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On Numerical Coupling Errors in the Atmosphere–Ocean–Sea Ice System

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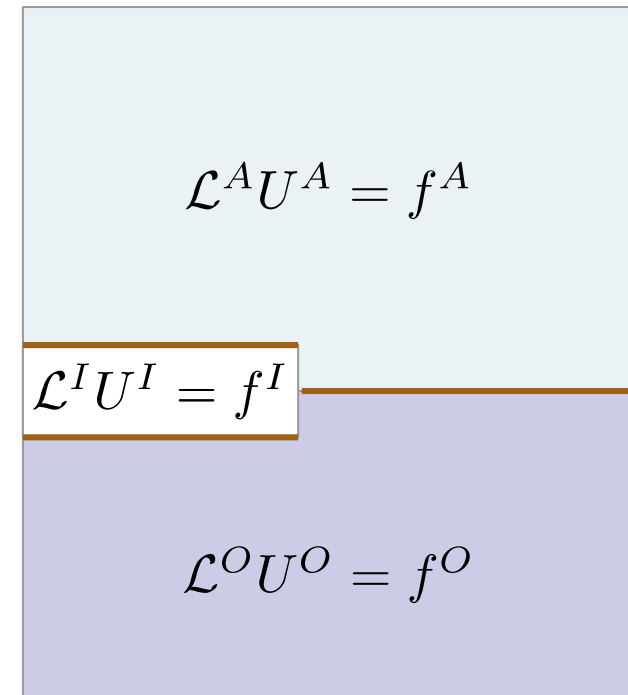
I want to make three cases...

1. ... for iterative coupling as a model development tool
2. ... against discontinuous physics parameterizations
3. ... for revisiting atmosphere–ocean–sea ice coupling

Our perspective:

ESMs solve a coupled problem

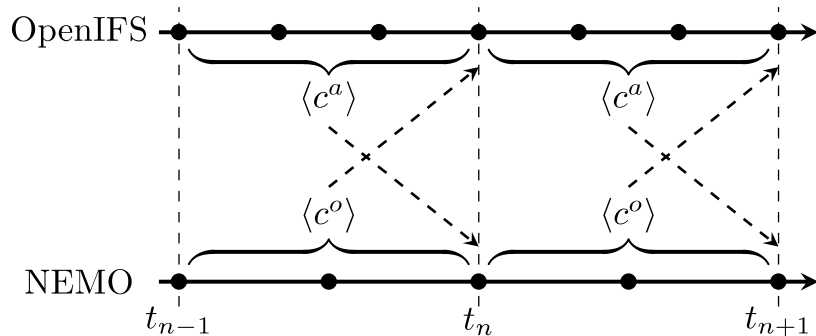
- What data should be exchanged at the interface(s)?
- How big are coupling errors in current models?
- How can we reduce them?



What do we mean by “coupling error”?

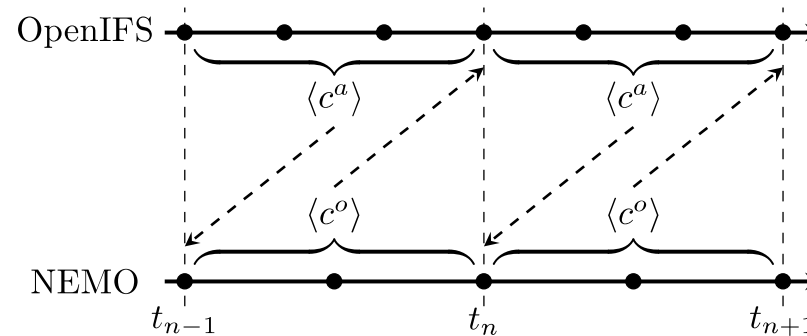
Parallel

(standard in, e.g., EC-Earth)

