



# Numerical Weather Prediction Parametrization of Subgrid Physical Processes

## **Clouds (3)**

### Sub-grid heterogeneity of clouds

**Richard Forbes**

(With thanks to Adrian Tompkins, Christian Jakob, Maike Ahlgrimm)





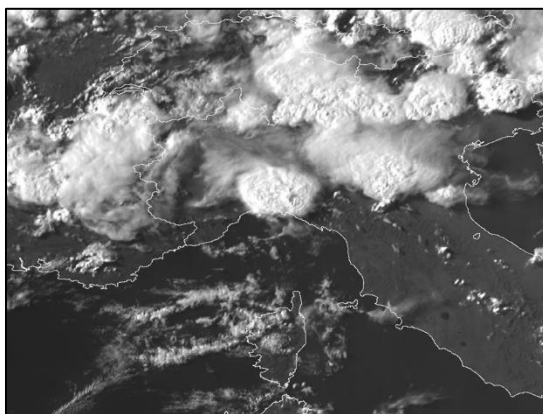
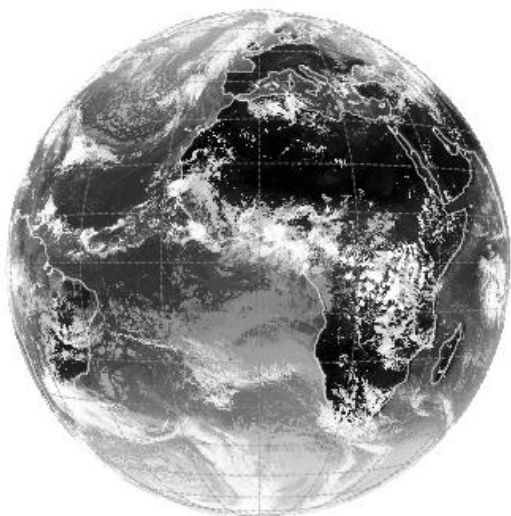
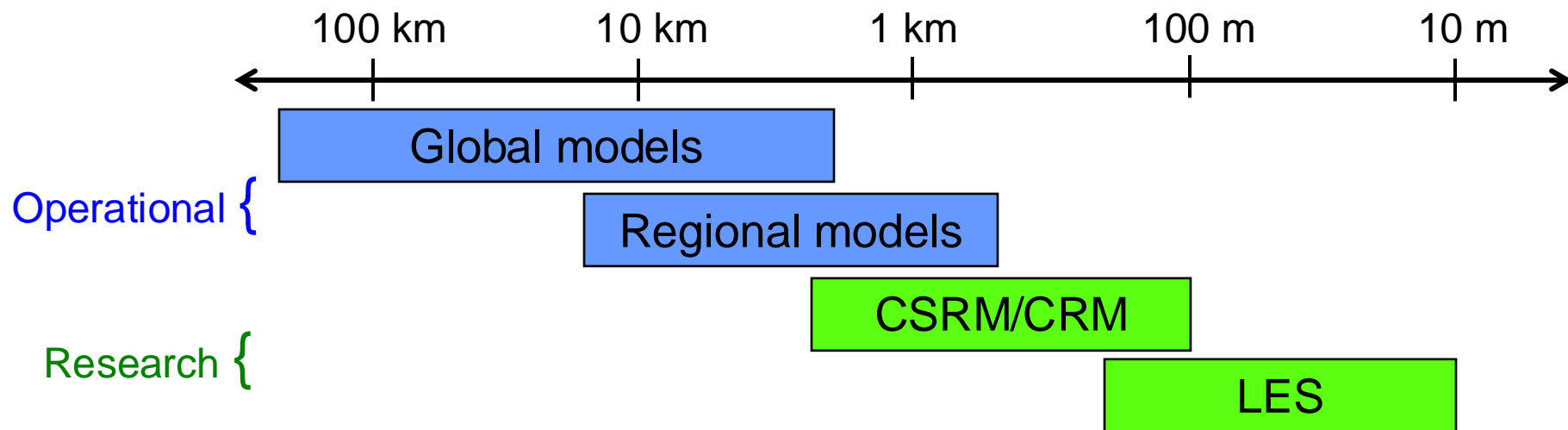
(1) Scales of heterogeneity  
and why they matter

(2) Representing sub-grid  
heterogeneity in models

(3) Summary

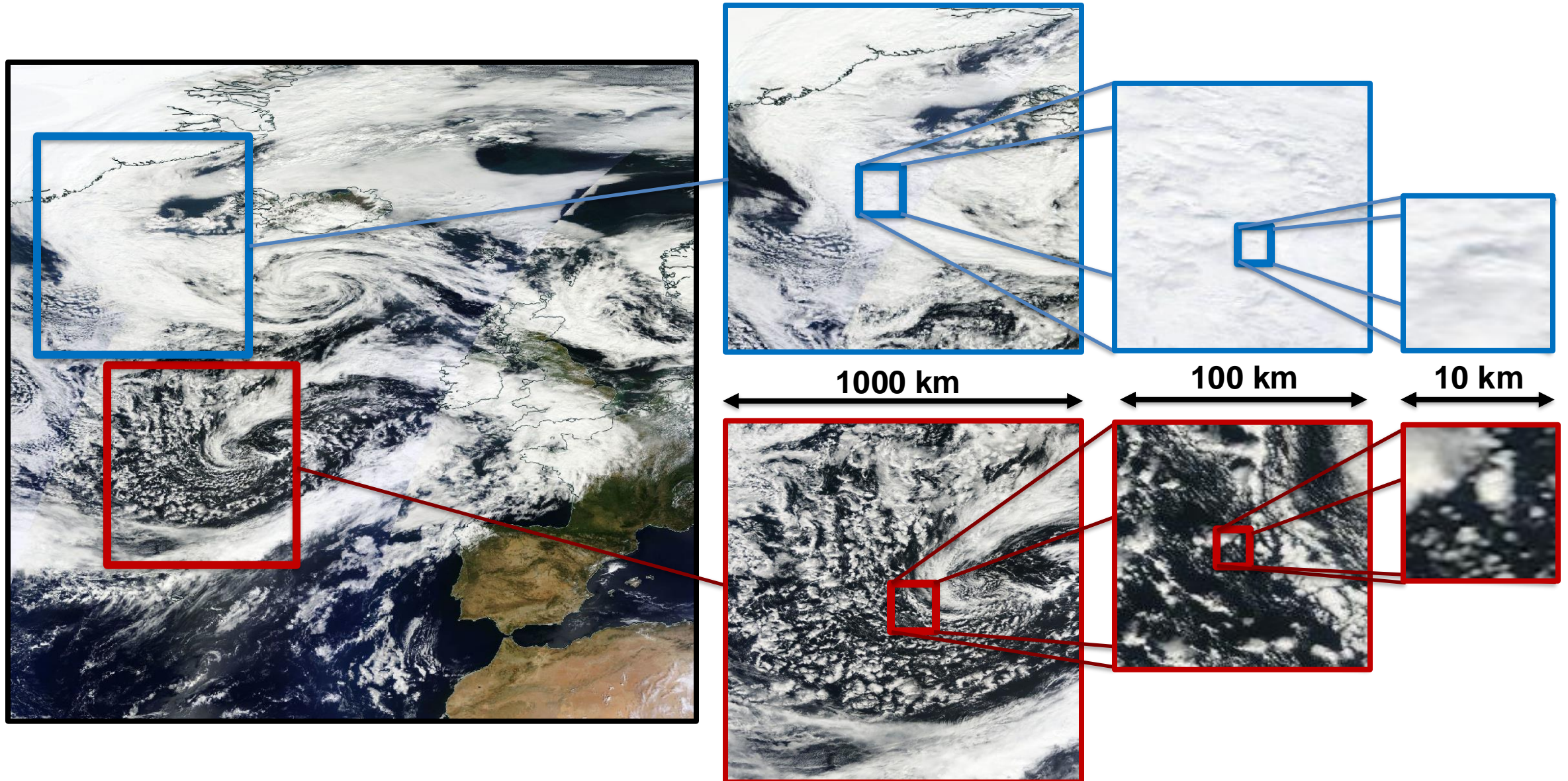


# Scales of heterogeneity: Wide range of model resolutions





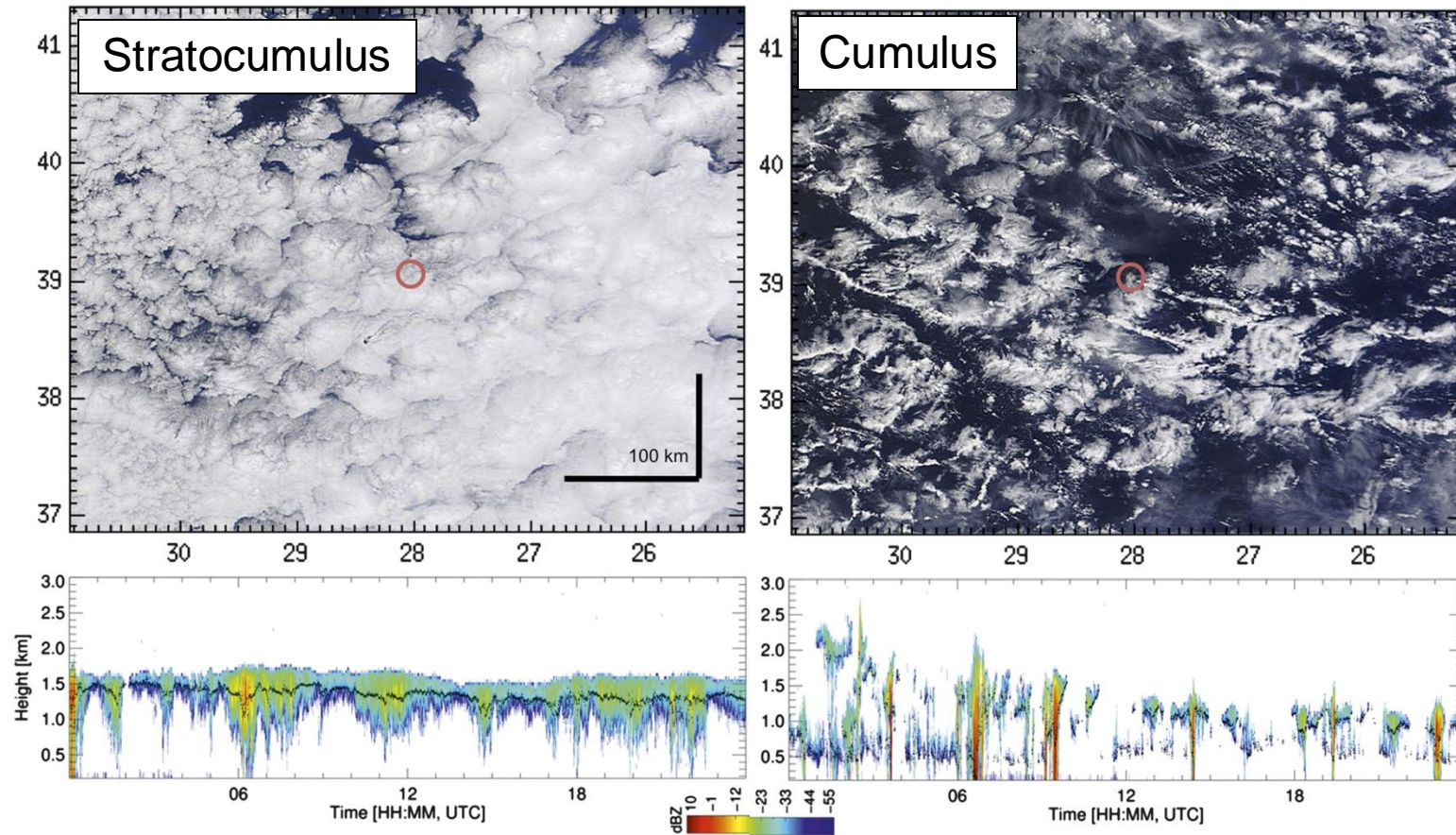
# Scales of heterogeneity: Significant across scales – cloudy/clear *and* in-cloud



