

# Microwave spectrum

Measurement, modelling and information content

Alan Geer

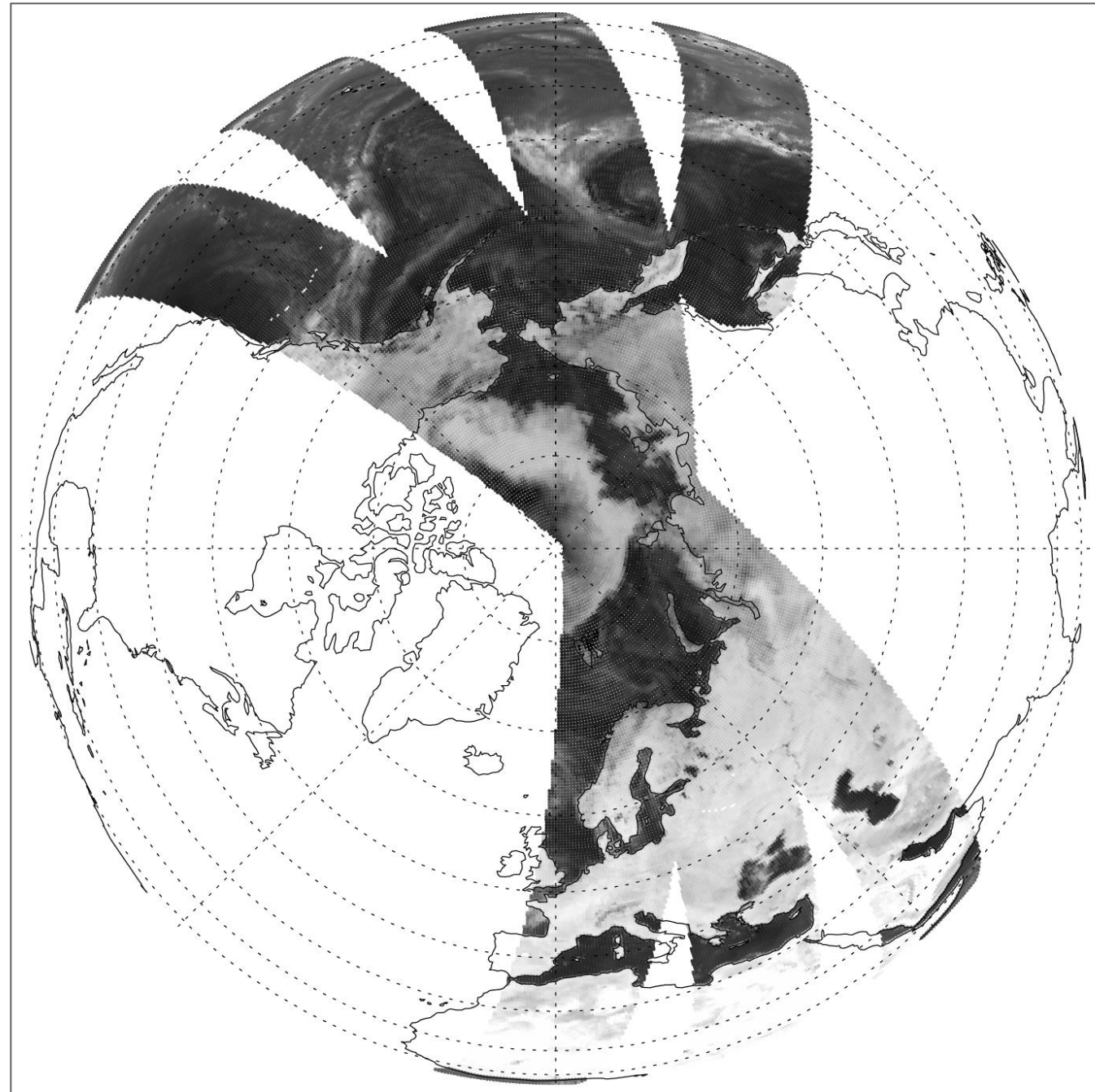
Thanks to: Peter Bauer, Bill Bell

EUMETSAT/ECMWF NWP-SAF satellite data assimilation training course, 11 – 15 March, 2024

# Advanced Scanning Microwave Radiometer (AMSR-2)

Observation composite for 1<sup>st</sup>  
Nov 2021

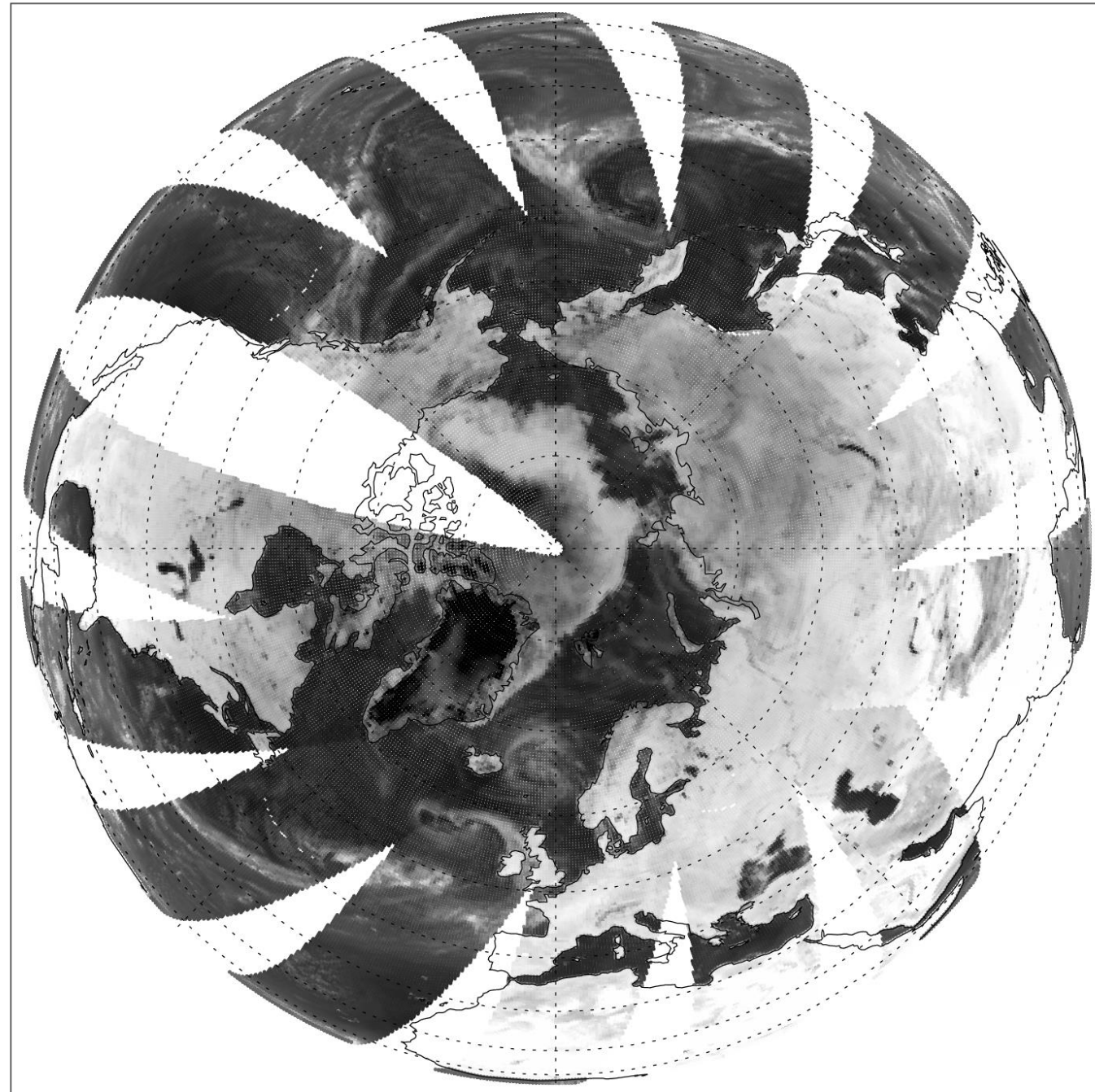
Brightness temperatures  
[Kelvin] at 37 GHz, v-polarised



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Observation composite for 1<sup>st</sup>  
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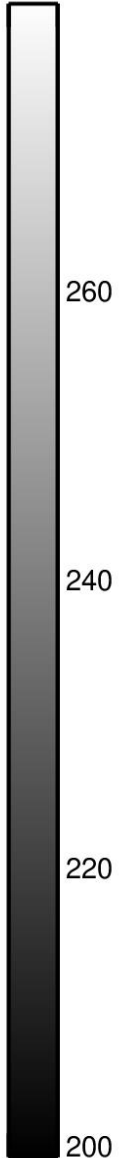
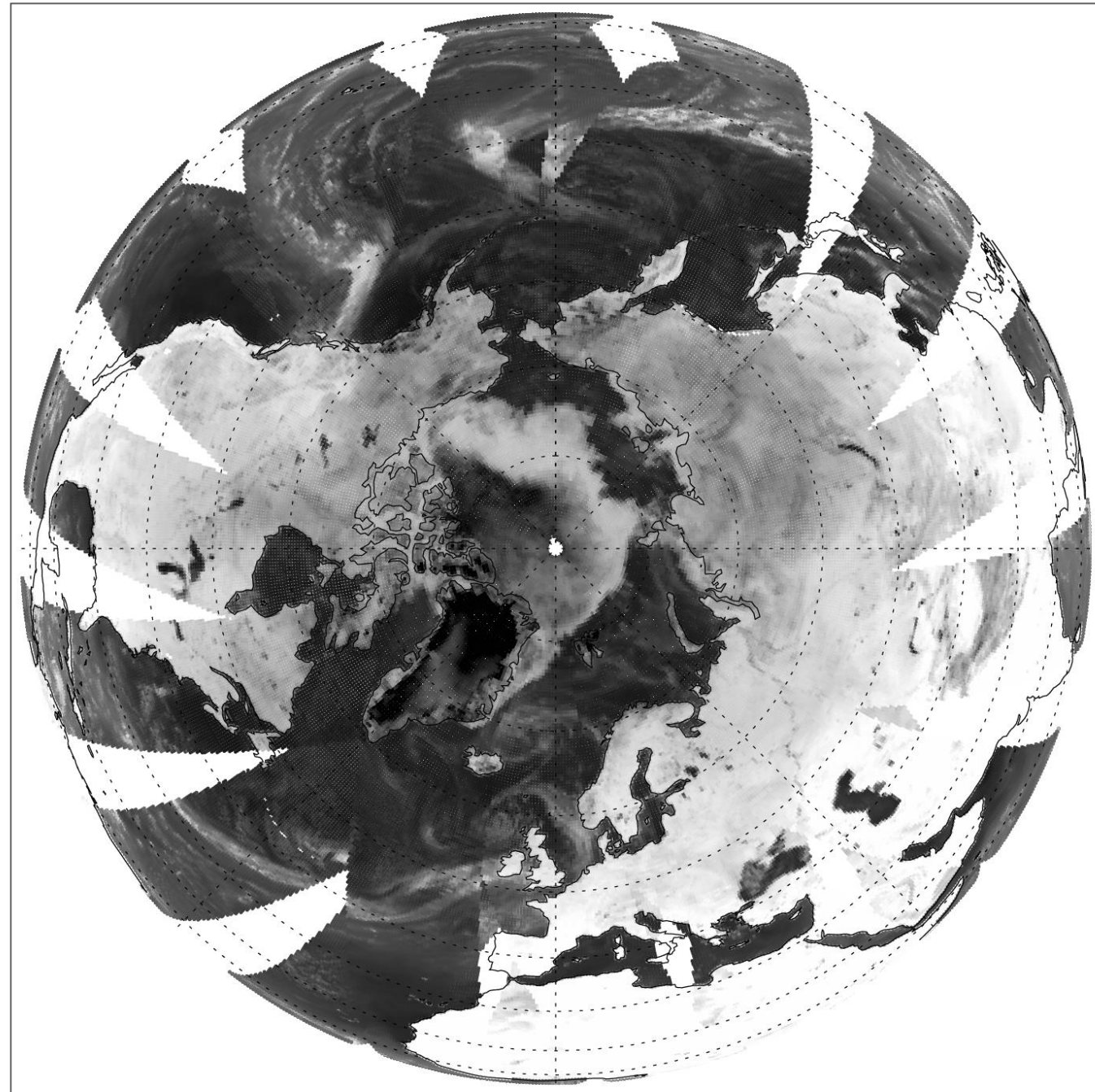
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# Advanced Scanning Microwave Radiometer (AMSR-2)

Observation composite for 1<sup>st</sup>  
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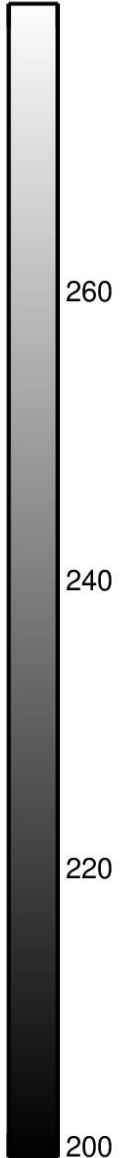
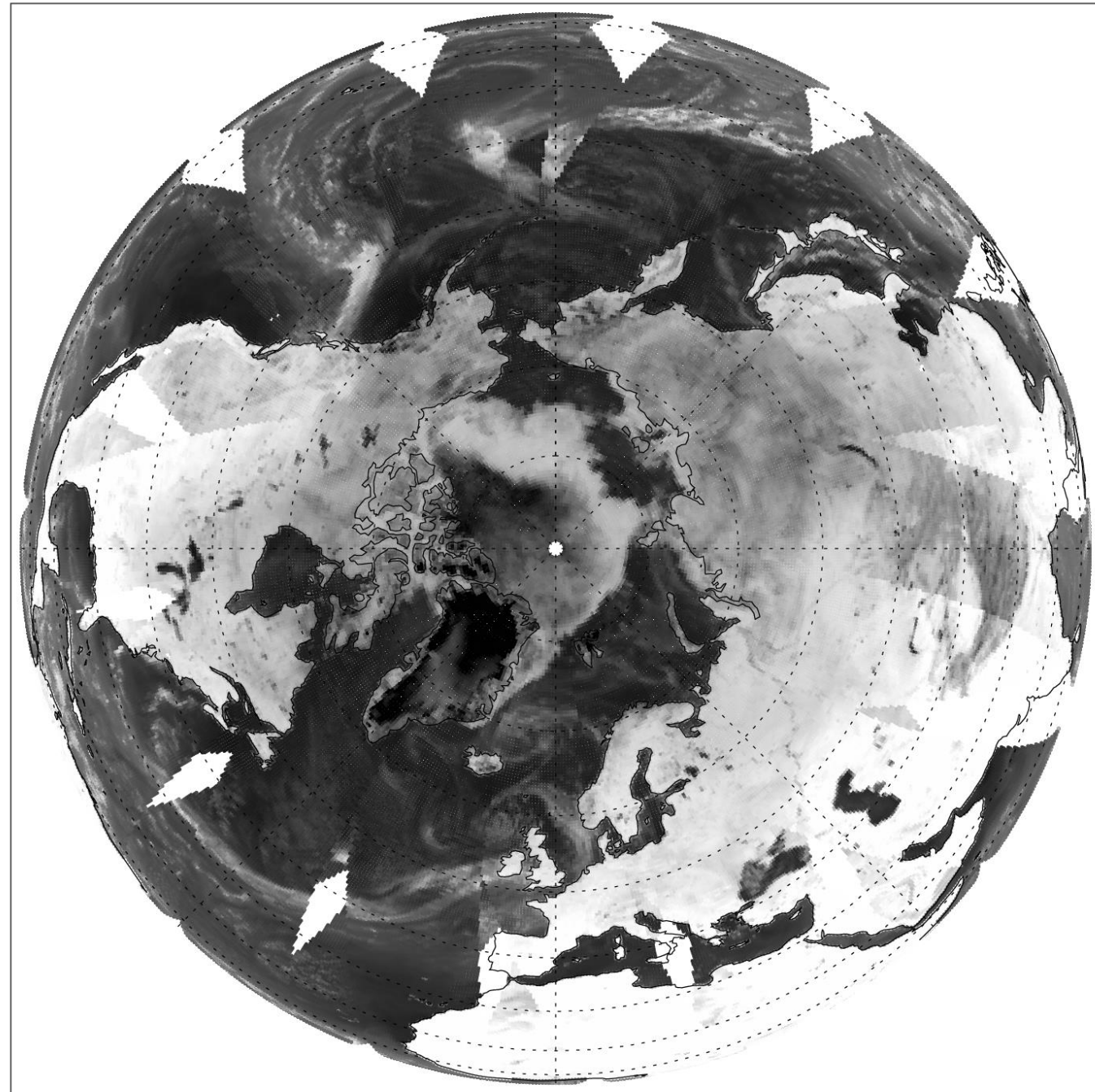
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# Advanced Scanning Microwave Radiometer (AMSR-2)

