

# The IFS dynamical core in openIFS

## A hands-on introduction to Numerical Weather Prediction Models

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# Talk Outline

- Equation sets, grids, and dynamical core overview
- Motivation, historical context for the introduction of semi-implicit, semi-Lagrangian methods
- Fundamental algorithms and their limitations
- The pros and cons of the IFS formulation:
  - conservation aspects and errors in IFS and how we deal with them
- Atlas, Atlas multiple grids and applications on advection

# The ECMWF hydrostatic global operational model equation set

$$\frac{D\mathbf{V}_h}{Dt} + f\mathbf{k} \times \mathbf{V}_h + \nabla_h \Phi + R_d T_v \nabla_h \ln p = P_v$$

$$\frac{DT}{Dt} - \frac{\kappa T_v \omega}{(1 + (\delta - 1)q) p} = P_T$$

$$\frac{Dq_x}{Dt} = P_{q_x}$$

$$\frac{\partial}{\partial t} \left( \frac{\partial p}{\partial \eta} \right) + \nabla_h \cdot \left( \mathbf{V}_h \frac{\partial p}{\partial \eta} \right) + \frac{\partial}{\partial \eta} \left( \dot{\eta} \frac{\partial p}{\partial \eta} \right) = 0$$

$$\Phi = \Phi_s - \int_1^\eta R_d T_v \frac{\partial}{\partial \eta} (\ln p) d\eta$$

$\eta$  : hybrid pressure based vertical coordinate

$\mathbf{V}_h$ : horizontal momentum

$T$ : temperature

$T_v$ : virtual temperature (used as spectral variable)

$q_x$ : specific humidity, specific ratios for cloud fields and other tracers  $x$ ,  $\delta = c_{pv}/c_{pd}$

$\Phi$ : geopotential

$p$  : pressure

$\omega = dp/dt$  : diagnostic vertical velocity

$P$ : physics forcing terms

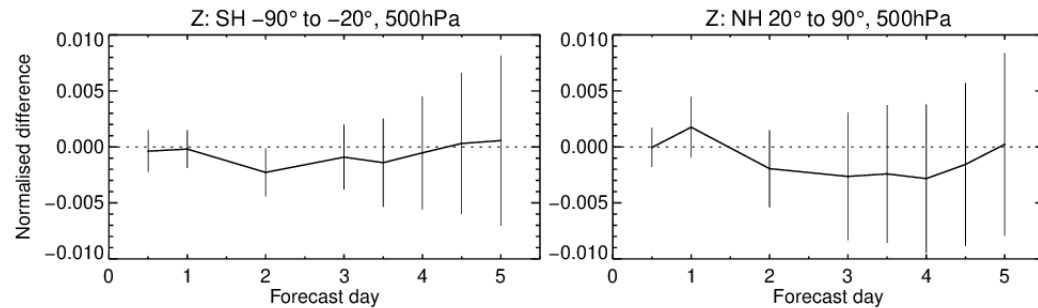
Continuity equation in terms of full (moist) pressure: the model conserves the total (rather than dry) atmospheric mass.

- Primitive equation hydrostatic
- A **non-hydrostatic** option is available for **research** purposes but not used operationally or in openIFS
- Spectral Transform with spherical harmonics basis
- Cubic spline Finite Elements in the vertical
- **Timestepping: semi-Lagrangian semi-implicit**