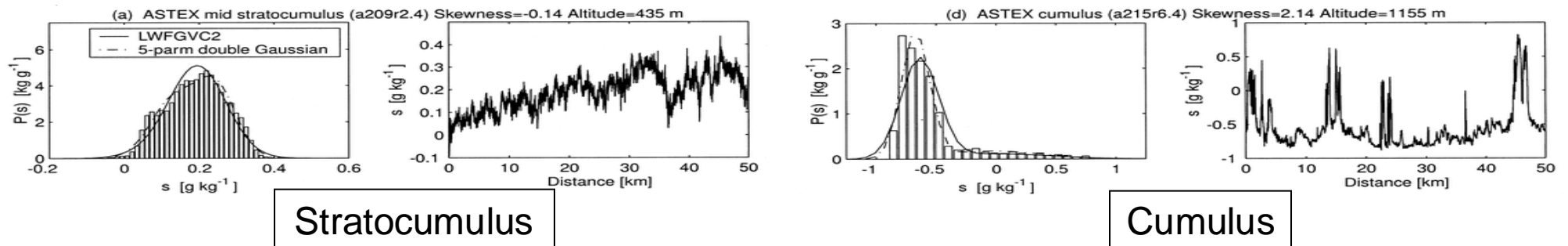


# Scales of heterogeneity: Humidity, cloud and precipitation $\leftrightarrow$ turbulence

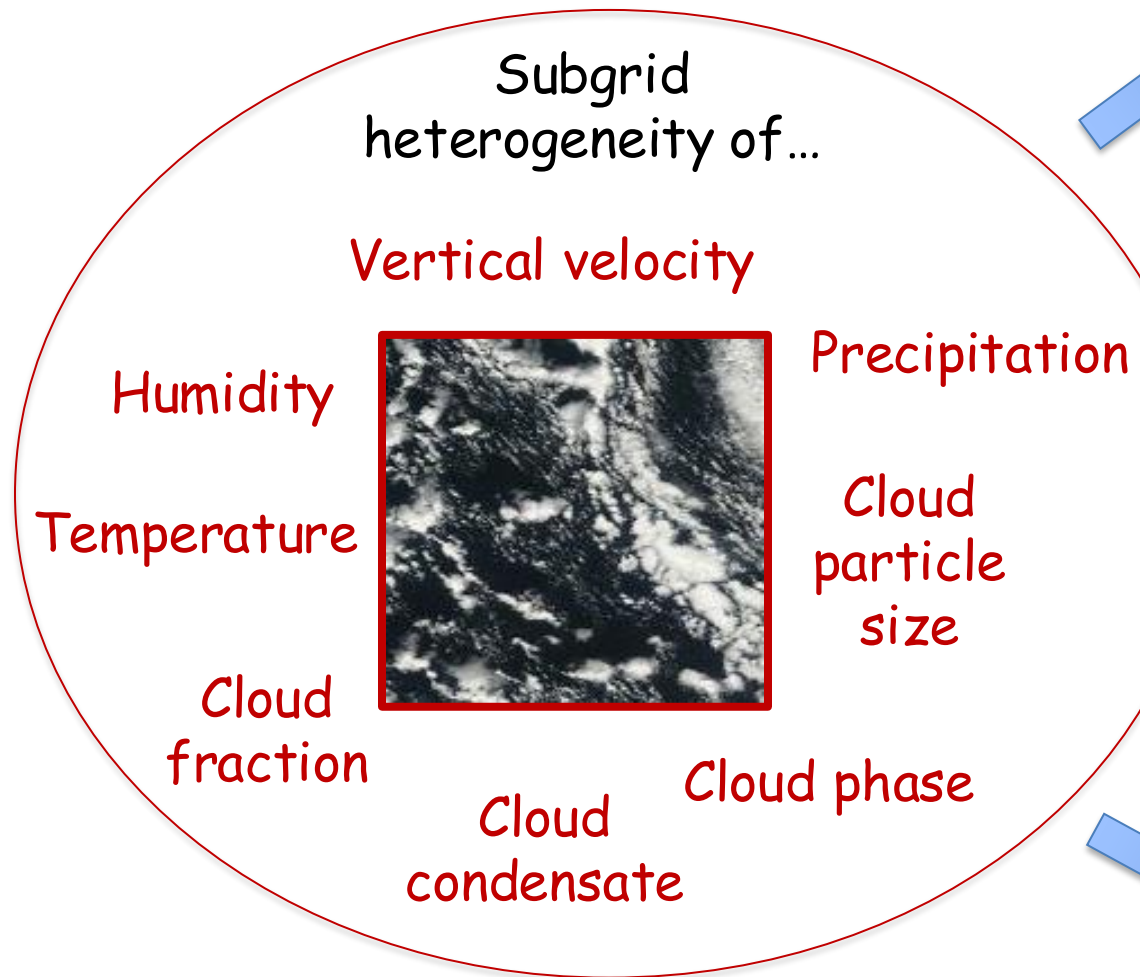
North Atlantic, Azores  
MODIS and radar data  
Rémillard et al. (2012)



ASTEX aircraft data  
(Larson et al. 2001)



# Scales of heterogeneity: Impacts on radiation, precipitation, latent heating

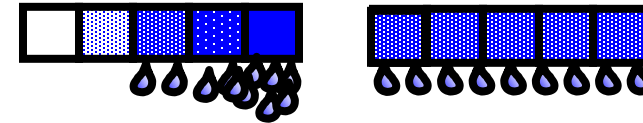


## Radiative Impacts

Cloudy sky versus clear sky fraction matters  
Assuming homogeneity → radiation biases  
Overlap of cloud in the vertical

## Hydrological Impacts

Rain formation related to subgrid liquid water contents



## Thermodynamical Impacts

Condensation occurs before gridbox RH=100%  
Evaporation in clear sky fraction

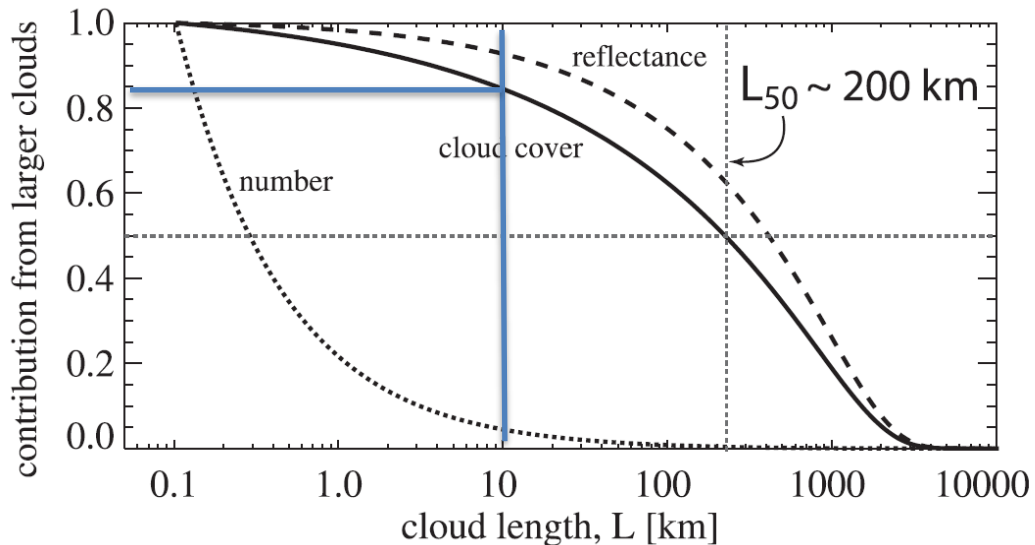
## Transport, Chemistry

Cloud associated with dynamics (T, q, u, v, w)  
Chemistry in clouds

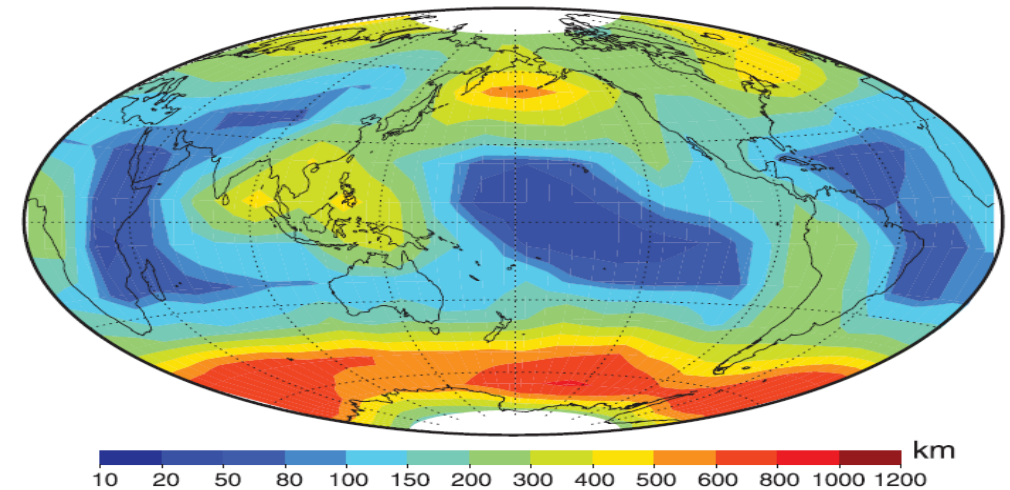
# Scales of heterogeneity: Global cloud cover and reflectance

From Wood and Field (2011, JCLim)

Contribution to global cloud cover, number and visible reflectance from clouds with chord lengths greater than  $L$  (from MODIS, aircraft & NWP data).

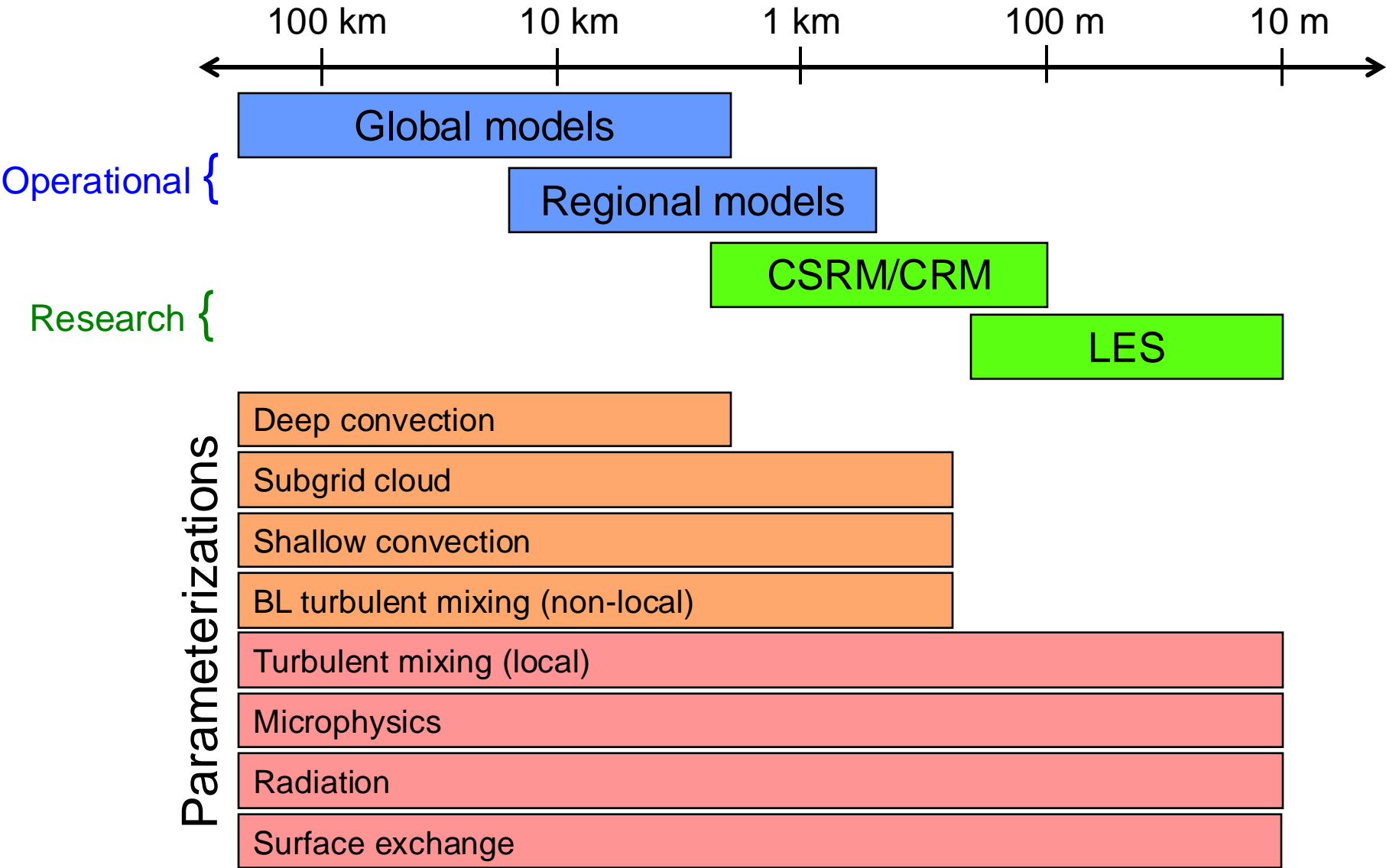


Map of the cloud size for which 50% of cloud cover comes from larger clouds (from 2 years of MODIS data)