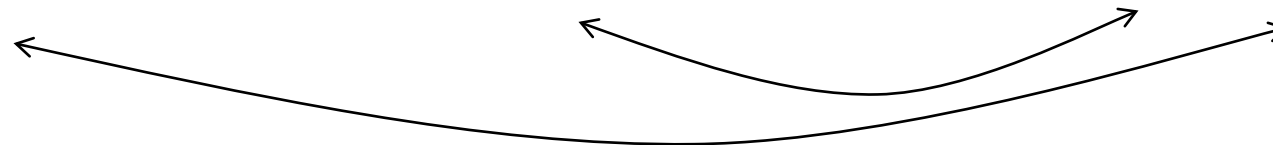
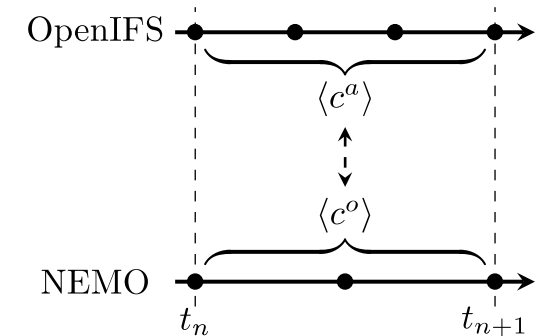


Atmosphere-first

(standard in IFS)



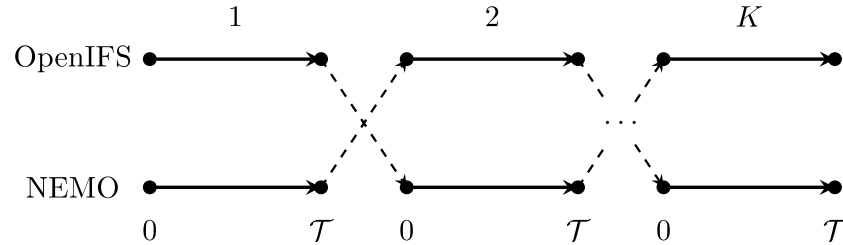
Reference



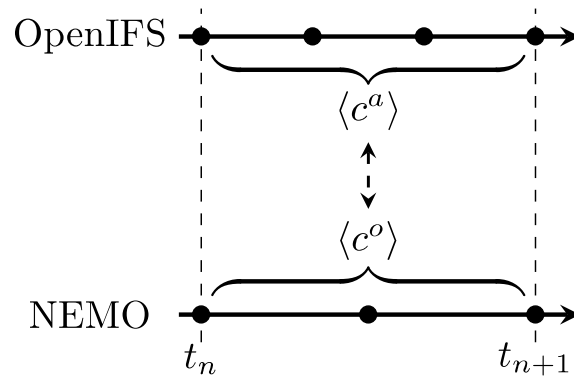
How big is this difference?

→ **Numerical** coupling error in time

Iterative coupling — The idea



$K \rightarrow \infty$



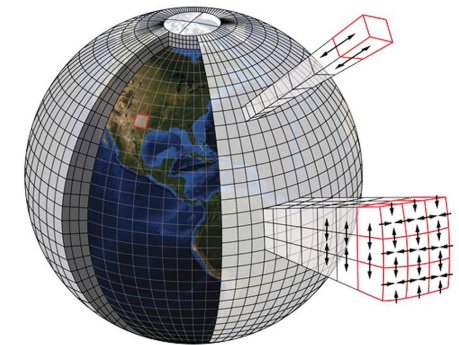
- If the coupled problem is set up **correctly**, the iteration will **converge**
 - Well-posed problem?
 - Parameterizations compatible?
 - Is the right data exchanged?
- Idea: Use coupling iteration, with K large
 - If the iteration does not converge: 🚧
 - If iteration converges: we get a **reference solution** (the limit) and a **metric** ("coupling error")

Model: EC-Earth AOSCM

- Single column version of EC-Earth
- OpenIFS SCM, NEMO1D (including LIM3/SI³)
- Cheap to run
- Same physics as in 3D, forced dynamics
- Note: Coupling is part of vertical physics!