# Non-hydrostatic versus Hydrostatic IFS systematic comparisons

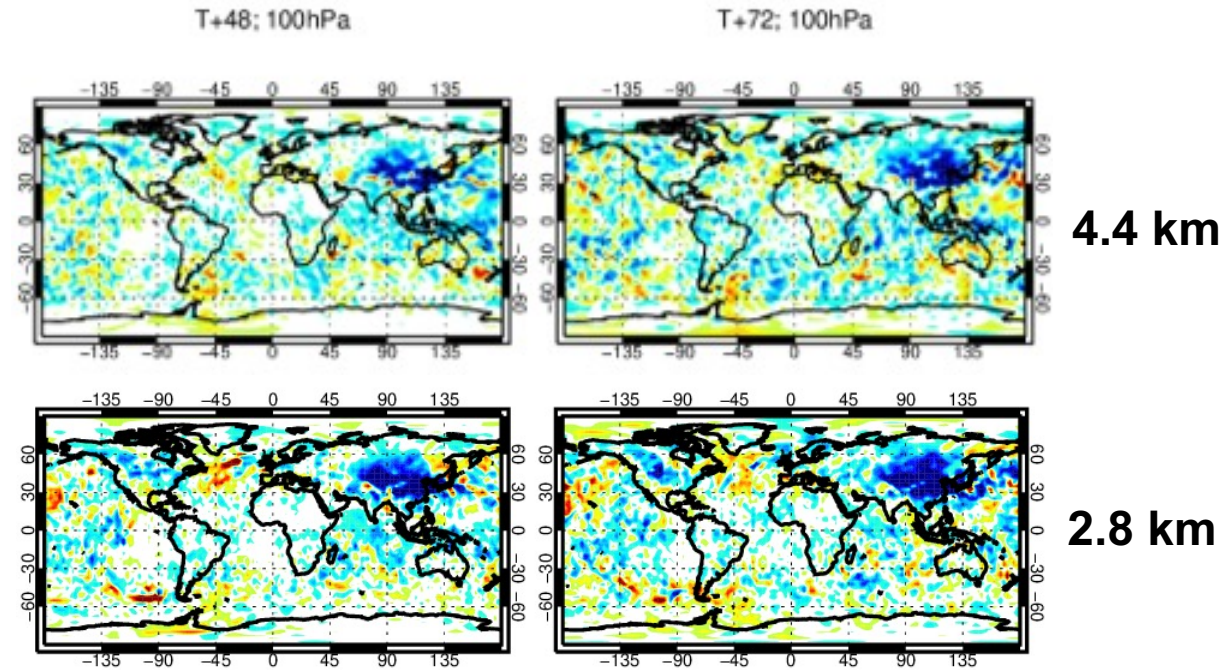
- **Is the hydrostatic assumption in IFS valid at 3-10km grid spacing?**
- **Consider that its effective resolution is 4-6 times higher**

20-Jan-2022 to 13-Sep-2023 from 72 to 83 samples. Verified against M0001M0001M0001.  
Confidence range 95% with AR(1) inflation and Sidak correction for 4 independent tests.