Observation composite for 1<sup>st</sup>  
Nov 2021

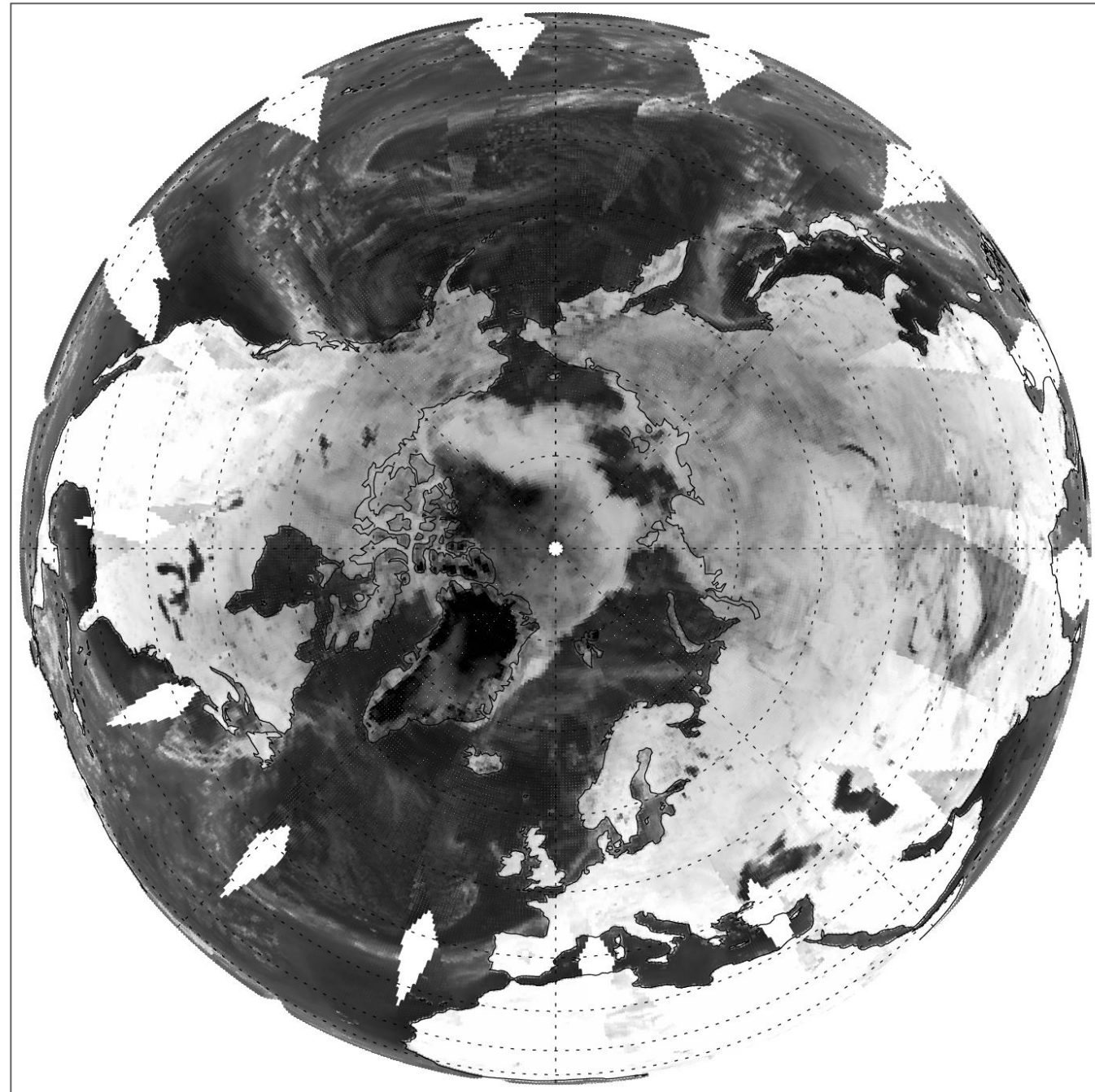
Brightness temperatures  
[Kelvin] at 37 GHz, v-polarised



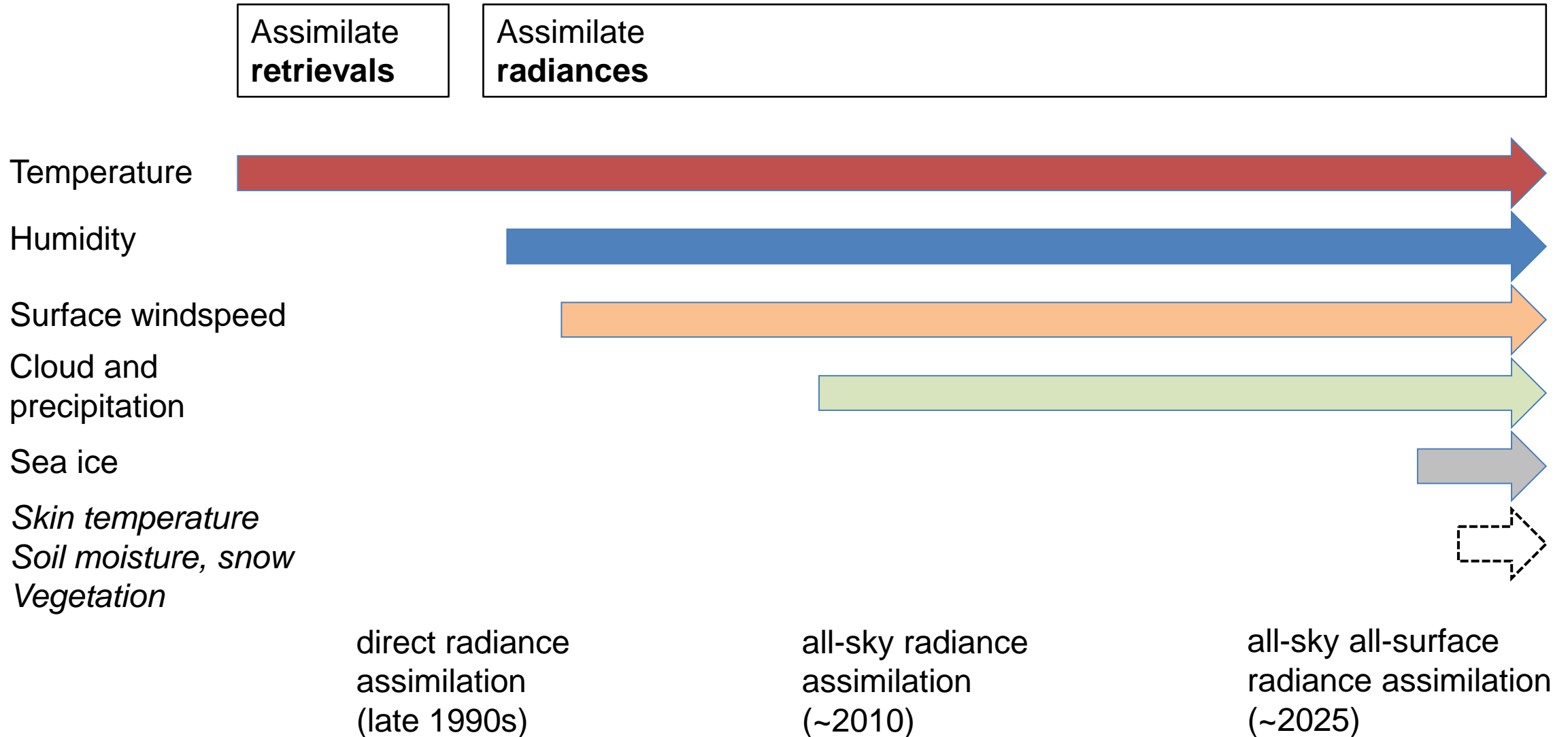
# Advanced Scanning Microwave Radiometer (AMSR-2)

Observation composite for 2<sup>nd</sup>  
Nov 2021

**Radiances** shown as  
brightness temperatures  
[Kelvin] at 37 GHz, v-polarised



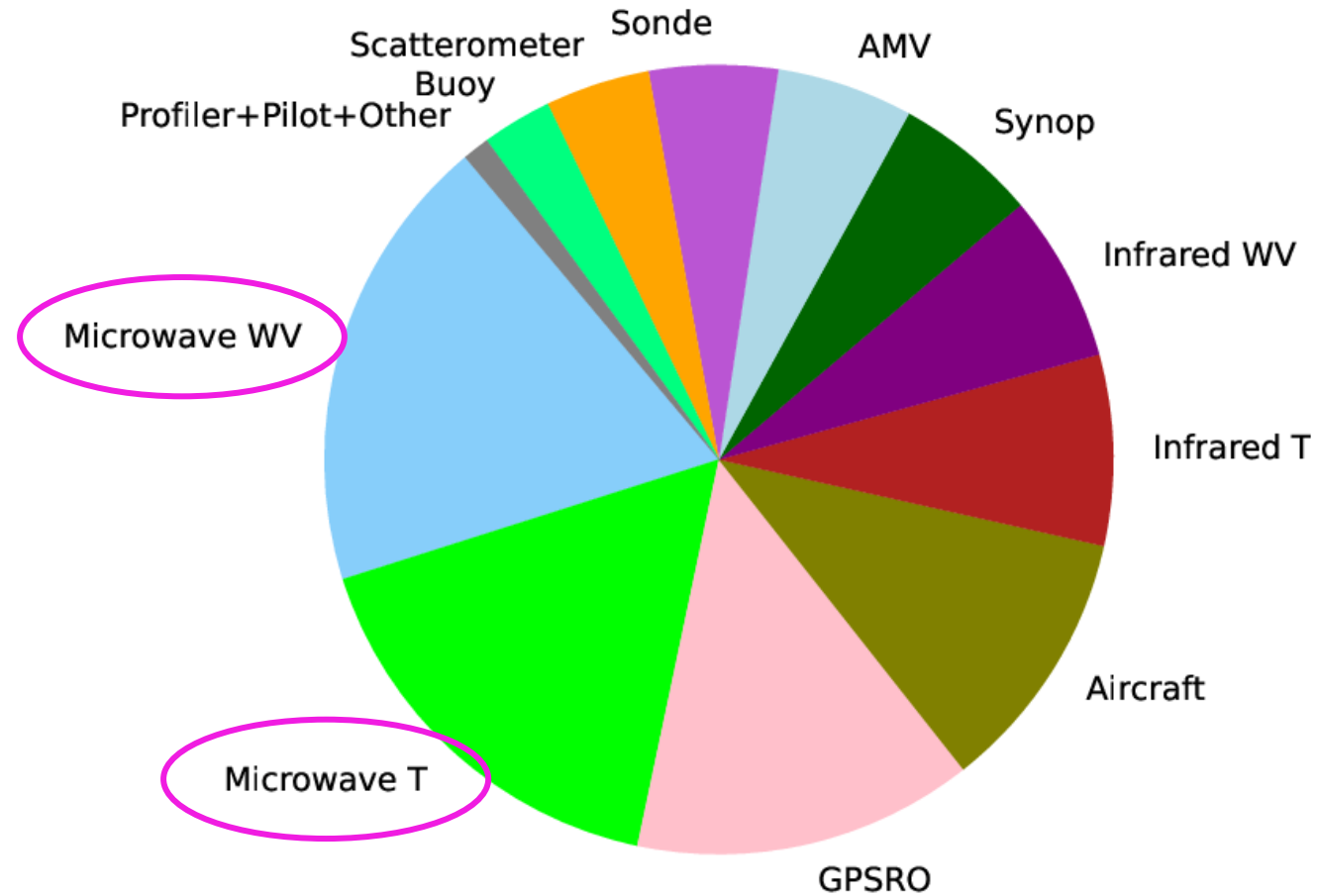
# Rough timeline of satellite microwave data assimilation in 'atmospheric' DA



# Relative impact of observations at ECMWF: February 2024

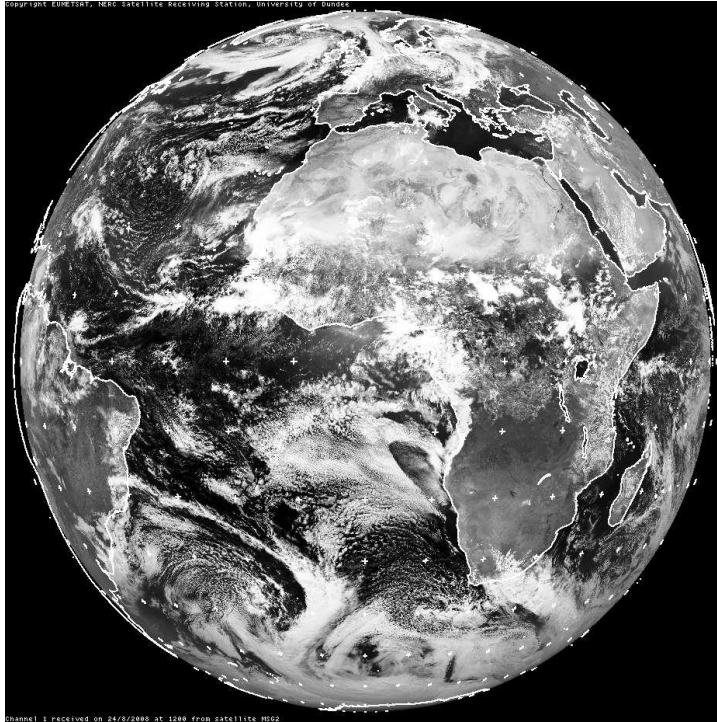
ops 1-Feb-2024 to 29-Feb-2024

Relative sensitivity  
of 24 hour forecast  
error to observation  
impact (FSOI)



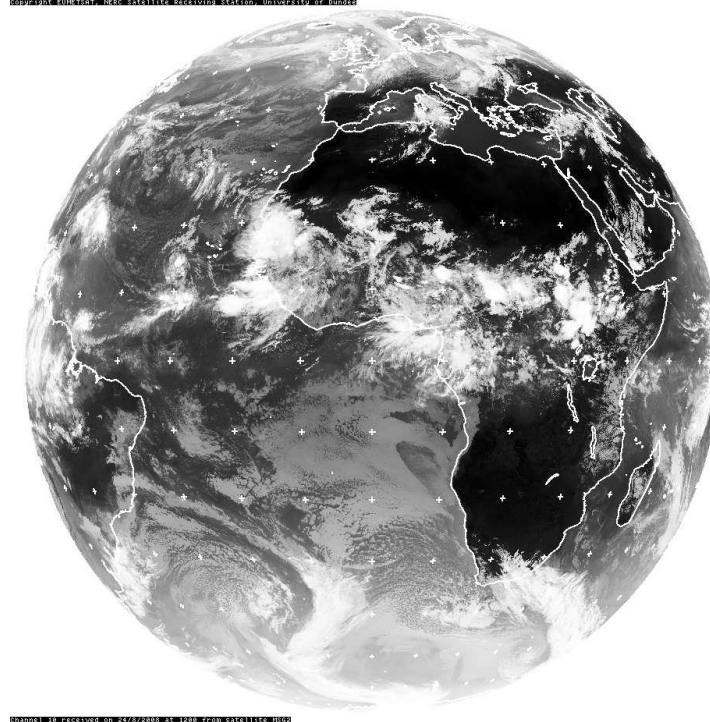


# Visible, infrared and microwave views of the earth



## Visible

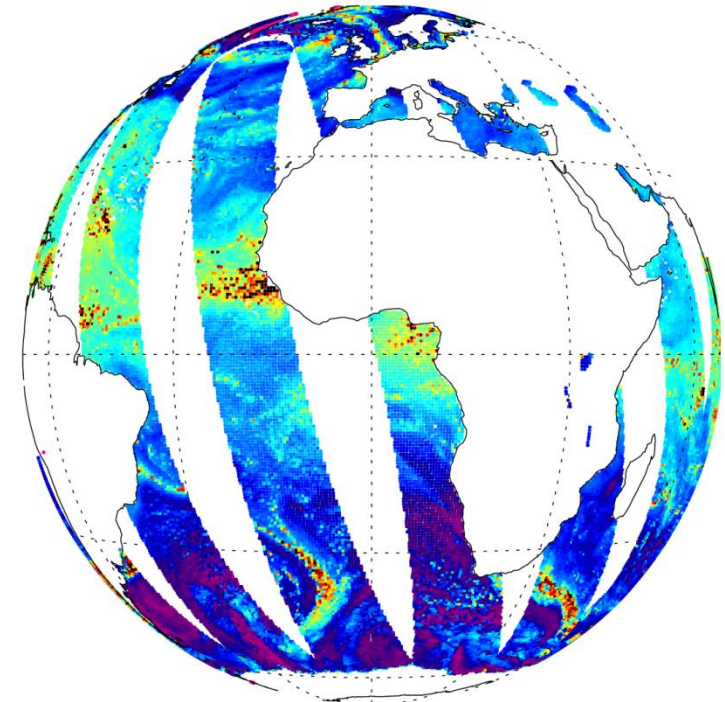
SEVIRI channel 1  
0.56-0.71  $\mu\text{m}$



## Infrared

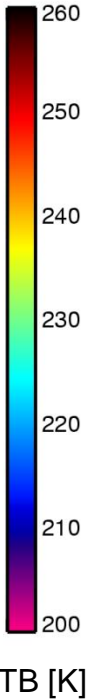
SEVIRI channel 10  
11-13  $\mu\text{m}$

