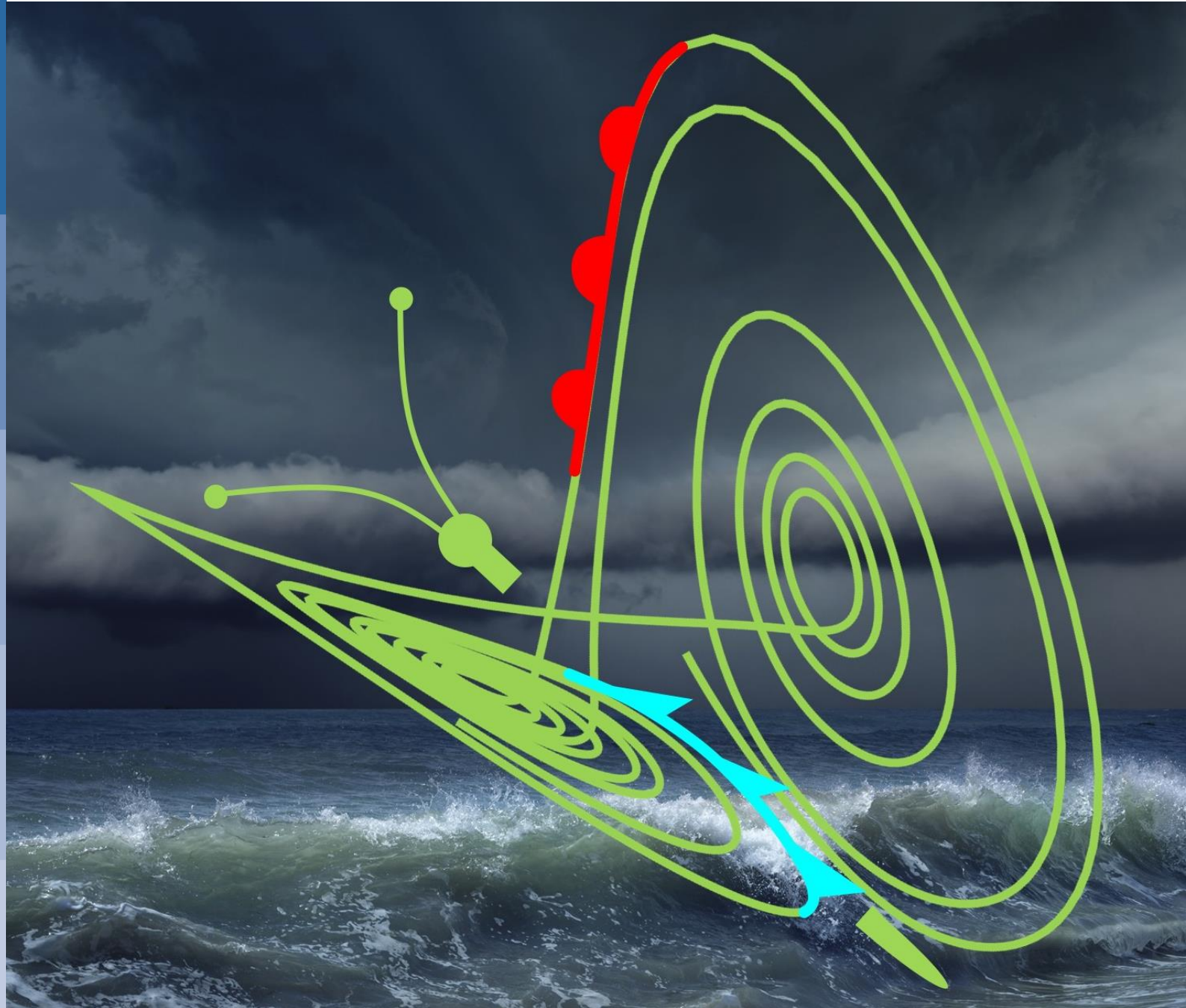


Diagnostics 2

Mark Rodwell



ECMWF Training Course on
Predictability

6 November 2024, ECMWF Reading

- Tropical forcing of midlatitude Rossby waves
- Predictability, reliability and sharpness

- Tropical forcing of midlatitude Rossby waves
- Predictability, reliability and sharpness

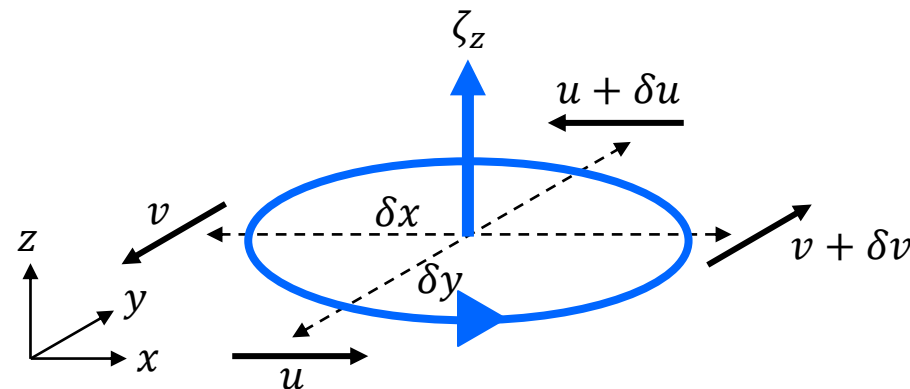
The Vorticity Equation

Motivation (2D flow) :

$$\zeta_z = \frac{\partial v}{\partial x} - \frac{\partial u}{\partial y} \quad (\equiv \hat{\mathbf{k}} \cdot \nabla_z \times \mathbf{v}) \text{ is the vorticity}$$

$\hat{\mathbf{k}}$ is the unit vertical vector

$\nabla_z \times$ is the horizontal curl operator



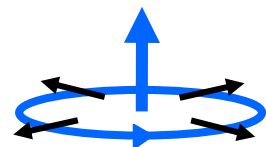
Curl of the 3D momentum equation in absolute frame of reference:

$$\frac{d\zeta}{dt} = -\zeta(\nabla \cdot \mathbf{u}) + (\zeta \cdot \nabla)\mathbf{u} + \frac{1}{\rho^2} \nabla \rho \times \nabla p + \nabla \times \mathbf{F}_u$$

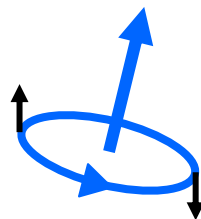
Lagrangian tendency



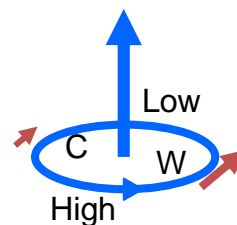
Divergence



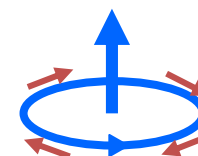
Tilting



Baroclinic



Friction

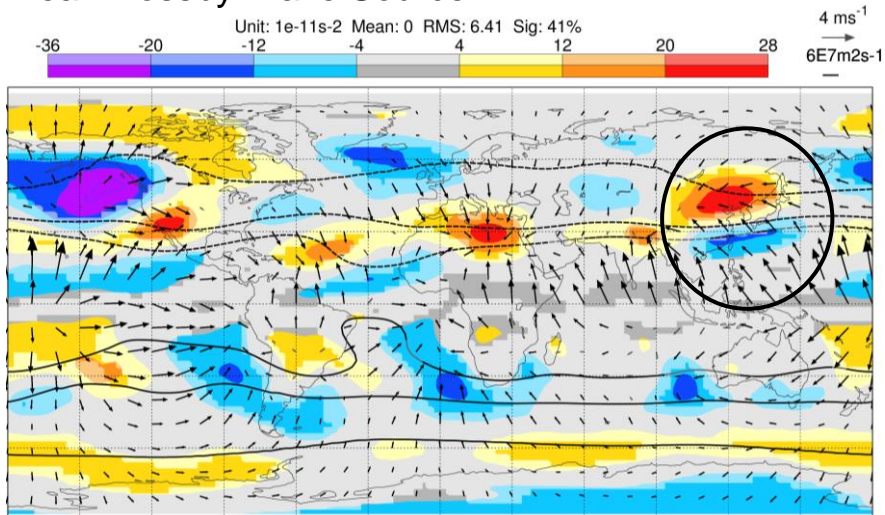


Shallow atmosphere approximation & assuming horizontal, barotropic, frictionless flow:

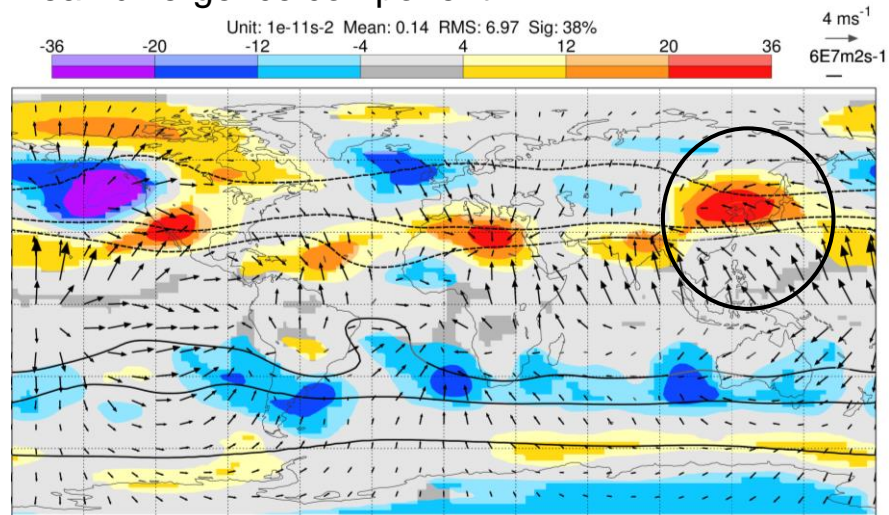
$$\begin{aligned} \frac{\partial \zeta}{\partial t} + \mathbf{v}_\psi \cdot \nabla \zeta &= -\mathbf{v}_\chi \cdot \nabla \zeta - \zeta \nabla \cdot \mathbf{v}_\chi \\ &= -\nabla \cdot (\mathbf{v}_\chi \zeta) \quad \text{“Rossby Wave Source”} \end{aligned}$$

Terms in the Vorticity Equation (upper troposphere)

Mean Rossby Wave Source



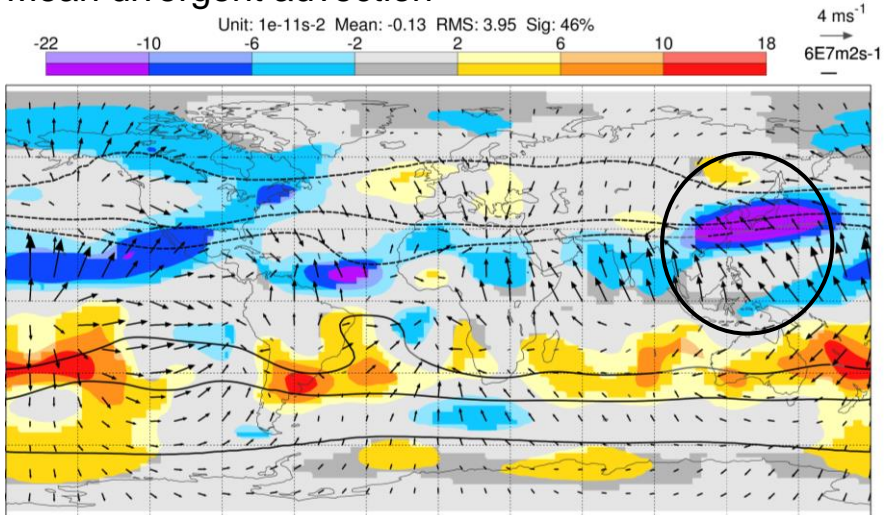
Mean divergence component



Shading: Terms
Contours: Streamfunction
Vectors: Divergent winds

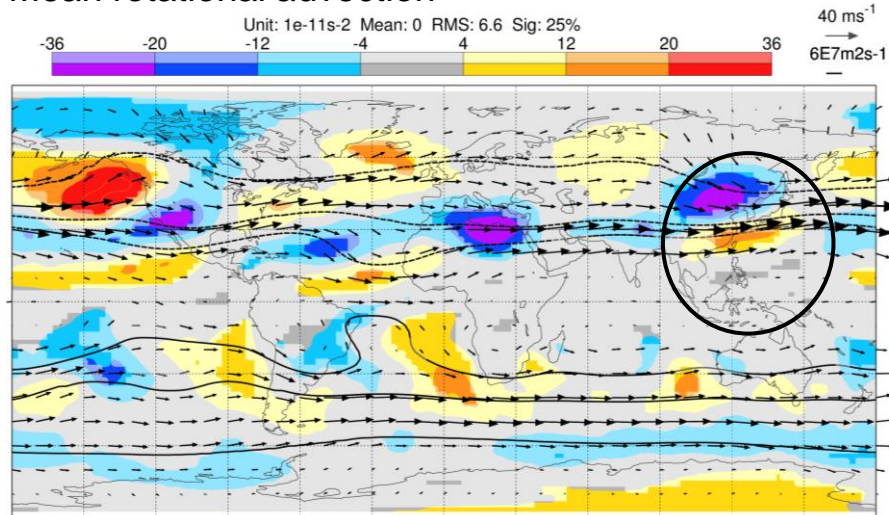
Convergence associated with “stretching”

