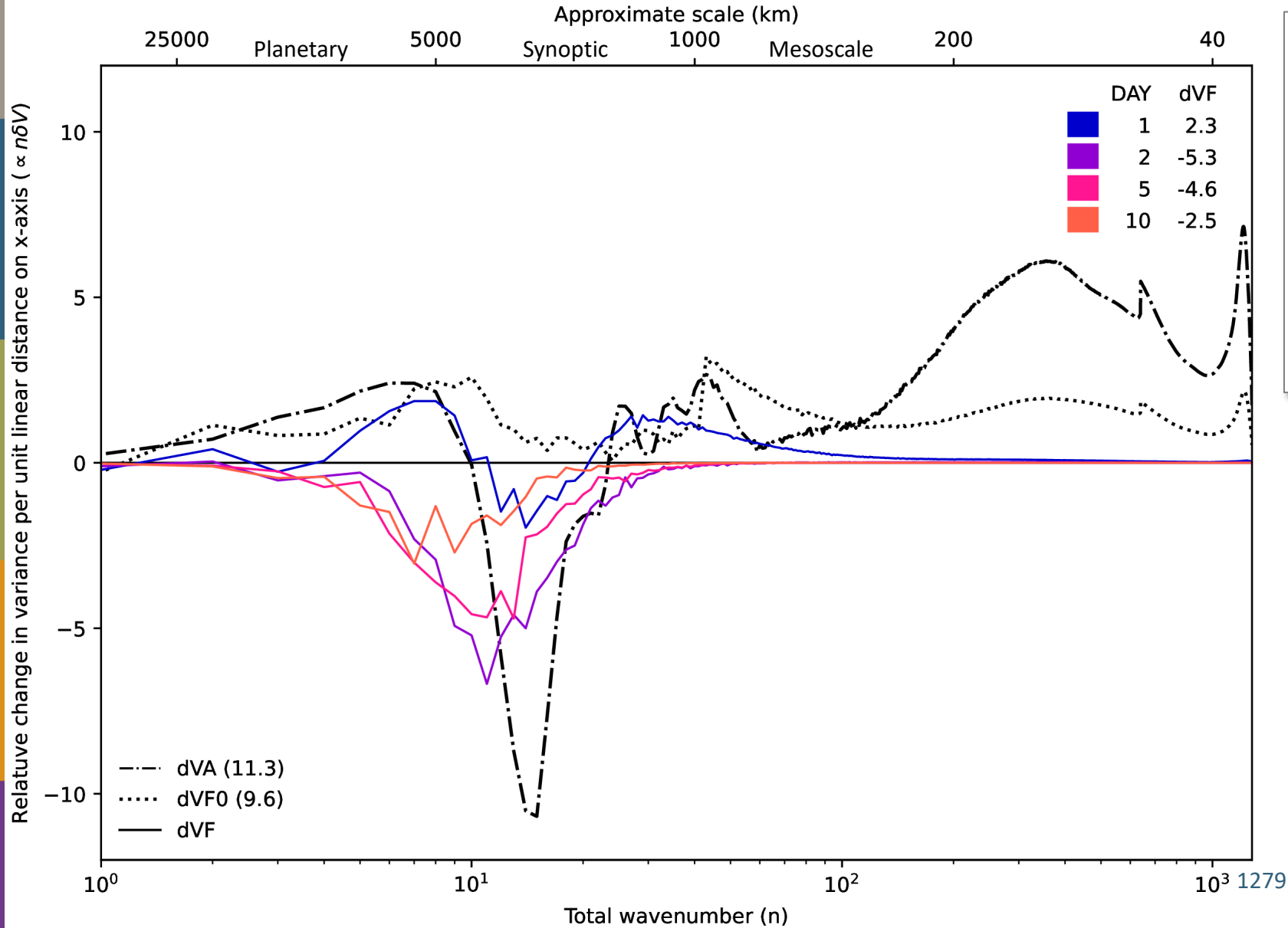
ENS initial conditions

- Initialisation adds slightly more variance

ENS days 1–10

- Reduction in synoptic-scale over-dispersion (due to major change in stochastic physics: SPPT \rightarrow SPP?)
- Global budgets: reduced bias, error variance and better match between VE and VF+VA

New-Current IFS cycle: Z250 power spectra of the medium-range ensemble: DJF24 0Z



EDA

- The higher resolution EDA looks much better
- Reduced synoptic-scale wobbles
- Less drop-off in variance at scales 200 – 40 km)

