

Diagnostics 1

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Training Course on Predictability

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Outline

- Tropical waves, teleconnections, and the propagation of errors
- Identifying the root-causes of forecast biases and assessing models
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Tropical Waves (longitude-time "Hovmöller" diagram)

 -90

 -70

 -50

 -30

 -10

Plots from Bureau of Meteorology. Based on Outgoing Longwave Radiation (OLR), 15oS-15oN

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Equatorial wave theory – the model

Use of the shallow water equations on the β-plane (f=βy) for understanding tropical atmospheric waves. Note: No coupling with convection in this model

Equatorial wave theory – limiting solutions

Kelvin waves: $v \equiv 0$

Gravity waves: Fast; pressure gradient force dominates

(G3)
$$
\frac{\partial \eta}{\partial t} = -\frac{c_e^2}{g'} \left(\frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} \right)
$$

Equator

Rossby waves: Slow; Coriolis affect important, less convergence

(R1)
$$
\frac{\partial \xi}{\partial t} = -\beta v - \beta y \left(\frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} \right)
$$

$$
\approx -\beta v
$$
 Vorticity an

$$
\frac{\partial^2 \eta}{\partial t^2} = c_e^2 \frac{\partial^2 \eta}{\partial x^2}
$$
 (K1 & K3)
\n
$$
\eta \propto \sin(kx - \omega t)\hat{\eta}(y)
$$

\n
$$
k = \text{zonal wavenumber}
$$

\n
$$
\rho \text{base} = \frac{\omega}{k} = c_e
$$

\n
$$
\hat{\eta}(y) = e^{-\frac{\beta}{2c_e}y^2}
$$
 (K2 & K3) ρ Decays away
\n
$$
\frac{\partial^2 \eta}{\partial t^2} = c_e^2 \left(\frac{\partial^2 \eta}{\partial x^2} + \frac{\partial^2 \eta}{\partial y^2}\right)
$$
 (G1, G2 & G3)
\n
$$
\eta \propto \sin(kx - \omega t)\hat{\eta}(y)
$$

\n
$$
\rho \text{base} = \frac{\omega}{k} = \pm c_e \left(1 - \frac{1}{k^2 \eta} \frac{\partial^2 \hat{\eta}}{\partial y^2}\right)^{\frac{1}{2}}
$$

\n
$$
\hat{\eta} \text{ and } \frac{\partial^2 \hat{\eta}}{\partial y^2} \text{ have opposite sign}
$$

\n
$$
(\text{larger} \Rightarrow \text{ faster}, \frac{\omega}{k} \rightarrow \pm c_e \text{ as } |k| \rightarrow \infty)
$$

\n
$$
\frac{\partial \nabla^2 \psi}{\partial t} = -\beta \frac{\partial \psi}{\partial x}
$$
 (R1) $\psi = \text{streamfunction}$
\n
$$
\psi \propto \sin(kx - \omega t)\hat{\psi}(y)
$$

\n
$$
\rho \text{base} = \frac{\omega}{k} = -\beta \left(k^2 - \frac{1}{\hat{\psi}} \frac{\partial^2 \hat{\psi}}{\partial y^2}\right)^{-1}
$$

\n
$$
\psi = \text{streamfunction}
$$

\n
$$
\psi \text{ is an } (kx - \omega t)\hat{\psi}(y)
$$

\n
$$
\rho \text{base} = \frac{\omega}{k} = -\beta \left(k^2 - \frac{1}{\hat{\psi}} \frac{\partial^2 \hat{\psi}}{\partial y^2}\right)^{-1}
$$

\n
$$
\psi = \text{square function}
$$

\n
$$
\psi = \
$$

(larger ⇒ faster)

have opposite sign Multi-node $(v = 0)$

 ω/k

 \underline{v}

Free Equatorial Waves

• E & W prop. **Mixed Rossby-Gravity**

Note: y has been non-dimensionalised by the factor $(\beta/c_e)^{1/2}$

In dispersion relation, gravity waves mainly associated with first two terms on lhs, Rossby waves with last two terms on lhs, mixed Rossby-gravity waves with all three terms