\*reverse colour scale – bright is really cold/dim

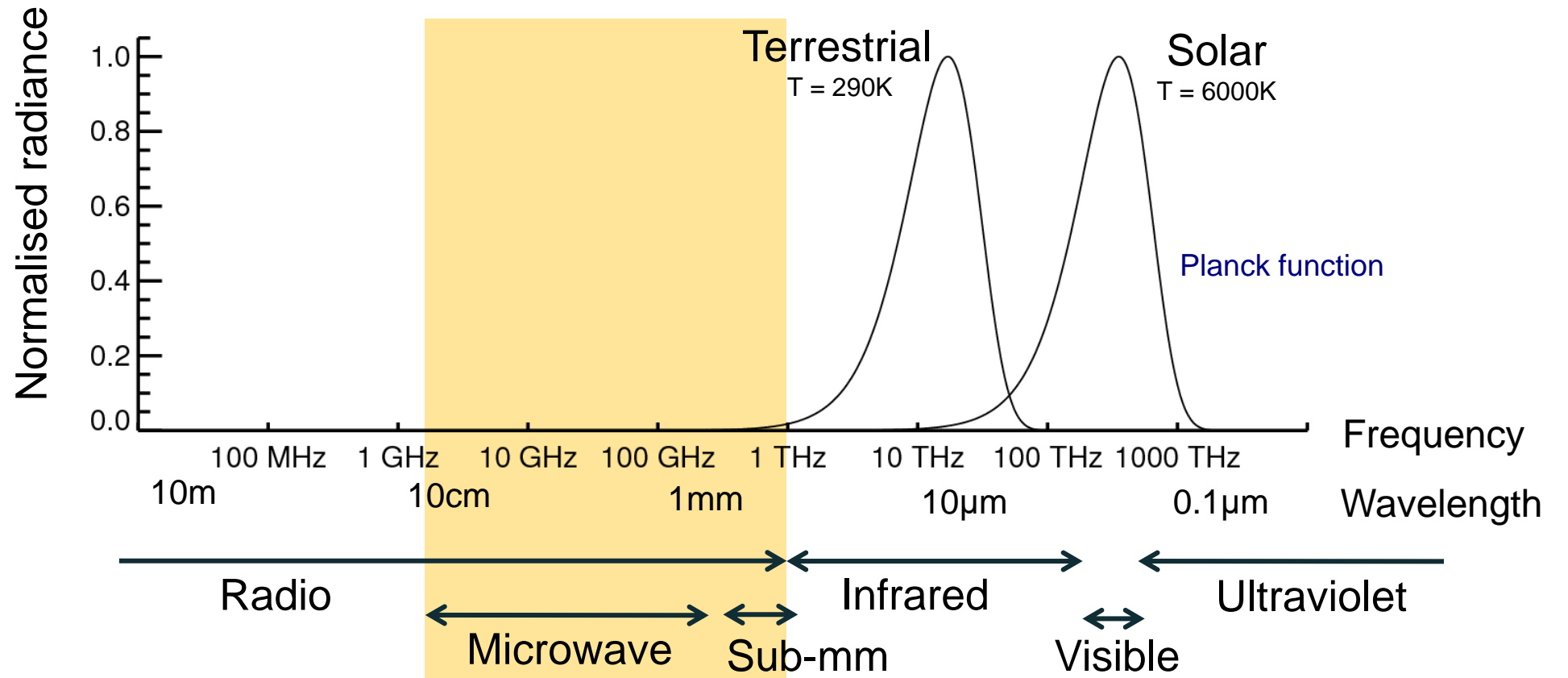
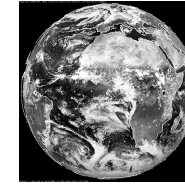
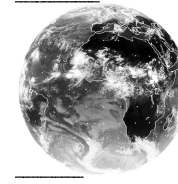
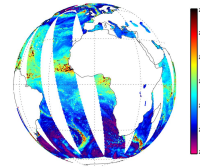


## Microwave

AMSR-E channel 37v  
8108  $\mu\text{m}$  (37 GHz v-pol)



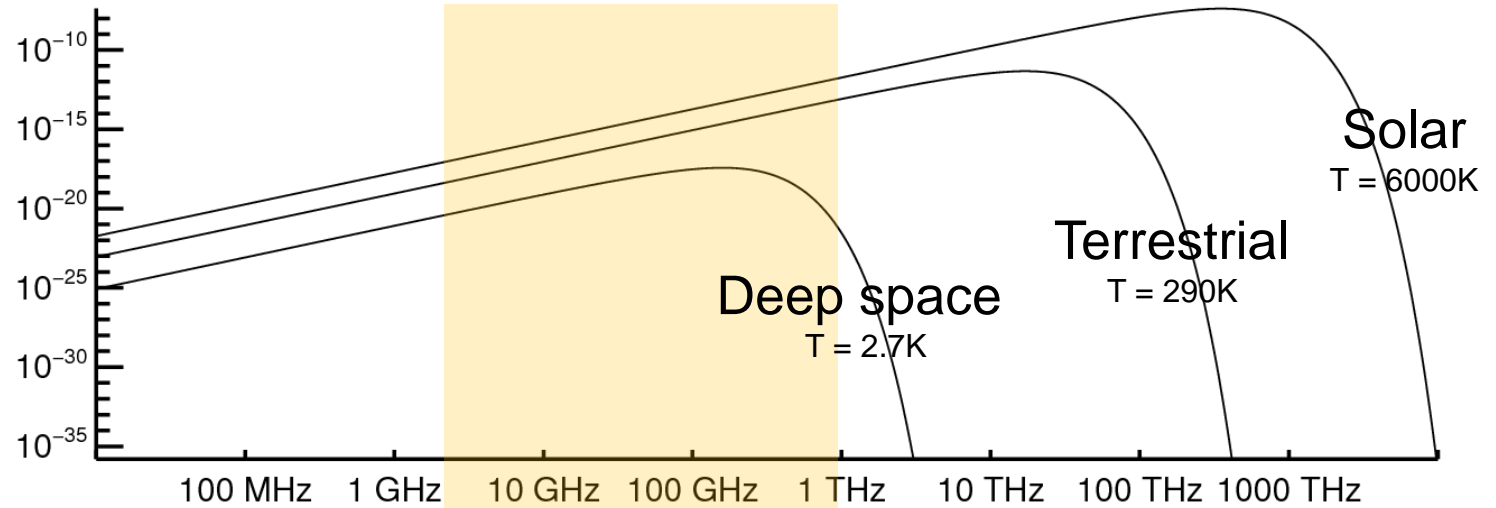
# Where is the microwave in the electromagnetic spectrum?



# How much energy?

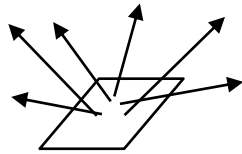
Travelling in a beam

Planck Function Radiance  
 $W m^{-2} sr^{-1} Hz^{-1}$

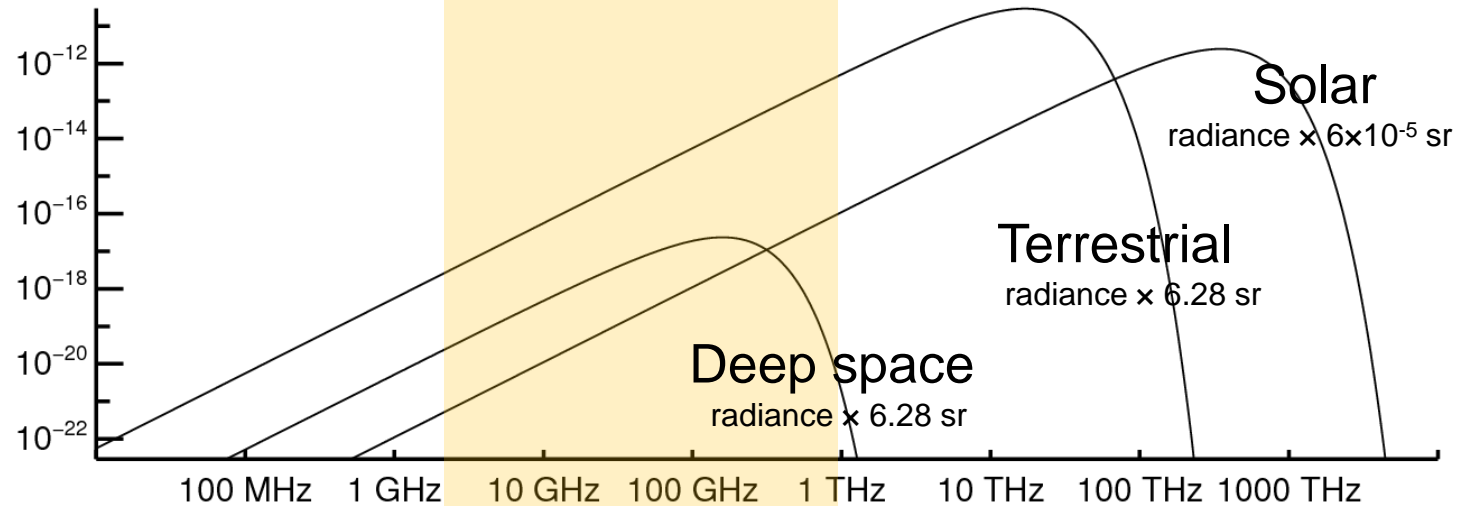


Travelling through an area (in one direction)

Flux  
 $W m^{-2} Hz^{-1}$



sr – Steradian (unit of solid angle)



Microwave

# Radiance and brightness temperature

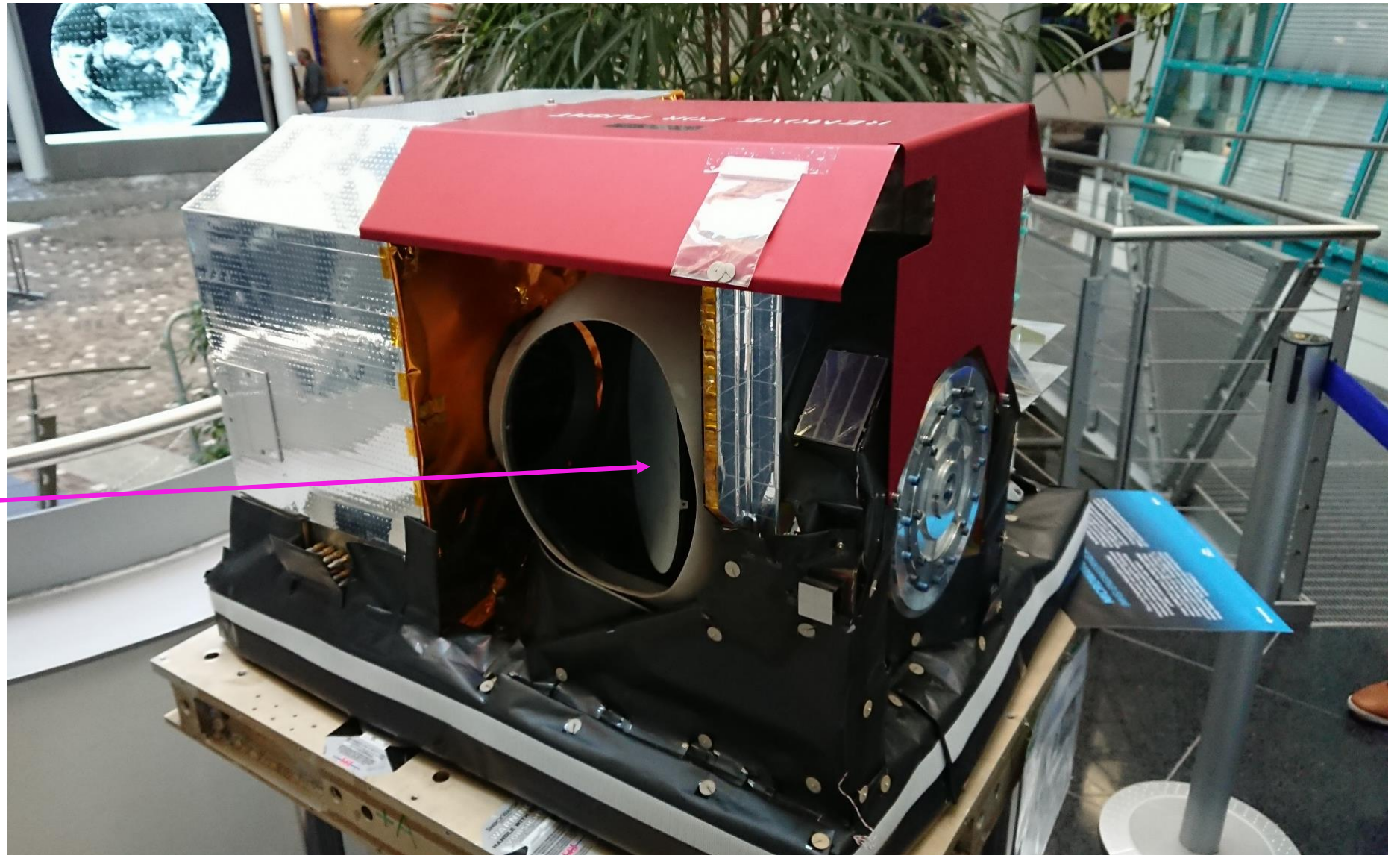
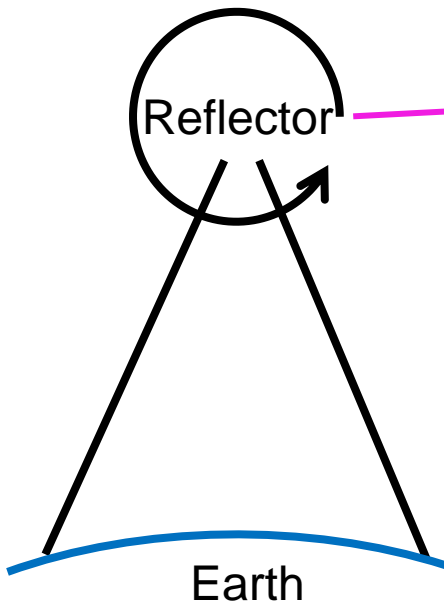
- Radiance:  $\text{W m}^{-2} \text{sr}^{-1} \text{Hz}^{-1}$ 
  - Watts (energy)
  - per metre squared
  - per unit of “direction” (solid angle)
  - per unit frequency
- Planck’s function (Rayleigh-Jeans approximation, valid in microwave)

$$\text{Radiance} \longrightarrow B_{\lambda}(T_B) = \frac{2c}{\lambda^4} k_B T_B \longleftarrow \text{Brightness temperature}$$

$c$  = speed of light;  $\lambda$  = wavelength;  $k_B$  = Boltzmann’s constant

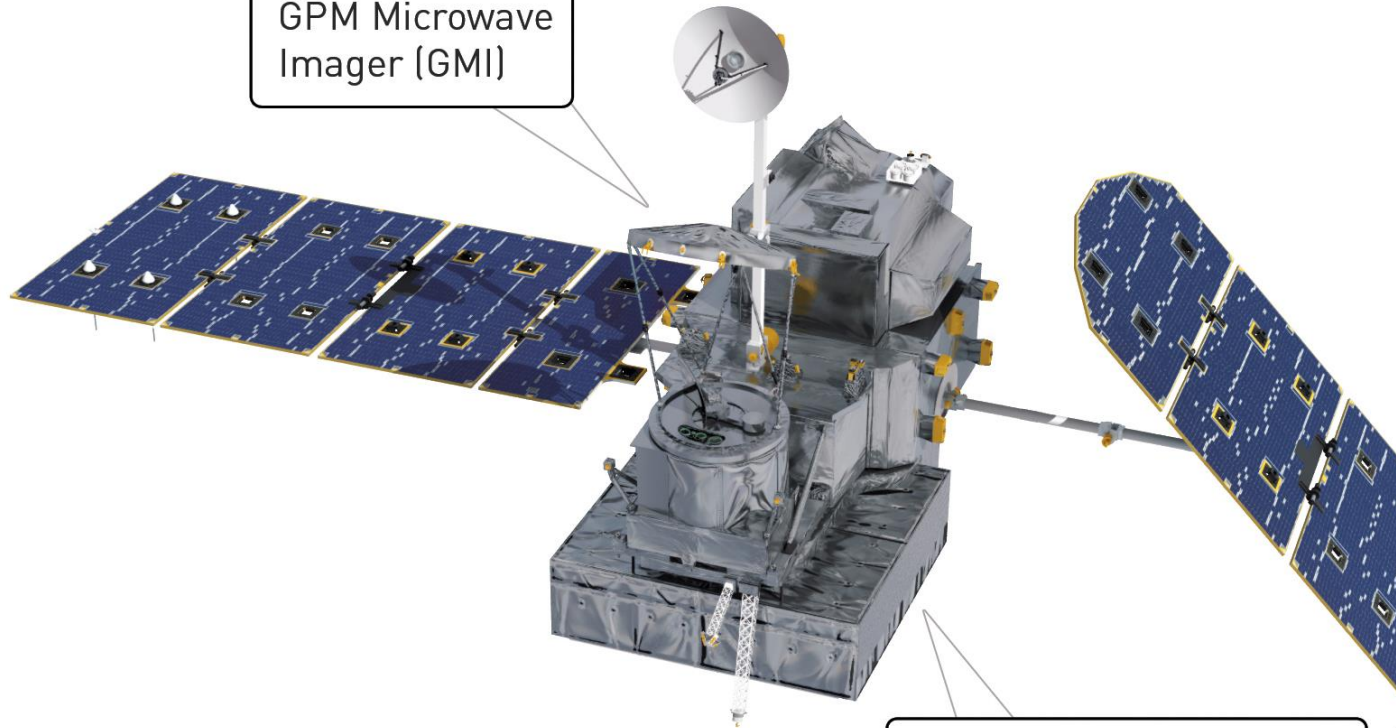
# The Microwave Humidity Sounder (MHS) at EUMETSAT

Cross-track sounder



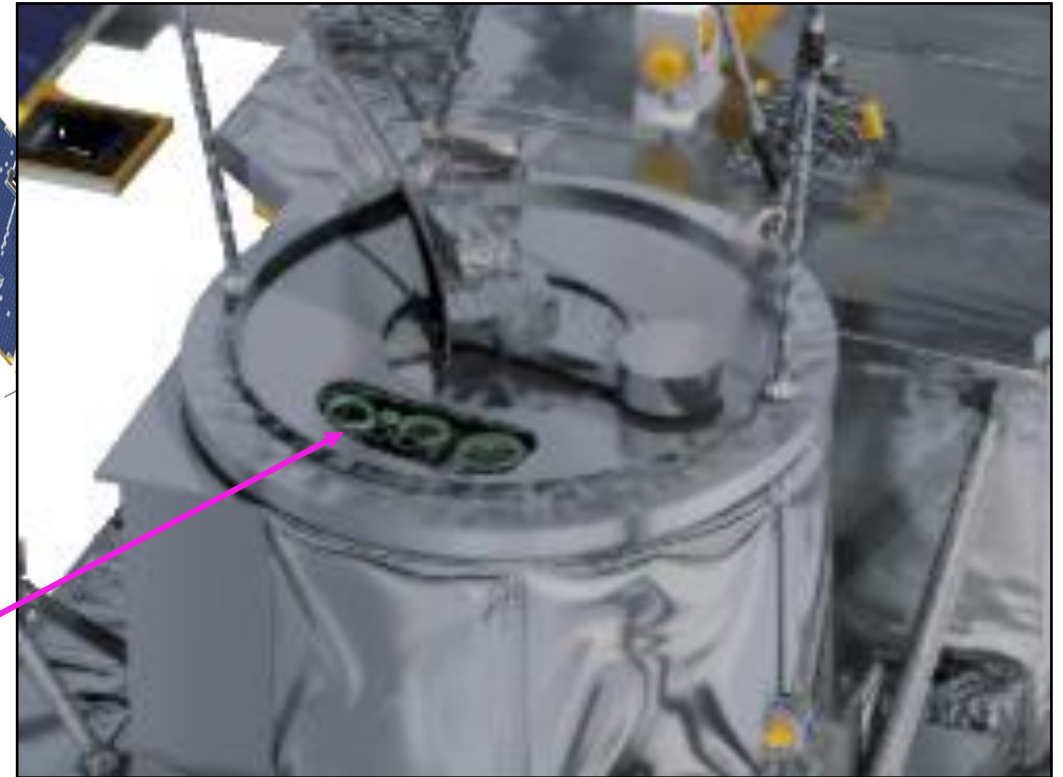
# Global precipitation mission (GPM)