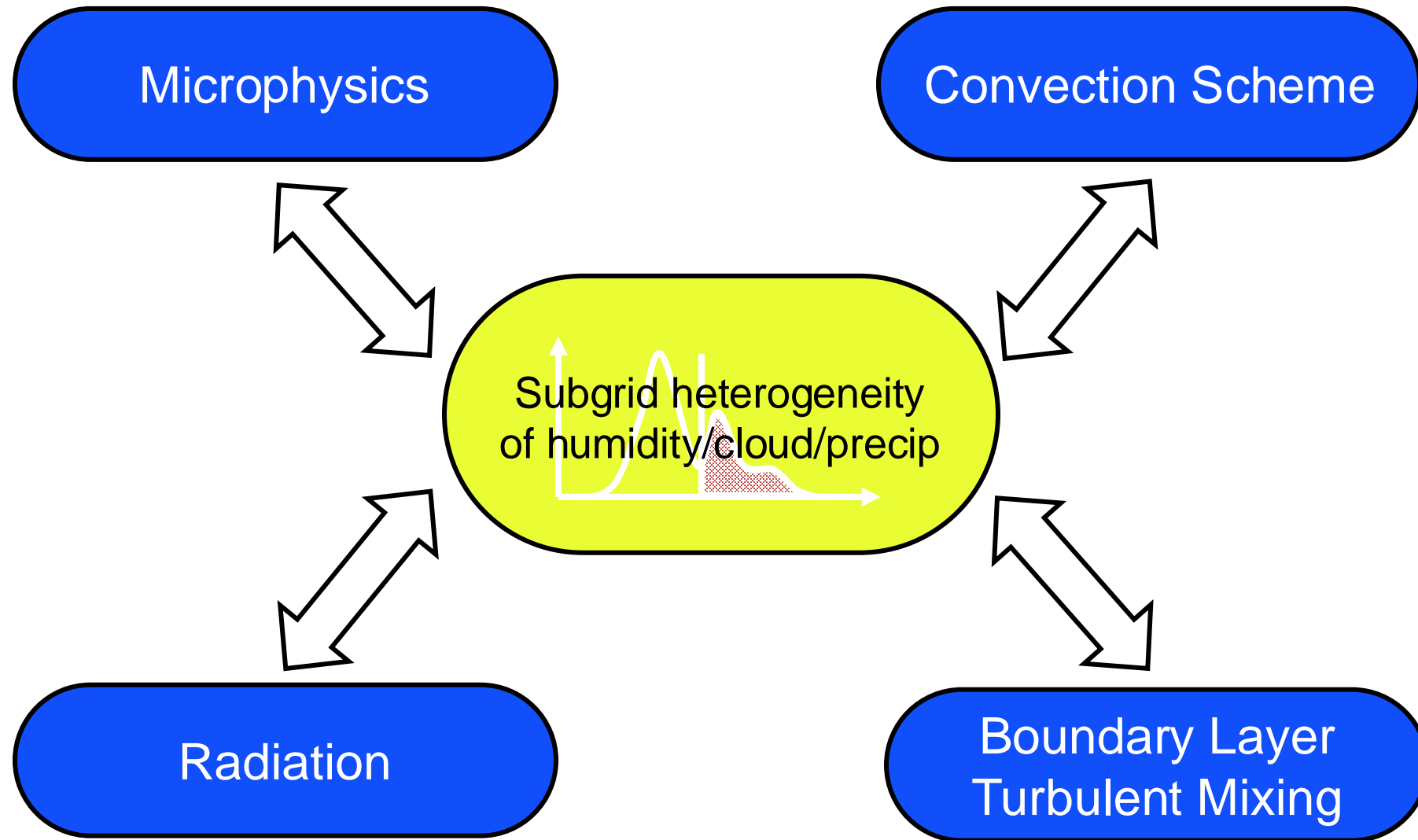
- 15% of global cloud cover comes from clouds smaller than 10 km  
→ smaller scales still important, particularly dominate over subtropical oceans
- 85% of global cloud cover comes from clouds larger than 10 km  
→ condensate heterogeneity more important than cloud cover?

# Scales of heterogeneity: Model parametrizations





## Scales of heterogeneity: Consistency across model parametrizations





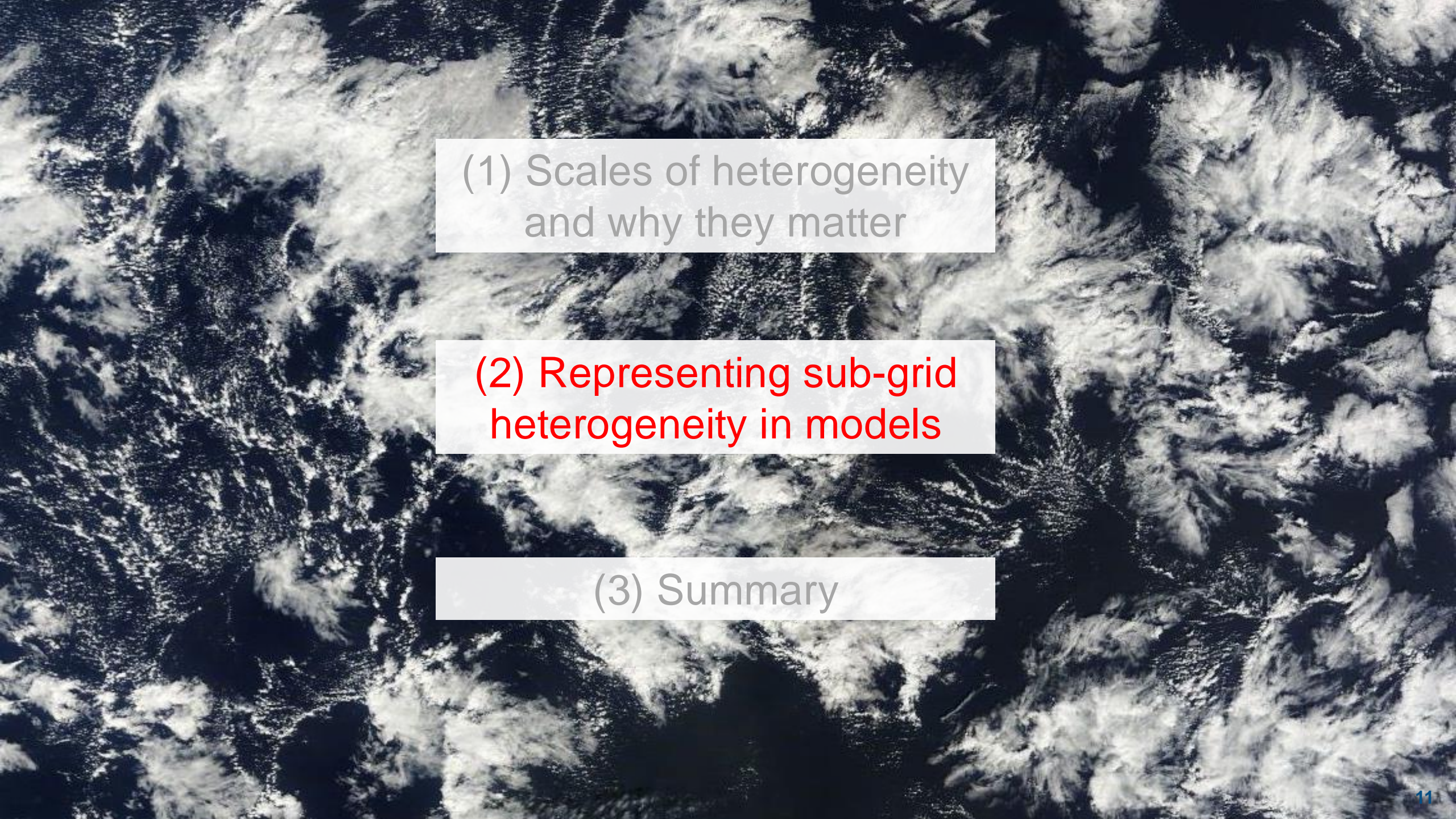
## (1) Scales of heterogeneity: Summary

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Sub-grid heterogeneity of cloud:

1. Humidity, cloud  $\leftrightarrow$  subgrid turbulence/convection
2. Important for radiation, precipitation, latent heating
3. Less important with increasing model resolution, but still relevant  $< 10\text{km}$
4. Aim for a consistent representation across model parametrizations



A satellite image of Earth showing complex, swirling cloud patterns over a dark ocean surface. The clouds are white and grey, creating a high-contrast, textured appearance. The overall image has a grainy, high-resolution quality typical of satellite photography.

(1) Scales of heterogeneity  
and why they matter

(2) Representing sub-grid  
heterogeneity in models

(3) Summary



# Representing subgrid heterogeneity in a cloud scheme

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## First some assumptions:

$q_v$  = water vapour mixing ratio

$q_c$  = cloud water (liquid/ice) mixing ratio

$q_s$  = saturation mixing ratio =  $F(T,p)$

$q_t$  = total water (vapour+cloud) mixing ratio

$RH$  = relative humidity =  $q_v / q_s$

1. Local criterion for formation of cloud:  $q_t > q_s$

This assumes that no supersaturation can exist

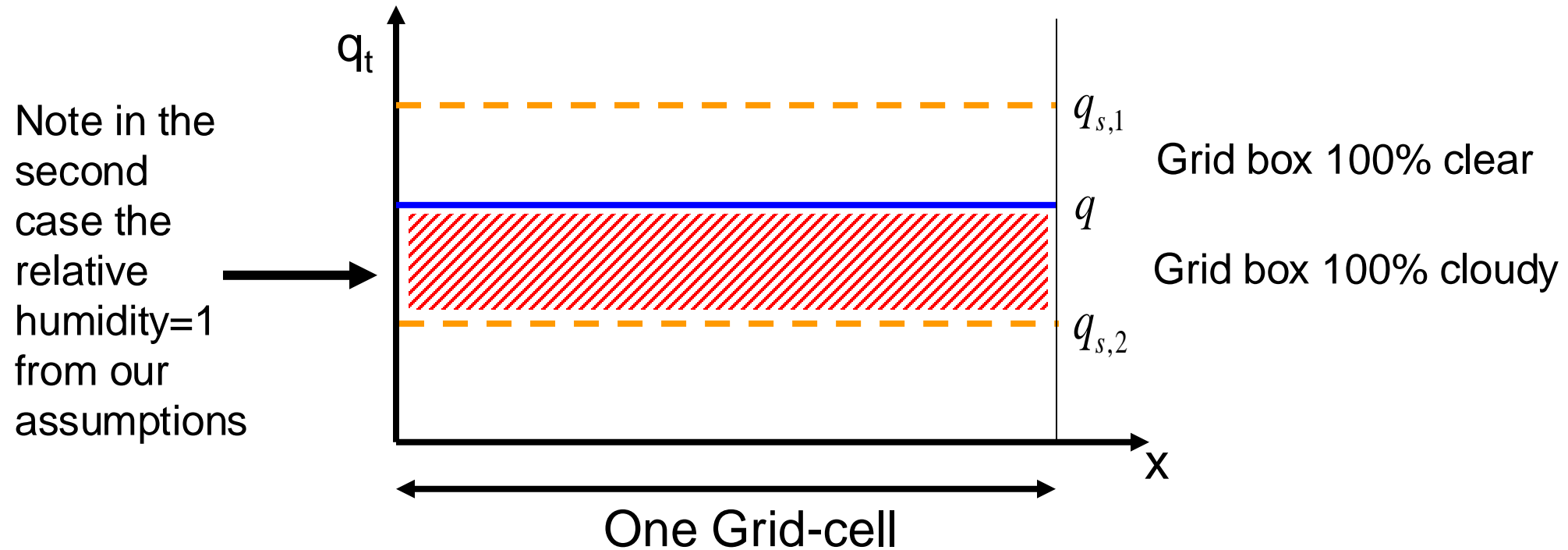
2. Condensation process is fast (cf. GCM timestep)

$$q_v = q_s \qquad q_c = q_t - q_s$$

!!Both of these assumptions less applicable in ice clouds!!