Interpretation of Free Equatorial Waves

Wave power for OLR, with dispersion relation overlaid

Based on data from NOAA & IFS cycle 32R3 for DJF 1990-2005

Wave Spotting! – How information (and errors) can propagate within the Tropics

Colours show height perturbation (red positive, blue negative), arrows show lower-level winds

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Colours show height perturbation (red positive, blue negative), arrows show lower-level winds

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Wave spotting: Your Answers

Animation of tropical waves – analysed then forecast

Thanks: Rebecca Emerton

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Tropical waves identified using wavenumber-frequency power of OLR, as in the previous dispersion diagram

Gill's steady solution to monsoon heating

Following Gill (1980). See also Matsuno (1966)

Damping/heating terms take the place of the time derivatives. Explicitly solve for the x-dependence

Obtain a Kelvin wave solution to the east (zero meridional flow) and a Rossby wave response to the west (super-position of two Rossby waves: one symmetric and one anti-symmetric about the equator)

Colours show perturbation pressure, vectors show velocity field for lower level, contours show vertical motion (blue = -0.1, red = 0.0,0.3,0.6,…)

Model climate response to a change in aerosol climatology

Outline

- Tropical waves, teleconnections, and the propagation of errors
- Identifying the root-causes of forecast errors and assessing models

Mean forecast error for meridional wind (v925) at different lead-times

In general, at short lead-times, mean errors are more coherent, statistically significant and linked to model deficiencies. Here they indicate a lack of convergence into the Hadley Circulation. Note this is only ~0.6ms⁻¹. Can we be sure it is a model error and not an analysis error? (see next slide)

December 2022 – February 2023. Saturated colours highlight mean errors (forecast minis analysis) which are statistically significant at the 5% level (~5% of points would pass the test by chance)

500 ECMWF

At longer lead-times, errors are more associated with lack of predictability (of equatorial waves, etc.)

Using data assimilation to better determine the root cause of the problem

Here the Scatterometer wind 'observations' show a consistent story with weaker convergence in the model (background). The analysis increments correct this mean departure

December 2022 – February 2023. Saturated colours highlight mean errors which are statistically significant at the 5% level (~5% of points would pass the test by chance)

The Ensemble of Data Assimilations (EDA) suggests we over-estimate the scatterometer errors (their variance is bigger than the squared departures in some regions) hence the mean analysis increments could be even stronger. This is evidence that the problem is with the model

The complexity of present-day model physics

Figure from Peter Bechtold

Ideally, we wish to identify deficiencies at the process level. Again, this should be easier at short timescales since interactions between physical processes and the resolved flow (including teleconnections) are minimised

The Initial Tendency approach to diagnosing model error

Analysis Observations H **Evolution Next First-guess Analysis Departure forecast** (e.g.) Temperature (e.g.) Temperature **Analysis Increment Dynamics Cloud Residual (other numerics) Convection Radiation Vertical Diffusion (&GWD)** Analysis step

Schematic of the data assimilation process – a diagnostic perspective

"Initial Tendency" approach discussed by Klinker & Sardeshmukh (1992). Refined by Rodwell & Palmer (2007)

Analysis increment corrects first-

First-guess = sum of all processes

Relationship between increment and individual process tendencies

guess error, and draws next analysis closer to observations.

can help identify key errors.

Data assimilation as a means of constraining climate sensitivity

Dyn Rad V.Dif Con LSP Net D+5 Bias *70% conf.int. T159, L60,30min. See also Sexton et al. (2019), Klocke and Rodwell (2014)*

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Dyn Rad V.Dif Con LSP Net D+5 Bias

Summary

- Tropical waves, teleconnections, and the propagation of errors
	- Important for predictability
	- Can complicate the diagnosis of forecast system deficiencies
- Identifying the root-causes of forecast errors and assessing models
	- Diagnosis at short leadtimes (associated with data assimilation) can localise errors (geographically, process-wise, model versus observation) before errors and uncertainties have had time to propagate and interact
	- Don't need mean error patterns to agree at short-range and long ranges (although sometimes bias patterns do simply grow in magnitude)
- Next lecture: Ensemble aspects, Uncertainty growth, "Classifying and modelling butterflies"