GPM Microwave Imager (GMI)



Dual-Frequency Precipitation Radar (DPR)

Feedhorns

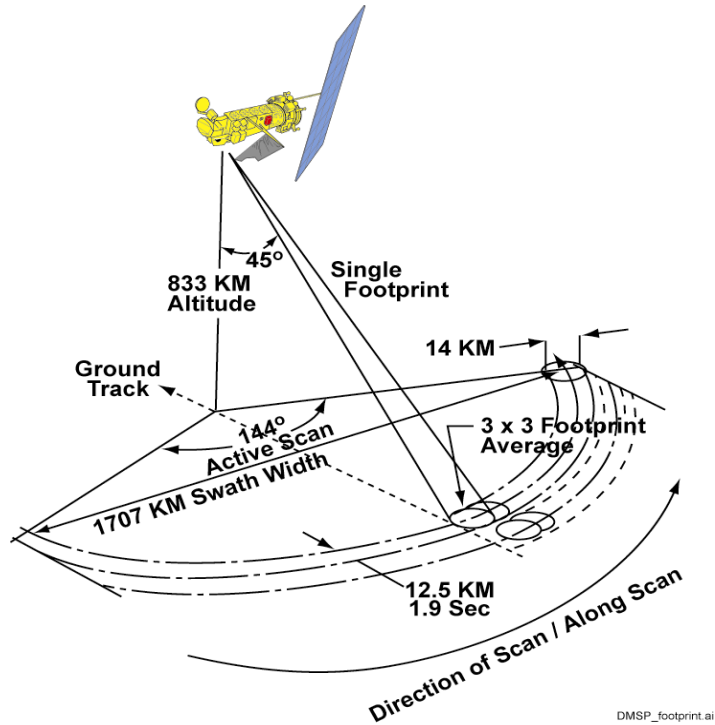


## Global precipitation mission:

- Launched Feb 2014

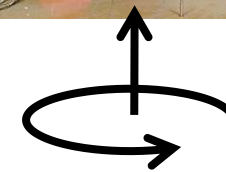
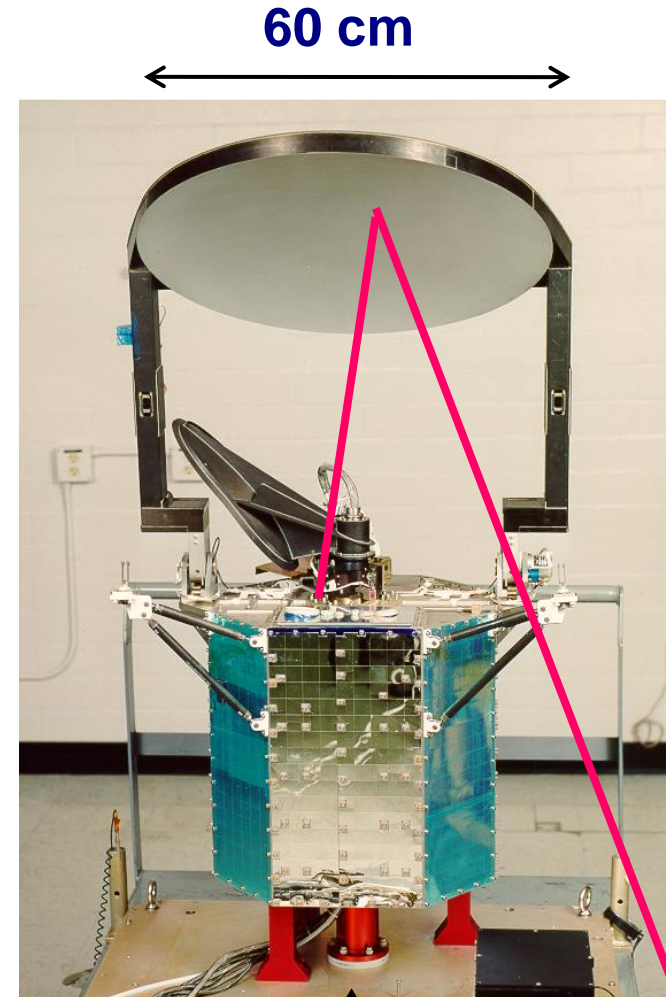
# Special Sensor Microwave Imager / Sounder (SSMIS)

Conical scanning geometry



Main Reflector

Cold Calibration Reflector  
Warm Load  
Feedhorns



From the earth

# Other users of the spectrum

3 KHz

## UNITED STATES FREQUENCY ALLOCATIONS THE RADIO SPECTRUM

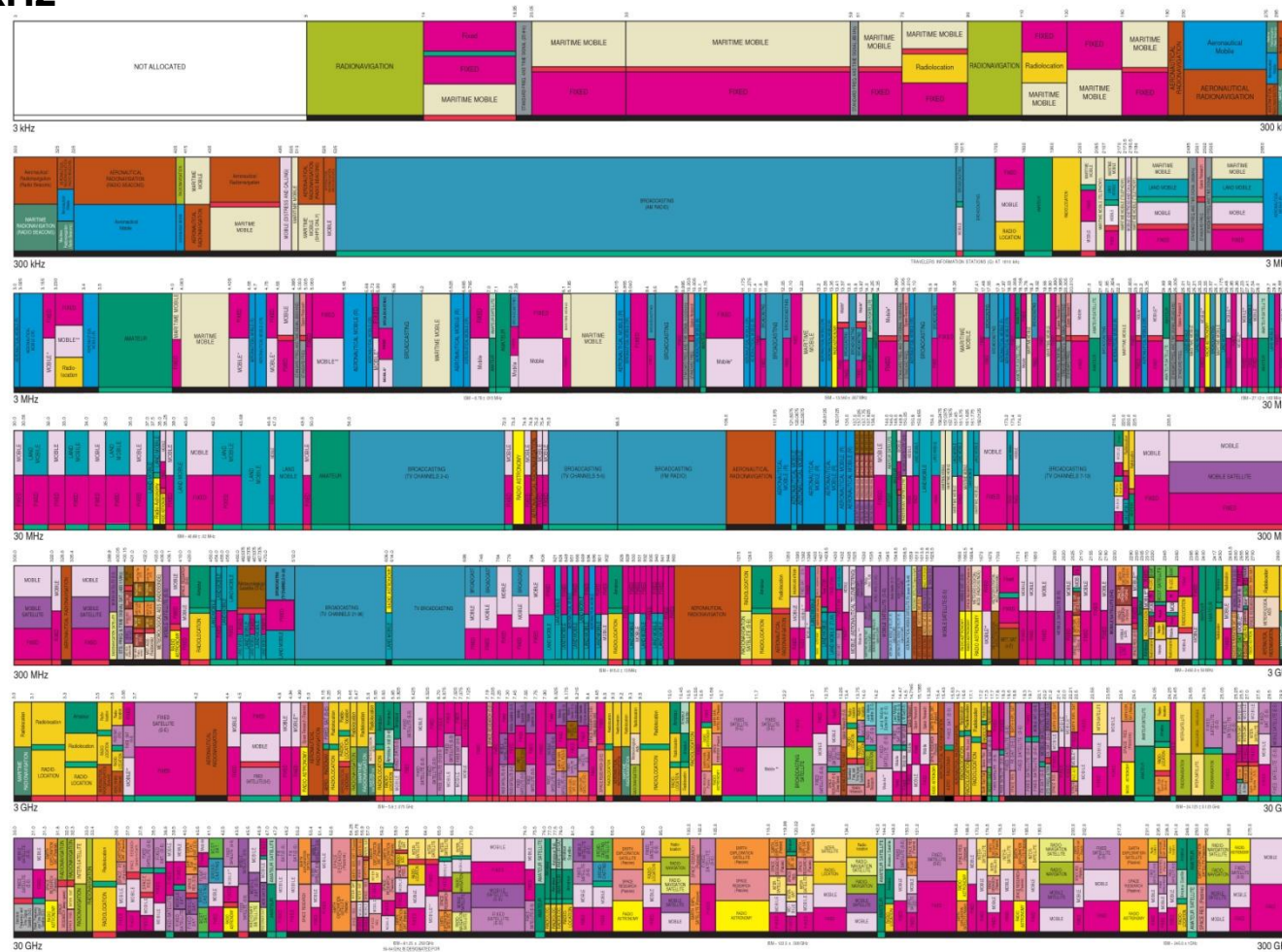
### RADIO SERVICES COLOR LEGEND


### ACTIVITY CODE


### ALLOCATION USAGE DESIGNATION

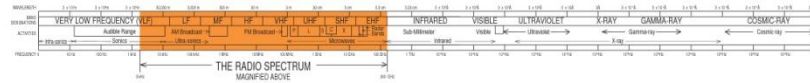
SERVICE	EXAMPLE	DESCRIPTION
Primary	FIXED	Capital Letters
Secondary	MOBILE	1st Capital with lower case letters

This chart is a graphic representation of the portion of the Table of Frequency Allocations used by the FCC and NTIA. It is not intended to be a substitute for the Table of Frequency Allocations. It is intended to provide a visual overview of the spectrum. It is not intended to be a substitute for the Table of Frequency Allocations. It is intended to provide a visual overview of the spectrum.



30 GHz

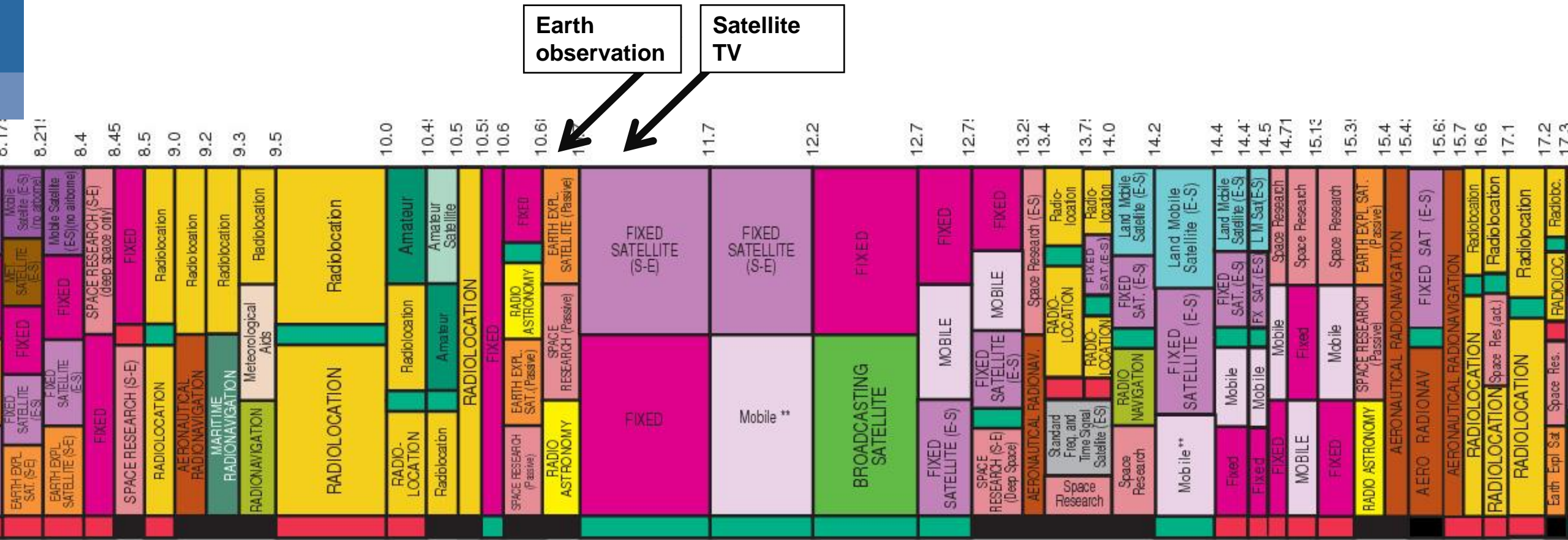
300 GHz



PLEASE NOTE: THE FREQUENCIES LISTED IN THIS CHART ARE SUBJECT TO CHANGE WITHOUT NOTICE. FOR THE MOST CURRENT INFORMATION, PLEASE VISIT THE FOLLOWING WEBSITE: <http://www.fcc.gov>