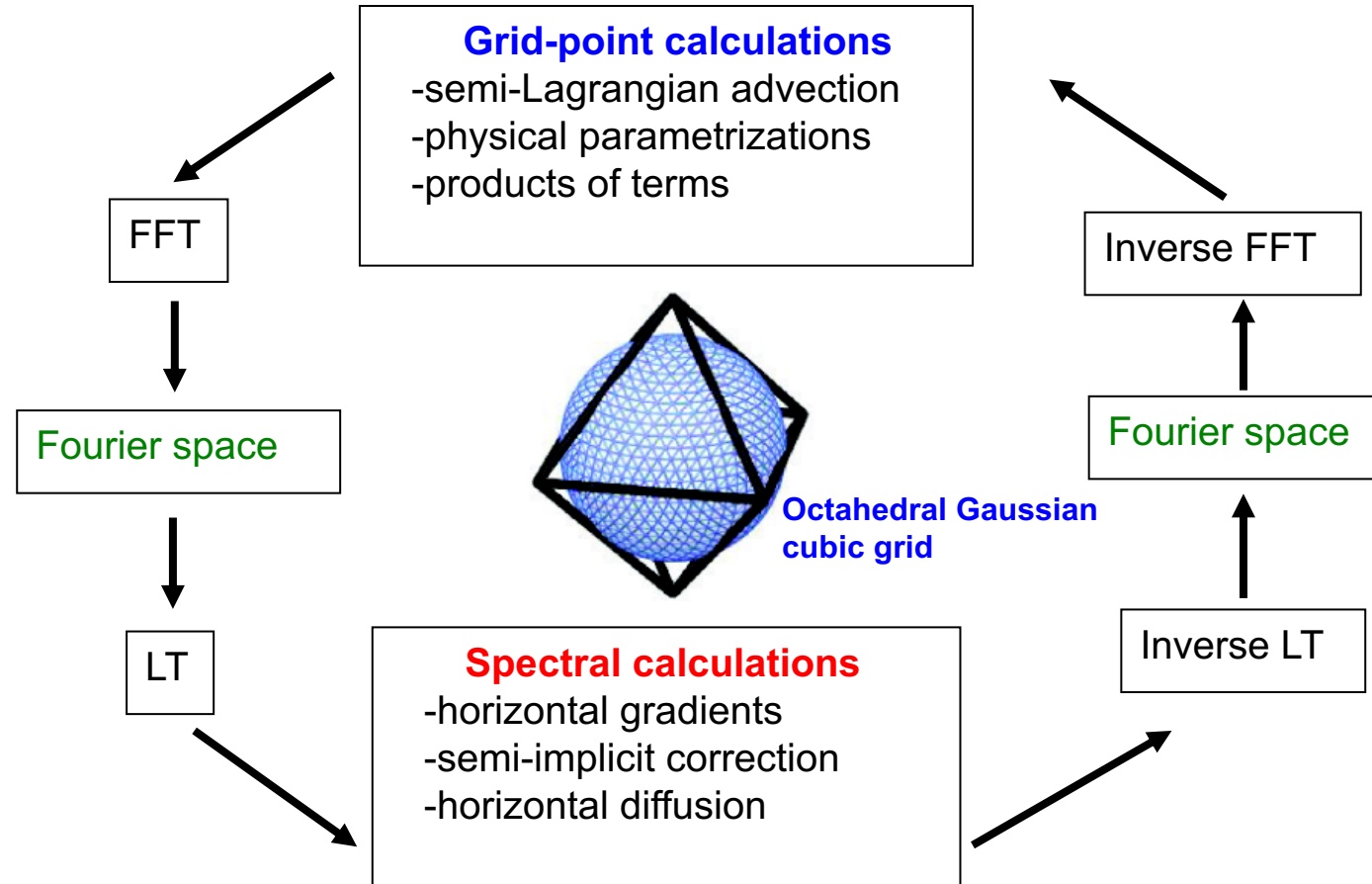
**Combined winter-summer headline 500 hPa RMSE score difference (NH versus H control) at 2.8km resolution**

- Two-season **systematic** and **fair** comparison: like-to-like comparisons with same numerics at 4.4km and 2.8km
- **Differences only** seen in **winter** over **Himalaya** in the **stratosphere**
- **Neutral** in the summer (including TC predictions)
- **Up to 2.8km resolution: little difference to justify use of the much more expensive non-hydrostatic option**
- Research experiments at 1.4km case studies show more significant differences



**NH-H: deep blue 10% reduction of vector wind RMSE – signal at 2.8km only slightly stronger than 4.4km**

# Solving the equations: spectral transform semi-implicit semi-Lagrangian (SISL) method



FFT: Fast Fourier Transform, LT: Legendre Transform

## Vertical discretization

- Hybrid pressure based vertical coordinate  $\eta(p)$
- 8<sup>th</sup> order Finite Element discretization based on cubic spline basis functions
  - Accurate vertical integrals with benefits seen mostly in the stratosphere
  - More accurate vertical velocity

Cycle 48r1 scheme upgrade based on Vivoda et al, [10.1175/MWR-D-18-0043.1](https://doi.org/10.1175/MWR-D-18-0043.1):

- Unified for hydrostatic and non-hydrostatic model
- Better for single precision (SP) – IFS runs SP forecasts from cycle 47r2