# Representing subgrid heterogeneity in a cloud scheme

Homogeneous distribution of water vapour and temperature:

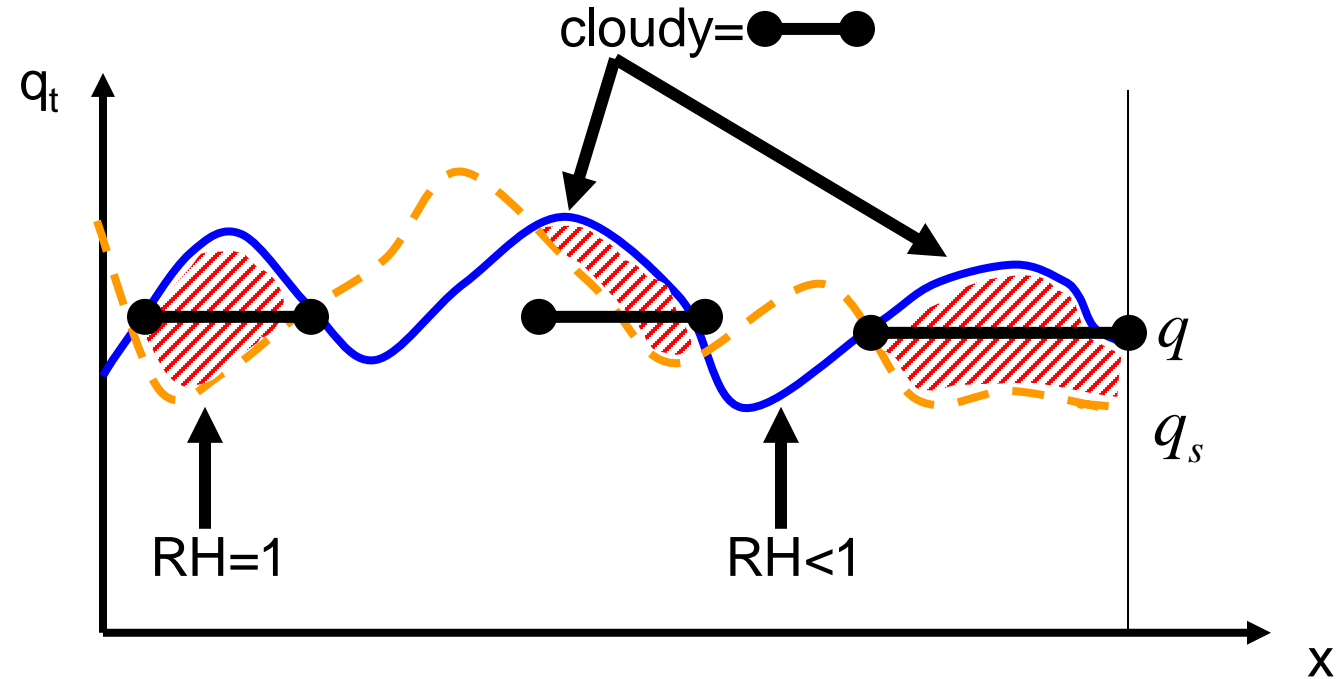


Partial coverage of a grid-box with clouds is only possible if there is an inhomogeneous distribution of temperature and/or humidity.



# Representing subgrid heterogeneity in a cloud scheme

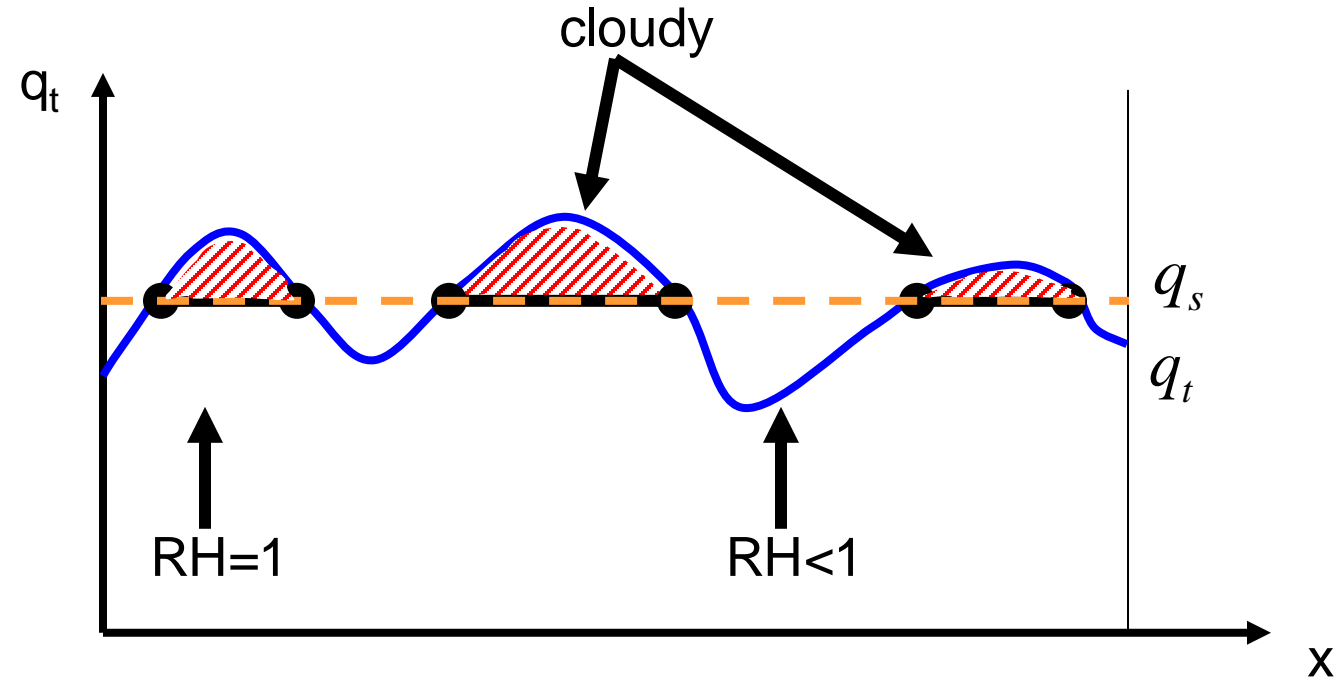
## Heterogeneous distribution of $T$ and $q$



An implication of the above is that clouds must exist before the grid-mean relative humidity reaches 1.

# Representing subgrid heterogeneity in a cloud scheme

## Heterogeneous distribution of $q$ only

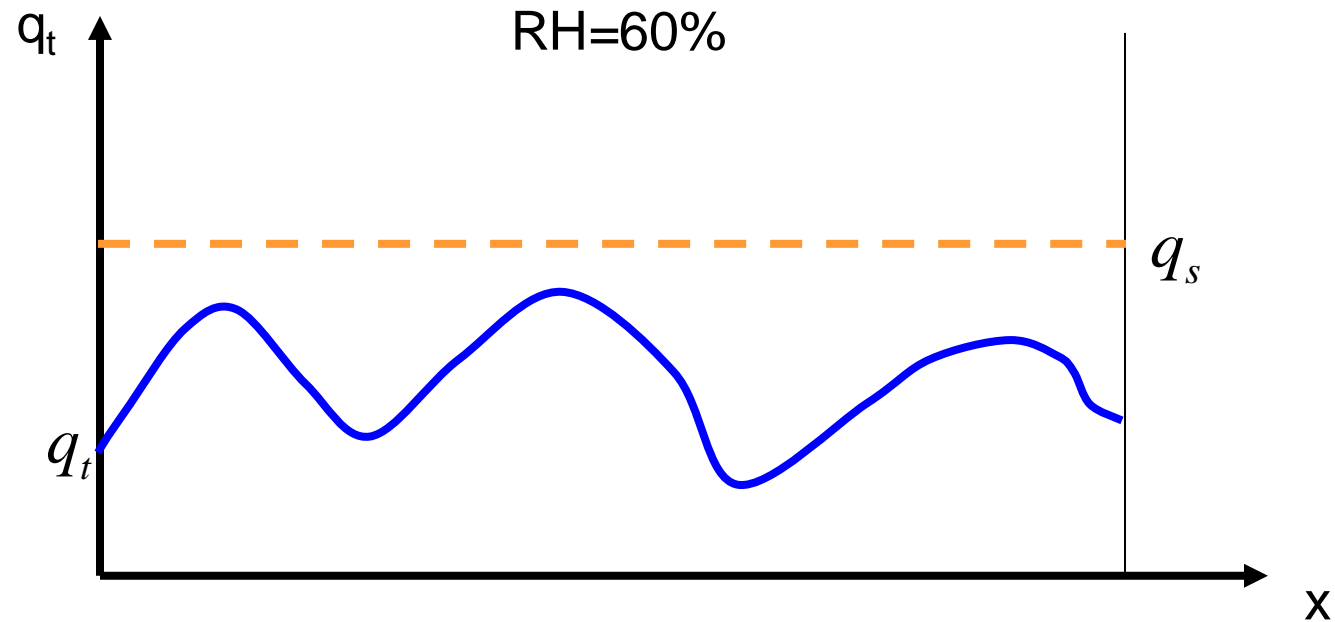


- The interpretation does not change much if we only consider humidity variability and assume uniform temperature (and therefore uniform saturation humidity =  $f(T,p)$ )
- Analysis of observations and model data indicates humidity fluctuations are more important *most* of the time.



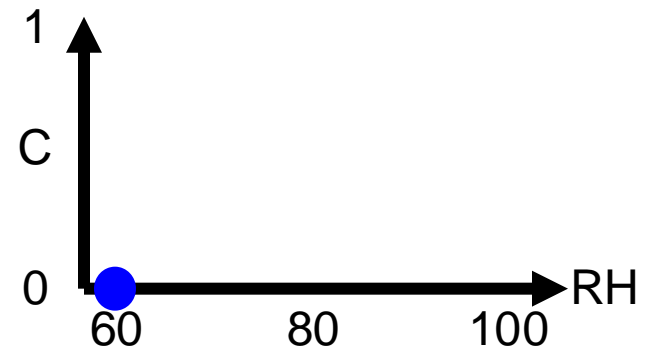
# Representing subgrid heterogeneity in a cloud scheme

## Simple Diagnostic Cloud Schemes: Relative Humidity Scheme



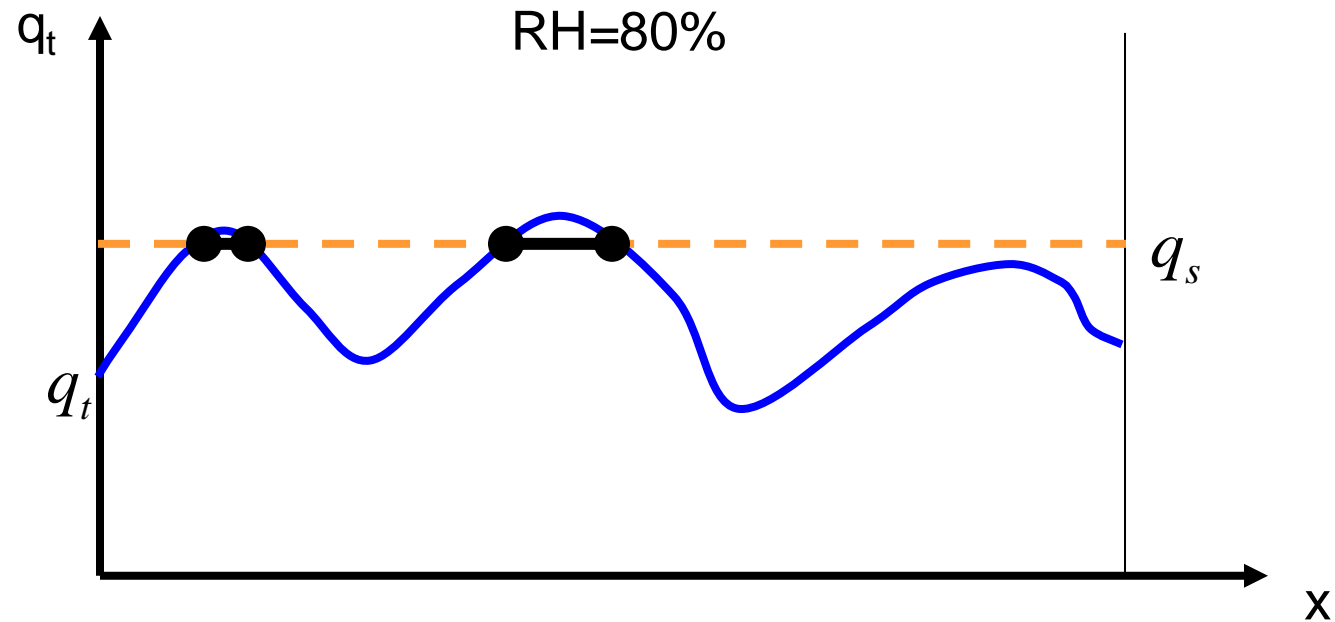
Take a grid cell with a certain (fixed) distribution of total water.