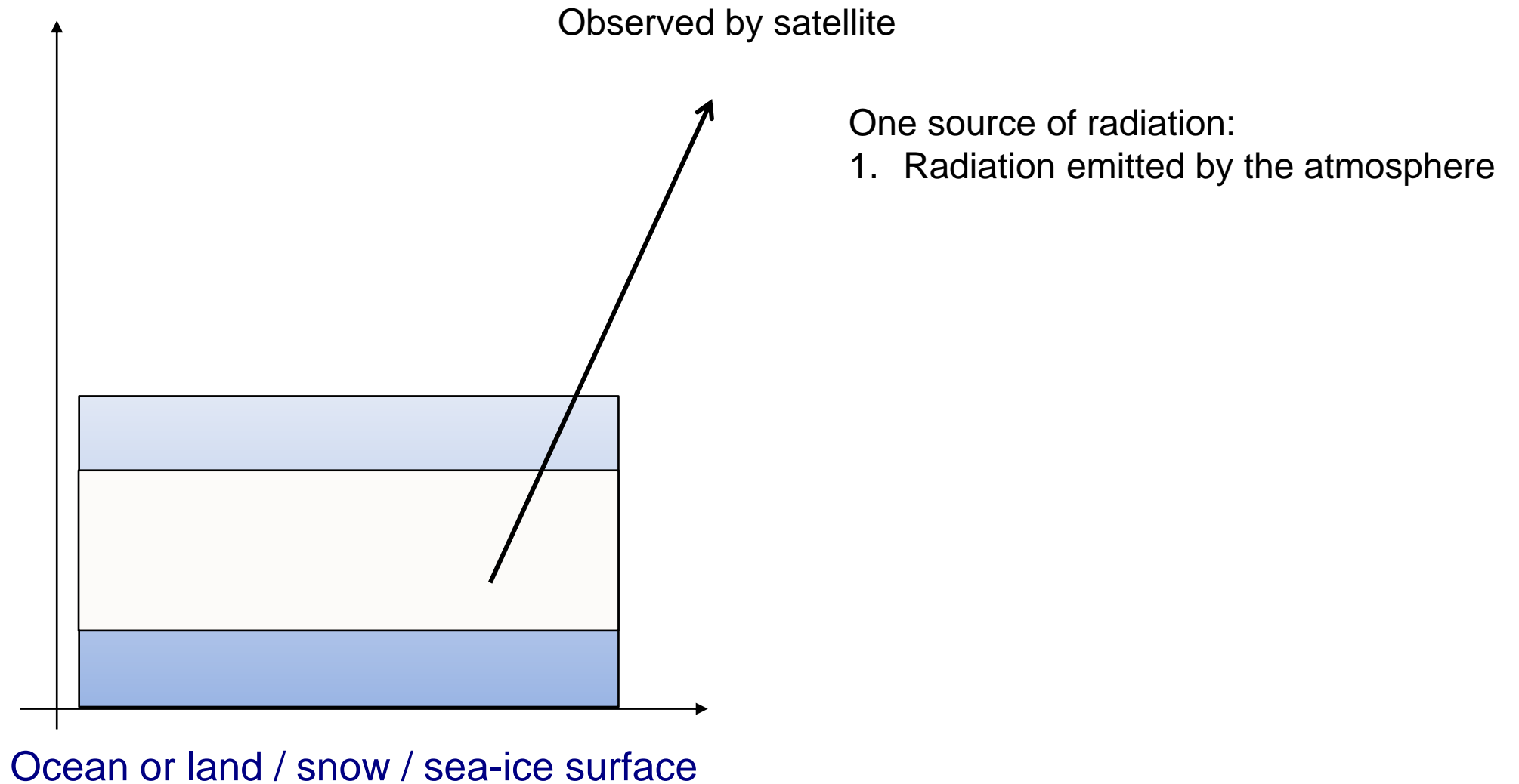


# Other users of the spectrum



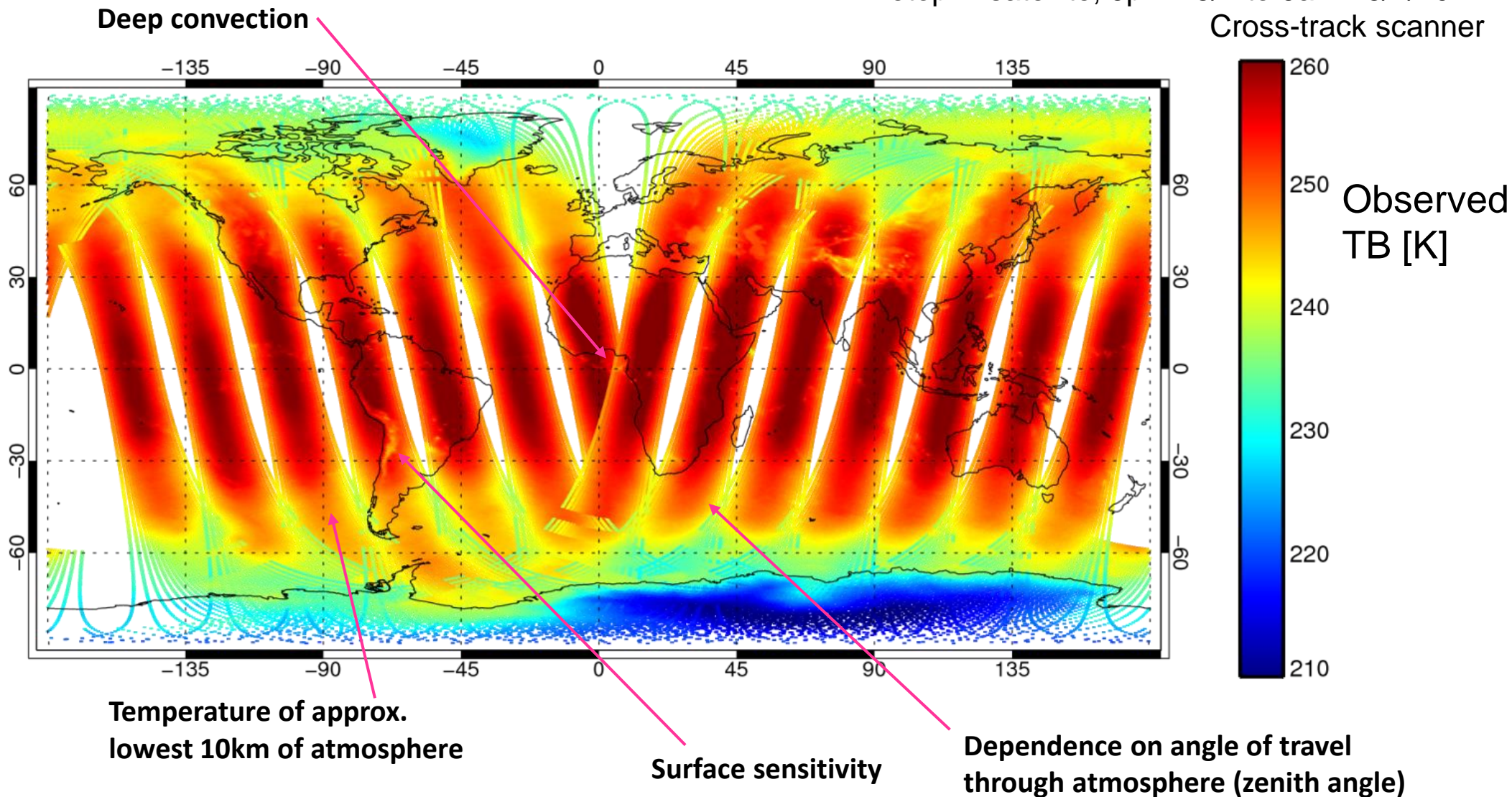
# Information content

# Radiative transfer: sounding channels (ignoring scattering)

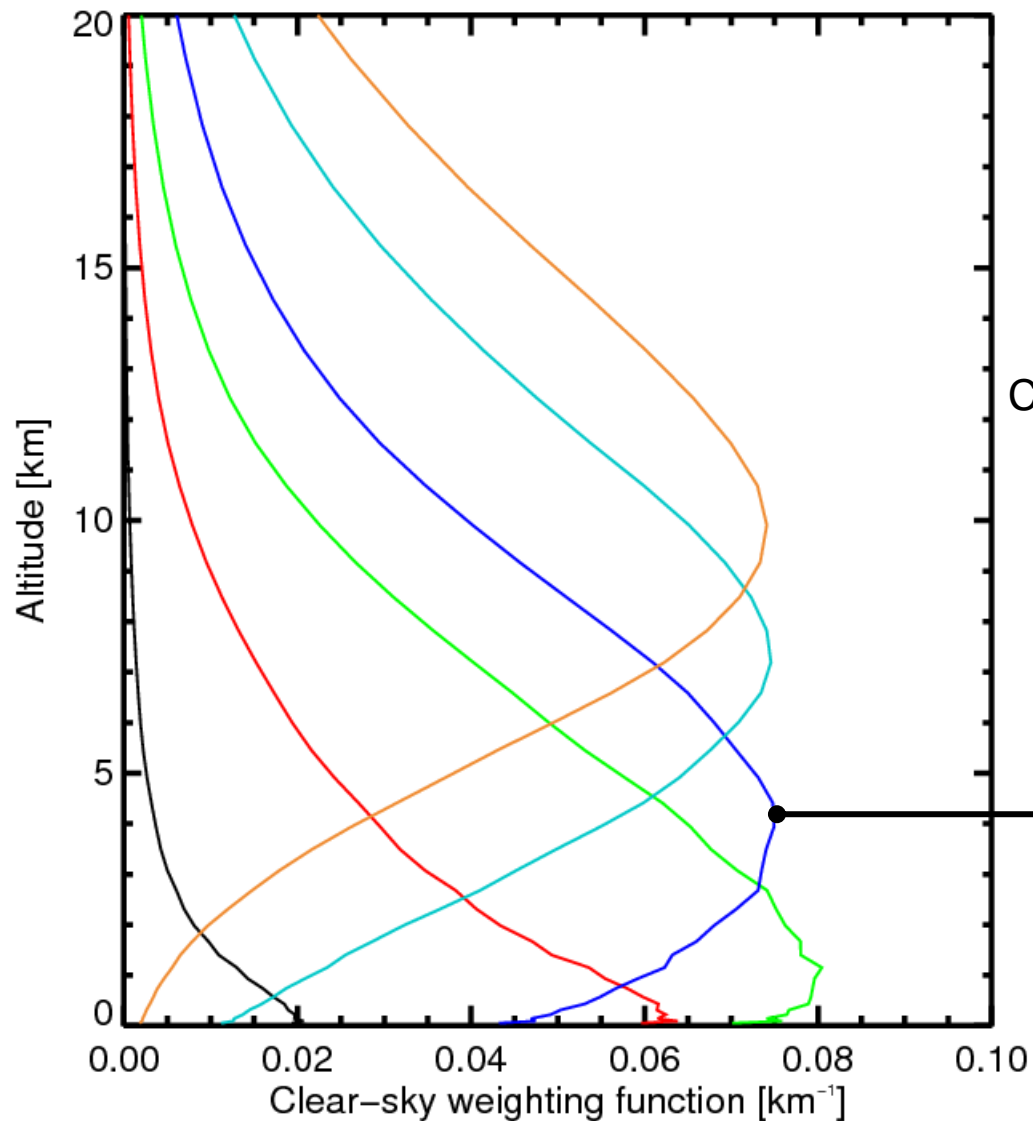


# Sensitivities: temperature sounding channels

AMSU-A channel 5 radiances:  
Metop-A satellite, 9pm 25/4 to 9am 26/4/2012  
Cross-track scanner



# Clear sky AMSU-A weighting functions (nadir)

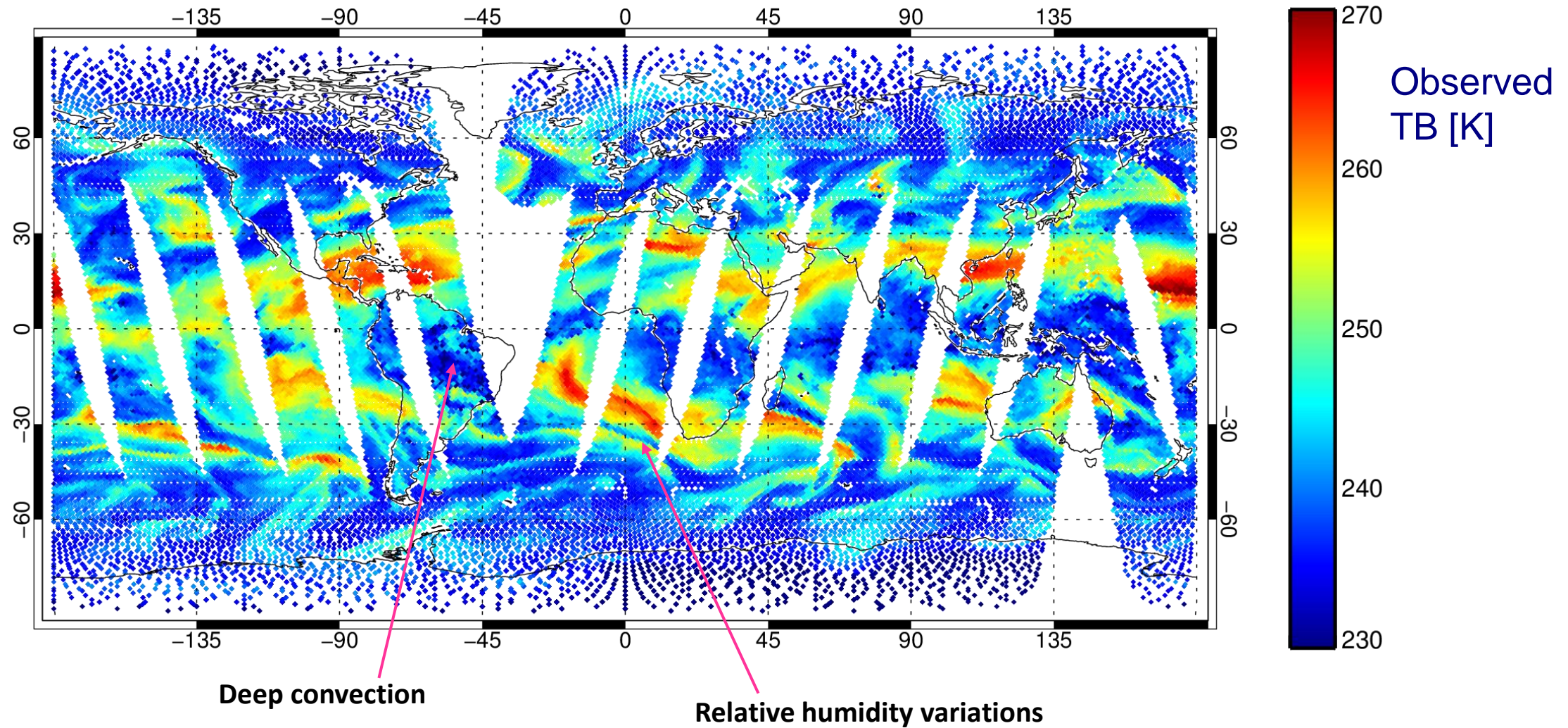


AMSU-A channels are at frequencies mainly sensitive to oxygen, a well-mixed gas: weighting functions are effectively fixed

Channel	Transmittance surface to space
7	0%
6	0%
5	5%
4	19%
3	56%
2	92%

# Humidity sounding channels

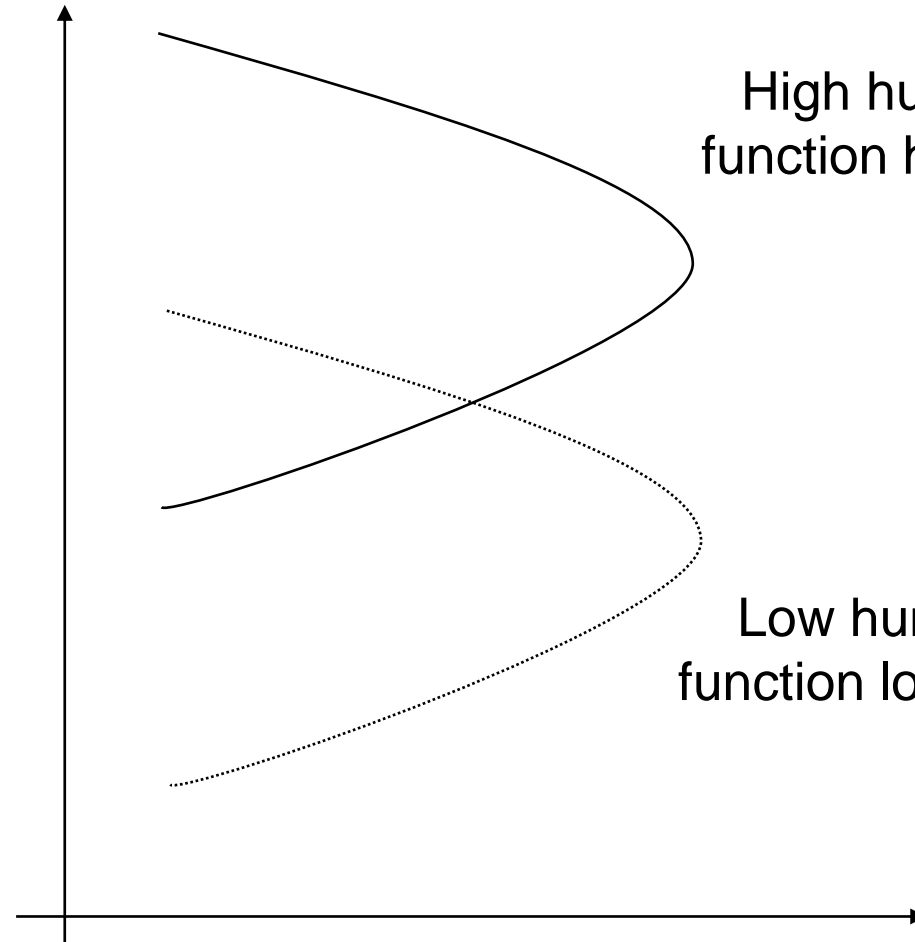
SSMIS F-17 channel 11 (183±1 GHz)  
Conical scanning imager and sounder



# Water vapour is a highly variable gas in the atmosphere: weighting function is not fixed

TB = 230 K  
(found at  
approx. 400  
hPa)

TB = 265 K  
(found at  
approx. 700  
hPa)



High humidity: weighting  
function high in troposphere

Low humidity: weighting  
function lower in troposphere

# Gas absorption: the microwave spectrum

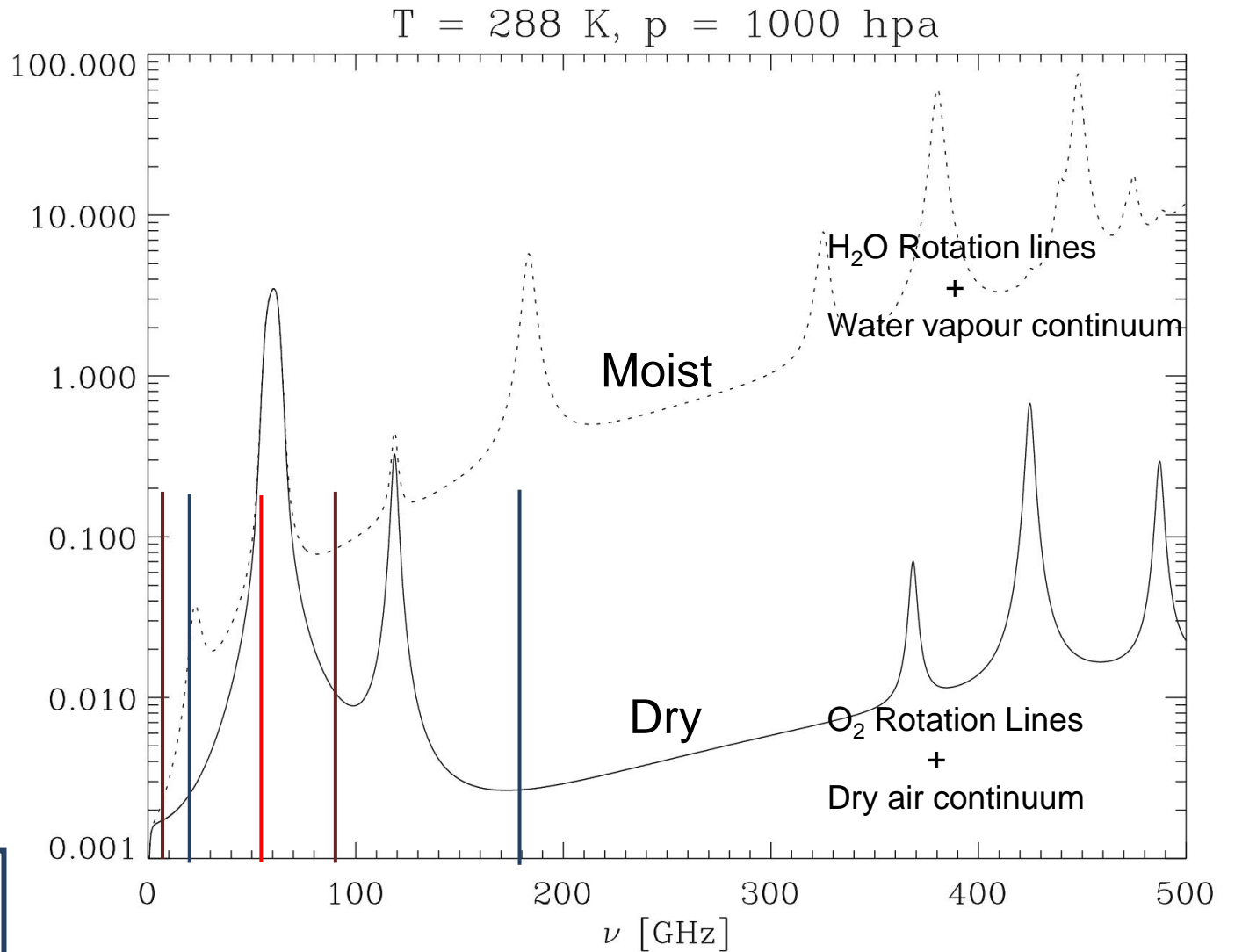
Absorption coefficient  $\beta_a$  [1/km]