# Spectral transforms on spherical harmonics

Spectral coefficient      longitude      latitude      Spherical harmonics

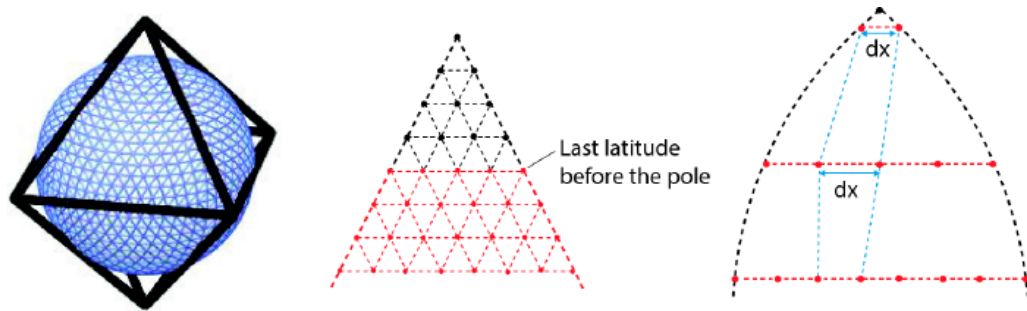
$$f(\lambda, \phi) = \sum_{m=-\infty}^{\infty} \sum_{n=|m|}^{\infty} f_n^m Y_n^m(\lambda, \phi), \quad Y_n^m(\lambda, \phi) = P_n^m(\sin \phi) e^{im\lambda}$$

m: zonal wavenumber  
n: total wavenumber

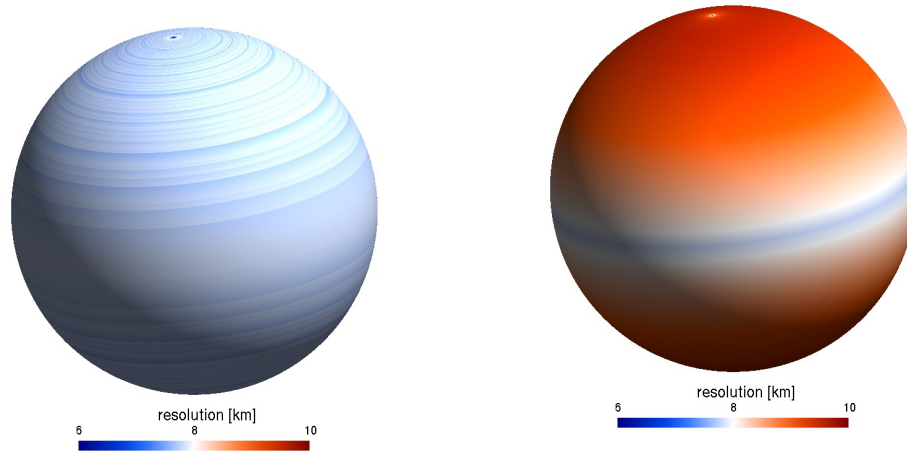
Associated Legendre Polynomials (normalised)

- We can compute derivatives without approximations using analytical formulae
  - The common “pole singularity” problem is overcome
  - Spherical harmonics are the eigenfunctions of the Laplace operator: in time-stepping the derived “Helmholtz equation” can be decoupled and solved by a very cheap & simple diagonal solver
- 
- Advancements in algorithms, hardware and software have enabled us to keep running efficiently the spectral transform method at **ever increasing resolutions**
  - ecTrans: a multi-node GPU enabled spectral transform library