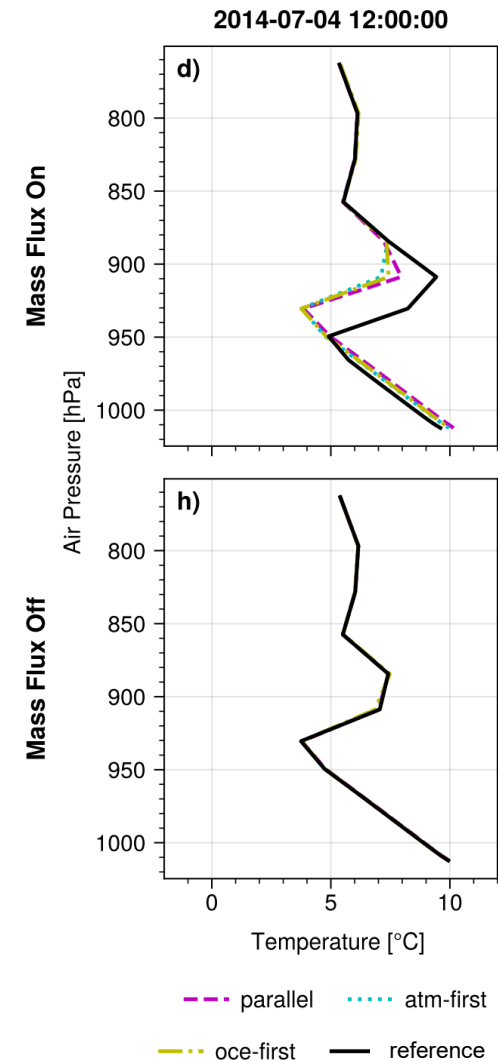


(Hartung et al., 2018)



AOSCM results — Open ocean

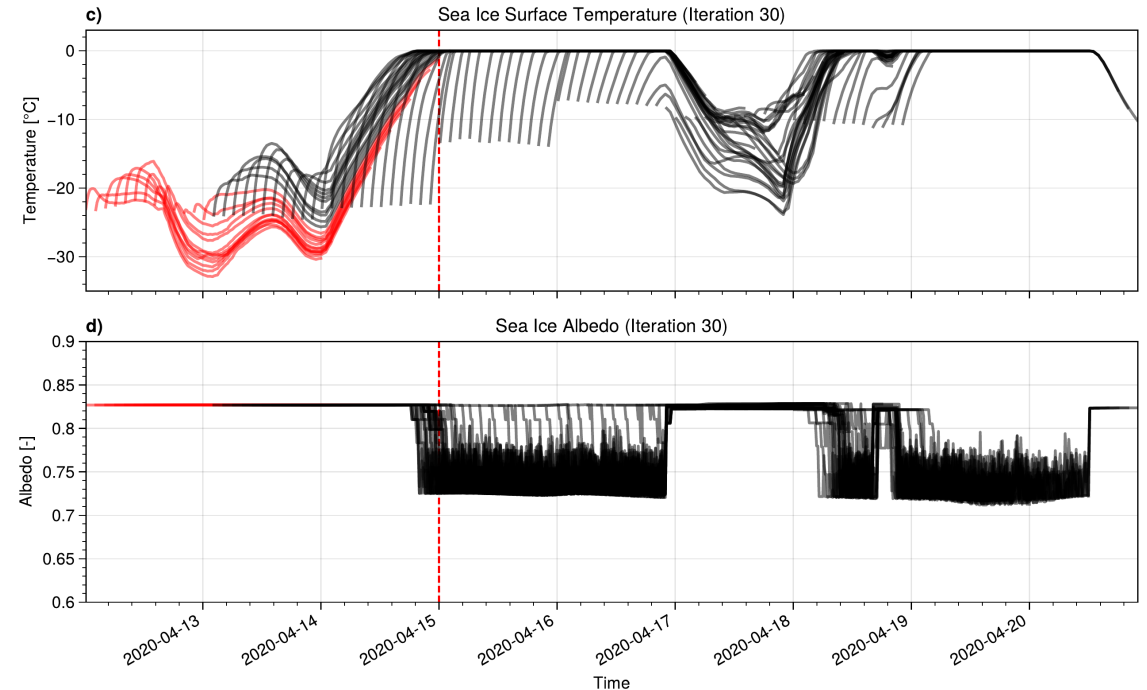
- Iteration converges consistently ✓
- Coupling errors small in the ocean
 - usually well below 0.1 °C for SST
 - Main source of error: phase shift in solar radiation
 - Simple fix: **atmosphere-first** scheme
- Coupling errors significant for atmospheric BL temperature T^a
 - Error $\in [0.7, 3.7]^\circ\text{C}$ for 25% of experiments
 - Related to discontinuity in OpenIFS mass flux scheme
 - No simple fix