ENS initial conditions

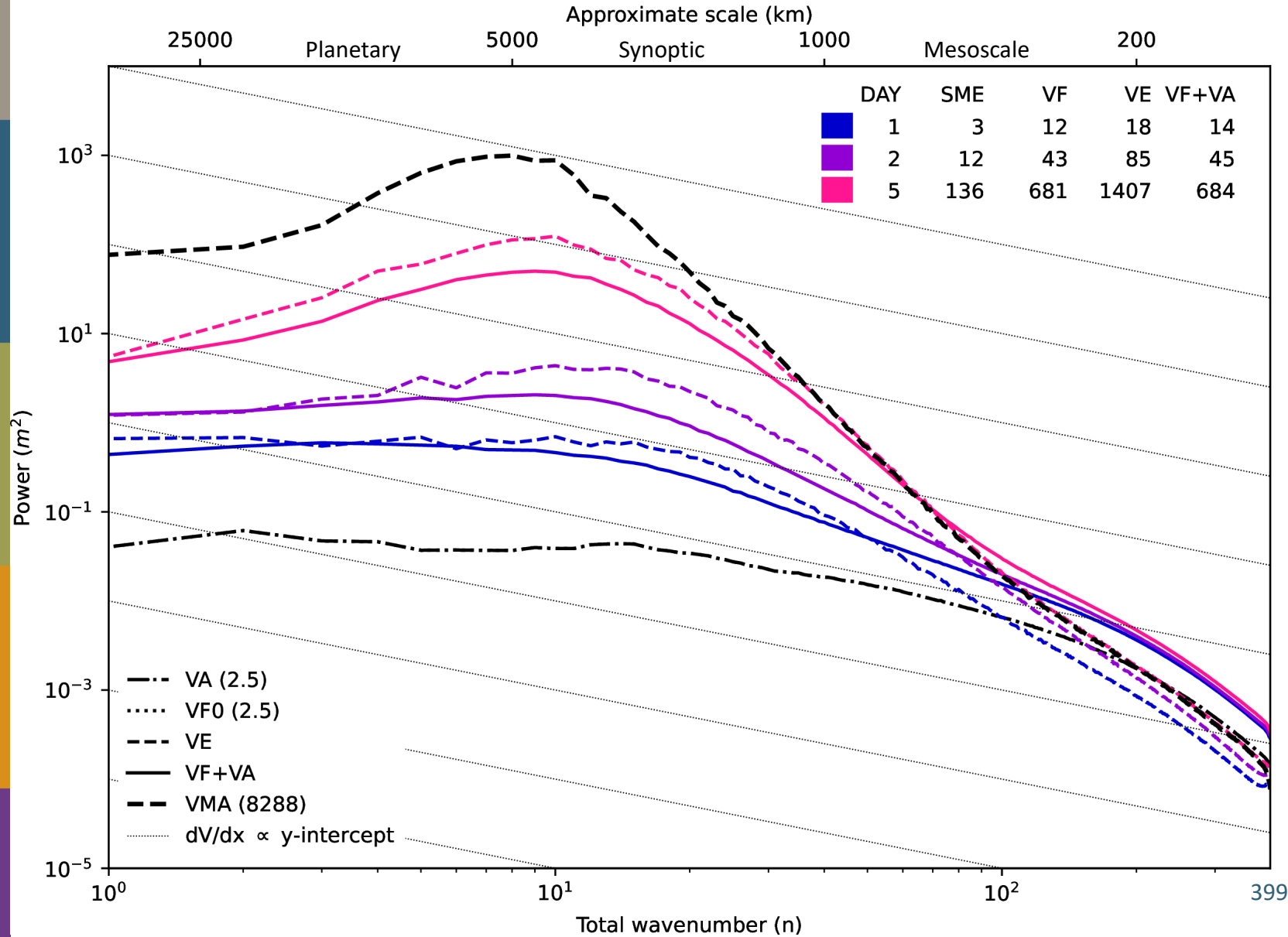
- Initialisation adds slightly more variance

ENS days 1–10

- Reduction in synoptic-scale over-dispersion (due to major change in stochastic physics: SPPT → SPP?)
- Global budgets: reduced bias, error variance and better match between VE and VF+VA

Experimental (49r1) – Operations (48r1)

Seamless Initialisation: Z250 power spectra of control experiment with no SVs: Sept 2022