Mean divergent advection



Advection of low planetary vorticity by divergent outflow

Mean rotational advection

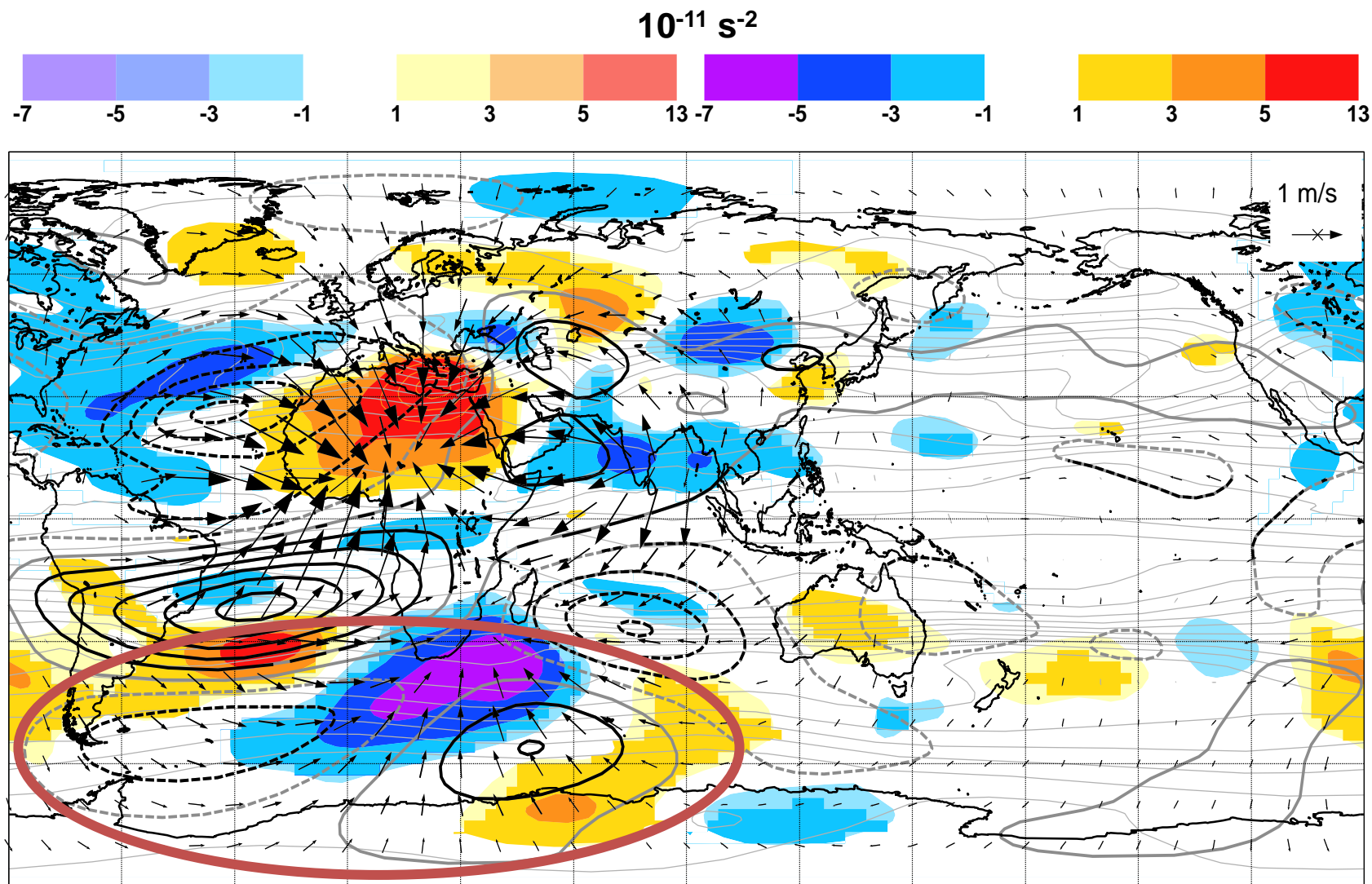


Adjustment of rotational flow balances RWS

Based on operational analyses for the period DJF 2015/16, with terms integrated between 100-300 hPa.

Aerosol impact on RWS, divergent wind & streamfunction

Rodwell and Jung (2008)



Shading: RWS
Thick contours: Streamfunction
Vectors: Divergent winds

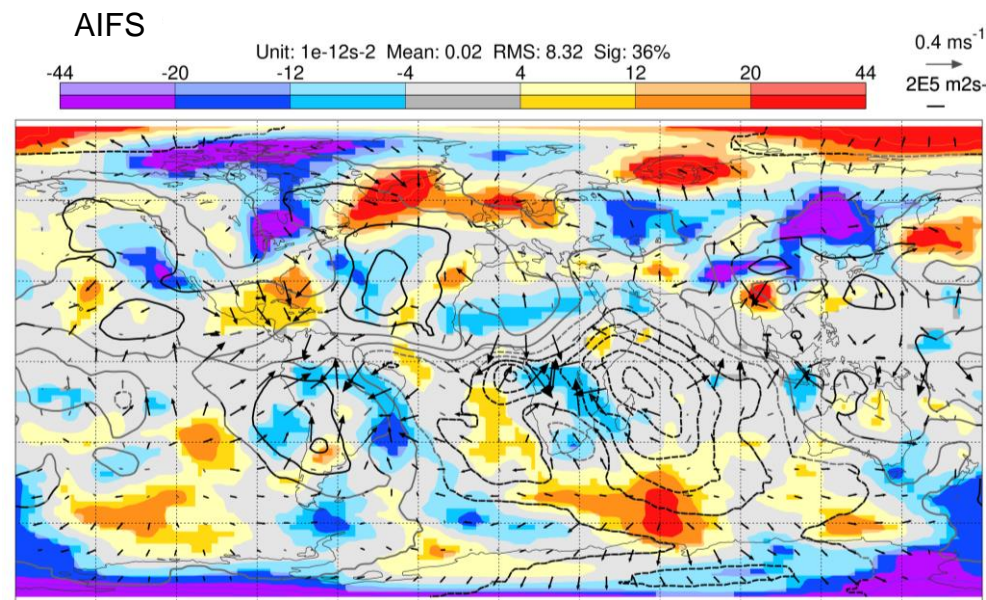
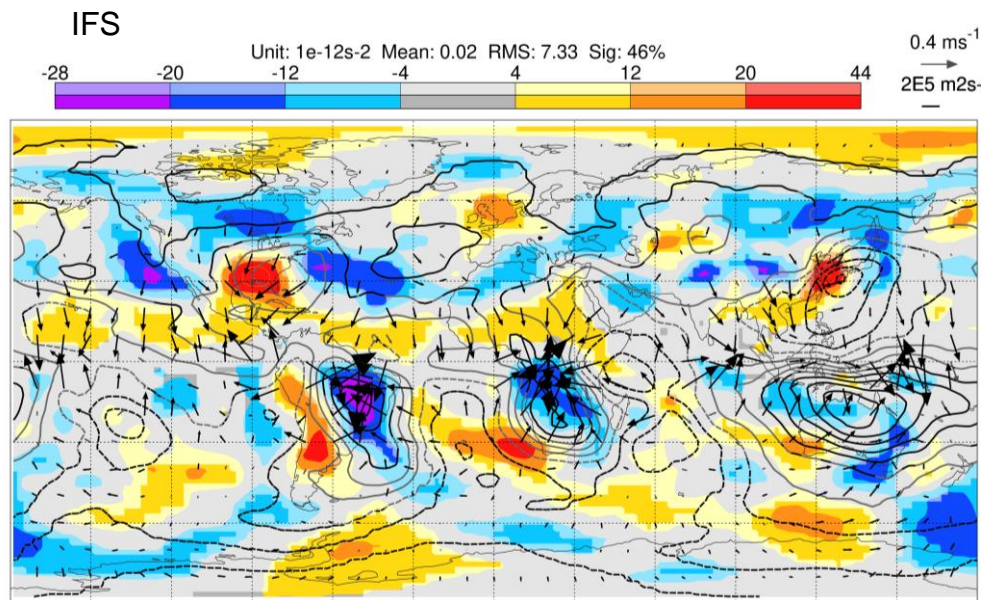
(Thin contours: mean absolute vorticity)

40-year mean JJA response to change in aerosol climatology deduced using seasonal-mean data. Anomalies integrated 100-300 hPa. Southern Hemisphere stationary Rossby wave pattern explains response seen in previous lecture

Upper tropospheric errors in IFS and AIFS (2024 DJF)

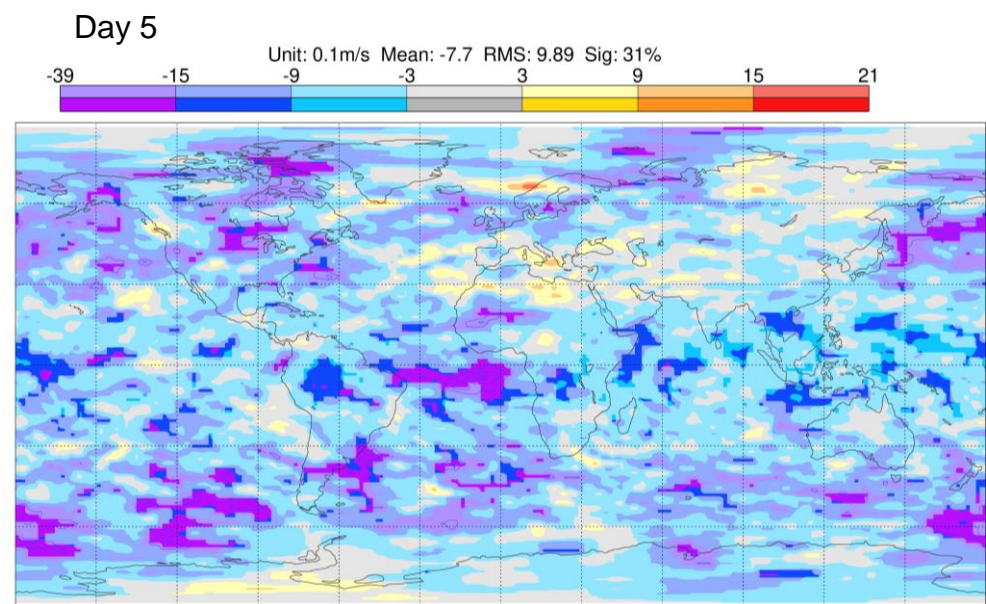
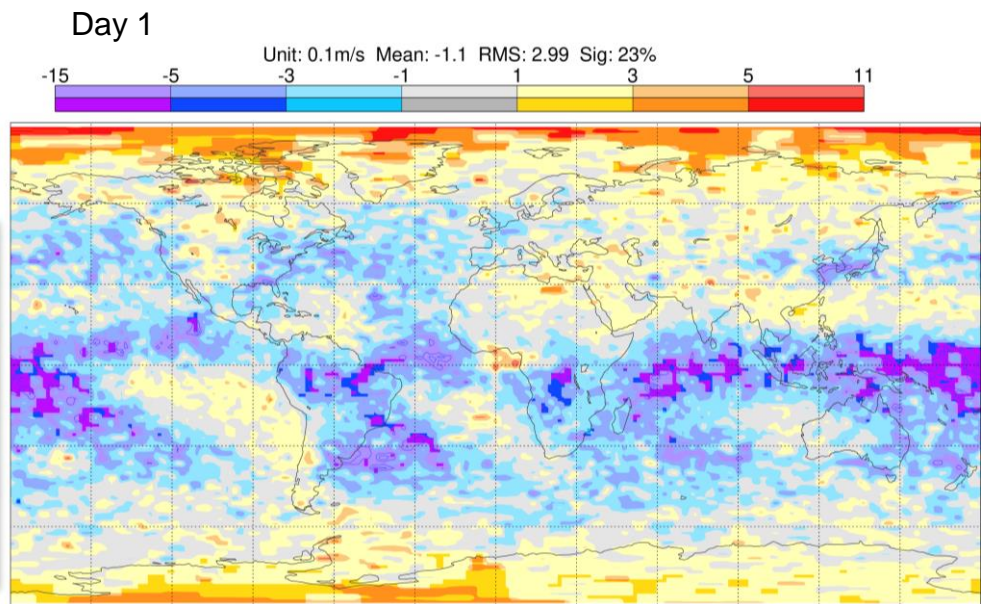
Day 1

Mean errors in streamfunction, divergent winds and Rossby wave source



AIFS-IFS

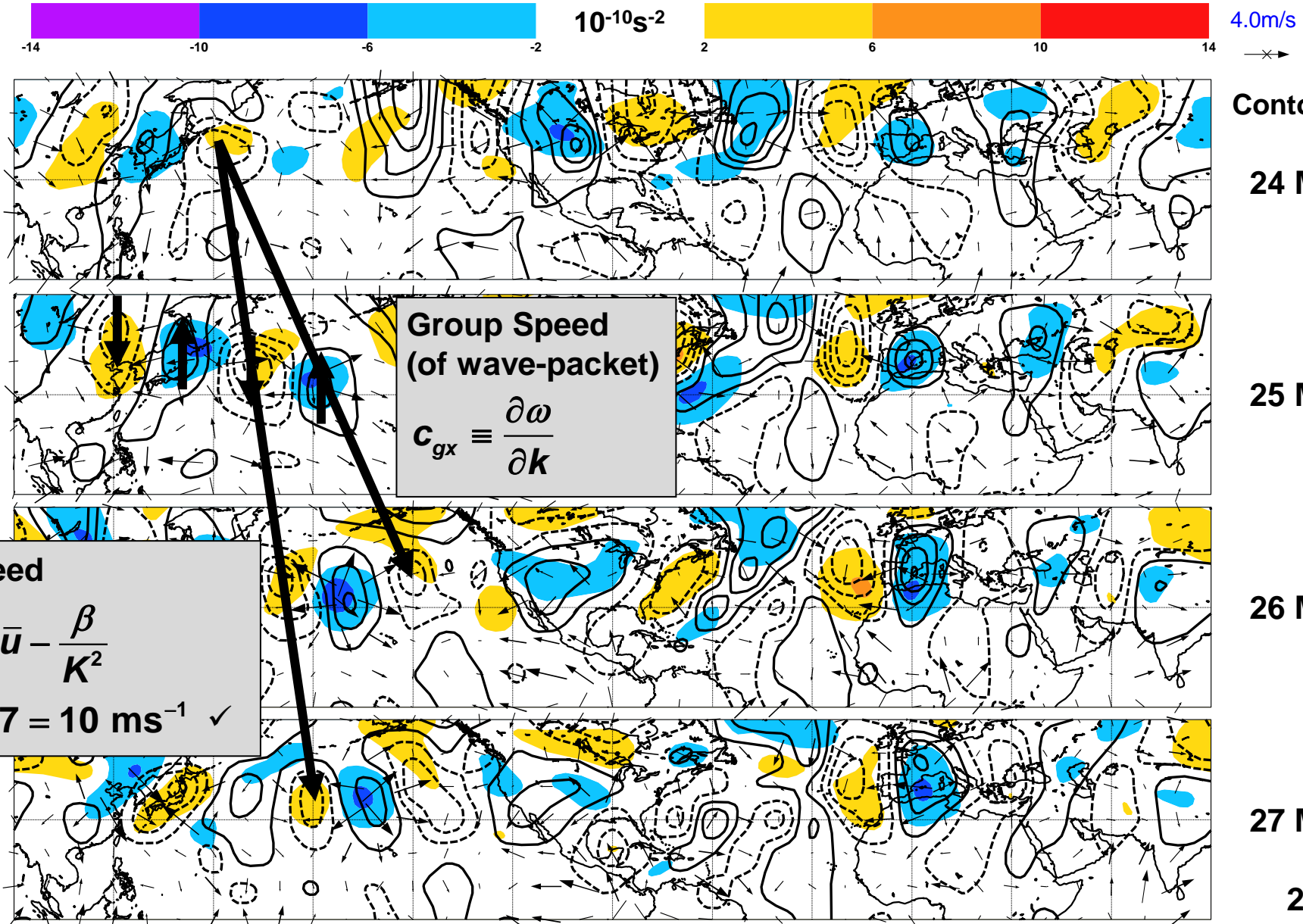
StDev in u250 errors



The Artificial Intelligence Forecasting System (AIFS) is trained to follow the 6 hourly analyses (ERA5). Does its predictive advantage come from the resulting reduction in (tropical) short-range error?