# The octahedral grid: accurate, efficient and scalable



Collignon projection on the sphere:  $Nlat_i = 4 \times i + 16, i = 1, \dots, N$

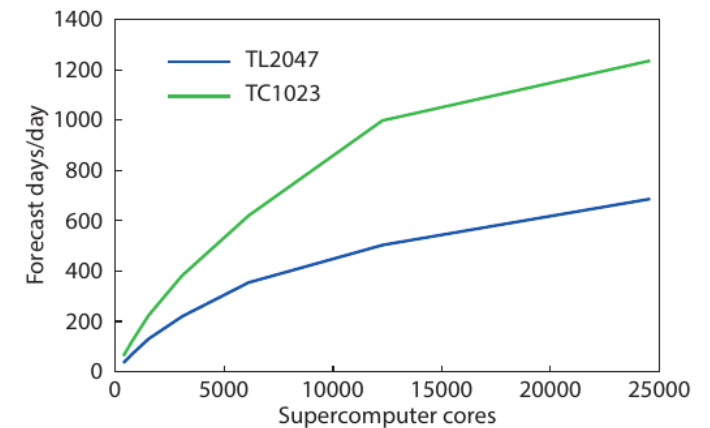


Latitudinal variation of resolution for standard cubic grid and octahedral cubic grid

Reference: "A new grid for the IFS" ECMWF newsletter 146, Winter 2015-2016, Malardel et al

Benefits of cubic octahedral grid compared with old linear grid:

- More accurate representation of fine scales at same spectral truncation
- Improved total mass conservation
- Improved efficiency and scalability
- Improved filtering effects: reduced diffusion (spectral viscosity) + no anti-aliasing filter



Cubic versus linear grid run at the same gridpoint resolution

Cubic grid achieves 2× more forecast-days-per-day than linear grid as core count increases

# Time-stepping: semi-implicit, semi-Lagrangian (SISL) technique

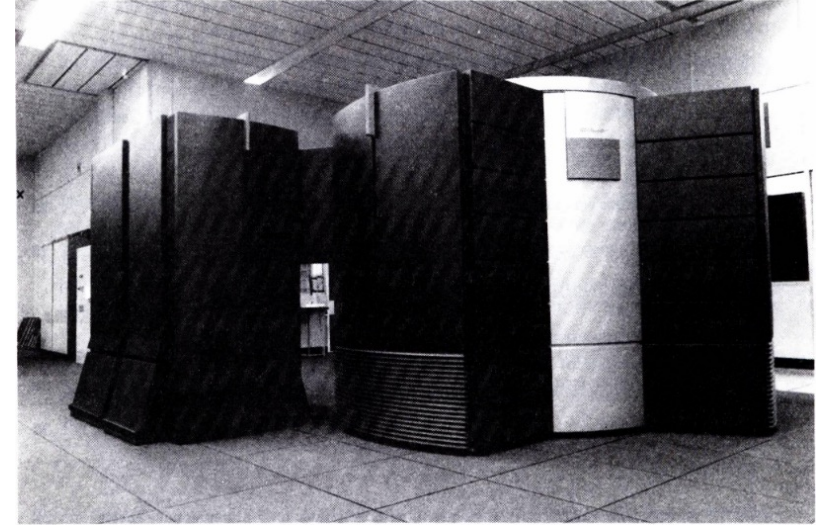
**Semi-Lagrangian (SL) semi-implicit (SI) technique is ideal for global NWP: stable efficient and accurate integration of the governing equations**

- ❑ Unconditionally stable SL advection scheme with small phase speed errors and little numerical dispersion
  - ✓ No CFL restriction in timestep: large timesteps can be used without accuracy penalty 😊
  - ✓ Multi-tracer efficient
- ❑ Unconditionally stable SI time stepping for the integration of fast dynamical processes
  - ✓ No timestep restriction from the integration of “fast forcing” terms (gravity wave and acoustic terms in non-hydrostatic models)
  - ✓ 2<sup>nd</sup> order accuracy



# History of SISL method at ECMWF

- 1991: IFS was a **spectral semi-implicit** Eulerian model on a full Gaussian grid at T106 horizontal resolution and 19 levels
  - An increase to T231 L31 resolution was planned
  - This upgrade required at least 12 x available CPU power
  - Funding was available for 4 x CPU increase ...
- Upgrade was made possible by introducing:
  - A **semi-Lagrangian, semi-implicit** scheme on a **reduced Gaussian grid**
  - The new model was 6 x faster!