AOSCM results — With sea ice (I)

⚠ Non-convergence ⚠ as soon as ice surface temperature $T^i = 0^\circ\text{C}$

- Reason: ice albedo **jumps** between melting & drying conditions
- Fix: **regularized** albedo scheme
 - Replace jumps with narrow, smooth transition region
 - Result: consistent convergence ✓

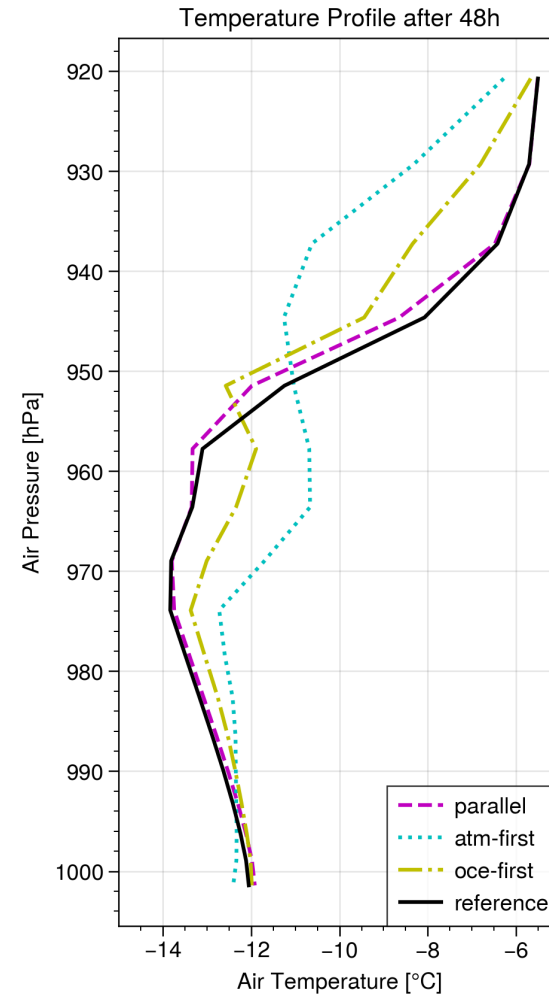


Iteration converged only for the **red** experiments.

AOSCM results — With sea ice (II)

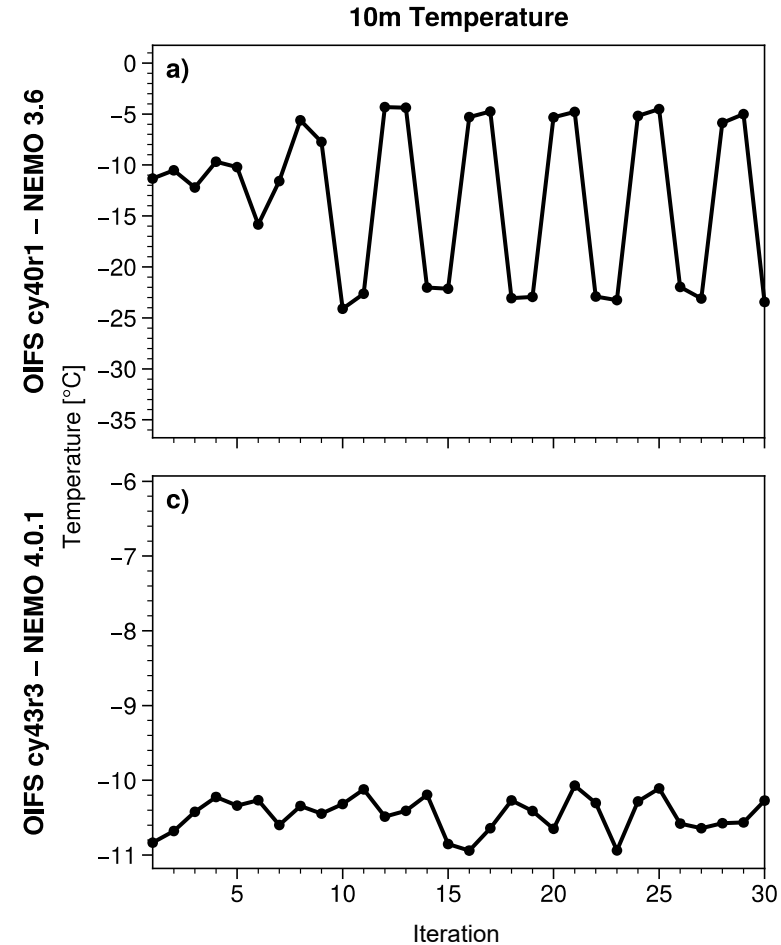
(with regularized albedo)