Extra-tropical Rossby waves

100–300 hPa
 $v_\psi, \underline{v}_\chi$, RWS



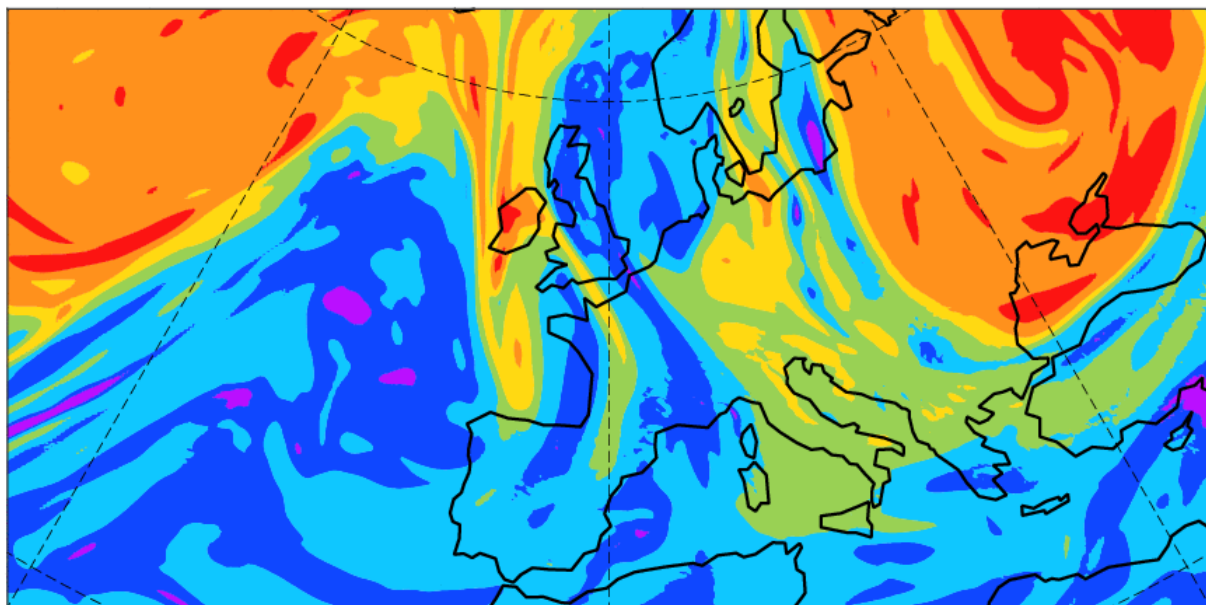
- Tropical forcing of midlatitude Rossby waves
- Predictability, reliability and sharpness

Animation of a very poor medium-range single forecast

Potential Vorticity on the Potential Temperature = 320K surface. 20110410 0 UTC. Step (days, hours) = 0 00.0

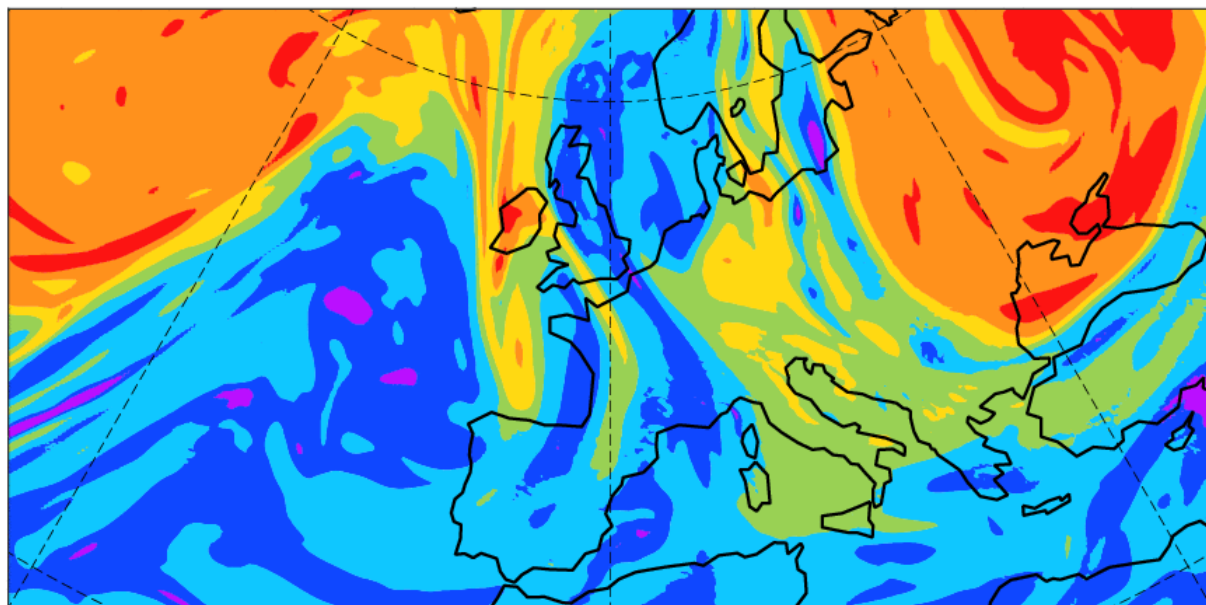
Observed

PVU



Forecast

PVU



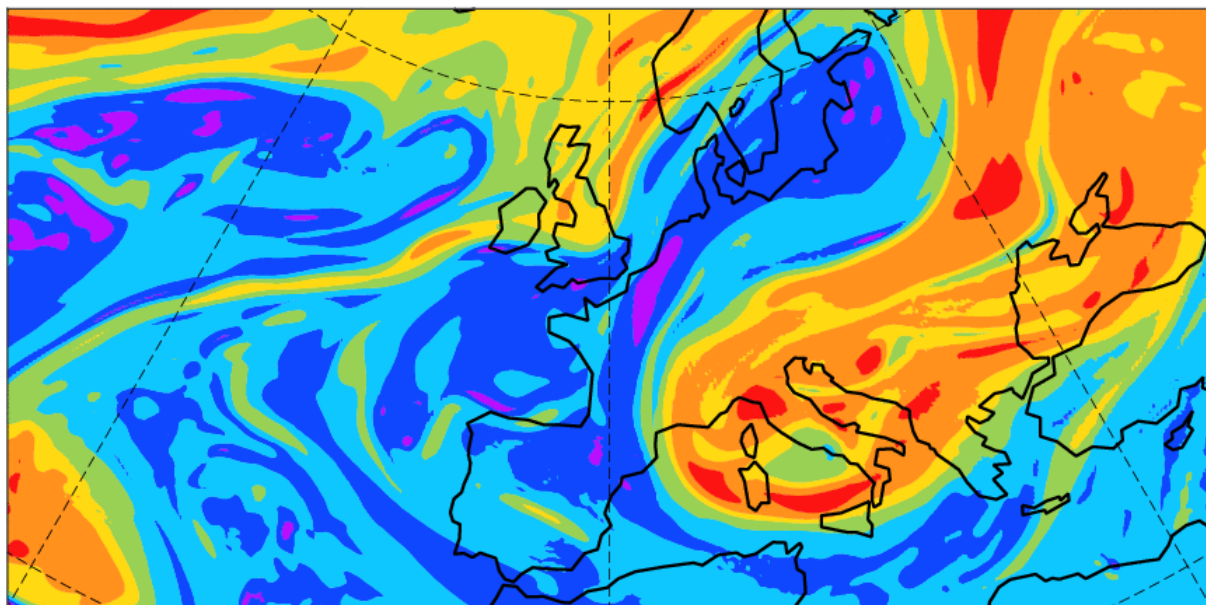
The field plotted is Potential Vorticity (PV). It indicates air masses, with blue being more tropical-tropospheric and red being more polar-stratospheric. PV has other useful properties (some mentioned in the notes)

Animation of a very poor medium-range single forecast

Potential Vorticity on the Potential Temperature = 320K surface. 20110410 0 UTC. Step (days, hours) = 6 00.0

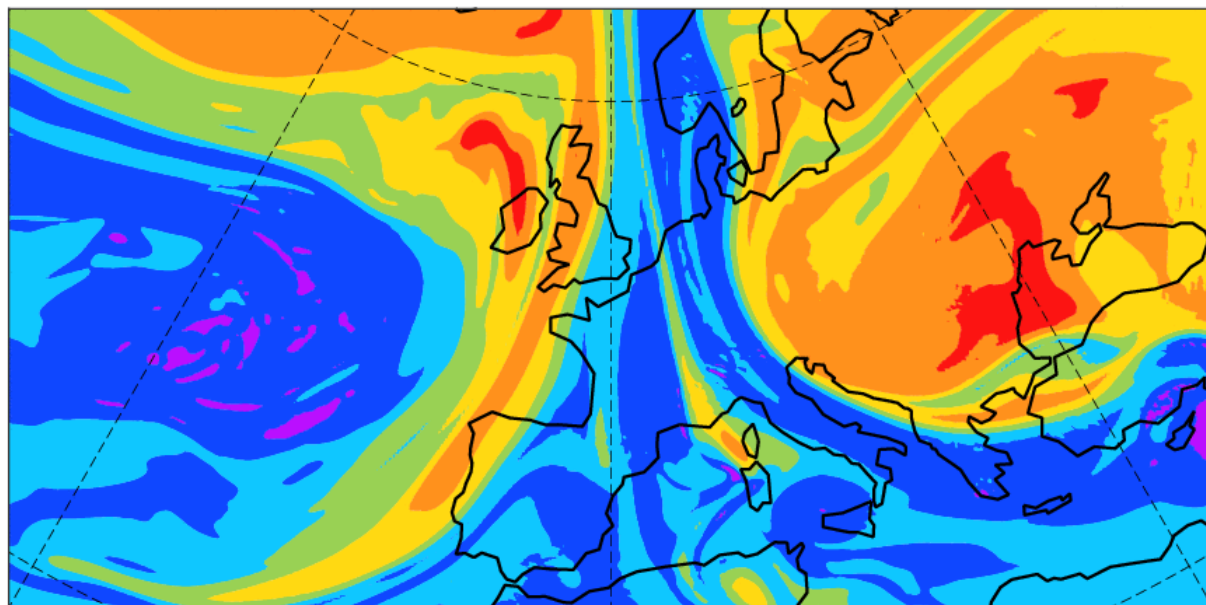
Observed

PVU

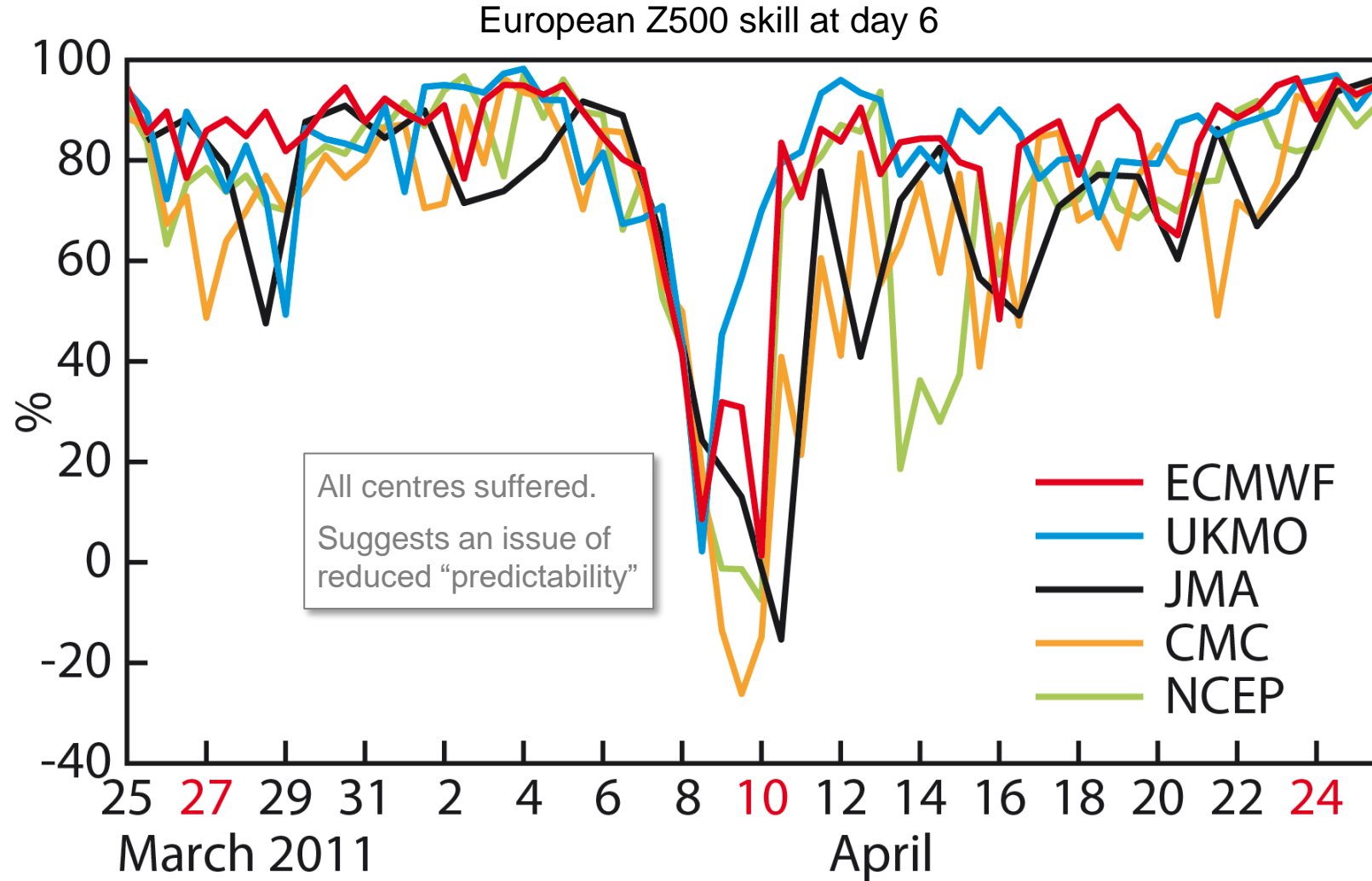


Forecast

PVU



We see the mixing of air masses. The eventual block (high pressure) over Northern Europe is not well predicted
With a single forecast, it is easy to quantify the error (pointwise differences, pattern correlations etc.)