“Imaging channels” in the windows

Temperature sounding: 60 GHz oxygen line

Moisture sounding: 22 GHz and 183 GHz water vapour lines

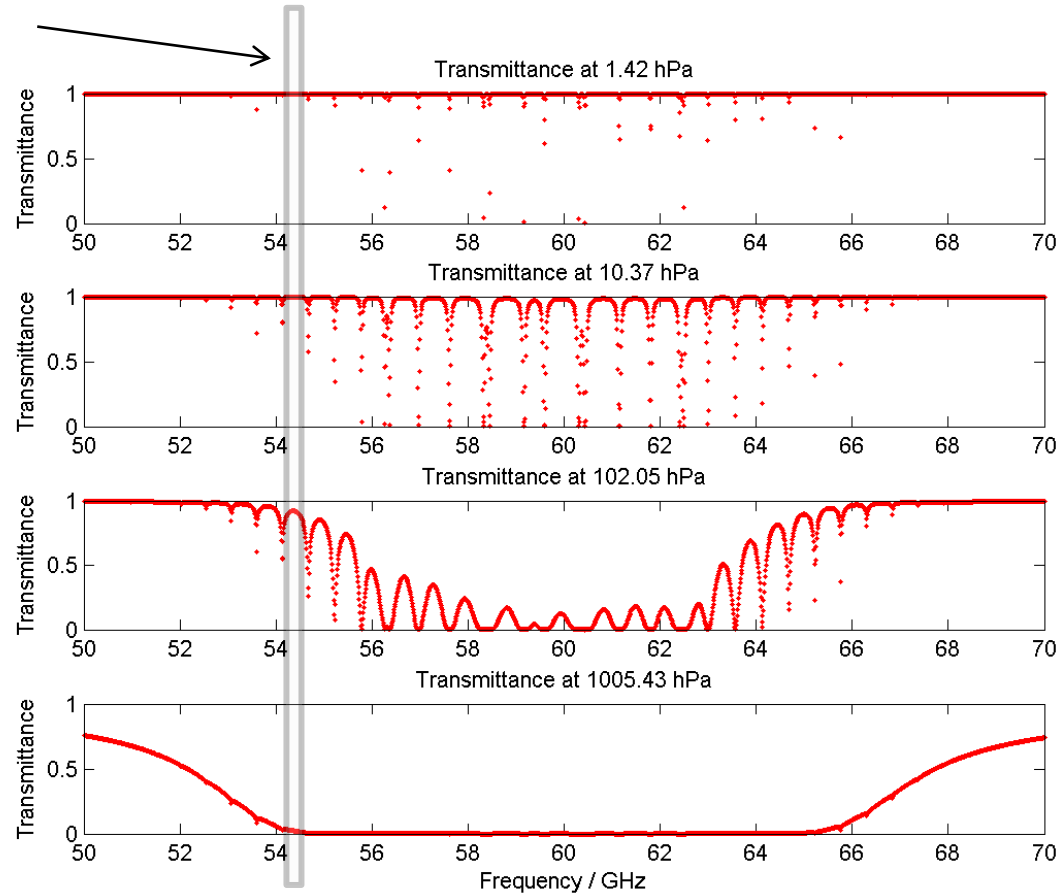
$k$  [1/km]





# Fine scale structure in the 60 GHz oxygen line

Typical MW radiometer passband  
at 54.4 GHz

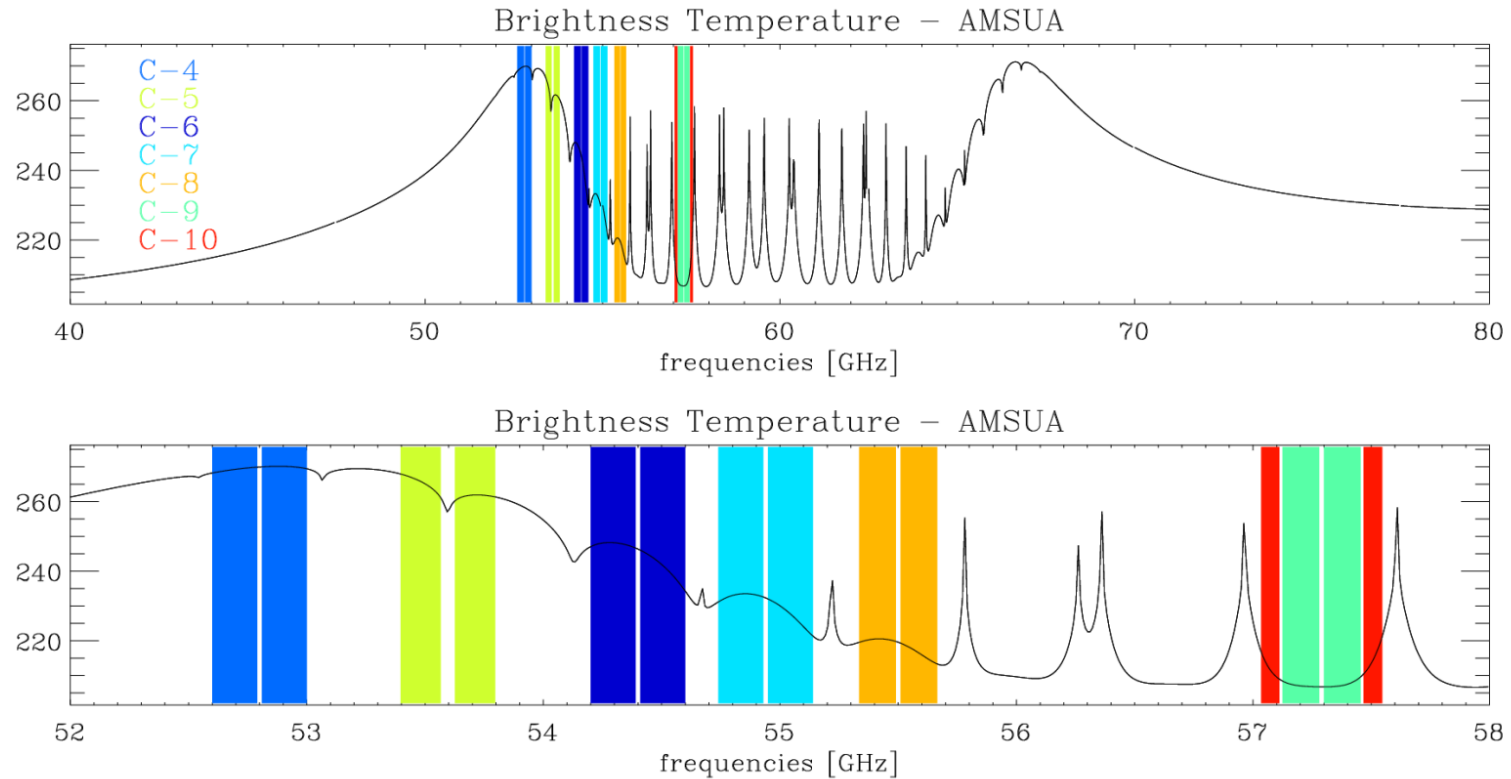


Level to TOA transmittance  
from Liebe MPM 92 model

Narrow lines ~ several MHz

Increasing pressure  
broadening

# AMSU-A 50 – 60 GHz channels



Channel positions and bandwidths are based on trade-offs aimed at simultaneously optimising :

- width of the band (wider bands give lower noise)
- *flatness* of optical depth across the band (narrow weighting functions)

# Information content: window (i.e. surface sensitive) channels

SSMIS F-17 channel 13 (19 GHz, v polarisation)  
Observed TB, 3<sup>rd</sup> December 2014

Ocean waves, wind, skin temperature

Atmospheric water vapour

Cloud and precipitation

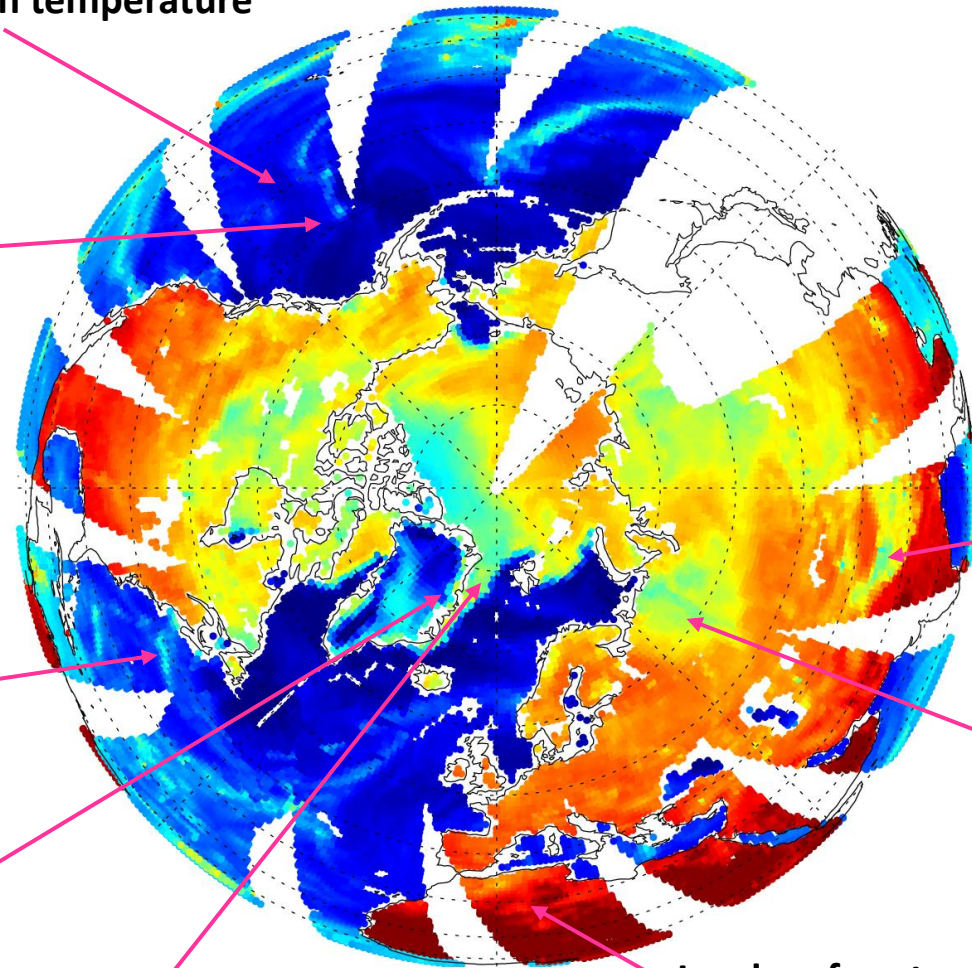
Special snow and ice conditions

Sea-ice

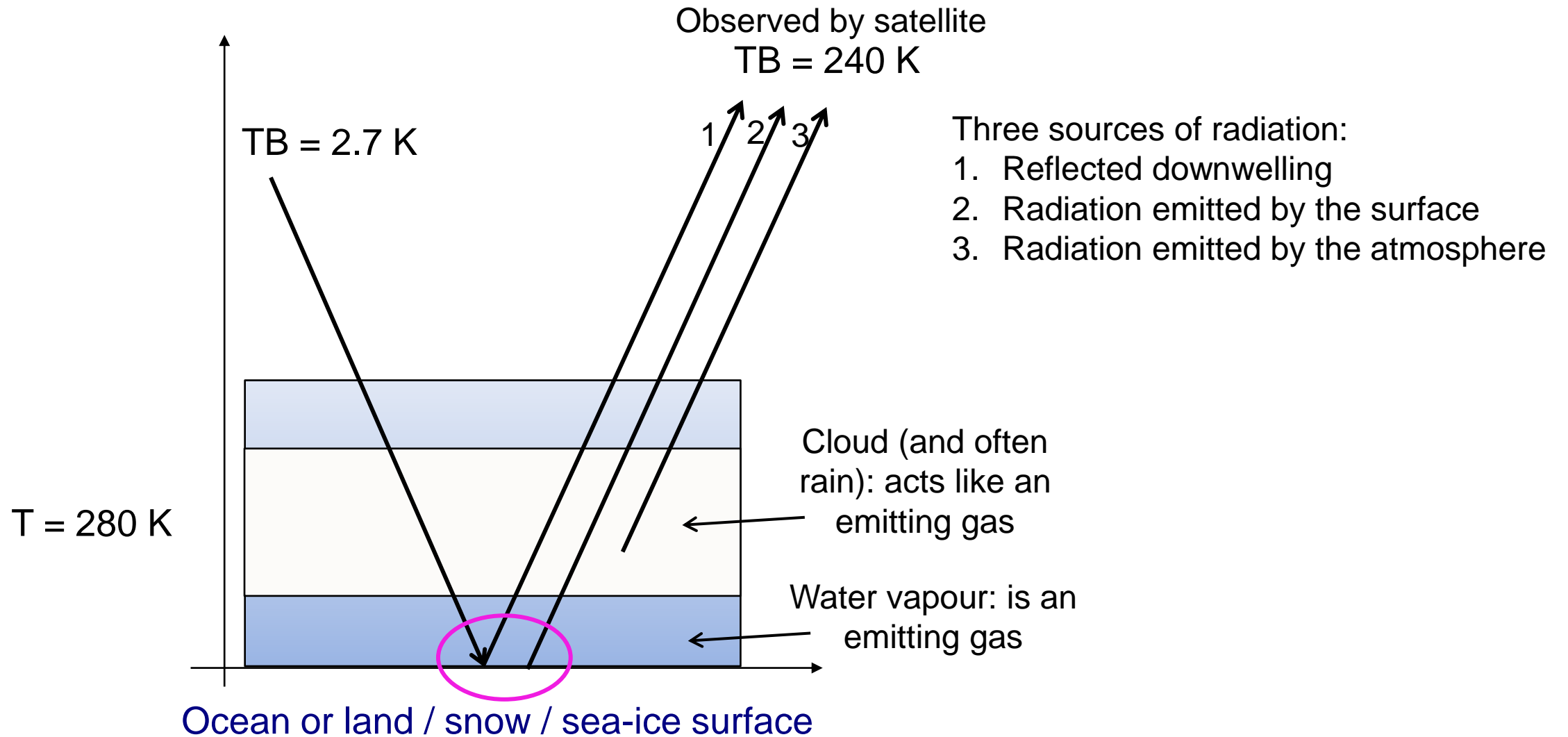
High altitude

Snow cover

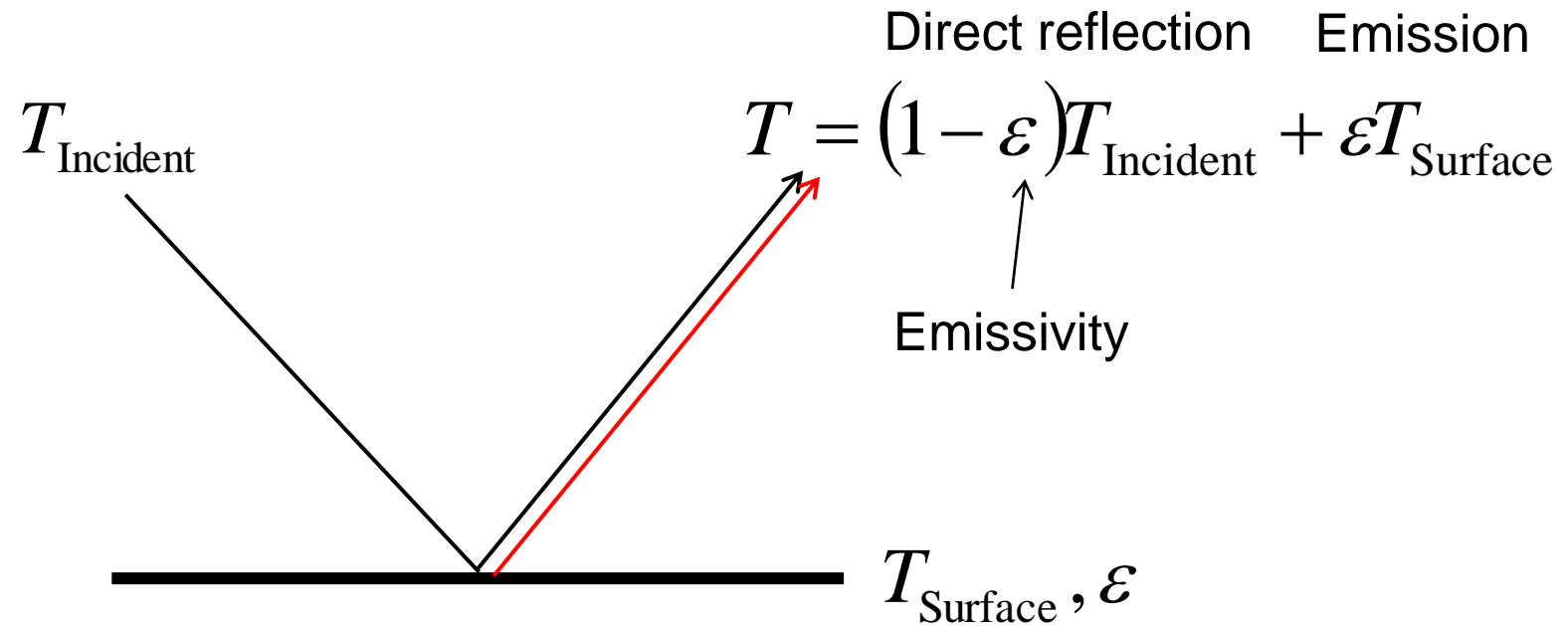
Land surface temperature, biomass, soil/rock, soil moisture