- Coupling errors significant for ice surface temperature T^i & atmospheric BL temperature T^a
- T^i error after 48h $\in [0.9, 4.7]$ °C for 25% of experiments
 - “Winner” highly test case–dependent (here: **parallel** scheme)
- No simple fix that addresses both!




A–O–SI coupling: Research needed!

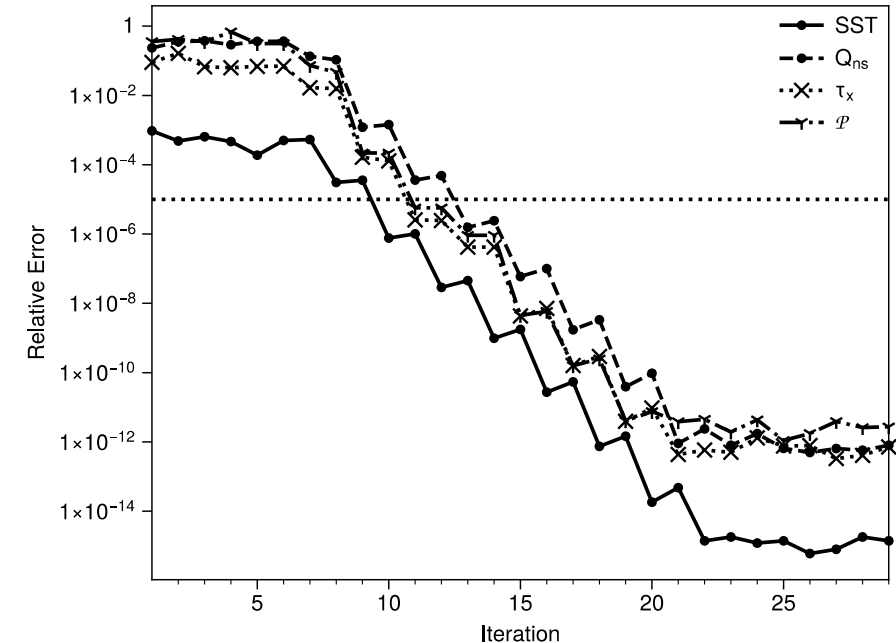
1. Convergence strongly model-dependent!
Much better results with NEMO 4, but why?
2. Lack of mathematical analysis for
atmosphere–ocean–sea ice interaction
3. Atmosphere–sea ice:
cf. atmosphere–surface coupling
 - T^{skin} over land is computed inside the atmosphere
 - T^i is computed inside SI³
 - Is this the right approach? Matter of time scales?