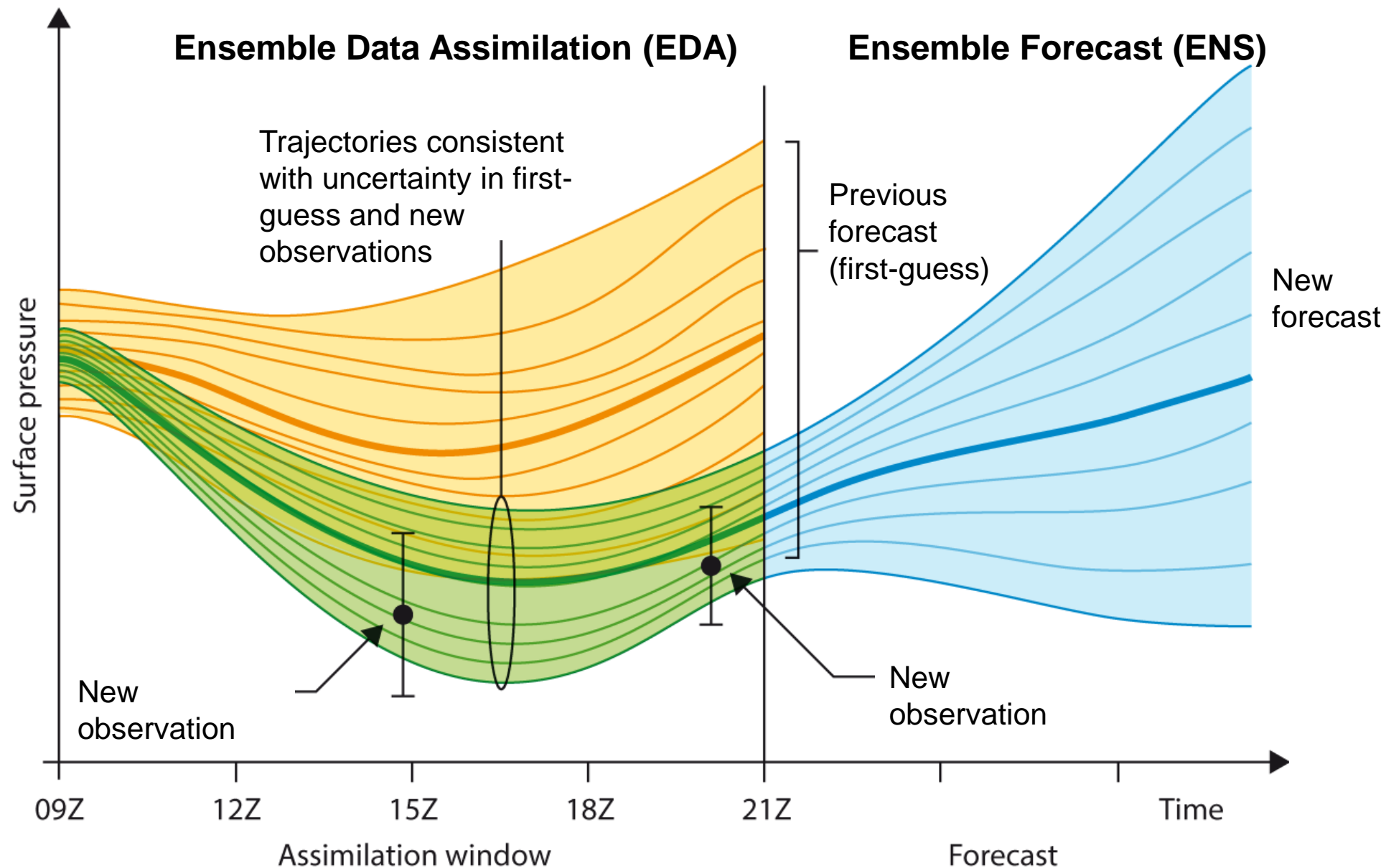


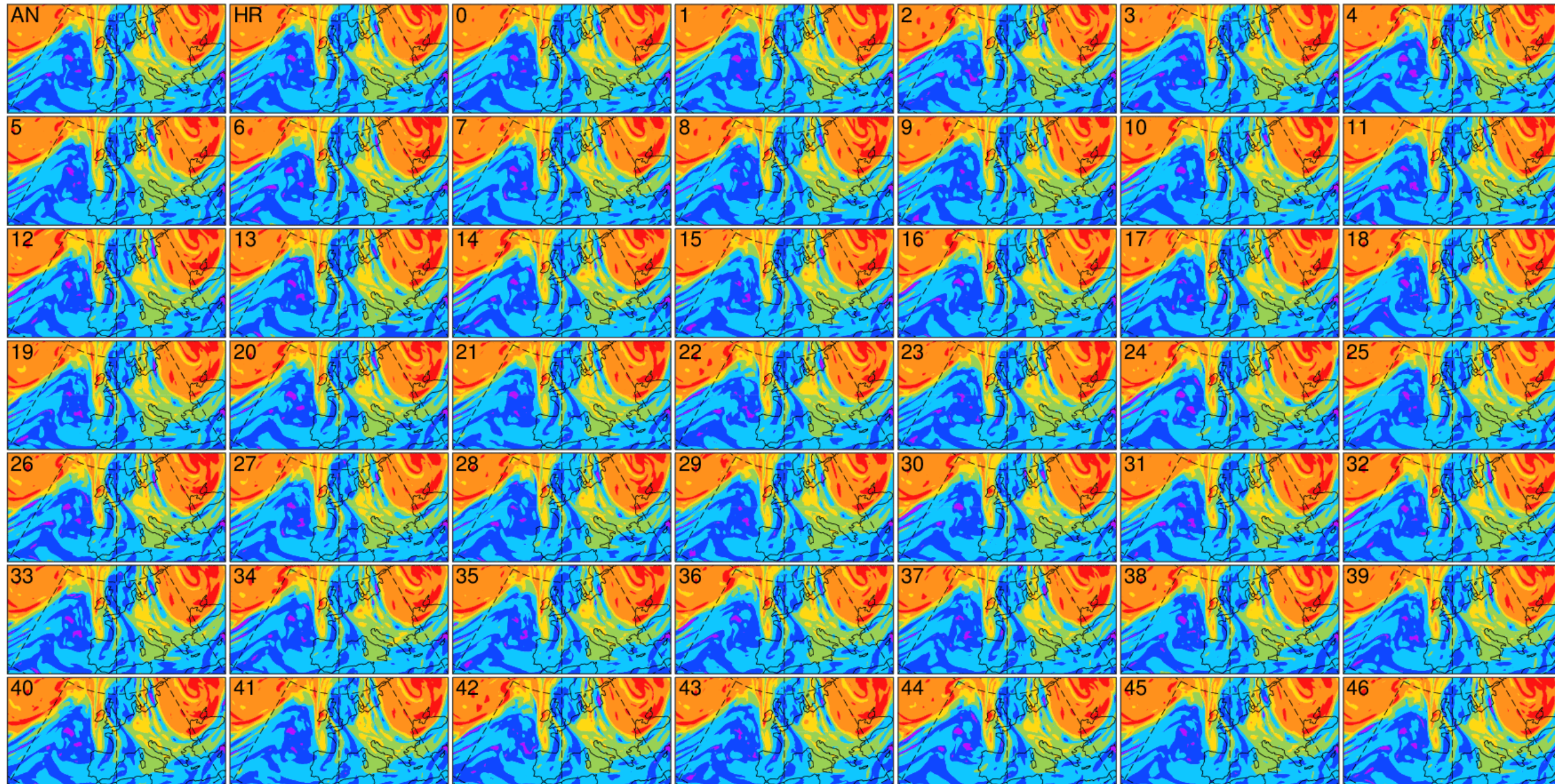
Spatial Anomaly Correlation Coefficient for 500 hPa geopotential height in [12.5°W–42.5°E, 35°N–75°N]. Date is forecast start

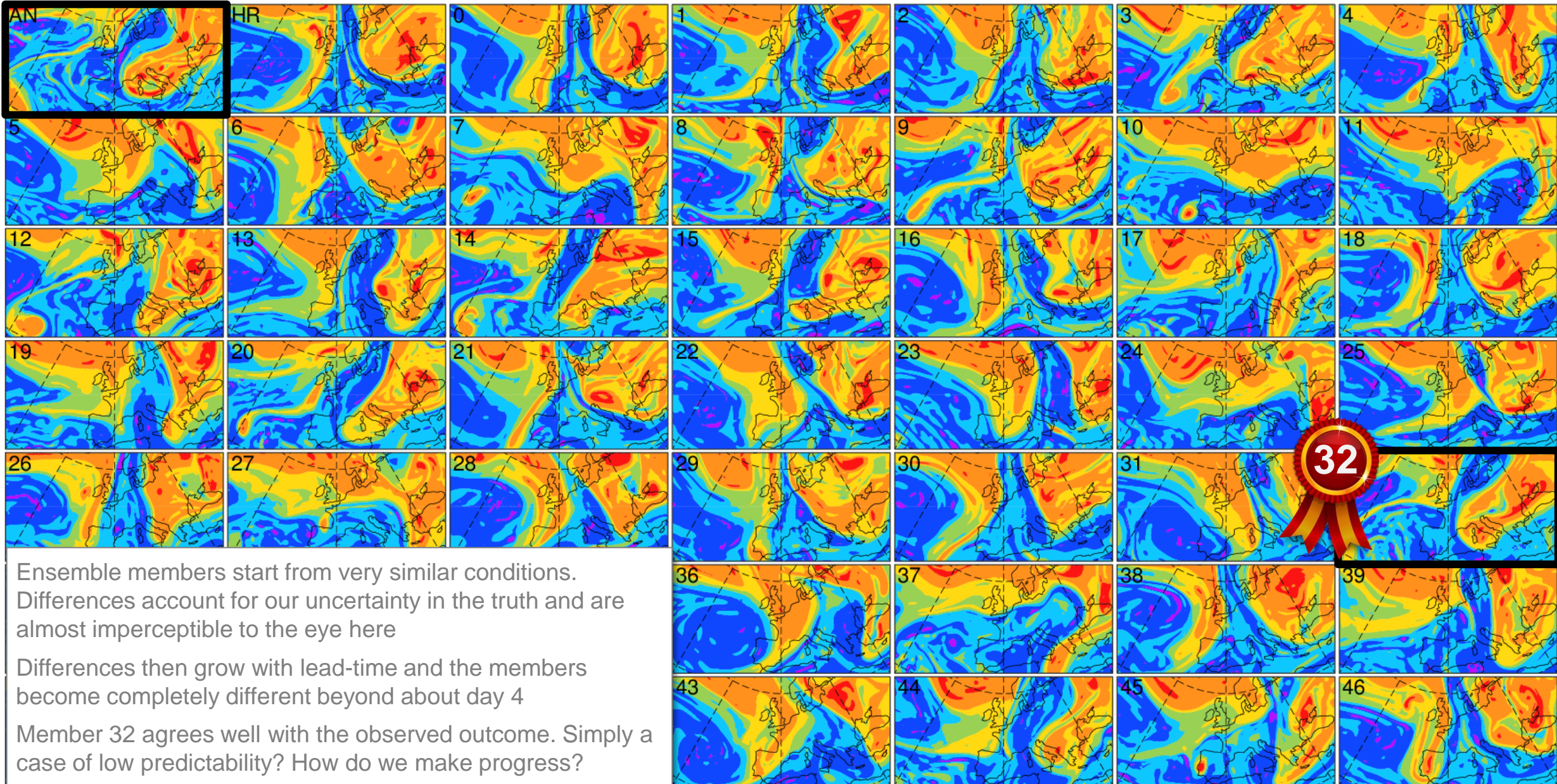
Traditional Ensemble Weather Prediction (ECMWF)

ECMWF global ensemble has 50 members and resolution ~9km. Millions of observations ingested each assimilation cycle.