At low mean RH, the cloud cover is zero, since even the moistest part of the grid cell is subsaturated

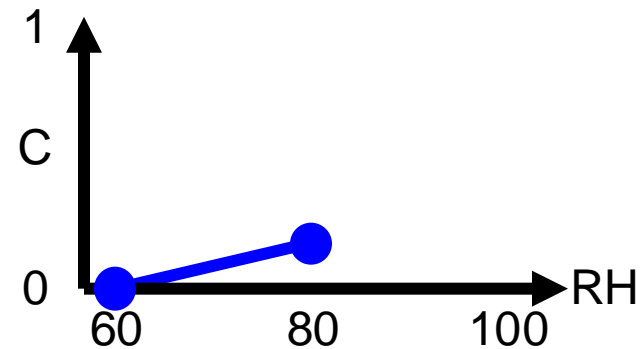


# Representing subgrid heterogeneity in a cloud scheme

## Simple Diagnostic Cloud Schemes: Relative Humidity Scheme



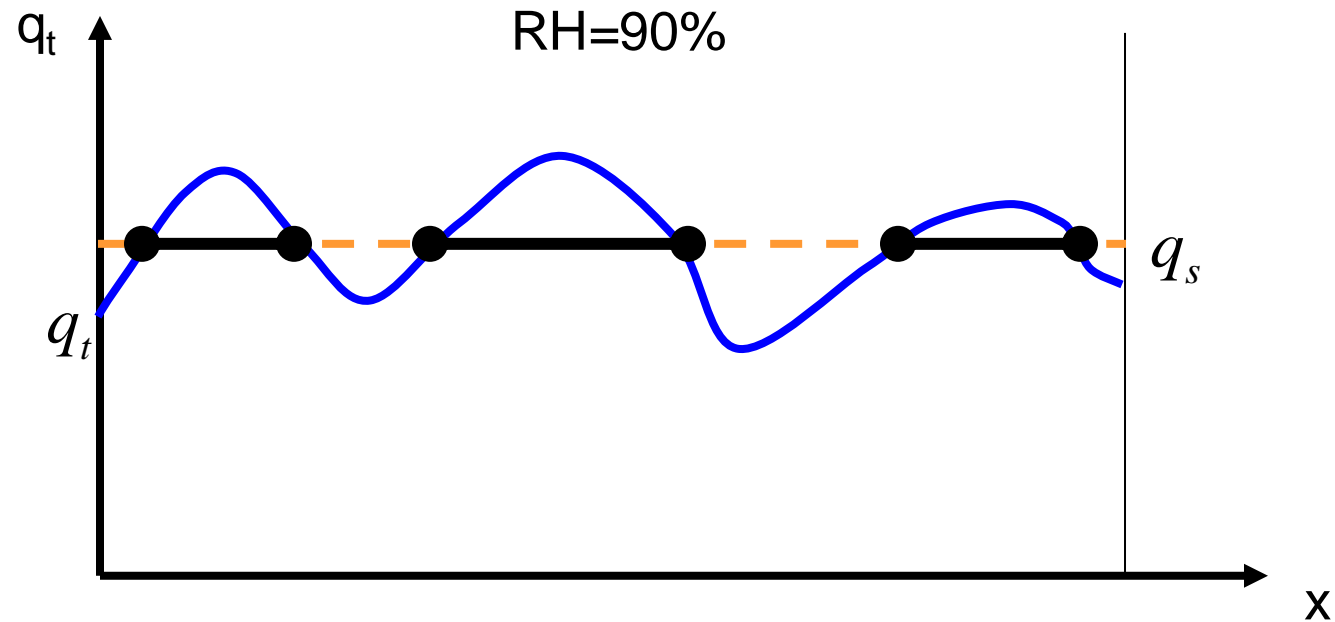
Add water vapour to the gridcell,  
the moistest part of the cell  
become saturated and cloud forms.  
The cloud cover is low.



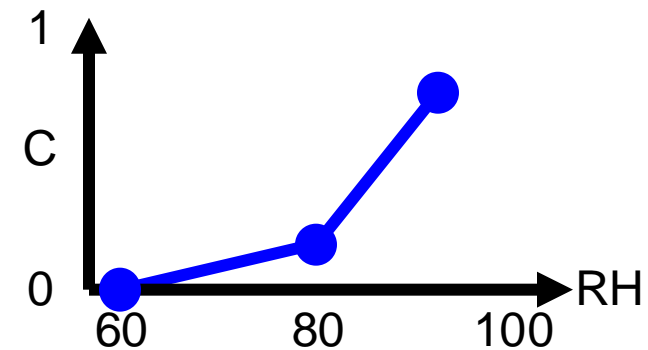


# Representing subgrid heterogeneity in a cloud scheme

## Simple Diagnostic Cloud Schemes: Relative Humidity Scheme

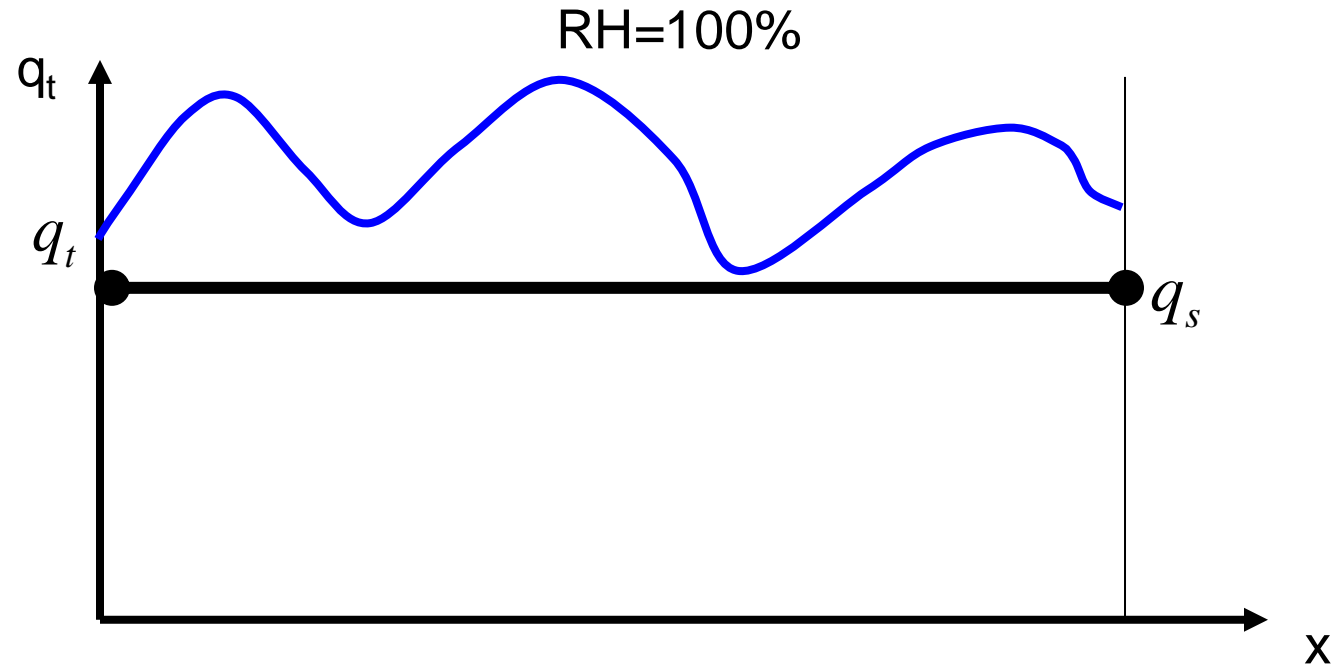


Further increases in RH increase the cloud cover

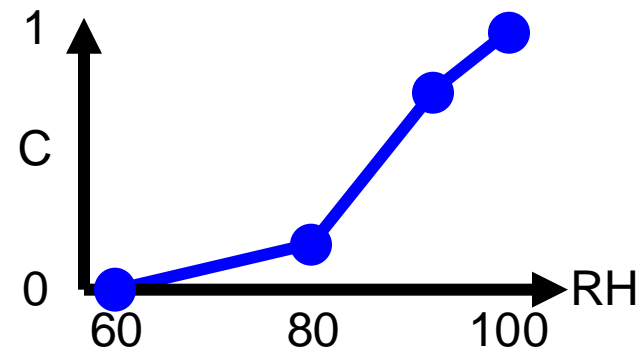


# Representing subgrid heterogeneity in a cloud scheme

## Simple Diagnostic Cloud Schemes: Relative Humidity Scheme



- The grid cell becomes overcast when  $RH=100\%$ , due to lack of supersaturation
- Diagnostic RH-based parametrization  $C = f(RH)$



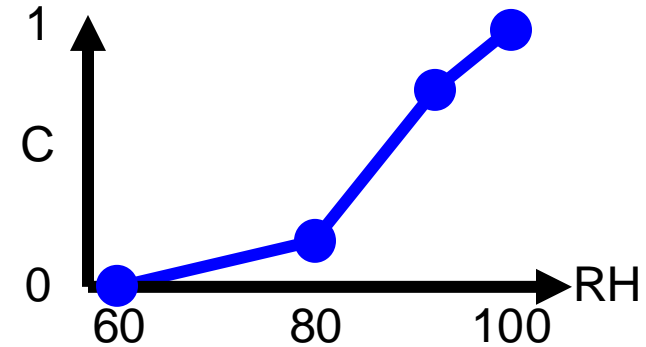


# Representing subgrid heterogeneity in a cloud scheme

## Simple Diagnostic Cloud Schemes: Relative Humidity Scheme

Many schemes, from the 1970s onwards, based cloud cover on the relative humidity (RH)

e.g. Sundqvist et al. MWR 1989:



$$C = 1 - \sqrt{\frac{1 - RH}{1 - RH_{crit}}}$$

😊 Remember this for later!

$RH_{crit}$  = critical relative humidity at which cloud assumed to form  
(= function of height, typical value is 60-80%)

## Simple Diagnostic Cloud Schemes: Relative Humidity Scheme

- Since these schemes form cloud when  $RH < 100\%$ , they implicitly assume subgrid-scale variability for total water,  $q_t$ , (and/or temperature,  $T$ ).
- However, the actual PDF (the shape) for these quantities and their variance (width) are often not known.
- They are of the form: “*Given a RH of  $X\%$  in nature, the mean distribution of  $q_t$  is such that, on average, we expect a cloud cover of  $Y\%$* ”.
- Ideally, we would like to represent the full PDFs (for humidity, temperature, condensate, vertical velocity etc) and how they vary in space and time...