Summary

1. Coupling iterations might not converge for your coupled GCM

2. Jumps in physics amplify perturbations: We suggest smooth transitions.
3. Atmosphere–ocean–sea ice coupling is not well-studied!
Paper submitted to GMD

Outlook



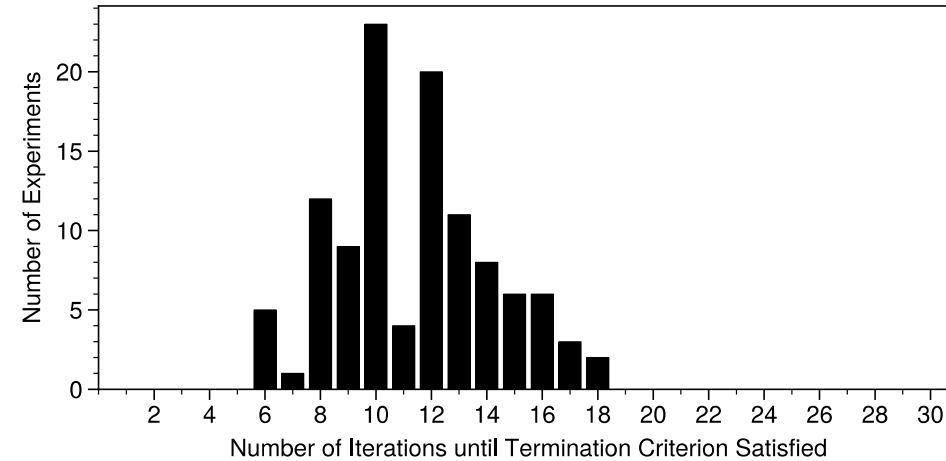
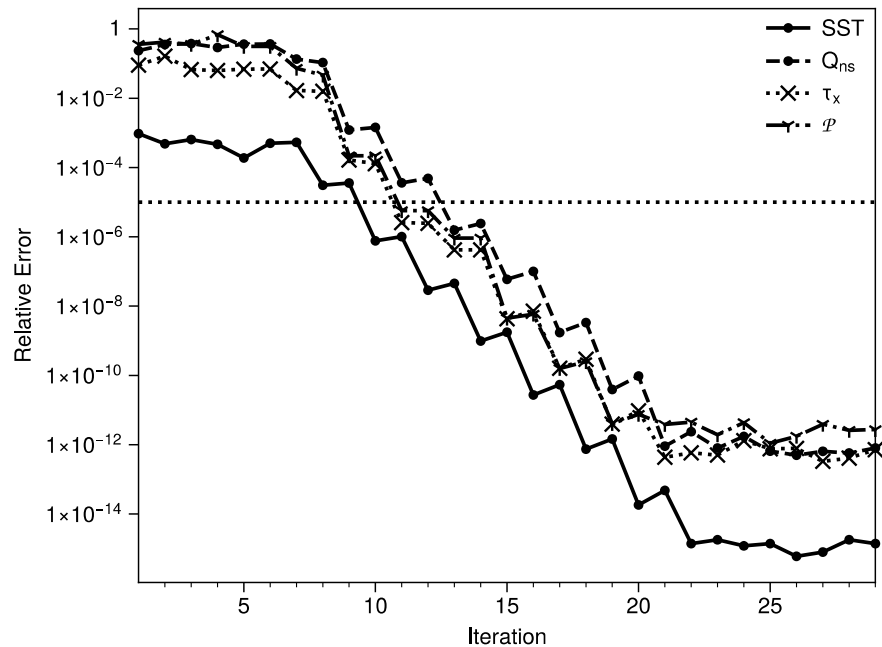
How much error reduction is possible with 2 iterations?