ENS spread arises from chaotic growth of EDA uncertainty, model uncertainty and singular vector perturbations



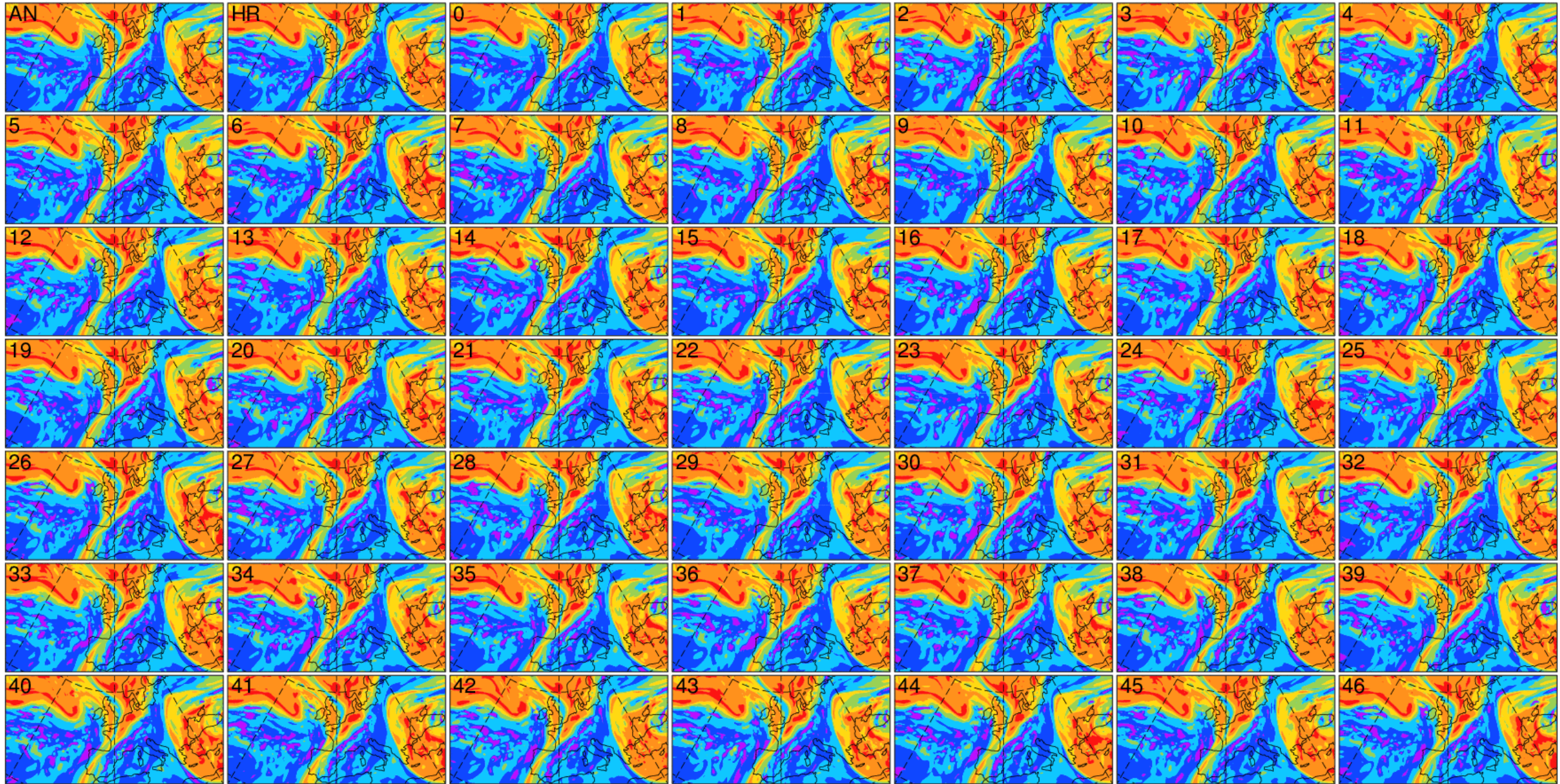


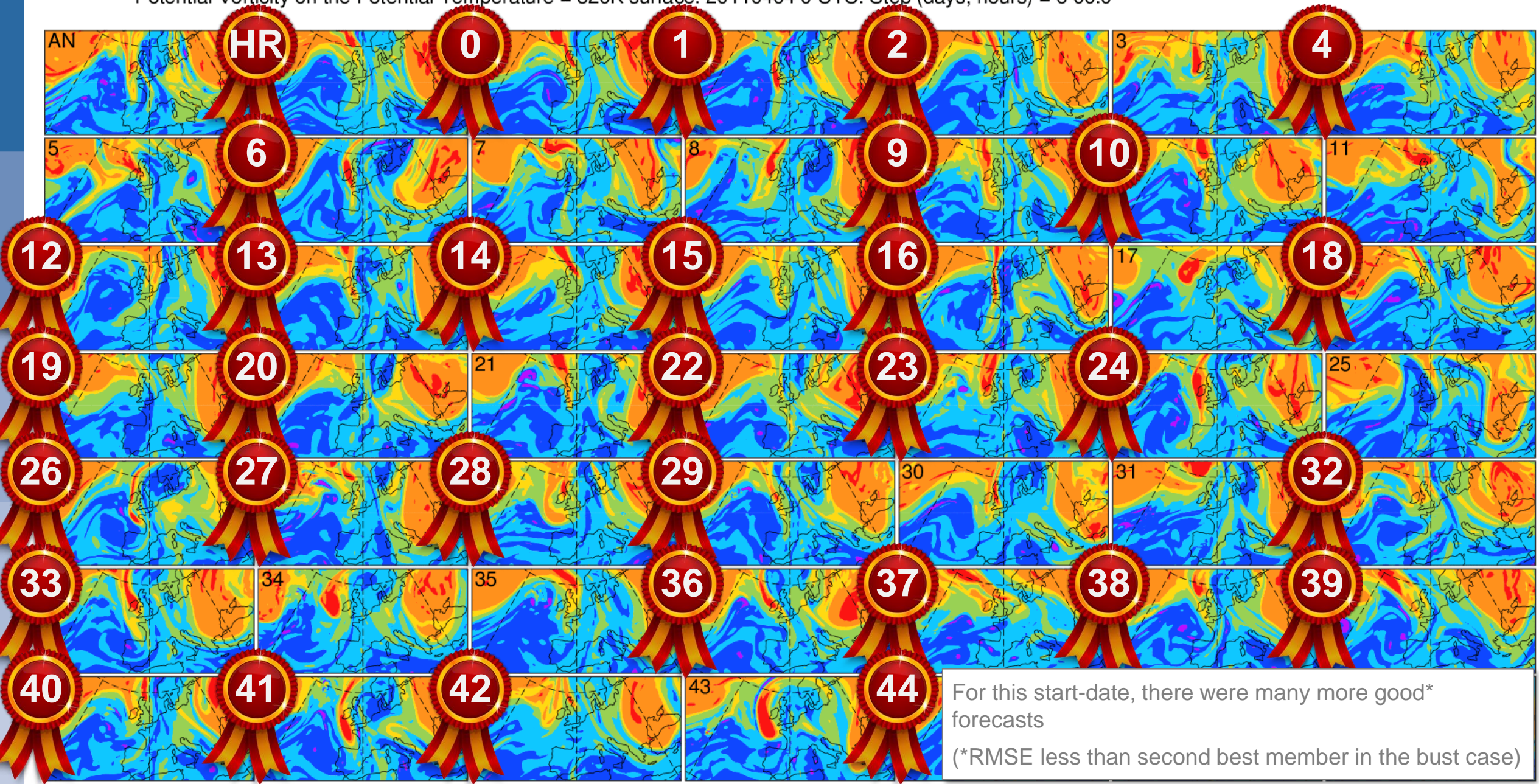


Ensemble members start from very similar conditions. Differences account for our uncertainty in the truth and are almost imperceptible to the eye here

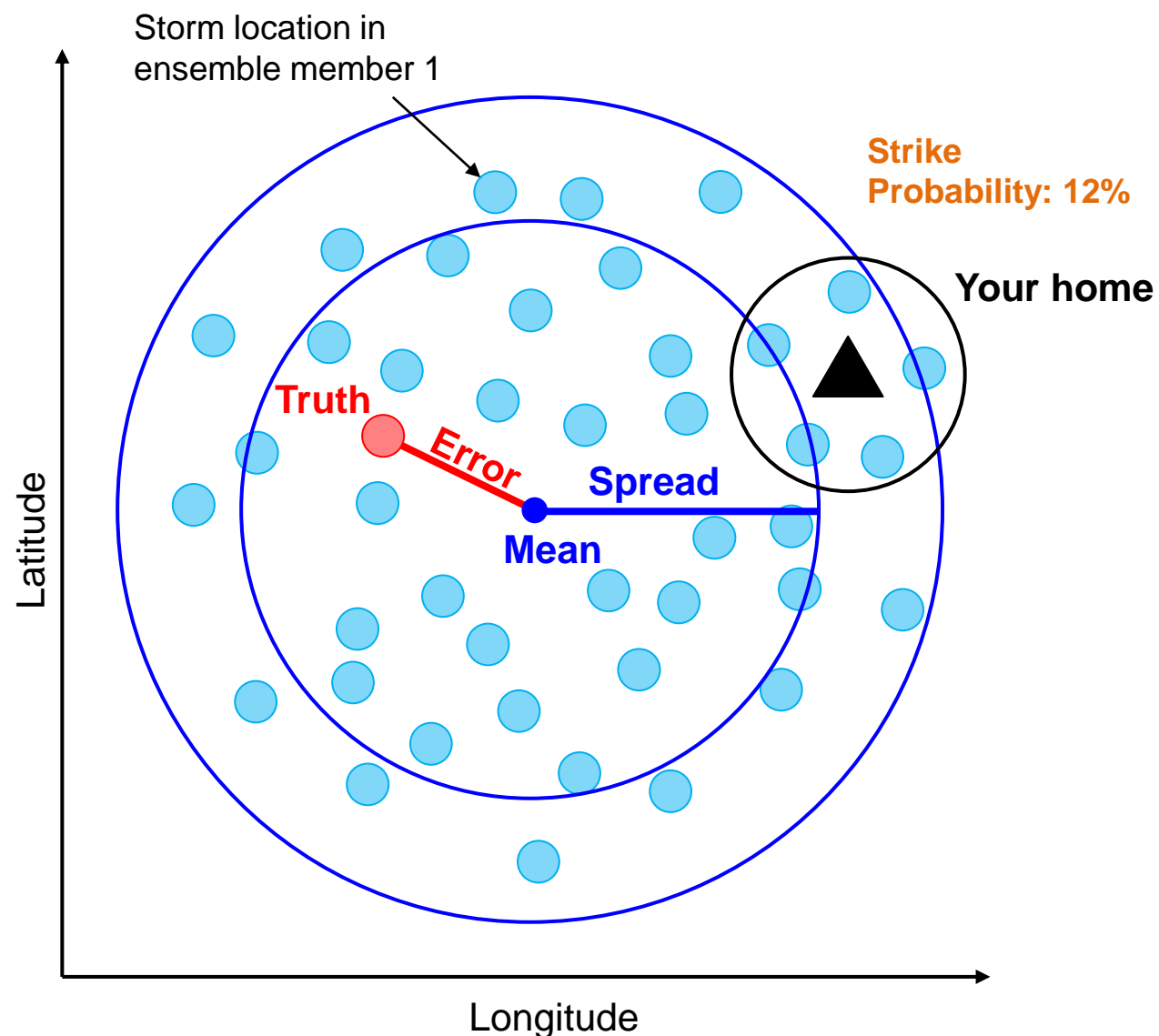
Differences then grow with lead-time and the members become completely different beyond about day 4

Member 32 agrees well with the observed outcome. Simply a case of low predictability? How do we make progress?





The aims of ensemble forecast system development



Aim 1

Improve the forecast model so that the truth* is statistically indistinguishable from any ensemble member (**Reliability**) \Rightarrow Unbiased decisions and Error should match Spread, *on average*

* We can take account of our uncertainty in the truth

Aim 2

Reduce uncertainty in the ensemble initial conditions to decrease forecast Spread** (**Sharpness**) while maintaining Reliability

** Chaos can imply an ultimate limit to the lead-time for which Spread can be reduced to a useful level

Caution!

Many cases are required to determine reliability. This needs to be assessed and improved in a flow-dependent sense

Ensemble spread and error

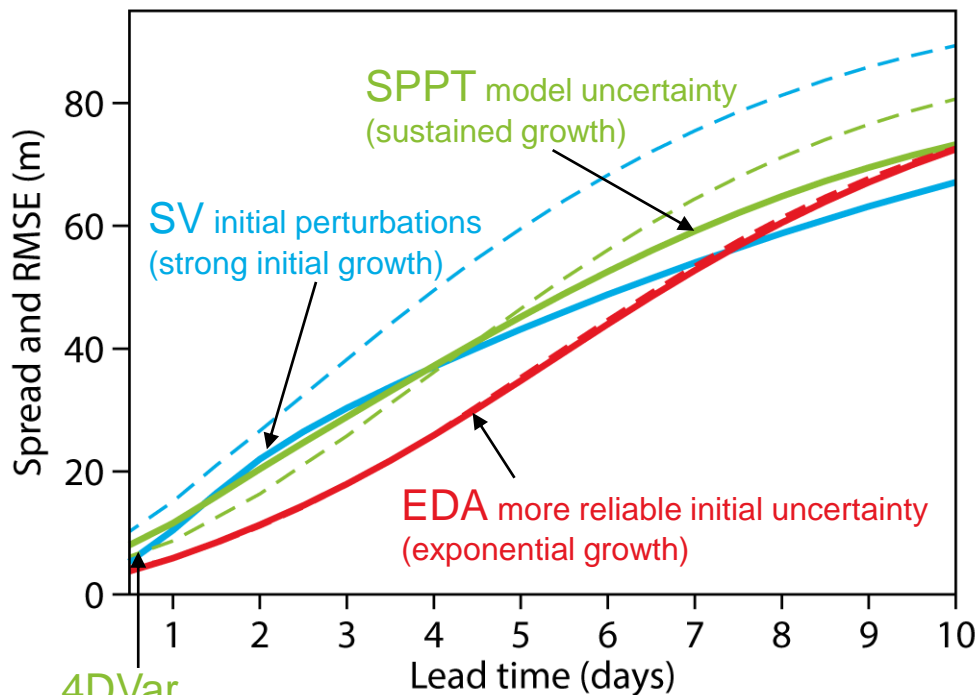
Z500

Rodwell et al. 2018, BAMS

Overall Error and Spread have reduced and come into alignment; due to better observations, initial conditions, forecast model and better representation of uncertainty

...but we make ensemble forecasts to represent the day-to-day variations in predictability and uncertainty. Can we evaluate it in our forecasts?