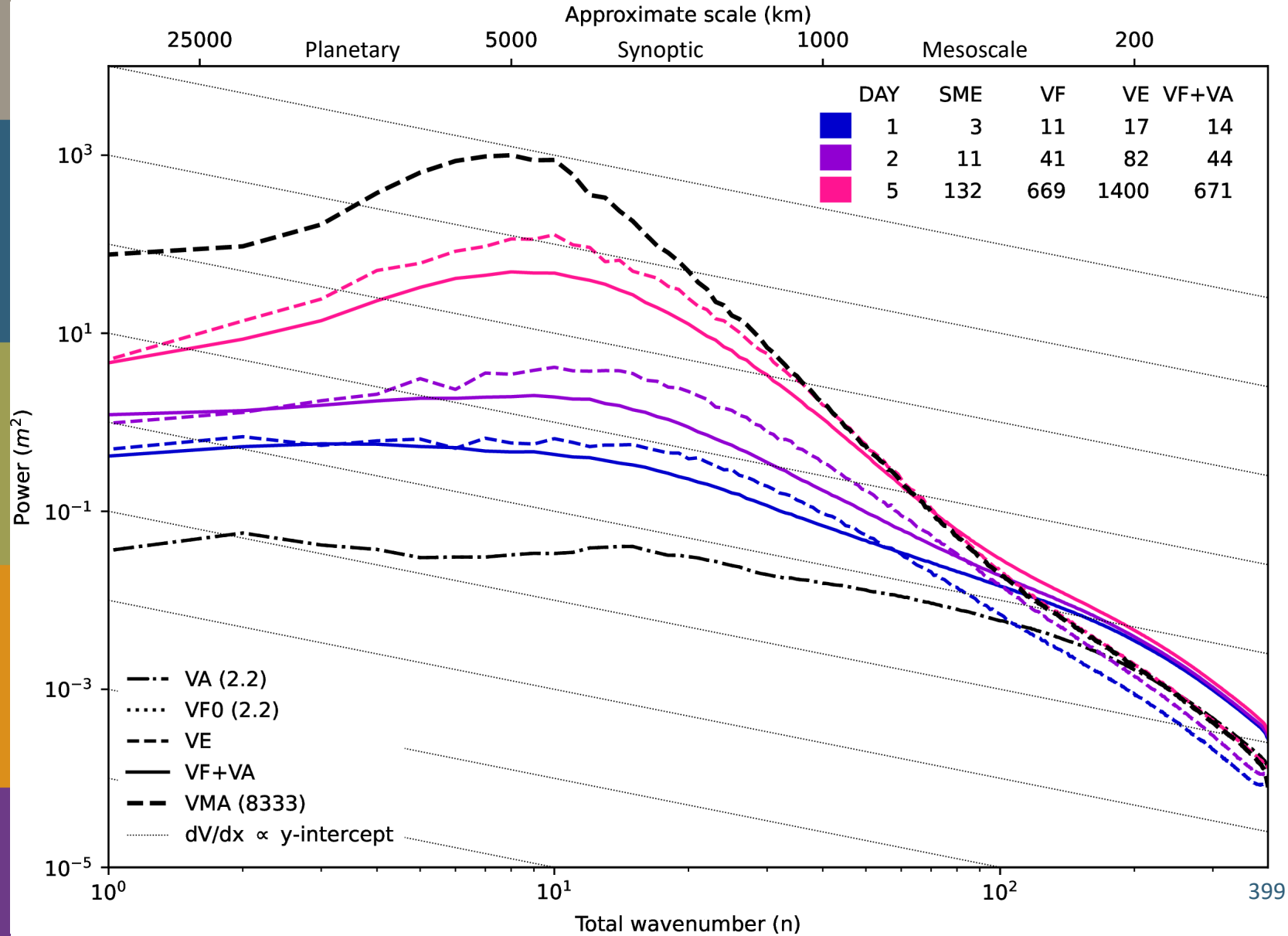


ENS days 1—5

- Cycle 48r1
- Spectral resolution $n = 399$ (≈ 100 km), 10 members
- No initialisation step, so $VF_0 = VA$
- Less of a jump in scales EDA \rightarrow Day 1
- ENS is now under-dispersive

Results based on 0/12 UTC forecasts verifying 10–30 September 2022

Additional data: Z250 power spectra of experiment with 30,000 new occultation observations



ENS days 1—5

- Introduction of 30,000 new Radio Occultation observations each analysis cycle (made available for evaluation as part of the IROWG ROMEX initiative)
- Extra observations reduce error and spread

IROWG=International Radio Occultation Working Group
ROMEX=Radio Occultation Modeling Experiment