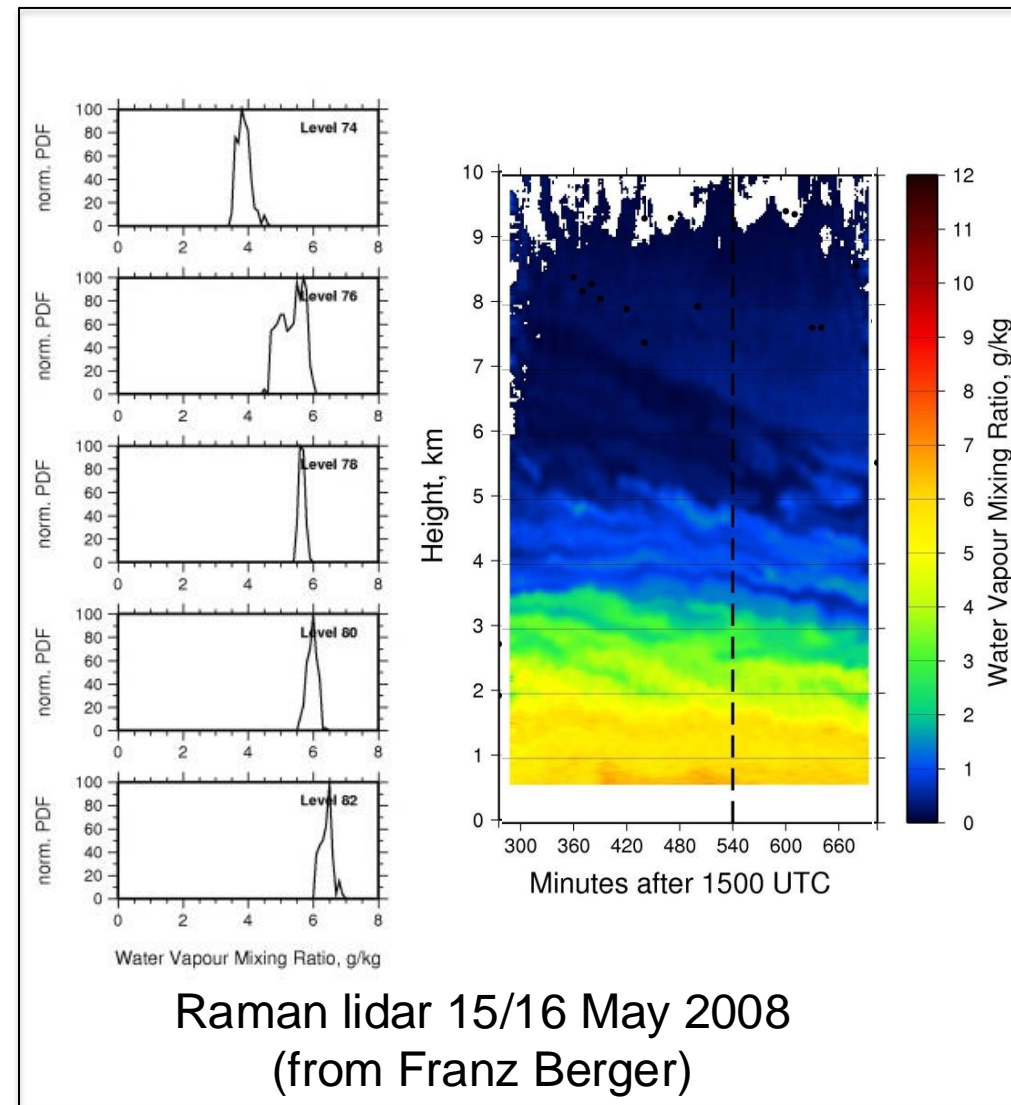
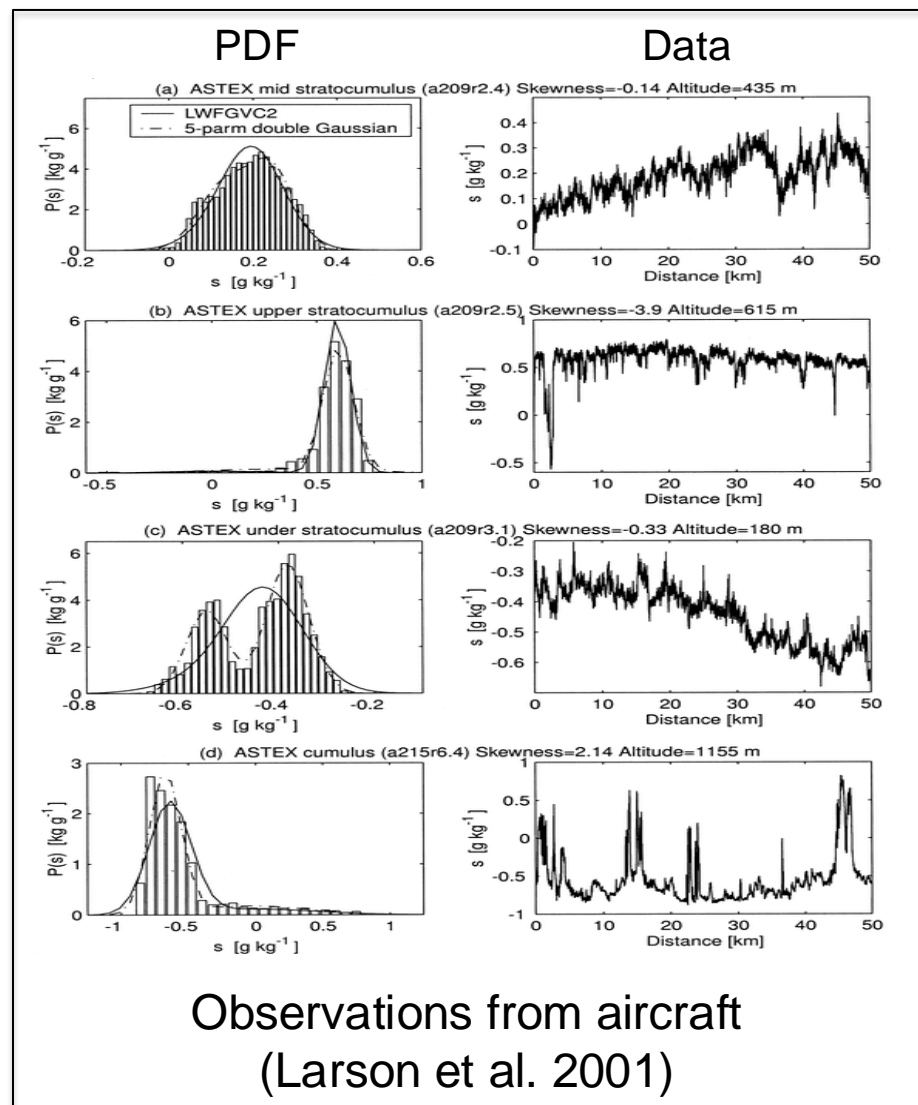


# Representing sub-grid heterogeneity: Observed PDF of total water

Observations from aircraft, tethered balloon, satellite, Raman lidar

...and LES model data...

...suggest PDFs can generally be approximated by uni or bi-modal distributions, describable by a few parameters



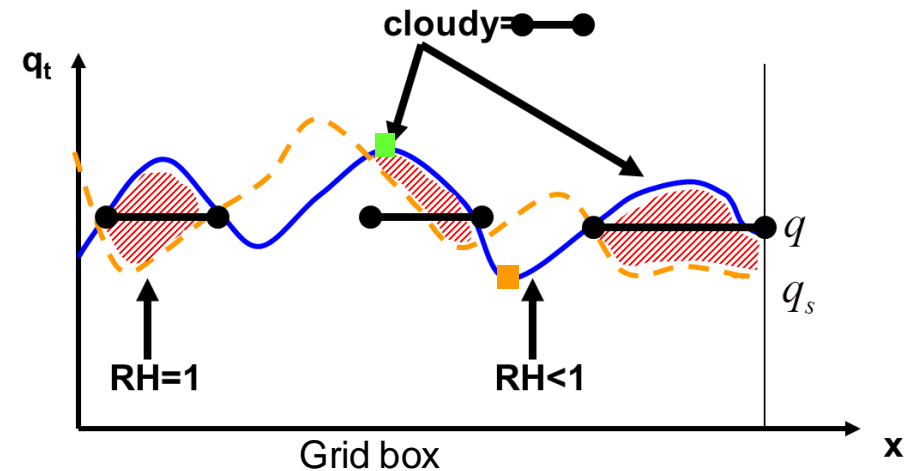
# Representing sub-grid heterogeneity: PDF of total water – statistical schemes



Statistical schemes explicitly specify the probability density function (PDF),  $G$ , for quantity,  $s$ , (or total water  $q_t$  if assume  $T$  homogeneous) (Sommeria and Deardorff 1977; Mellor 1977)

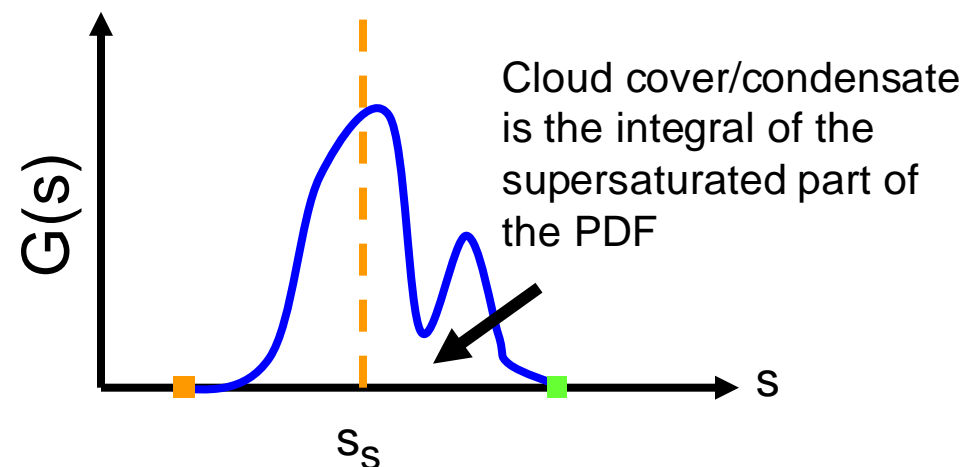
$$s = a_L(q_t - a_L T_L) \quad s^c = a_L(q_t^c - a_L T_L^c)$$

$$a_L = \left[ 1 + \frac{L}{C_p} \alpha_L \right]^{-1} \quad \alpha_L = \frac{\partial q_s}{\partial T}(\bar{T}_L) \quad \text{Liquid water temperature} \quad T_L = T - \frac{L}{C_p} q_L$$



Cloud cover  $C = \int_{s_s}^{\infty} G(s) ds$

Condensate  $q_l = \int_{s_s}^{\infty} (s - s_s) G(s) ds$

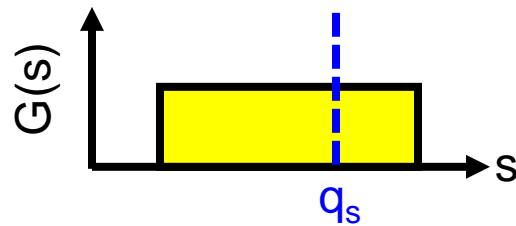




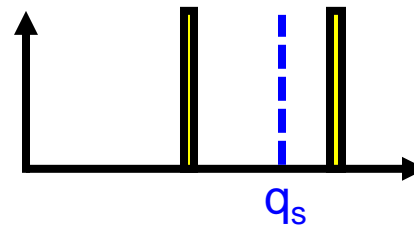
# Representing sub-grid heterogeneity: Modelled PDF of total water

Represent with a functional form, specify the:

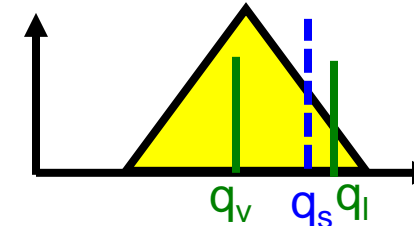
- (1) PDF type (delta, continuous, unimodal, bimodal, symmetrical, bounded?)
- (2) PDF variables (mean, variance, skewness / vapour, condensate, cloud fraction ?)
- (3) Diagnostic or prognostic (how many degrees of freedom?)



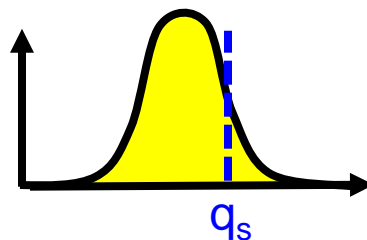
Uniform:  
Sundquist (1978)  
Letreut and Li (1991)



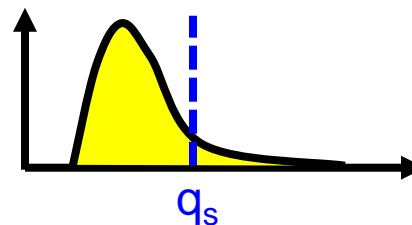
Double Delta Fn:  
Randall et al. (1992)  
Lappen and Randall (2001)



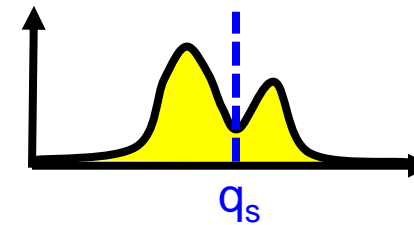
Triangular:  
Smith (1990)



Gaussian:  
Sommeria and Deardorff (1977)  
Mellor (1977)



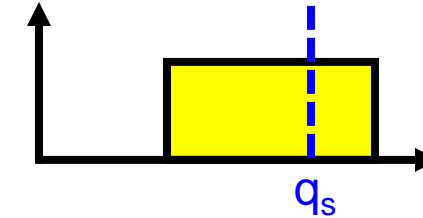
Gamma/Lognormal/Beta:  
Bougeault (1982)  
Barker et al. (1996)  
Tompkins (2002)



Double Gaussian (binormal):  
Lewellen and Yoh (1993)  
Larson et al. (2001)  
Golaz et al. (2002)

# Diagnostic statistical (RH) scheme: Sundquist (1989) – form used in many GCMs

- (1) Uniform PDF
- (2) Prognostic: Total water mean  
Diagnostic: Variance (width)
- (3) 1 cloudy degree of freedom + BL + convection