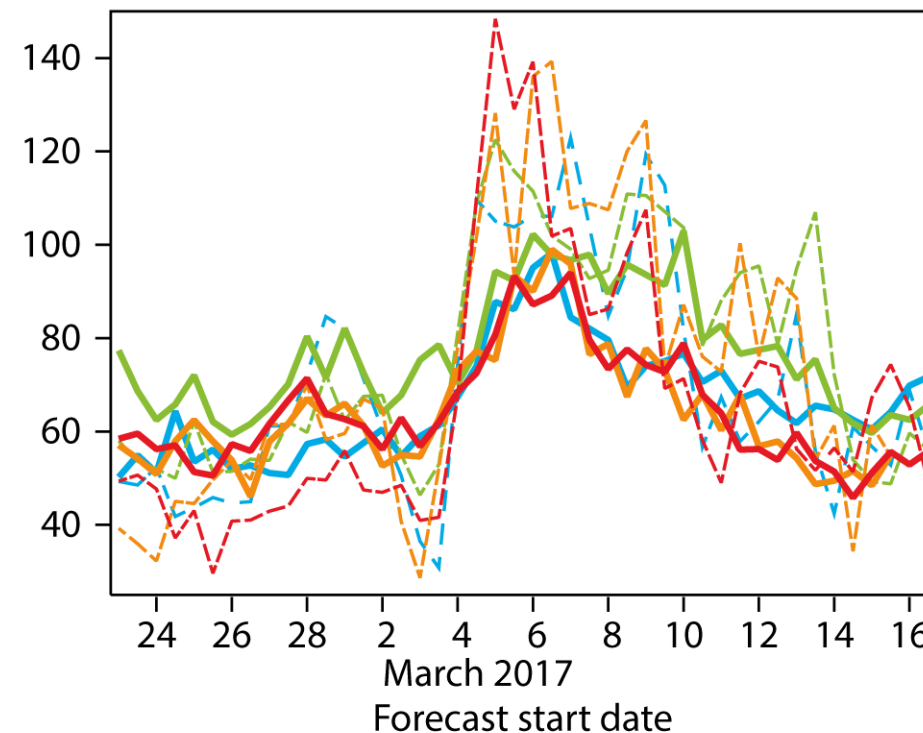
Annual means N.Hem. (ECMWF)



4DVar
reduced initial error

	1996	2005	2014
Spread			
Error			

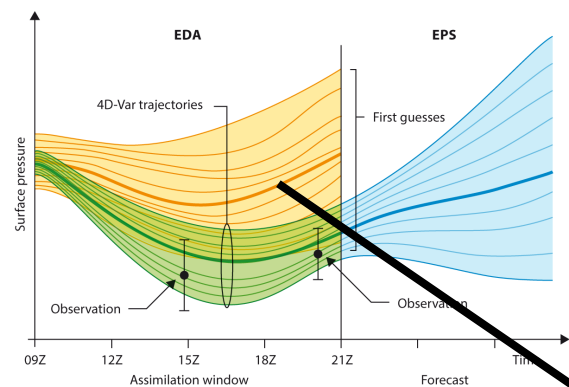
Timeseries for Europe at D+6 (TIGGE)



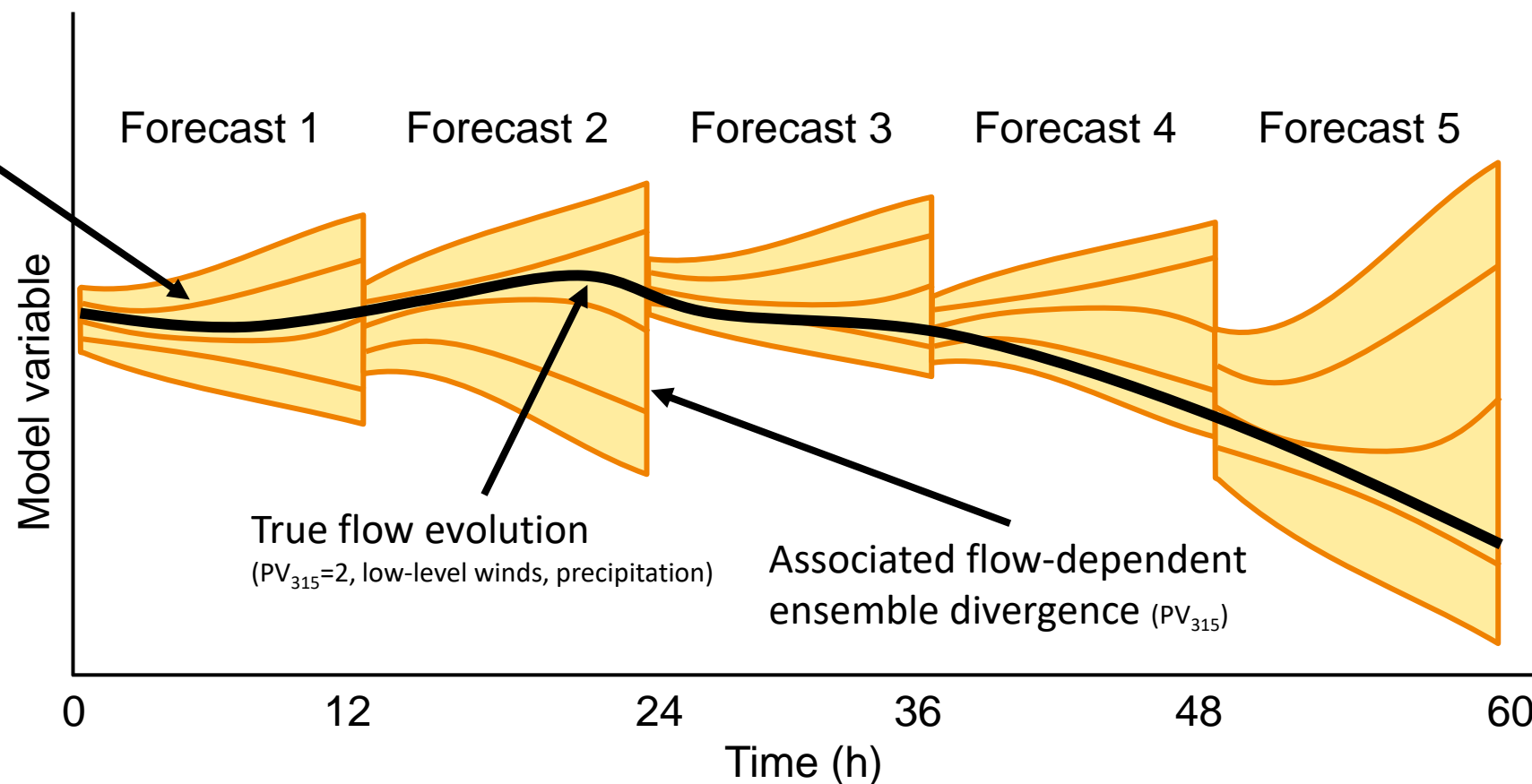
	ECMWF	UKMO	JMA	NCEP
Spread				
Error				

500 hPa geopotential height (Z500). "Error" is RMS of ensemble-mean error
Spread = ensemble standard deviation (scaled to take account of finite ensemble size)

Animating the true evolution of the flow and associated ensemble divergence



Can animate the shadow trajectory and super-impose uncertainty growth-rates – Focus on synoptic scales as these contribute most to initial growth



Animation of analysed circulation and corresponding EDA background divergence

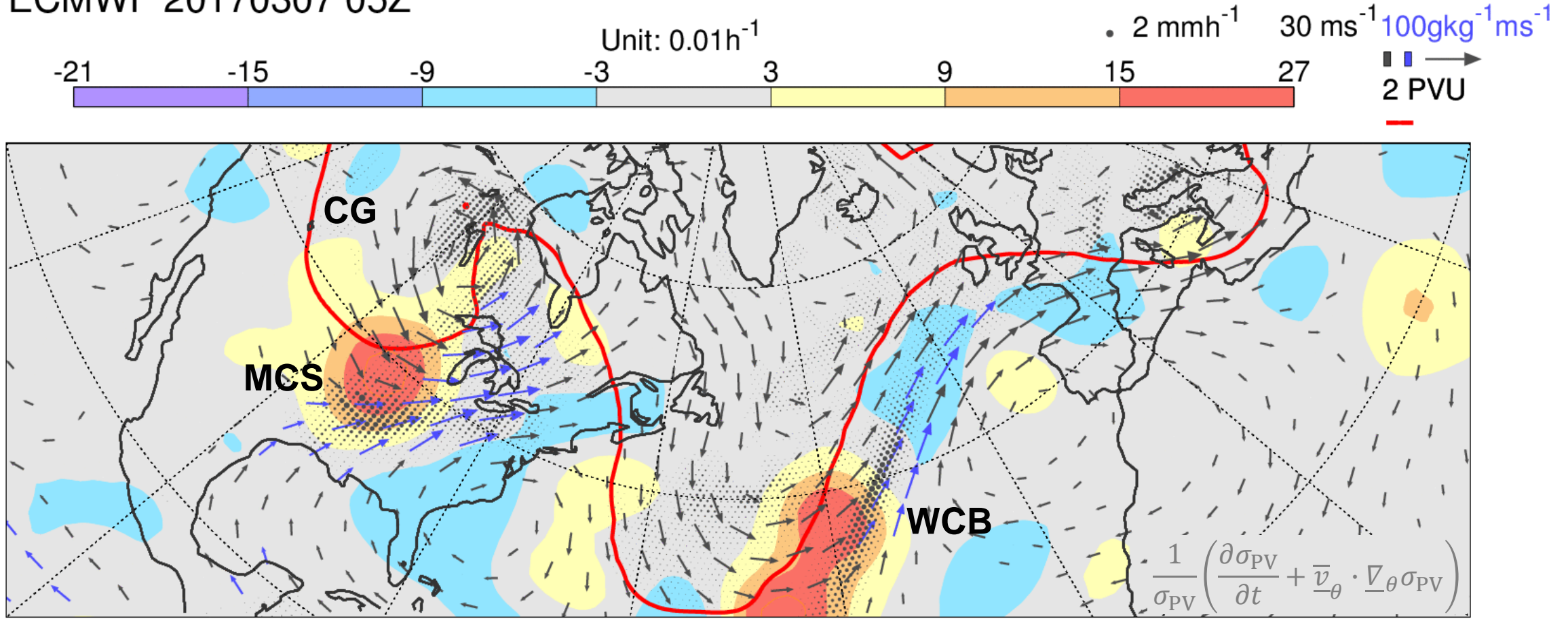
Much uncertainty growth associated with moist processes: **Warm Conveyor-Belts**, and **Meso-Scale Convection**

Interaction of uncertain features, large ENS spread & poor prediction of Euro blocking at D+6

Aim: Evaluate short-range synoptic flow-dependent representation of uncertainty

Is sensitivity to moist processes real or due to deficiencies in model uncertainty representation?

ECMWF 20170307 05Z



Control forecast $PV_{315}=2$, \underline{v}_{850} and $q|\underline{v}|_{850}$, ensemble-mean precipitation. Growth-rate of $\sigma_{PV_{315}}$. Synoptic filter: 1d, T21. Rodwell, Richardson, Parsons and Wernli (2018)

EDA reliability in u_{200} against aircraft observations in MCS situations

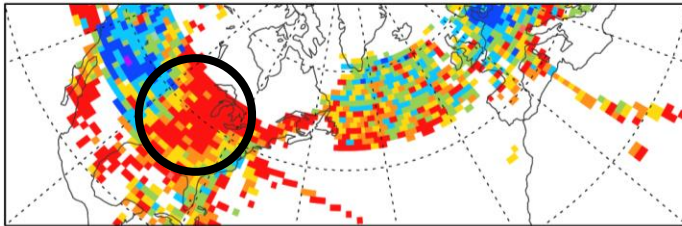
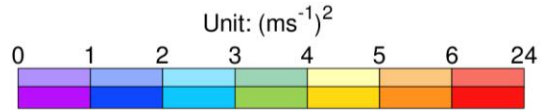
Rodwell et al. 2018, BAMS

$$\text{Departure}^2 = \text{Spread}^2 + \text{ObsErr}^2 (+ \text{Bias}^2 + \text{Residual})$$

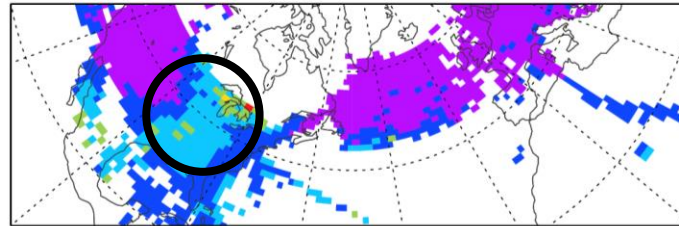
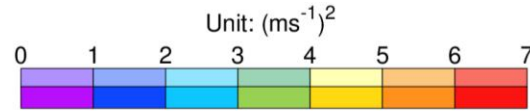
54 cases, 12h window

For more operational diagnostics, see the [Diagnostics Explorer](#)

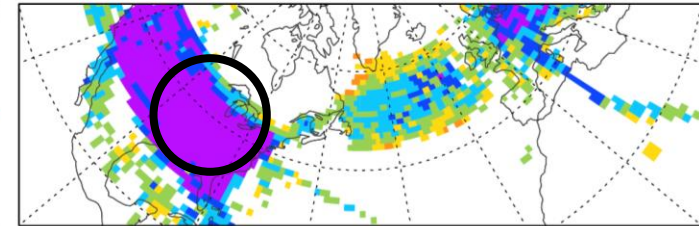
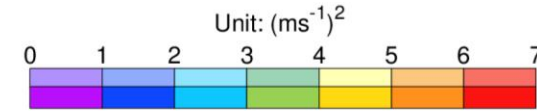
Departure²