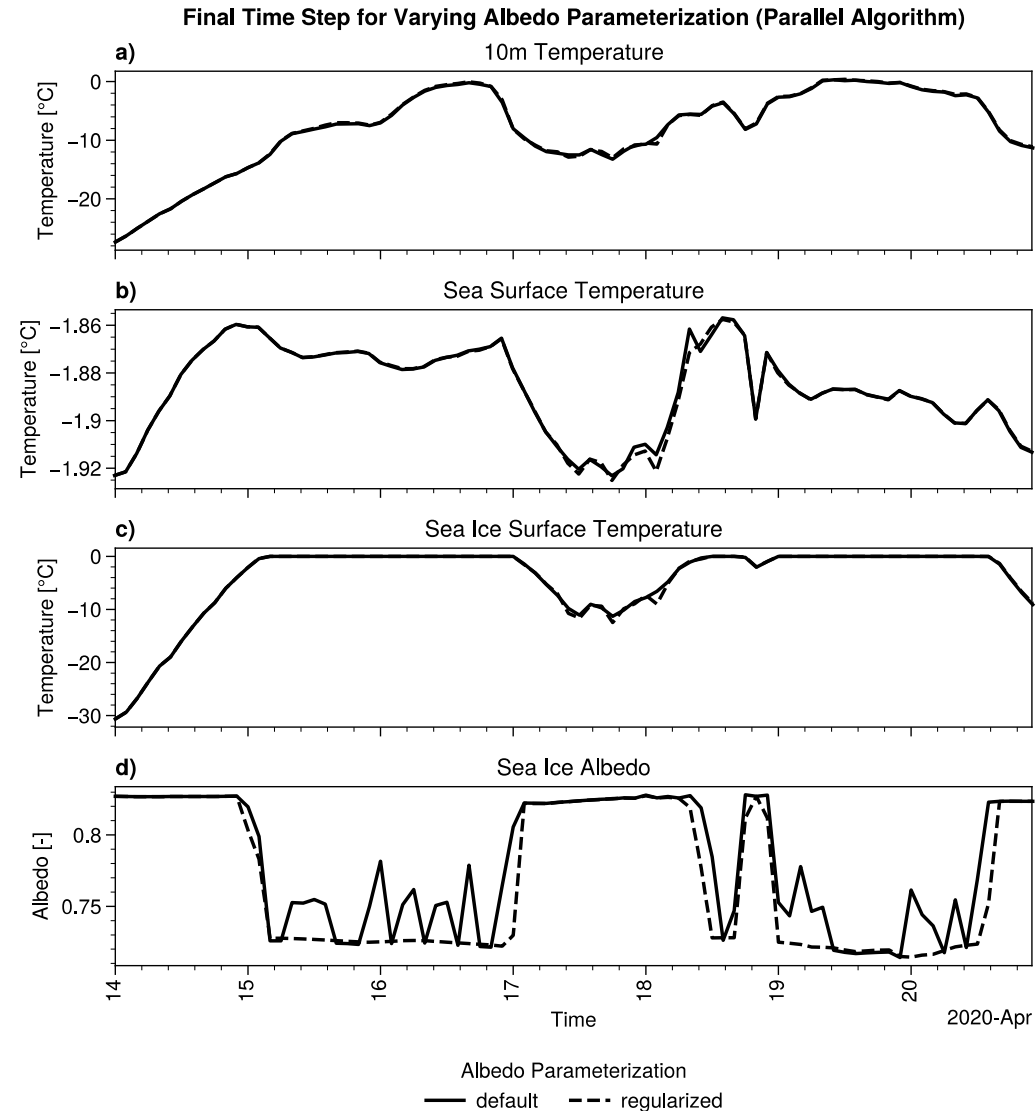
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How many iterations do you need?