## Advantages:

- First order approximation to obs
- Computationally inexpensive

## Disadvantages:

- Not enough degrees of freedom (tied to RH)
- Requires RH<sub>crit</sub> to specify width when clear sky
- Not all processes are formulated with the PDF
- Doesn't allow skewness

## Other schemes:

- Smith (1990) Met Office LAMs triangular distribution
- Xu and Randall (1996) extended to C=fn(RH,qc)

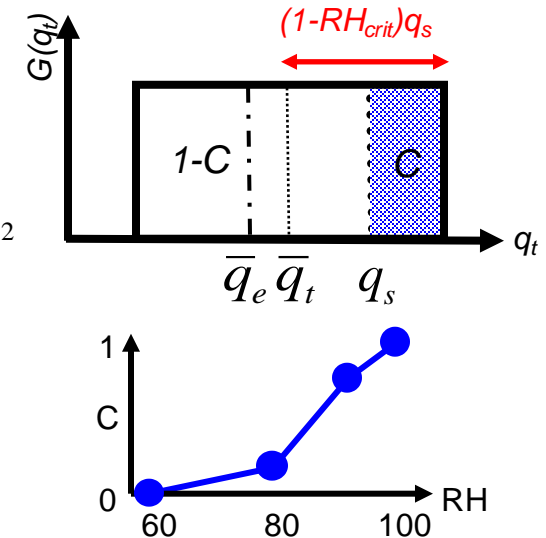
If PDF moments are fixed (i.e. in this case width of the “top-hat” function), then equivalent to a diagnostic “relative humidity” scheme:

$$\bar{q}_v = Cq_s + (1-C)\bar{q}_e$$

$$\bar{q}_e = q_s(1 - (1 - RH_{crit})(1 - C))$$

$$RH = \frac{\bar{q}_v}{q_s} = 1 - (1 - RH_{crit})(1 - C)^2$$

$$C = 1 - \sqrt{\frac{1 - RH}{1 - RH_{crit}}}$$



# Prognostic cloud fraction scheme: Tiedtke (1993) ECMWF operational since 1995

- (1) Uniform/delta function
- (2) Prognostic: humidity, condensate, cloud fraction
- (3) 3 cloudy degrees of freedom + BL + convection

## Advantages:

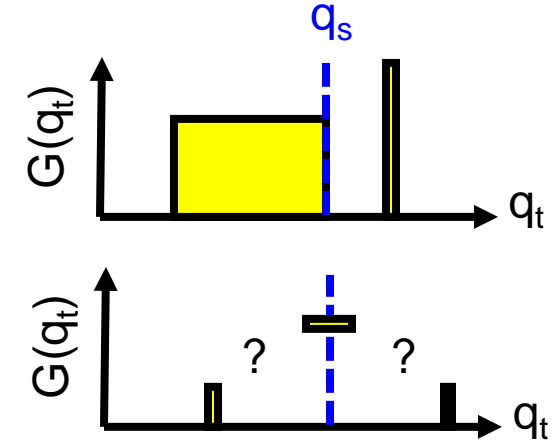
- Computationally inexpensive
- Sources and sinks for all processes
- Direct convective detrainment of condensate and cloud fraction important term
- In principle, allows positive and negative skewness
- Number of tunable parameters

## Disadvantages:

- Number of tunable parameters
- Not continuous PDF, no condensate heterogeneity
- Requires RHcrit to specify “top-hat” width when clear sky
- Not all processes are formulated with the PDF, some adhoc
- Not reversible in condensation/evaporation

## Other schemes:

- PC2 Met Office global (Wilson et al. 2008)





# Prognostic PDF scheme: Tompkins (2002) ECHAM

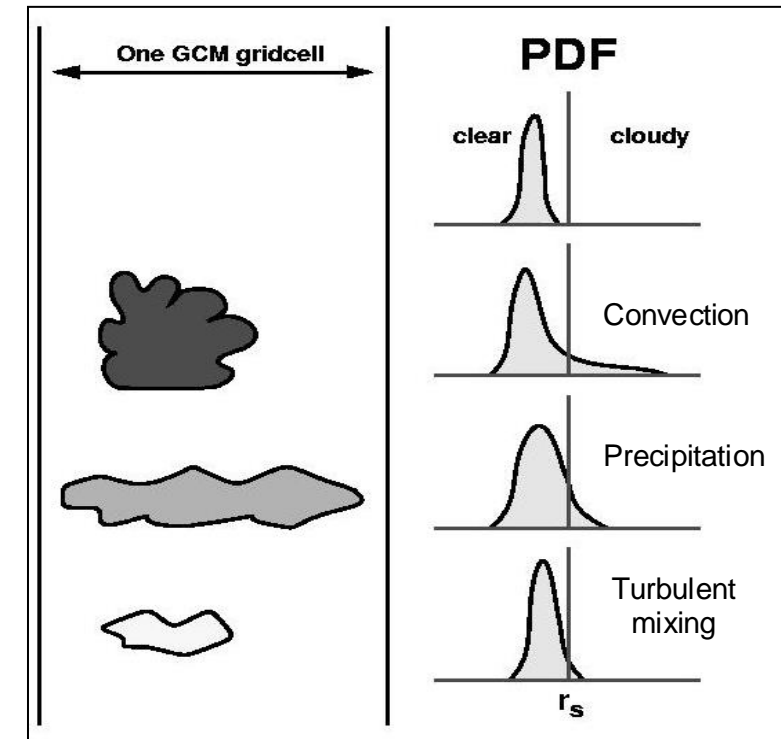
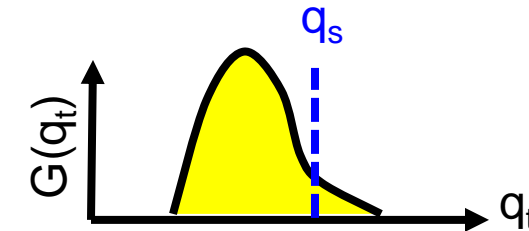
- (1) Bounded Beta function with positive skewness
- (2) Prognostic: Total water mean, condensate mean, upper bound
- (3) ~3 degrees of freedom + convection

## Advantages:

- Continuous bounded function, closer fit to obs
- Allows skewness
- Turbulence directly affects variance
- Treats sources/sinks other than turbulence (e.g. precipitation, convective detrainment)

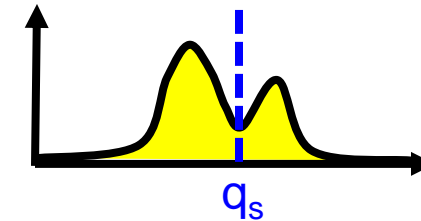
## Disadvantages:

- Assumes homogeneous temperature
- Some of the sources and sinks are rather ad-hoc in their derivation.
- Implemented in ECHAM but positive skewness only (Weber et al. 2011)



# Prognostic PDF high order closure scheme: Golaz et al. (2002), CLUBB

- (1) Joint double Gaussian  $P(w, \theta_l, q_t)$
- (2) Prognostic:  $w, \theta_l, q_t, w'^2, \theta_l'^2, q_t'^2, w'\theta_l', w'q_t', \theta_l'q_t', w'^3$   
Diagnostic: other third order moments
- (3) 10 degrees of freedom (6 ~cloudy)



## Advantages:

- Unifies treatment of boundary layer turbulence, shallow conv & subgrid cloud
- Both shallow Cu and Sc clouds described by a single consistent equation set. (Golaz et al. 2002; 2007; Larson and Golaz 2005, Larson et al. 2012)
- Flexible PDF fits observations (Larson et al. 2001)
- Use predicted vertical velocity ( $w$ ) for aerosol activation?
- Tested in WRF, CAM (Bogenschutz et al. 2013), GFDL (Guo et al. 2014)

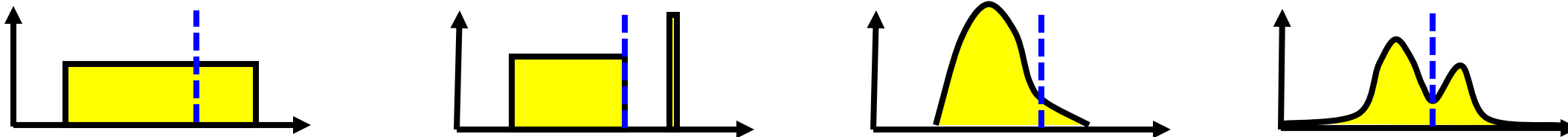
## Disadvantages:

- Computationally more expensive (7 new prognostic equations)
- Needs short timestep (seconds)
- Doesn't contain effects of all processes (ice supersaturation, precipitation)

## Other schemes:

- Bogenschutz and Krueger (2013) – simplified and computationally efficient rewrite making higher order moments diagnostic – needs good SGS TKE

## Representing sub-grid heterogeneity: Key characteristics for the PDF?



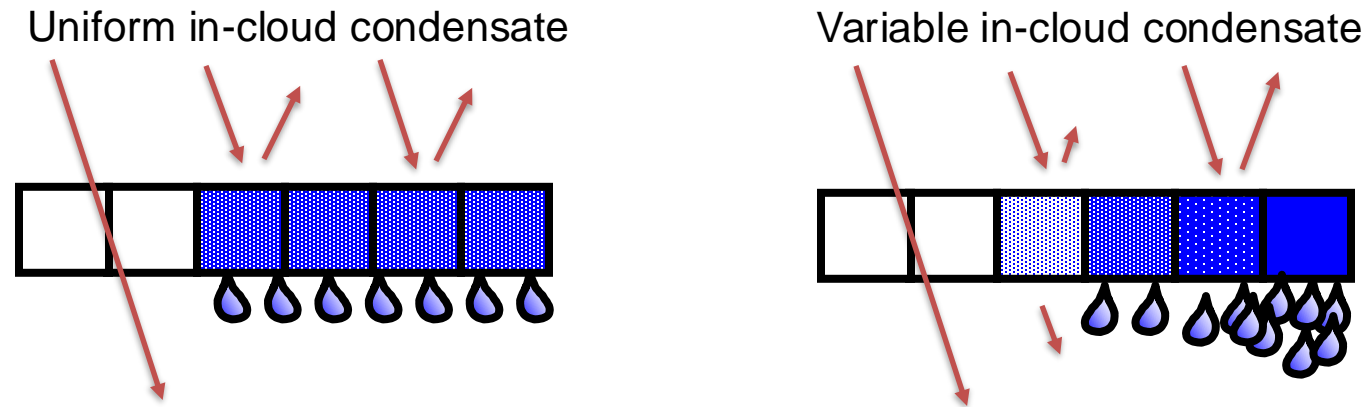
- Obs suggest PDFs can generally be approximated by uni or bi-modal distributions, describable by a few parameters.
- Almost all schemes can be formulated in terms of an “assumed PDF”, but vary widely in PDF form, diagnostic and prognostic variables and degrees of freedom.
- Many different schemes are used in NWP/climate models, but the most important characteristics of a scheme are:
  1. To represent sub-grid cloud fraction – if  $q$  or  $q_s(T)$  changes, how does this affect cloud fraction/condensate
  2. To represent subgrid heterogeneity of condensate – for unbiased radiation, microphysics
  3. Enough degrees of freedom to represent the main variations in different cloud regimes – mean, variance and skewness (skewed PDF for convection – can have low grid-box mean humidity, but convective clouds in part of the gridbox)



# Representing in-cloud sub-grid heterogeneity of cloud/precipitation

Representation of subgrid heterogeneity of cloud (and precipitation) important for radiation and microphysics:

- Radiation – non-linear impact of cloud optical thickness
- Microphysics – non-linear impact on autoconversion, and accretion (covariance of cloud and rain)