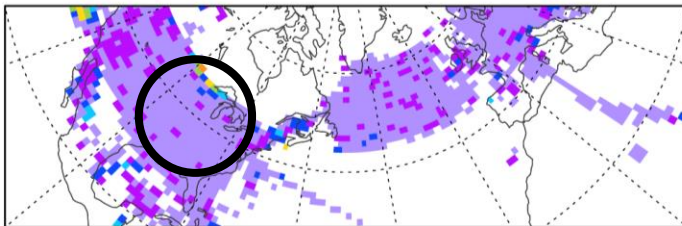
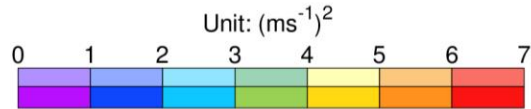
Spread²



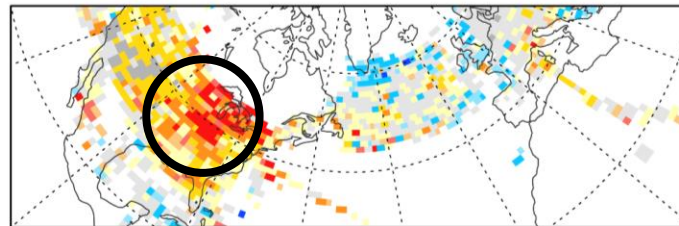
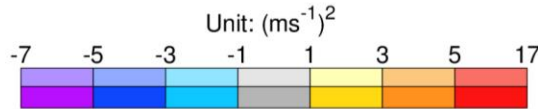
ObsErr²



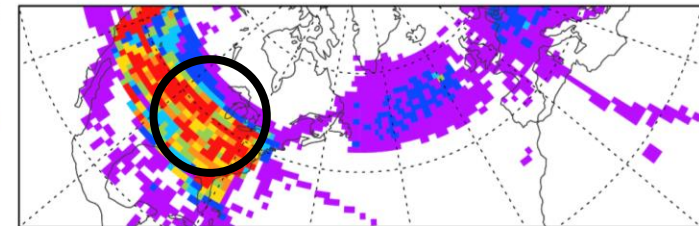
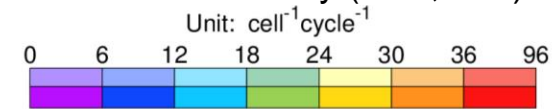
Bias²



Residual



Observation density (O80, 12h)

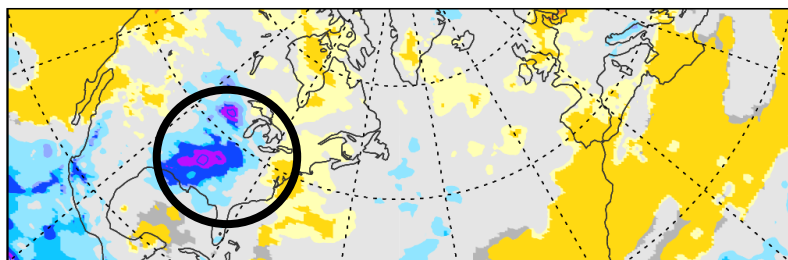
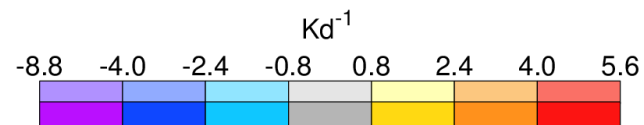


Enhanced spread (Background variance) in Great Lakes / Mississippi River region
Even larger Departures² of the ensemble-mean from the observations ensue
Bias²≈0 (important for reliability), but Residual ≫ 0 indicates insufficient Background variance

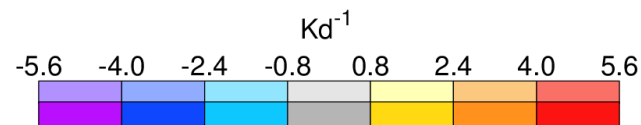
Uncertain forecasts for Europe may still be over-confident

EDA unperturbed initial tendency budget for T300 in MCS situations

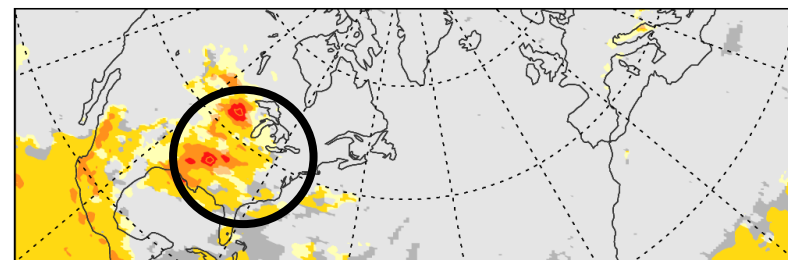
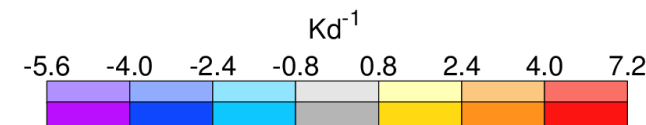
(a) Dynamics



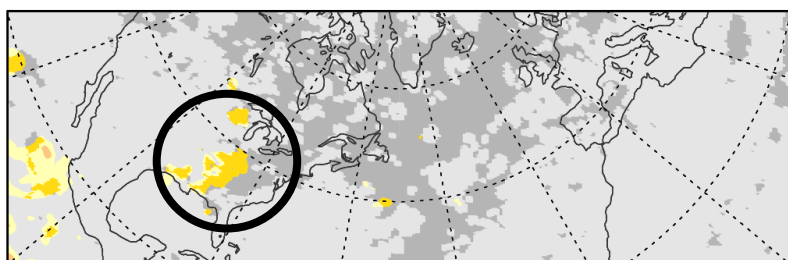
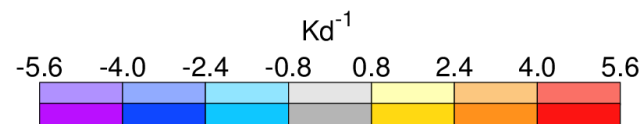
(b) Radiation



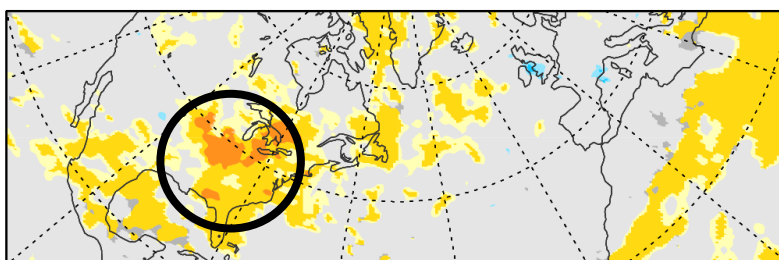
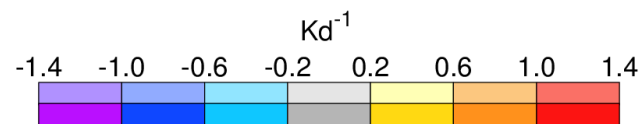
(c) Convection



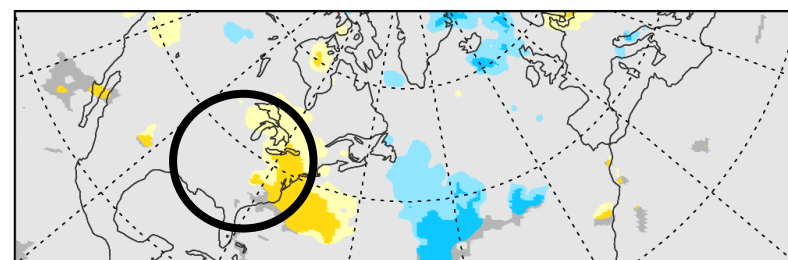
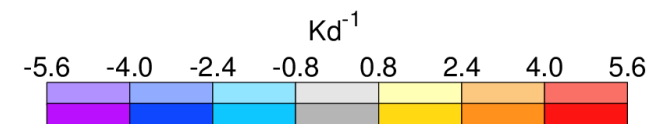
(d) Cloud



(e) Increment



(f) Evolution



Budget: **Evolution = Dynamics + Radiation + Convection + Cloud micro-physics + analysis Increment**


54 cases, 12h window

Shows how the model represents dynamics and physics of MCS

Positive (and statistically significant) increment suggests that the background forecast is too cold near the top of the convection

The Jetstream and mesoscale convection: “The piano string and hammer”

54 cases

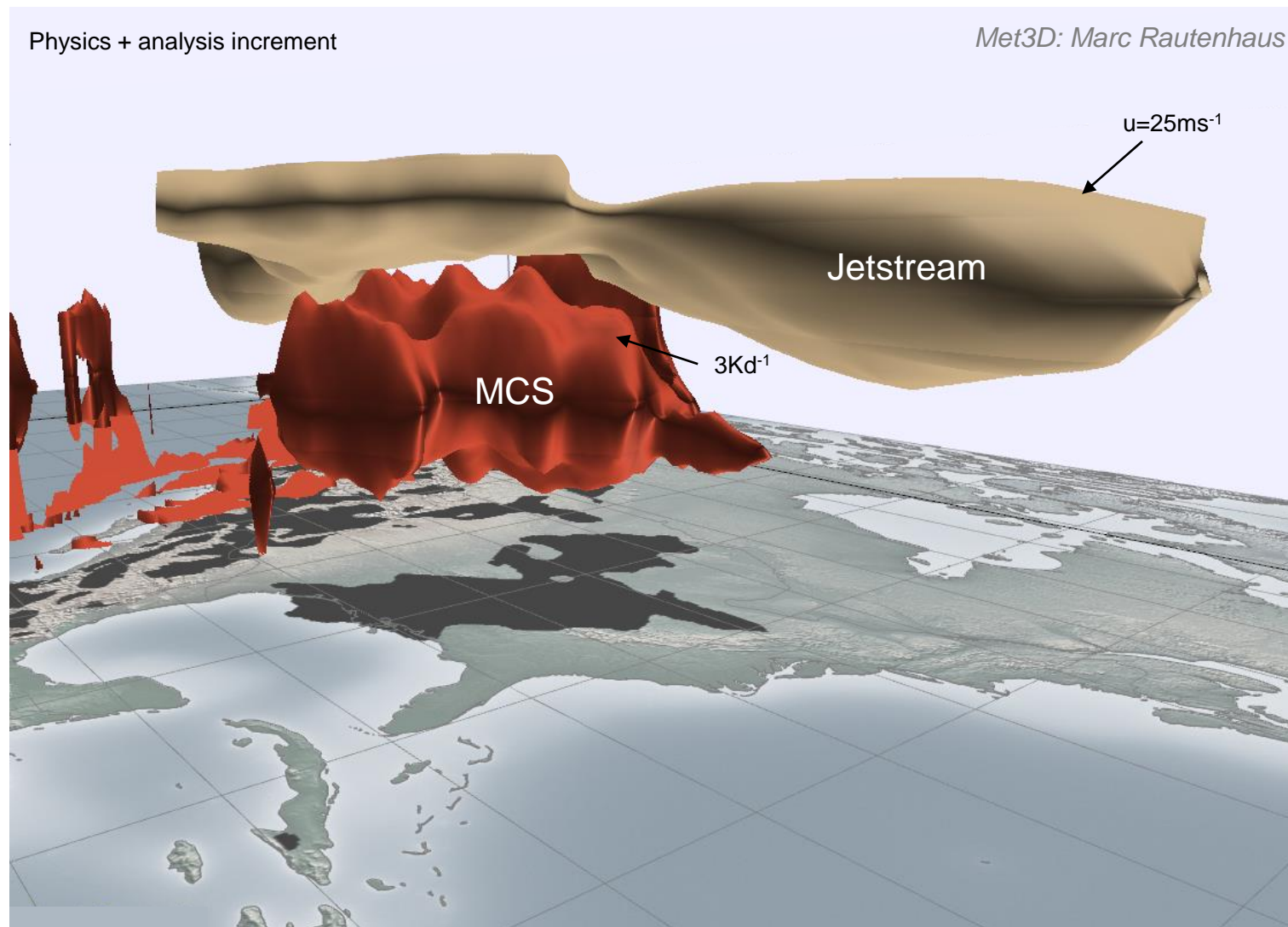


If we don't hit the string hard enough, the wave in the string will be too weak

If we hit the string at the wrong time, the wave will arrive over Europe at the wrong time

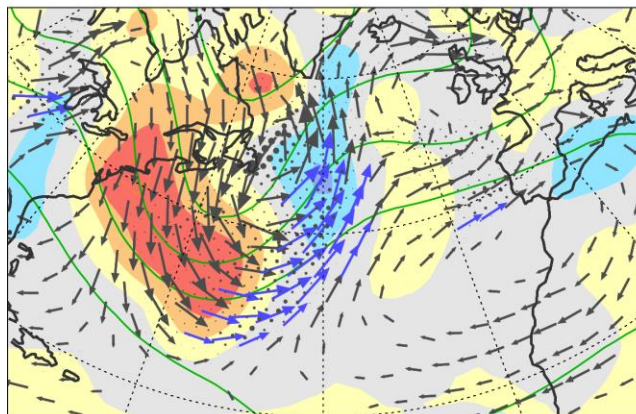
We do not know when to press the key (mesoscale convection itself involves chaotic uncertainty)

What we want is that the ensemble members generate such convection with the “right” uncertainty

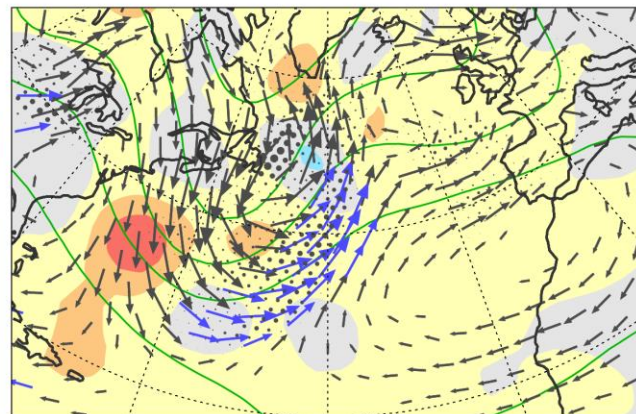


Animation of TIGGE models is a concatenation of 12h forecasts

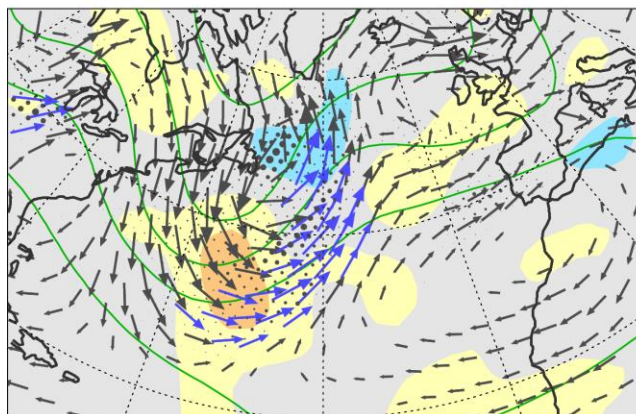
(a) ECMWF 20200118 00Z (IFS)