# Radiative transfer: window channels (ignoring scattering)



## Describing the surface interaction: specular emissivity

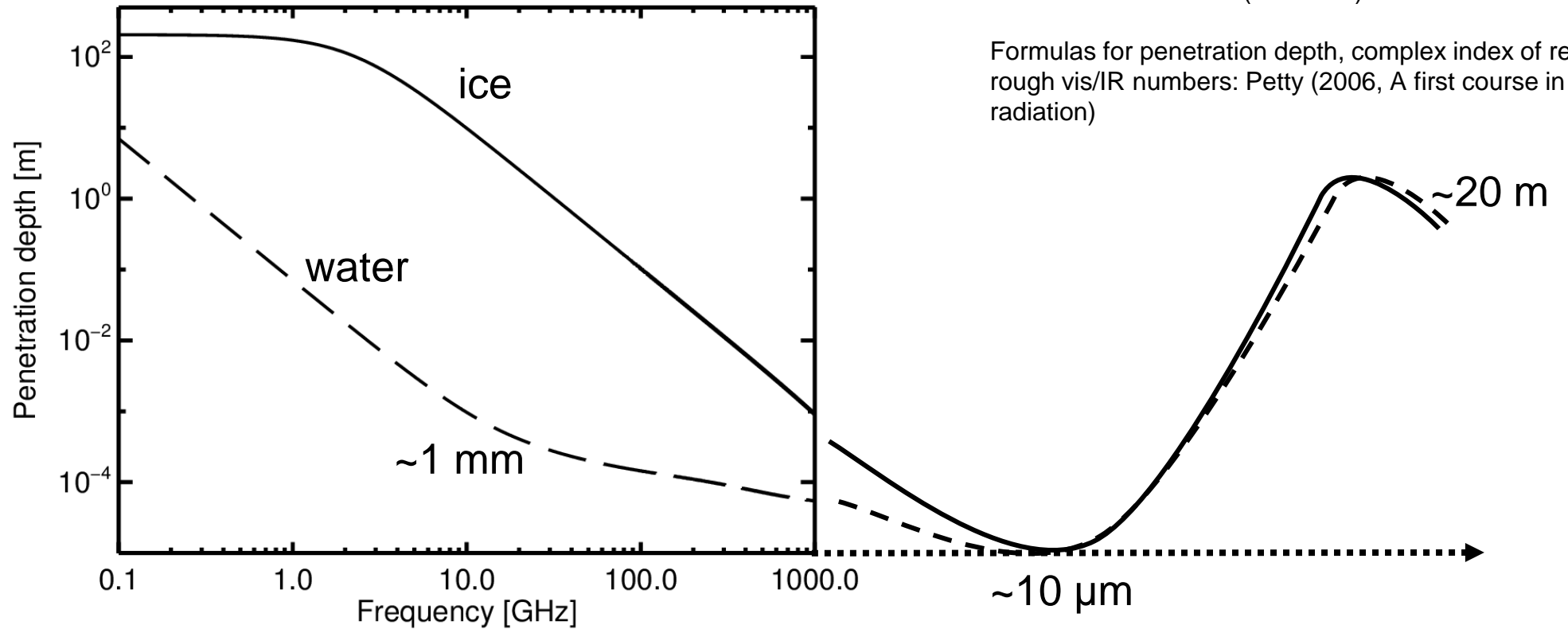


# Water and ice: penetration depth

Relative permittivity of pure ice at 263.0 K (up to ~1000 GHz):  
Mätzler (2006, Microwave dielectric properties of pure ice)

Pure water at 278.0 K (Liebe '89)

Formulas for penetration depth, complex index of refraction,  
rough vis/IR numbers: Petty (2006, A first course in atmospheric  
radiation)



Radio-frequency  
radar: e.g. SAR

L-band e.g.  
SMOS

Microwave  
imagers, e.g.  
AMSR2

Humidity  
sounders, e.g.  
MHS

Sub-mm,  
e.g. ICI

Hyperspectral  
infrared., e.g.  
IASI

Visible

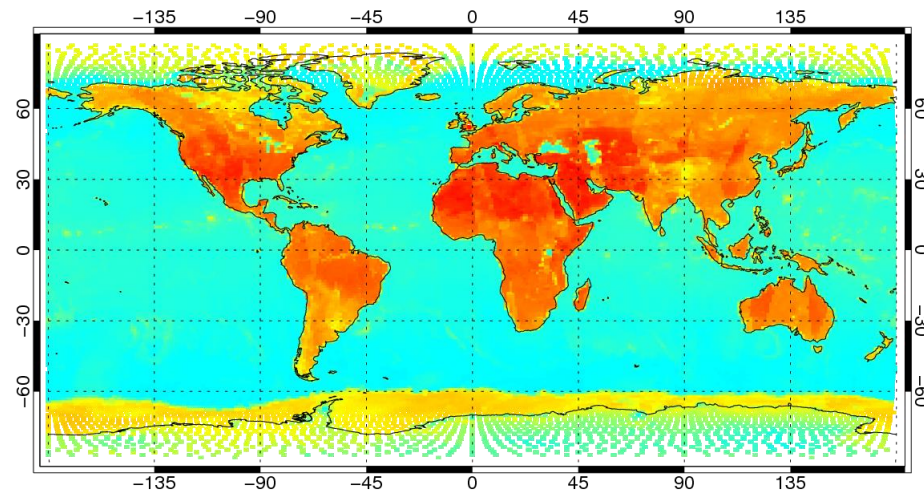
# Surface reflection and emission: ocean



- Plane water surface: low emissivity - Fresnel equations
- Macro structure: waves, swell – geometric optics
- Micro structure, e.g. cm: diffraction from capillary waves
- Foam: much higher emissivity than water
- Correction for non-specular reflection

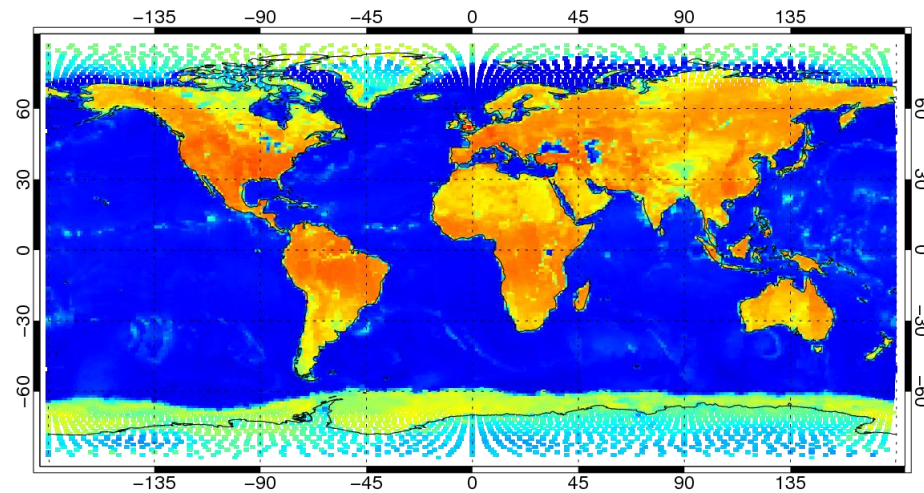
Approximately – a surface wind speed dependence

# Ocean surface: is strongly polarised and reflective at low frequencies



TB [K]  
10 GHz v-pol

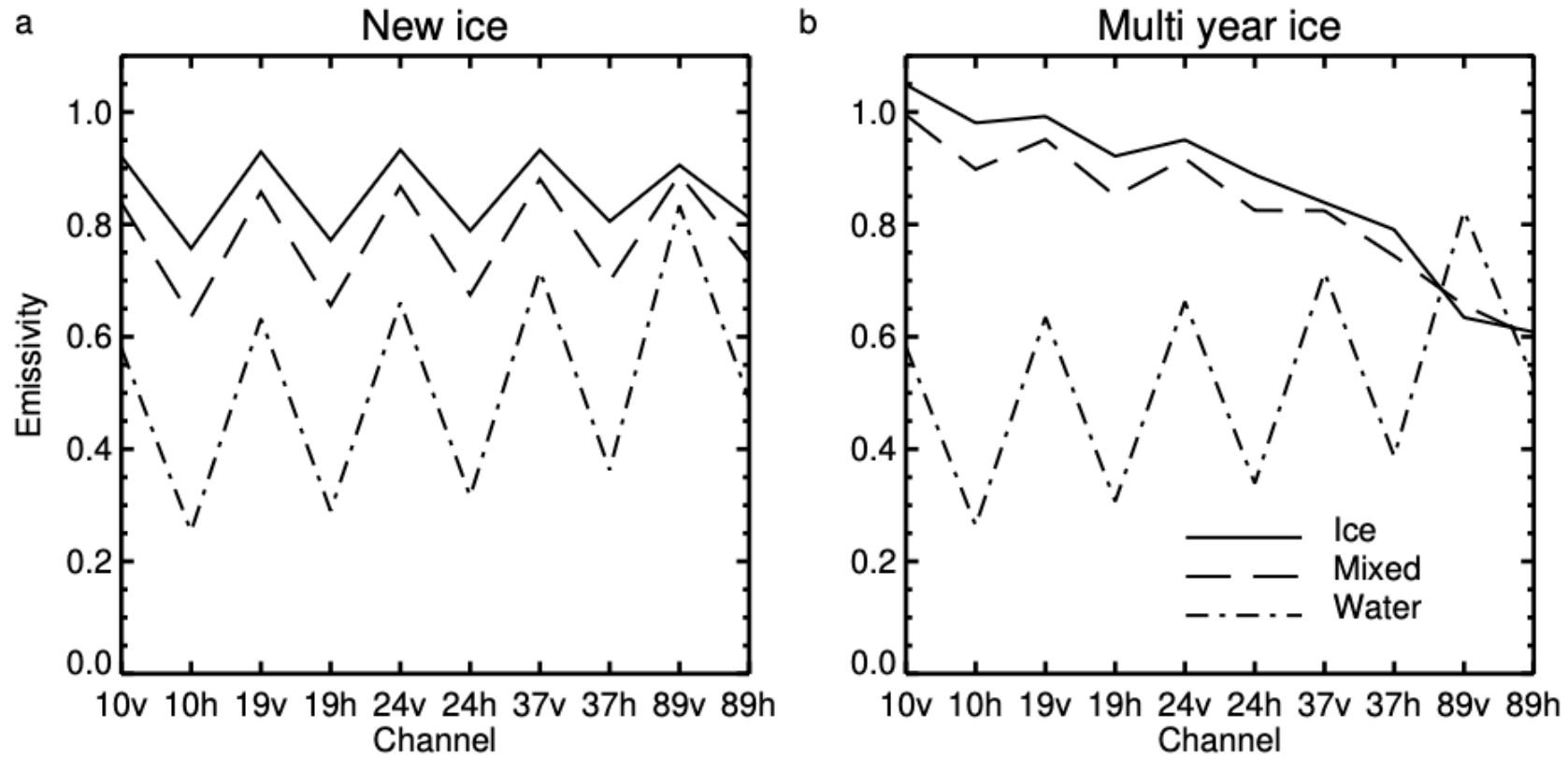
Ocean TB:  
~150 K vertical (v)-polarisation  
~90 K horizontal (h)-polarisation



TB [K]  
10 GHz h-pol



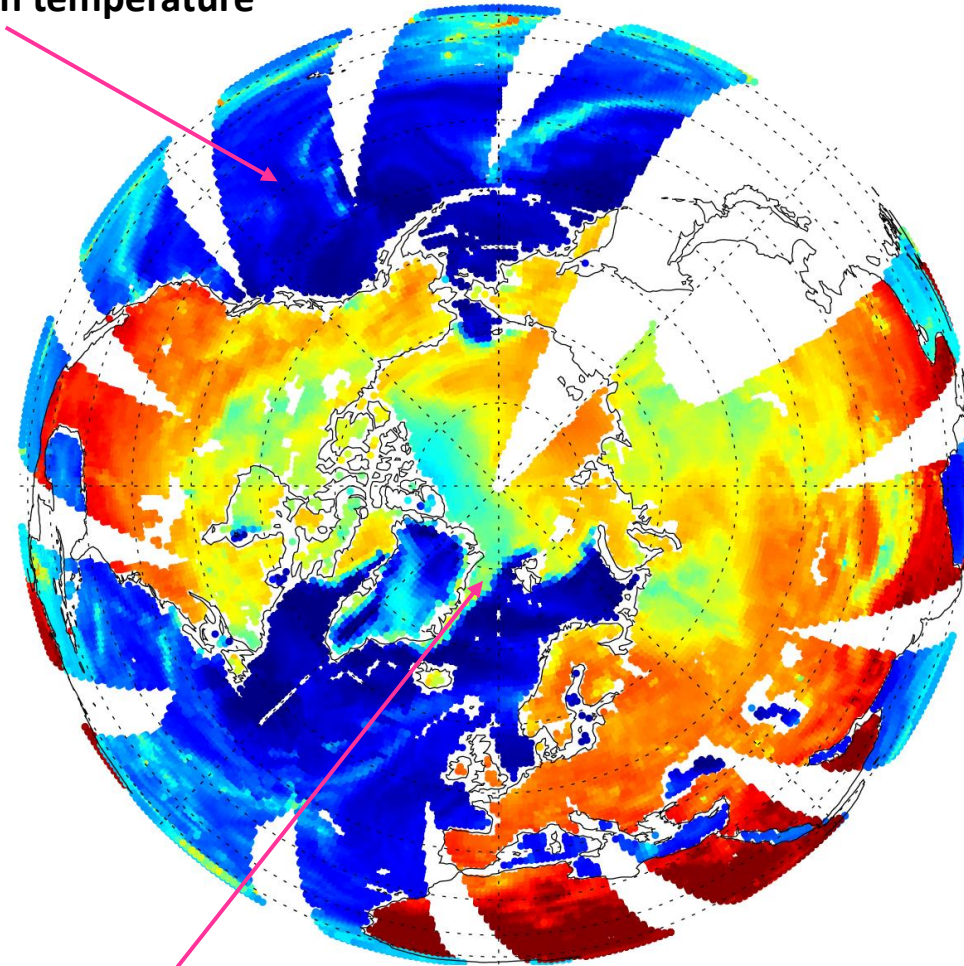
# Sea ice surface emissivity



# Information content: window (i.e. surface sensitive) channels

SSMIS F-17 channel 13 (19 GHz, v polarisation)  
Observed TB, 3<sup>rd</sup> December 2014