CRAY Y-MP/8: first HPC to run spectral SISL operationally (1992)

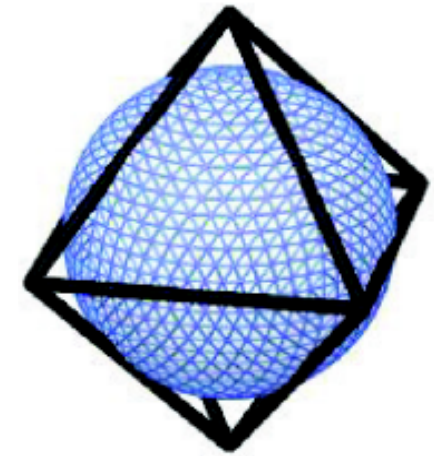
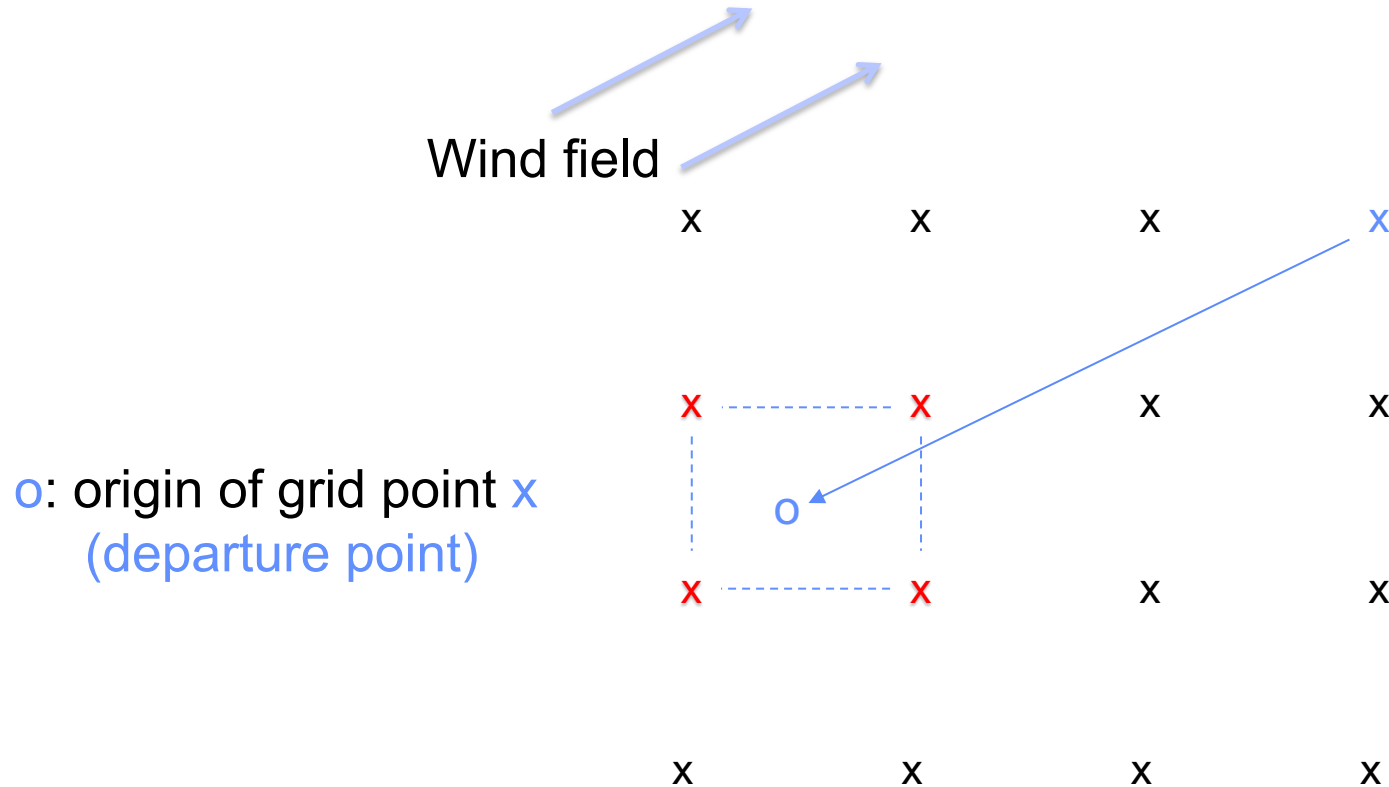
Source: ECMWF newsletter 60, Dec 1992