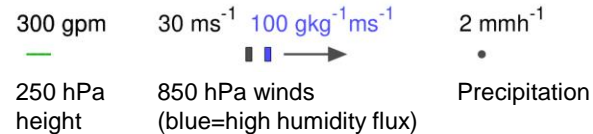
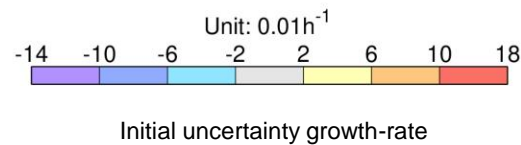
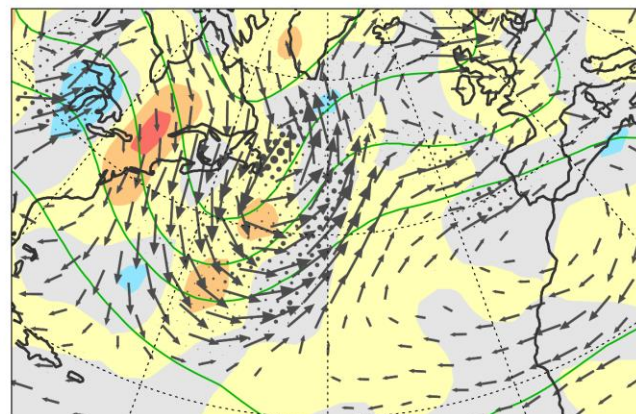
(b) JMA 20200118 00Z (GEPS)



(c) NCEP 20200118 00Z (GEFS)

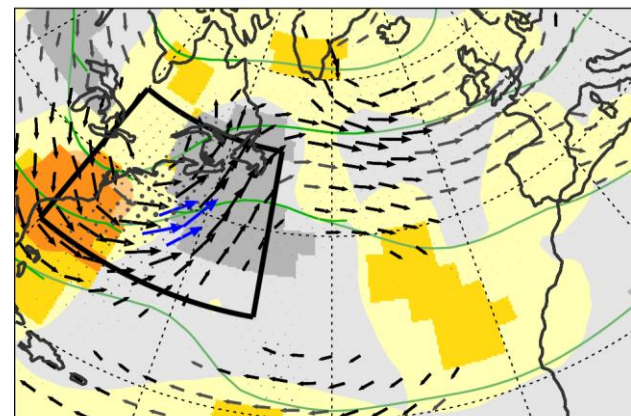


(d) UKMO 20200118 00Z (UM)



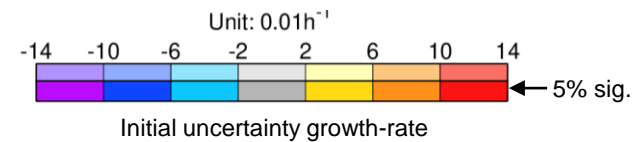
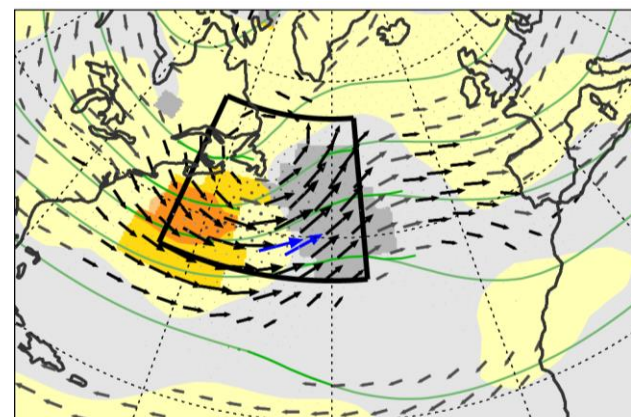
Clustering to identify cyclogenesis events

Clustering region 1 (32 events)

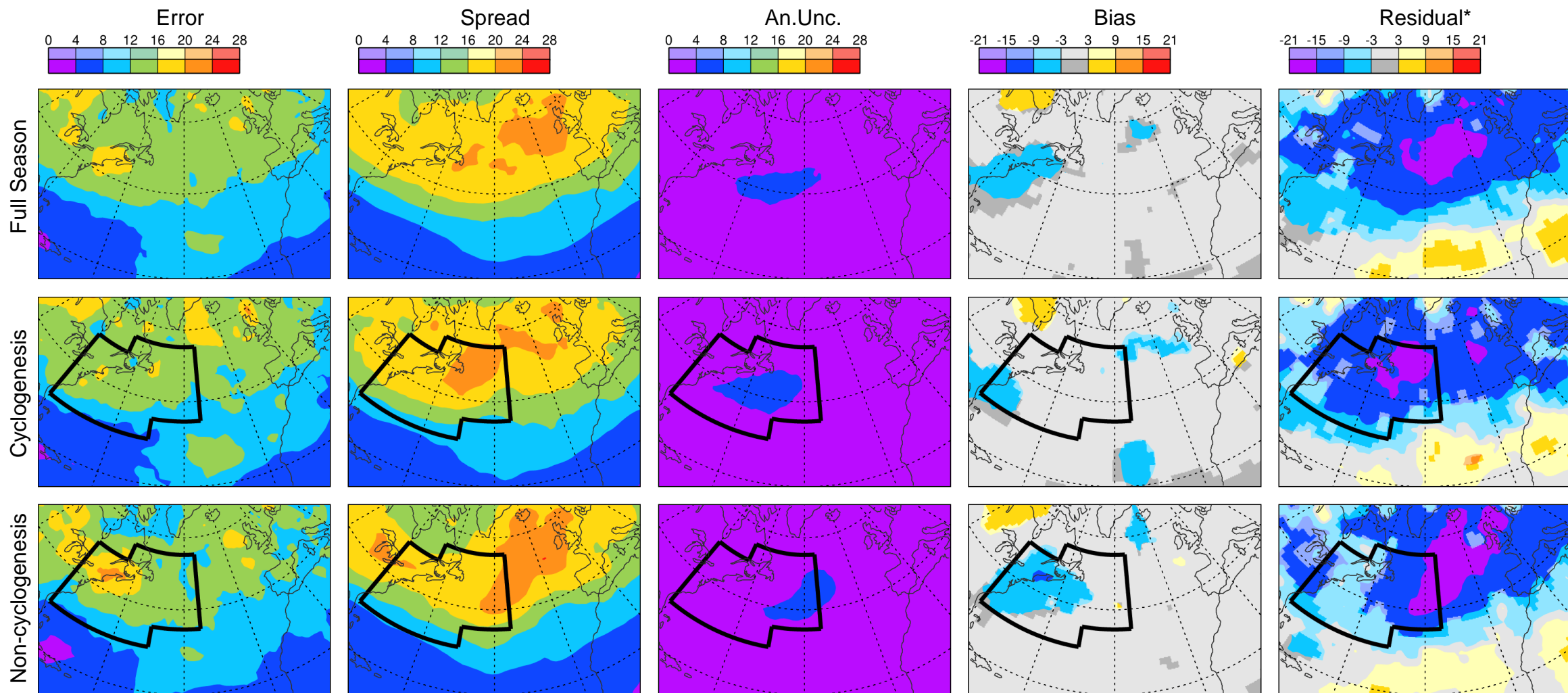


K-means clustering on analyzed Z250, u850, v850, and ensemble-mean 12h precipitation during DJF 2020/21 (not on growth-rate)

Clustering region 2 (+59 events)



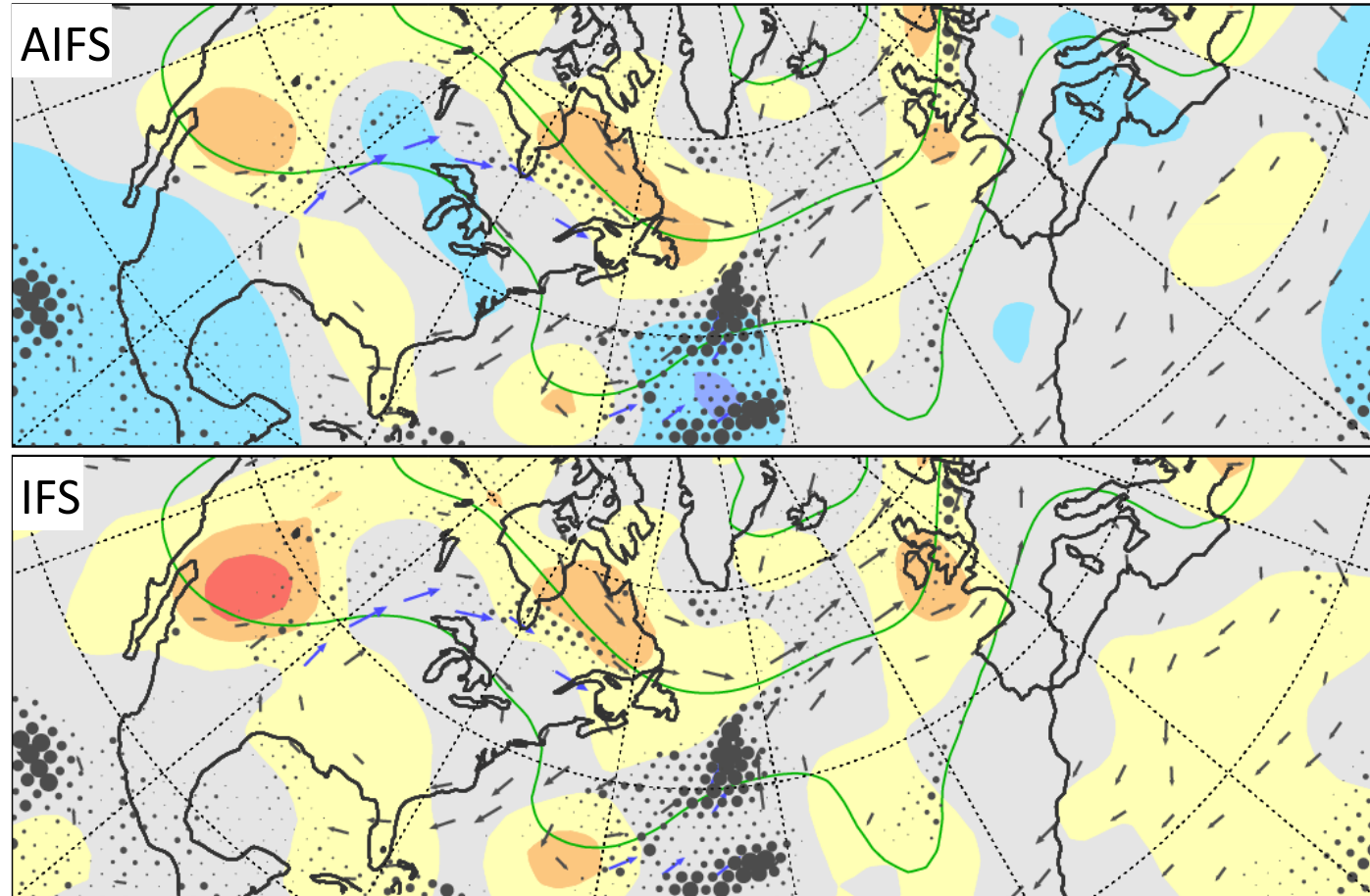
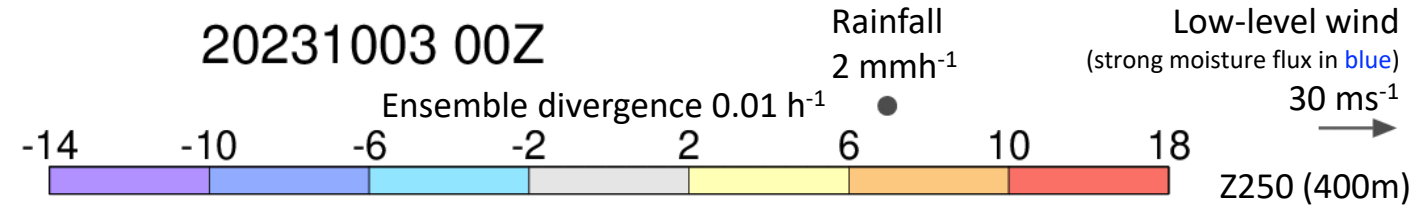
Reliability assessment at Day 2 (Z250 DJF 2020/21)



Full Season negative Residual indicates that ensemble is over-spread in the stormtrack
 Partitioning into cases of cyclogenesis / non-cyclogenesis in indicated region shows that the overspread is associated with cyclogenesis

DJF 2020/21 Z250 (m). Shown are the square-roots of the terms in the ensemble reliability budget. $Residual^* = SQRT(|R|)SGN(R)$

Uncertainty growth-rates in 12h forecasts of AIFS and IFS ensembles (Z250)



A glimpse of the future?:

The ECMWF 'AIFS' (Artificial-intelligence IFS) displays similar the patterns of synoptic-scale uncertainty growth to the IFS.

Magnitudes are slightly less, possibly because the AIFS does not include model uncertainty yet.

Does spatial agreement of growth-rates between AIFS and IFS reinforce confidence in both systems?

Uncertainty growth rates from the AIFS and IFS. Both animations show the same circulation and precipitation features, which are based on the operational analysis

- Tropical forcing of midlatitude Rossby waves
 - Extended range predictability
- Predictability, reliability and sharpness
 - Uncertainty growth-rates for different synoptic flow-types
 - IFS uncertainty growth: Too much for baroclinic situations, too little for convective situations
 - Flow-dependent reliability as a path to more skilful ensemble forecasts