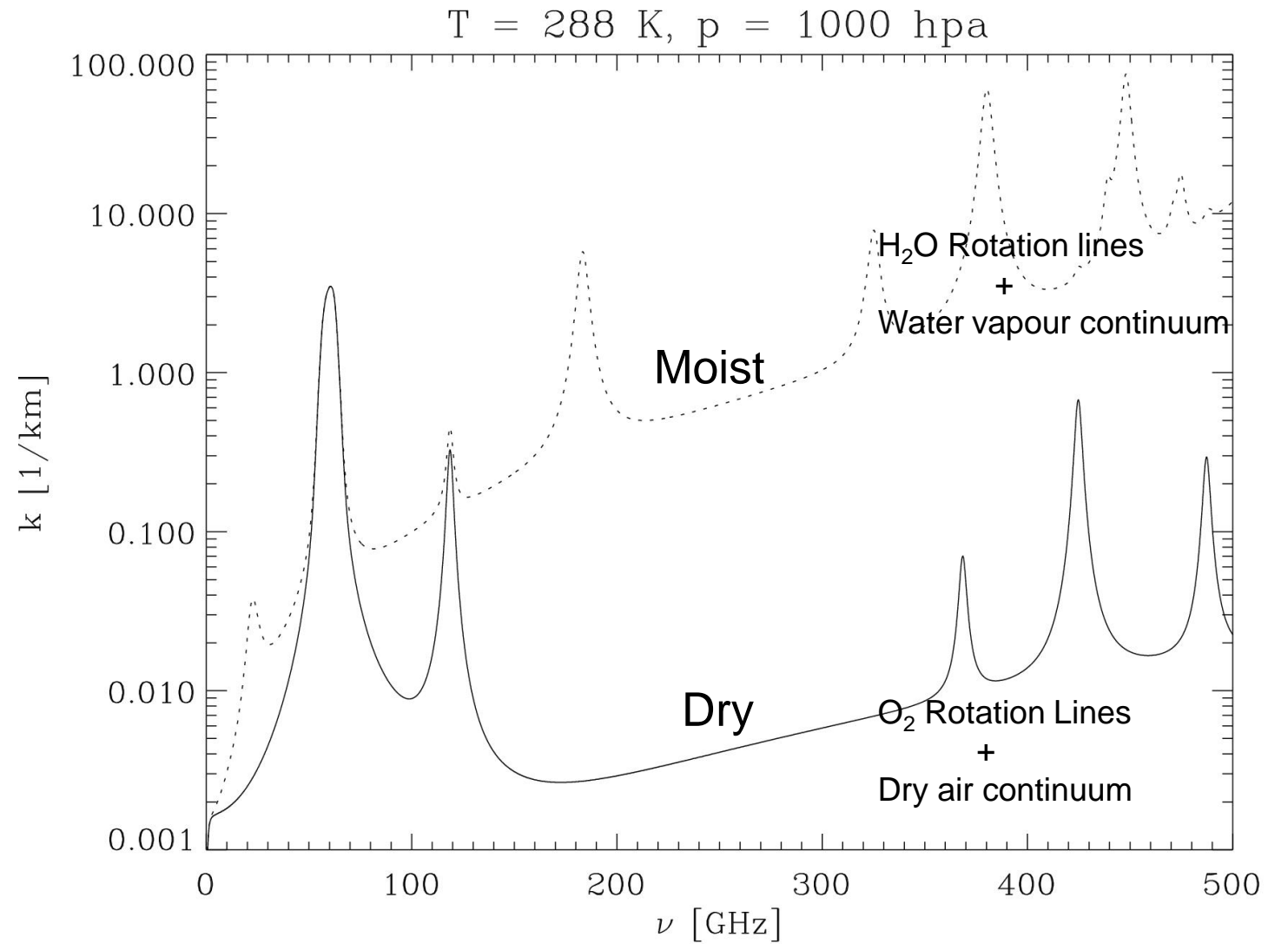
Ocean waves, wind, skin temperature



Sea-ice

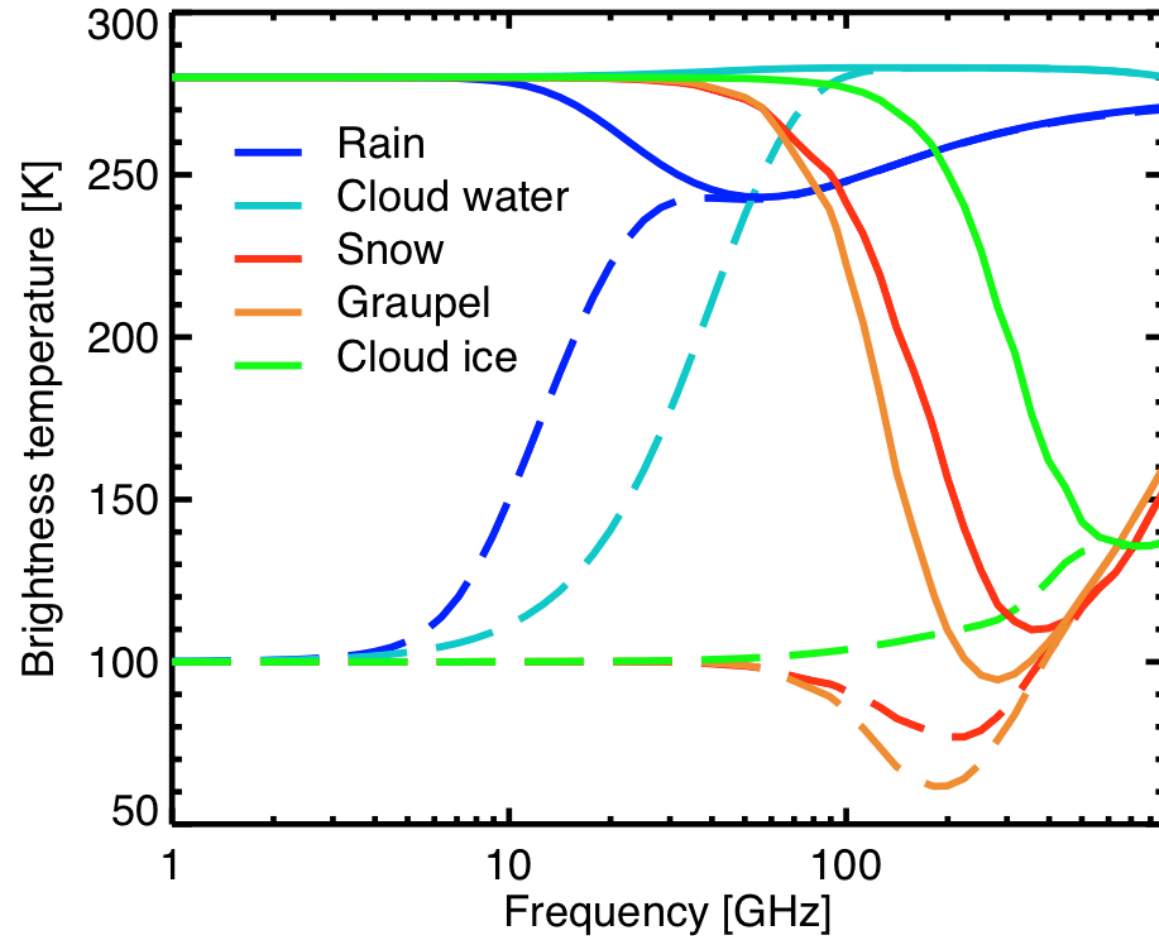
# Gas absorption: the microwave spectrum

Absorption coefficient  $\beta_a$  [1/km]



# Cloud and precipitation optical properties: the microwave spectrum

More in the next microwave lecture



Slab cloud at 283K above a 280K surface (solid)

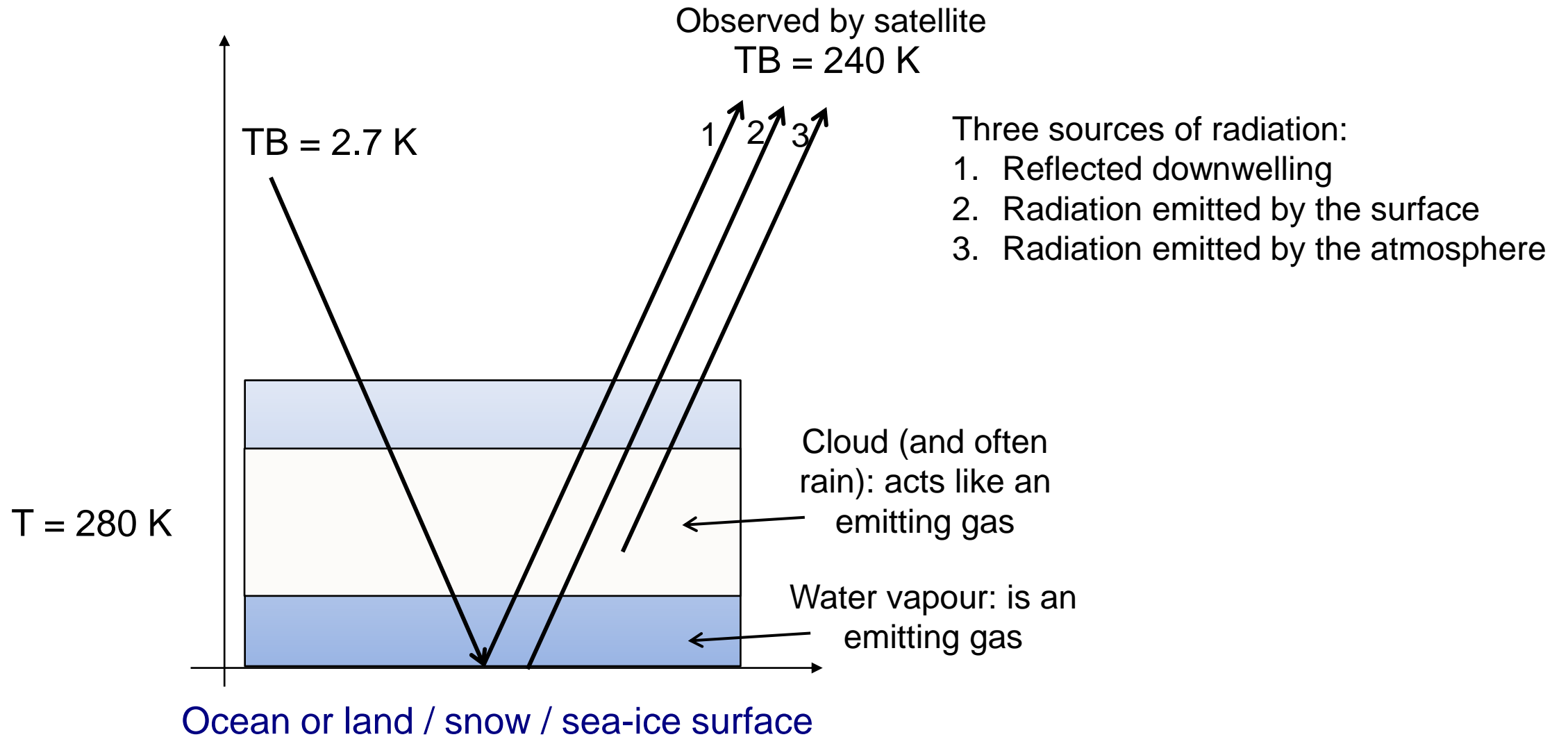
Slab cloud at 283K above a 100K surface (dashed)

Geer et al. (2021, GMD, Bulk hydrometeor optical properties for microwave and sub-millimetre radiative transfer in RTTOV-SCATT v13.0)

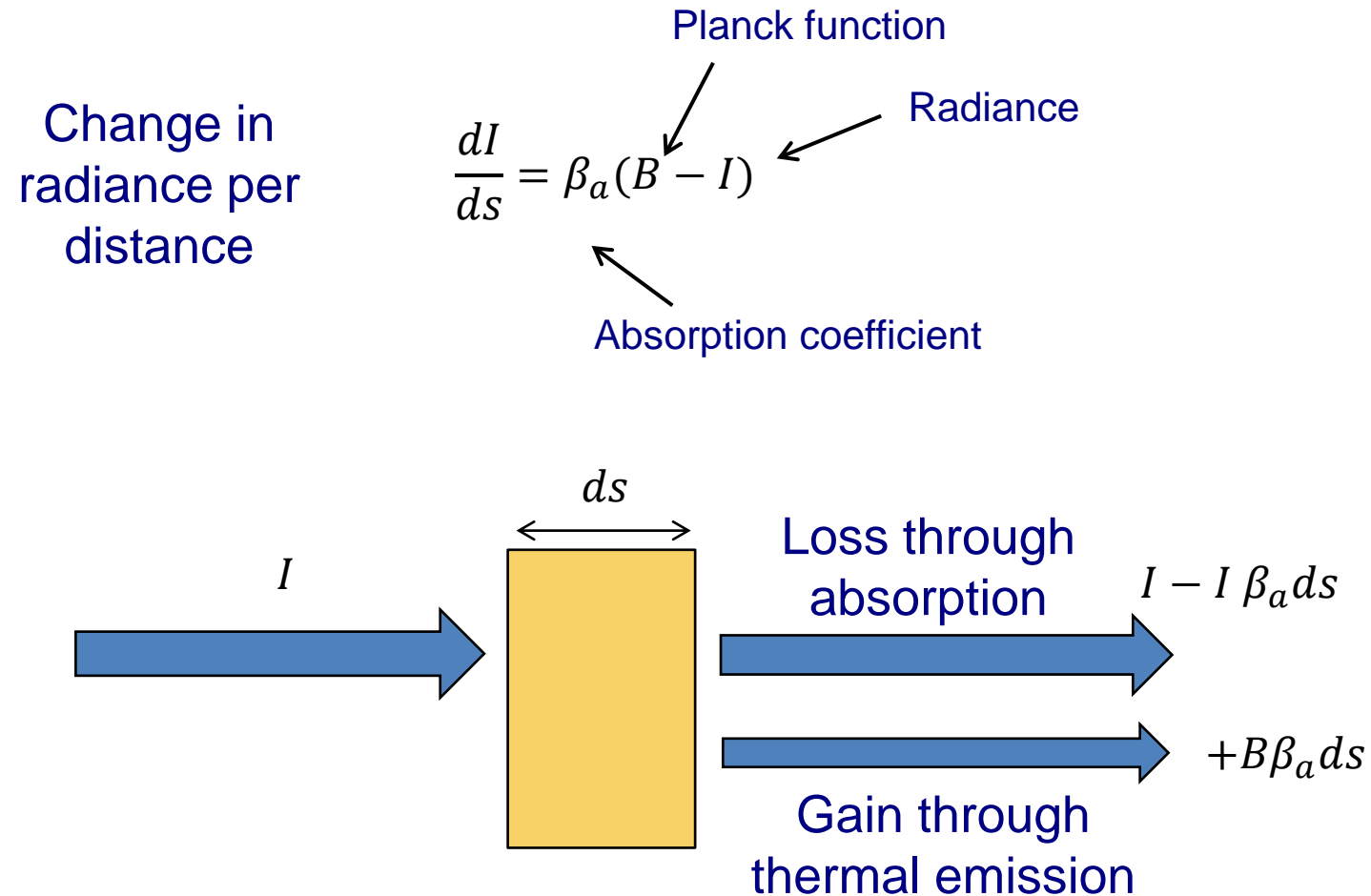
# Radiative transfer

(if time permits...)

# Radiative transfer: window channels (ignoring scattering)



# Rate of change of radiation travelling through an absorbing medium

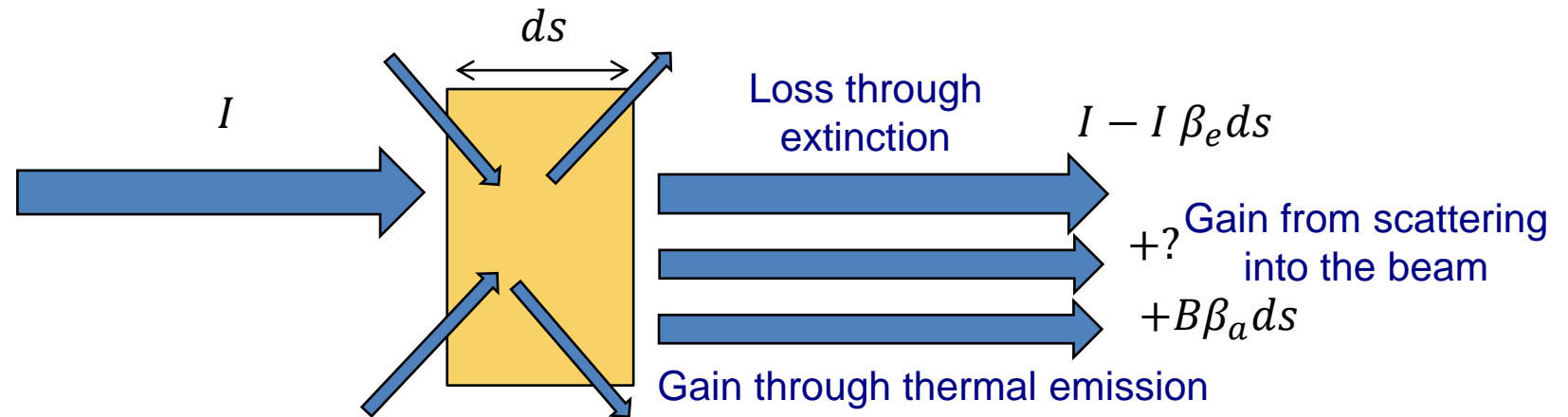


# Adding scattering

Extinction coefficient

$$\beta_e = \beta_a + \beta_s$$

Scattering coefficient (describing the amount of scattering out of the beam)





# Change in coordinates: optical depth

Change in optical depth  
 $d\tau$  in a non-scattering  
atmosphere

$$d\tau = -\beta_a ds$$

Change in optical depth  
 $d\tau$  including extinction by  
scattering

$$d\tau = -(\beta_a + \beta_s) ds = -\beta_e ds$$

## The full scattering radiative transfer equation

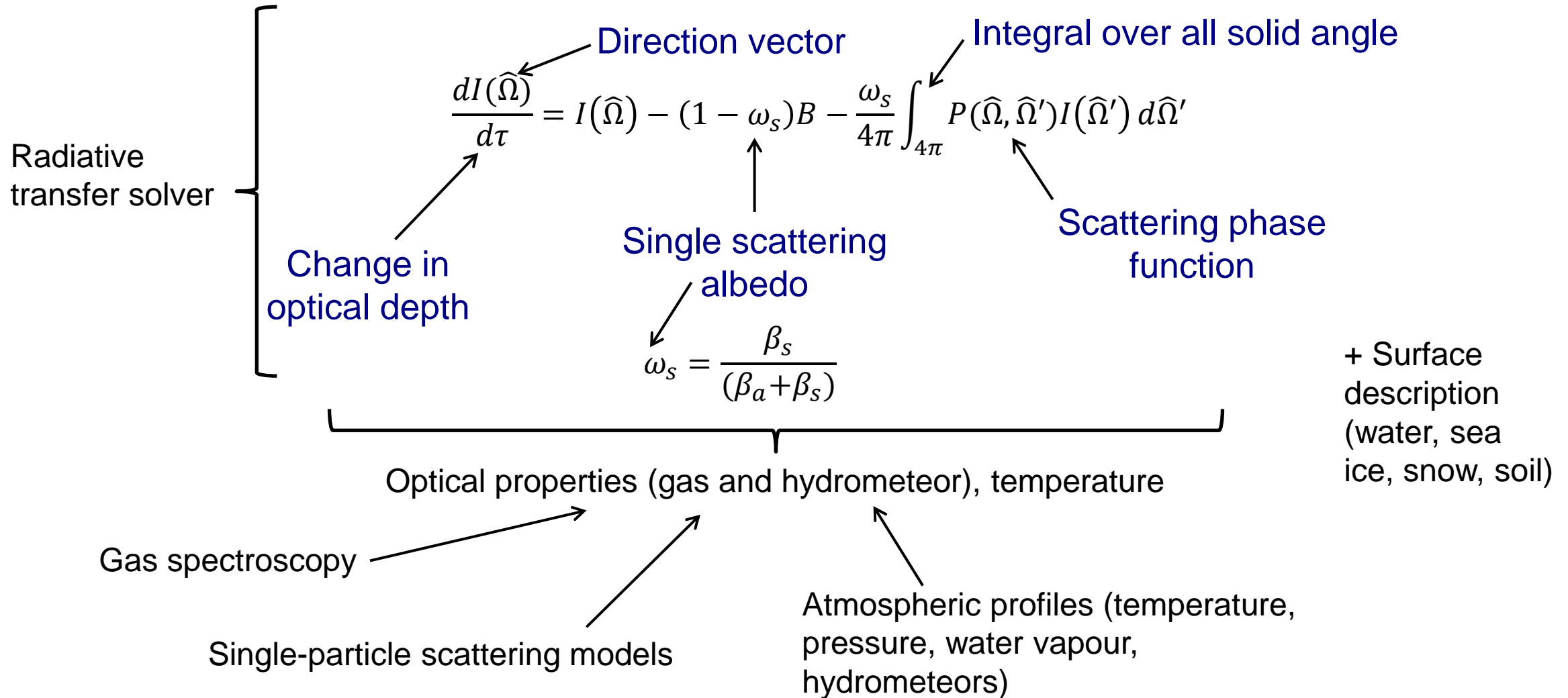
$$\frac{dI(\hat{\Omega})}{d\tau} = I(\hat{\Omega}) - (1 - \omega_s)B - \frac{\omega_s}{4\pi} \int_{4\pi} P(\hat{\Omega}, \hat{\Omega}') I(\hat{\Omega}') d\hat{\Omega}'$$

Direction vector  $\hat{\Omega}$   
 Integral over all solid angle  $\int_{4\pi}$   
 Change in optical depth  $\frac{dI(\hat{\Omega})}{d\tau}$   
 Single scattering albedo  $\omega_s$   
 Scattering phase function  $P(\hat{\Omega}, \hat{\Omega}')$

$$\omega_s = \frac{\beta_s}{(\beta_a + \beta_s)}$$

- Without scattering, just integrate this equation along the path travelled by the radiation (Tony's first lecture)
- With scattering, this can be complex to solve:  
 $I(\hat{\Omega})$ , the radiance in one direction, depends on radiance from all other directions:  $I(\hat{\Omega}')$   
 and all levels depend on each other

# The full scattering radiative transfer equation



Questions?