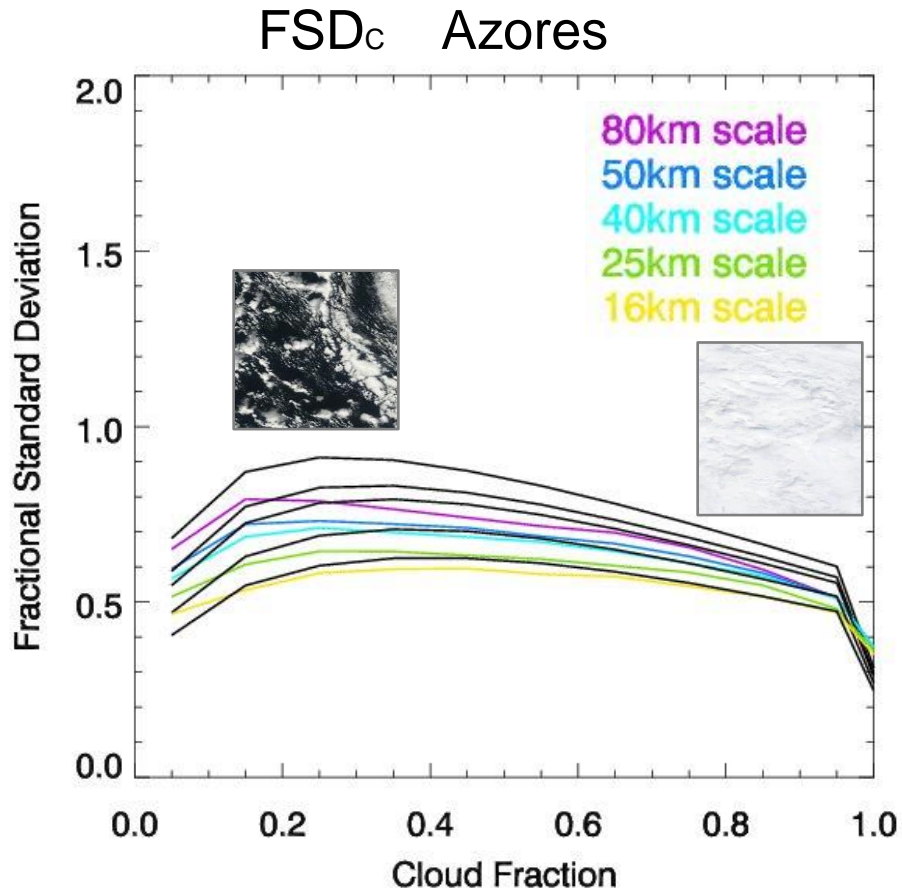
A simple measure of the variability that can be used as a modification to the radiation optical depth and autoconversion/accretion calculations is the **fractional standard deviation** of the condensate PDF (the standard deviation divided by the mean) which can be derived from observations:

$$FSD_c = stdev(q_c) / mean(q_c)$$

# Representing in-cloud sub-grid heterogeneity of cloud/precipitation

## Parametrizing fractional standard deviation of condensate

$$FSD_c = stdev(q_c) / mean(q_c)$$



e.g. Boutle et al. (2014), Ahlgrimm and Forbes (2016)

Parameterize as a function of **cloud fraction** and **scale length**.

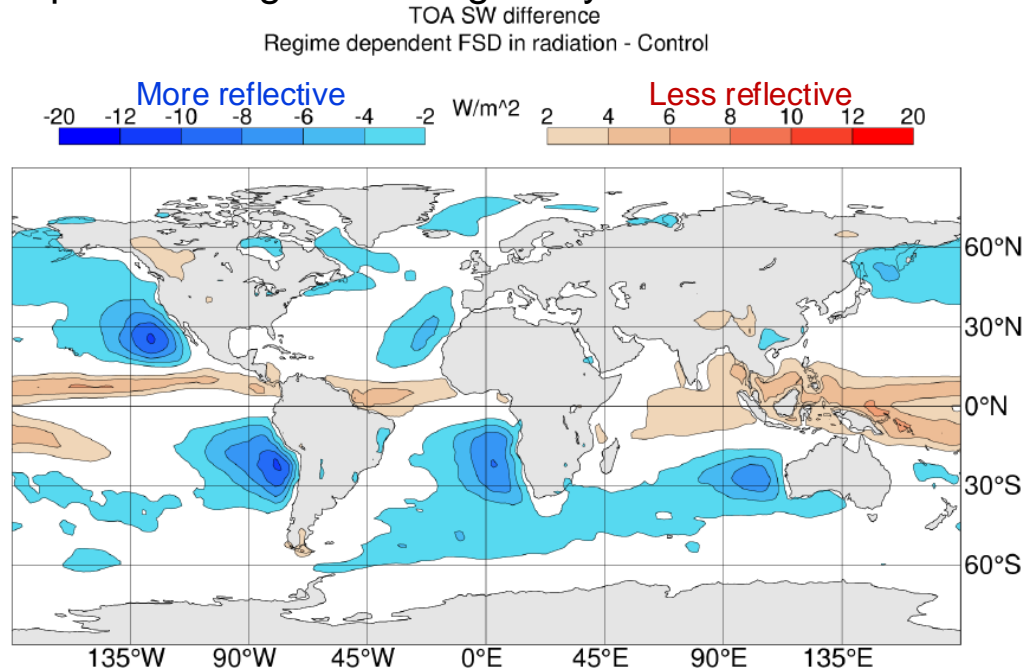
Captures the observed variation of FSD at multiple sites, different regimes

Use for radiation (McICA) and microphysics

# Representing in-cloud sub-grid heterogeneity of cloud/precipitation

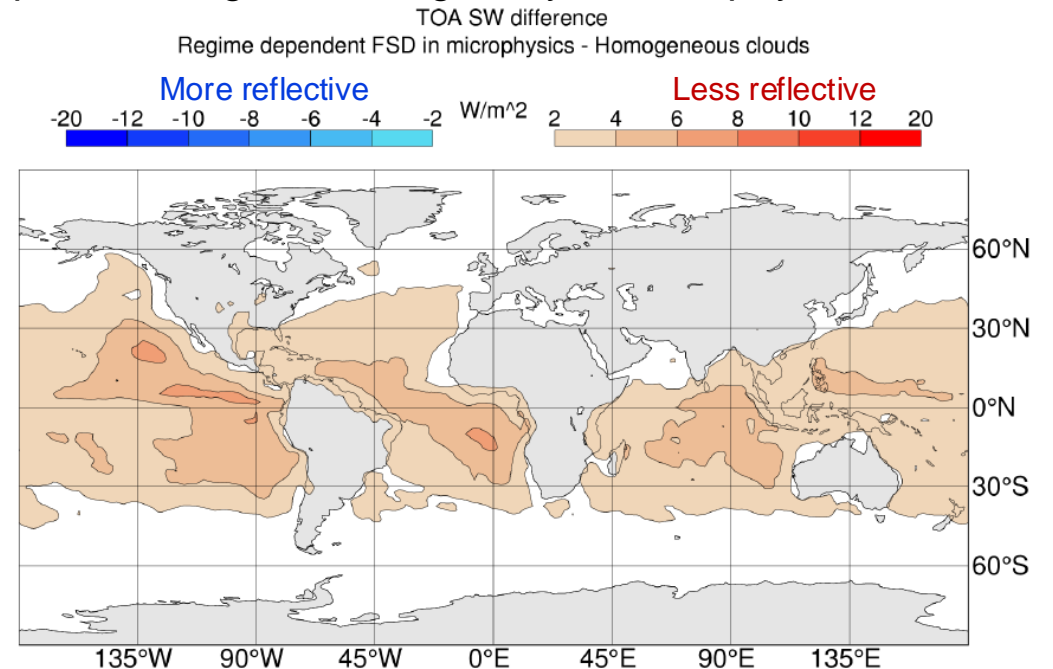
## Impact of representing subgrid heterogeneity of cloud liquid water on top-of-atmosphere shortwave radiation (IFS model climate)

### Impact of subgrid-heterogeneity in radiation scheme



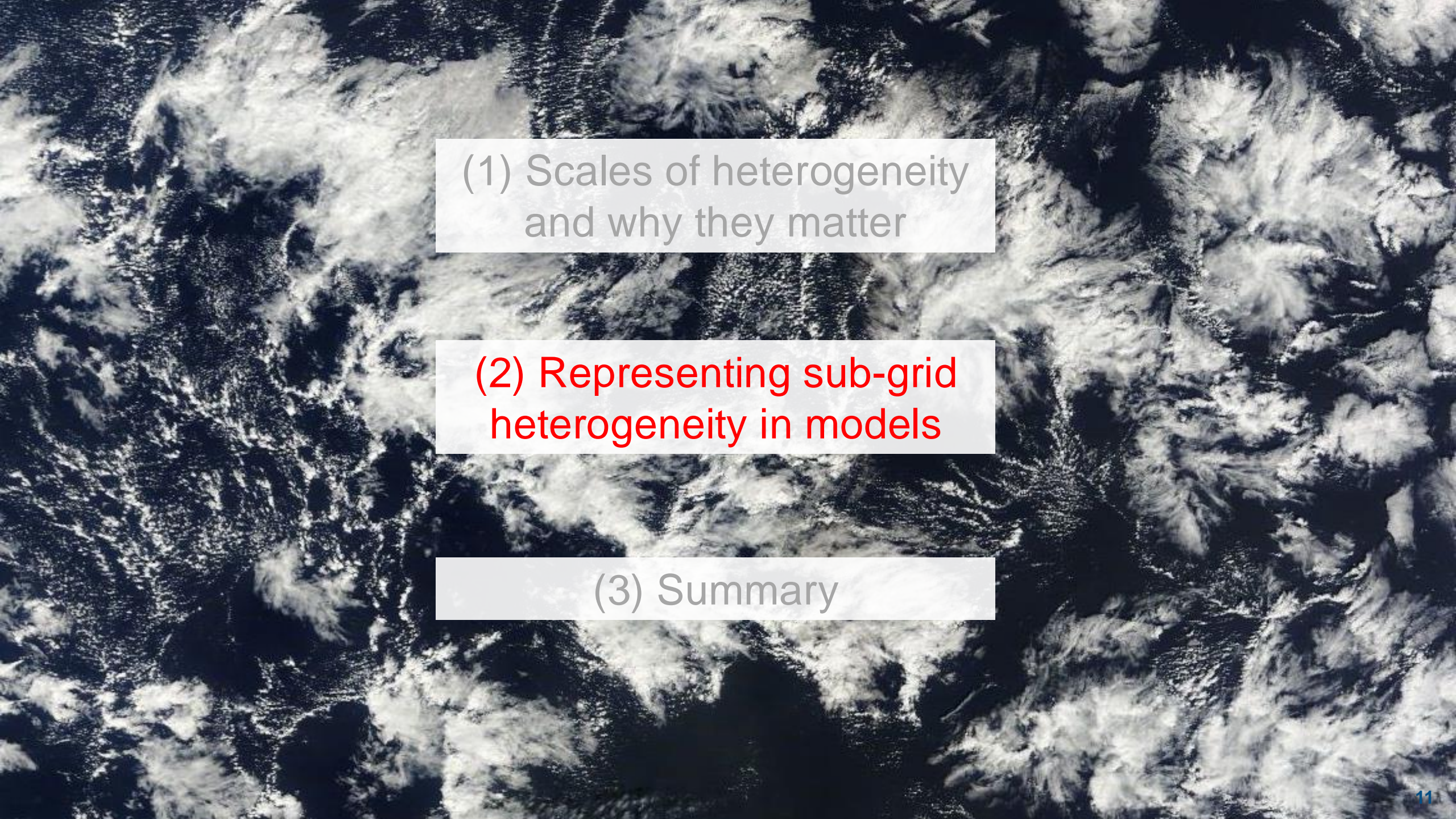
Stratocumulus cloud (high cloud fraction) more uniform reflective than standard FSD=0.7 and less reflective in highly heterogeneous tropical deep convection along ITCZ

### Impact of subgrid-heterogeneity in microphysics scheme



Autoconversion and accretion rates higher when include heterogeneity, so less cloud water and less reflection of SW radiation





(1) Scales of heterogeneity  
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(3) Summary



## Summary: Representing subgrid scale heterogeneity

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- Representing sub-gridscale heterogeneity in GCMs is important for cloud formation, microphysical processes, radiation etc. (still required sub-10km, even at 1km)
- BL turbulence, shallow convection, deep convection, cloud scheme are all part of the sub-grid representation. Important to have consistency of assumptions between schemes.
- High order closure turbulence schemes unifying BL/Cu processes with assumed PDF work well for liquid-phase turbulent boundary layers, but not so straight forward to include subgrid ice phase, mixed-phase and precipitation, vertical overlap, or representing deep convection – ongoing research topics.
- More complex schemes with higher degrees of freedom allow greater flexibility to represent the real atmosphere, but we need to have enough knowledge/information to understand and constrain the assumptions in the schemes (globally in all meteorological regimes). Can simpler schemes be as effective in terms of their impacts?
- Conceptual framework important, but details matter! – specification of sources and sinks, numerical solutions...

# Key driving concepts for the parametrization

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- Fidelity – improved realism, physical basis
- Consistency – across parametrizations
- Convergence – across resolutions
- Complexity vs Cost vs Uncertainty
- Focus on impacts – radiative, thermodynamical, hydrological



An aerial, high-contrast black and white photograph of a turbulent ocean. The water is dark, and the waves are covered in white foam, creating a complex, swirling pattern across the entire frame. The lighting emphasizes the texture and movement of the water.

# Questions?