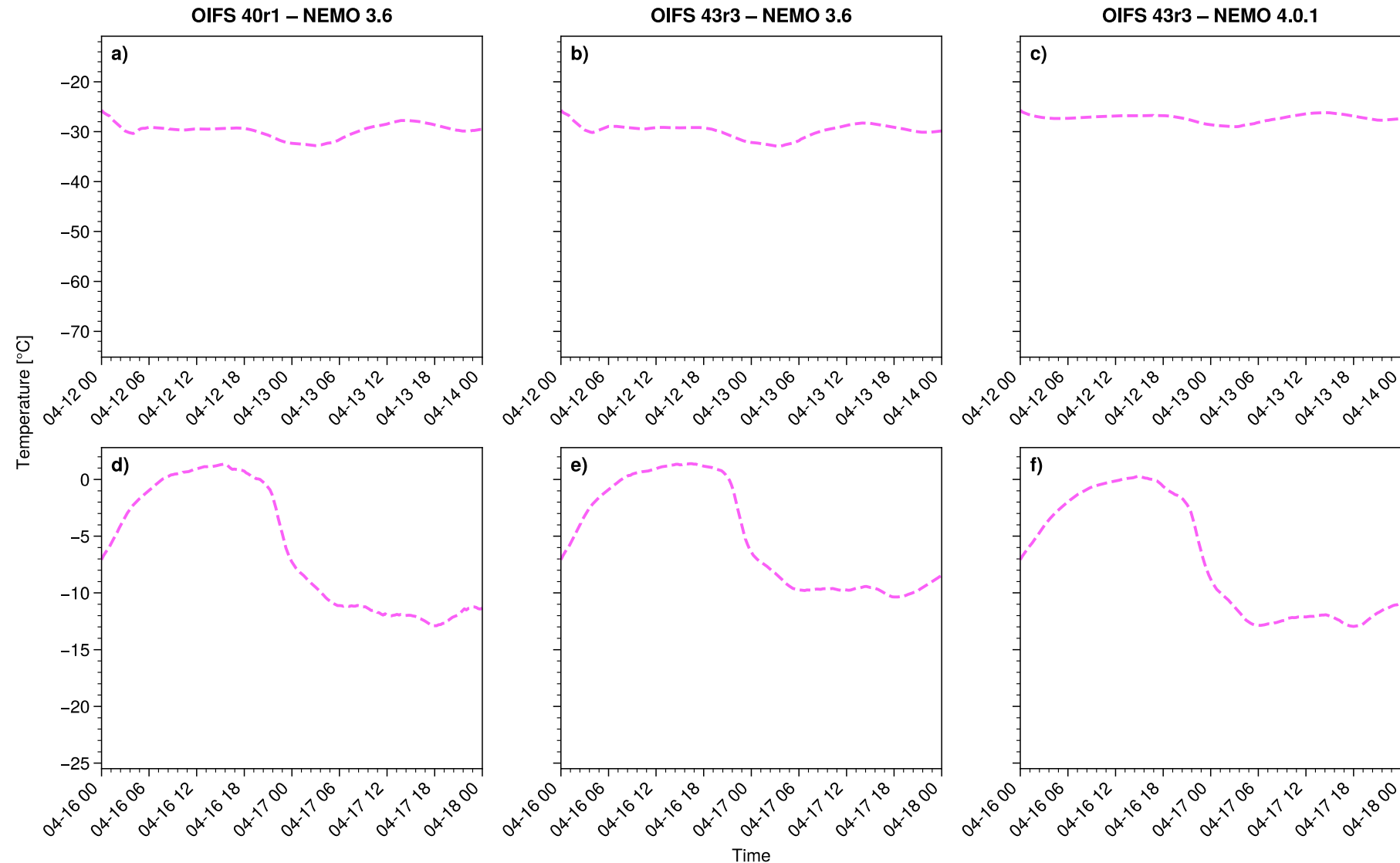


... too many!

Regularized Albedo Scheme



Version-Dependent Sea Ice Oscillations



Improving Coupling: Ideas

- Toy model for atmosphere–ocean–sea ice coupling:
 - Study coupling error for this problem, with increasing model complexity
 - Which parameters drive iteration convergence?
- Introduce a free Robin parameter (cf. optimized Schwarz methods) or relaxation step to get fast coupling error improvement
 - Maximum error reduction for a targeted iteration count (e.g., $K=2$)
- Improve the initial guess by learning from other coupling time windows

Why do you not compare with observations?

On the one hand...

As with new parameterizations, when a novel coupling scheme is implemented in a tuned model ([Hourdin et al. 2017](#)), the solution is likely to be worse for the new coupling method if the model is then not retuned, even if the new coupling scheme would lead to a superior solution in the absence of tuning. Model tuning inevitably tunes against errors that are independent of the parameters tweaked in the tuning process (i.e., compensating errors). In this case, multiple errors may exist, but the superposition of errors introduced to minimize other errors may result in “shadowing of errors” if only the final solution is taken into account during tuning processes. Remove one of these errors, and the result will be worse, despite having eliminated an error. For exam-

([Gross et al., 2018](#))

On the other hand...

- coupling with ocean & sea ice improves biases, increases forecast skill ([Ogata et al., 2016](#); [Smith et al., 2018](#))
→ stronger coupling = even better?
- iterative/monolithic coupling reduces spread ([Connors & Ganis, 2011](#), [Lemarié et al., 2014](#))

→ When is it too early to compare to observations?