ATOS HPC at Bologna data centre (2022)

# Semi-Lagrangian advection in a picture

SL is a numerical technique for solving advection type PDEs which applies *Lagrangian* type of calculations on grid-point models



A semi-Lagrangian trajectory (departure point) needs to be traced back for each grid-point of the Gaussian grid

# The SL solution of the advection equation

Start with the simple passive tracer advection equation (constant wind):

$$\frac{D\phi}{Dt} \equiv \frac{\partial\phi}{\partial t} + V \cdot \nabla\phi = 0, \quad V = (u, v, w)$$

At time  $t$  parcel is at  $d$  and at  $t + \Delta t$  arrives at a grid-point

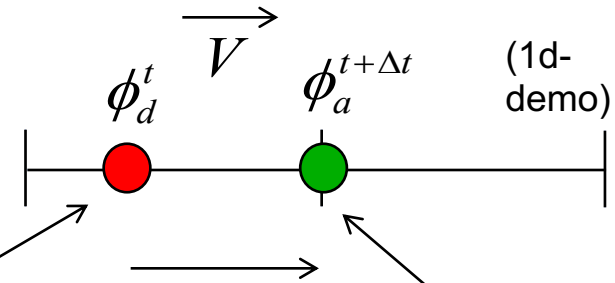
$$\int_{(r_d, t)}^{(r_a, t+\Delta t)} \frac{D\phi}{Dt} Dt = 0 \Rightarrow \phi_a^{t+\Delta t} = \phi_d^t, \quad r = (x, y, z)$$

This is the known result:  $\phi(r, t + \Delta t) = \phi(r - \Delta t V, t)$

d: **departure point (DP)**

parcel trajectory in  $\Delta t$

a: arrival point



- ◆ Solution at  $t + \Delta t$  is obtained by finding the DP location and interpolating the available (defined at time  $t$ ) grid-point  $\phi$  values at the DP
- ◆ Eulerian advection term  $V \cdot \nabla\phi$  is not explicitly computed - it is absorbed by the Lagrangian derivative (advection problem is reduced to interpolation)

# Computing the departure points in real atmospheric flows: SETTLS

Consider that air parcels move in time in straight line trajectories. Perform a 2nd order Taylor expansion of an arrival (grid) point to its departure point:

Stable Extrapolation Two  
Time Level Scheme  
(Hortal, QJRMS 2002)

$$r_a(t + \Delta t) = r_d(t) + \Delta t \cdot \left( \frac{Dr}{Dt} \right)_d^t + \frac{\Delta t^2}{2} \cdot \left( \frac{D^2r}{Dt^2} \right)_{AV} \quad \text{AV: average value along SL trajectory}$$

$$\left( \frac{Dr}{Dt} \right)_d^t = V_d(t), \quad \left( \frac{D^2r}{Dt^2} \right)_{AV} = \left( \frac{DV}{Dt} \right)_{AV} \approx \frac{V_a(t) - V_d(t - \Delta t)}{\Delta t}$$

Hence,

$$r_a(t + \Delta t) \approx r_d(t) + \frac{\Delta t}{2} \cdot (V_a(t) + \{2V(t) - V(t - \Delta t)\}_d)$$

DP can be computed by iterative sequence based on above SETTLS formula :

$$r_d^{(k)} = r_a - \frac{\Delta t}{2} \cdot (V_a(t) + \{2V(t) - V(t - \Delta t)\}_{r_d^{(k-1)}}) \quad k = 1, 2, \dots, K$$

Interpolate at  $r_d^{(k-1)}$   $r_d^{(0)}$  = initial guess

# Departure point iterations convergence

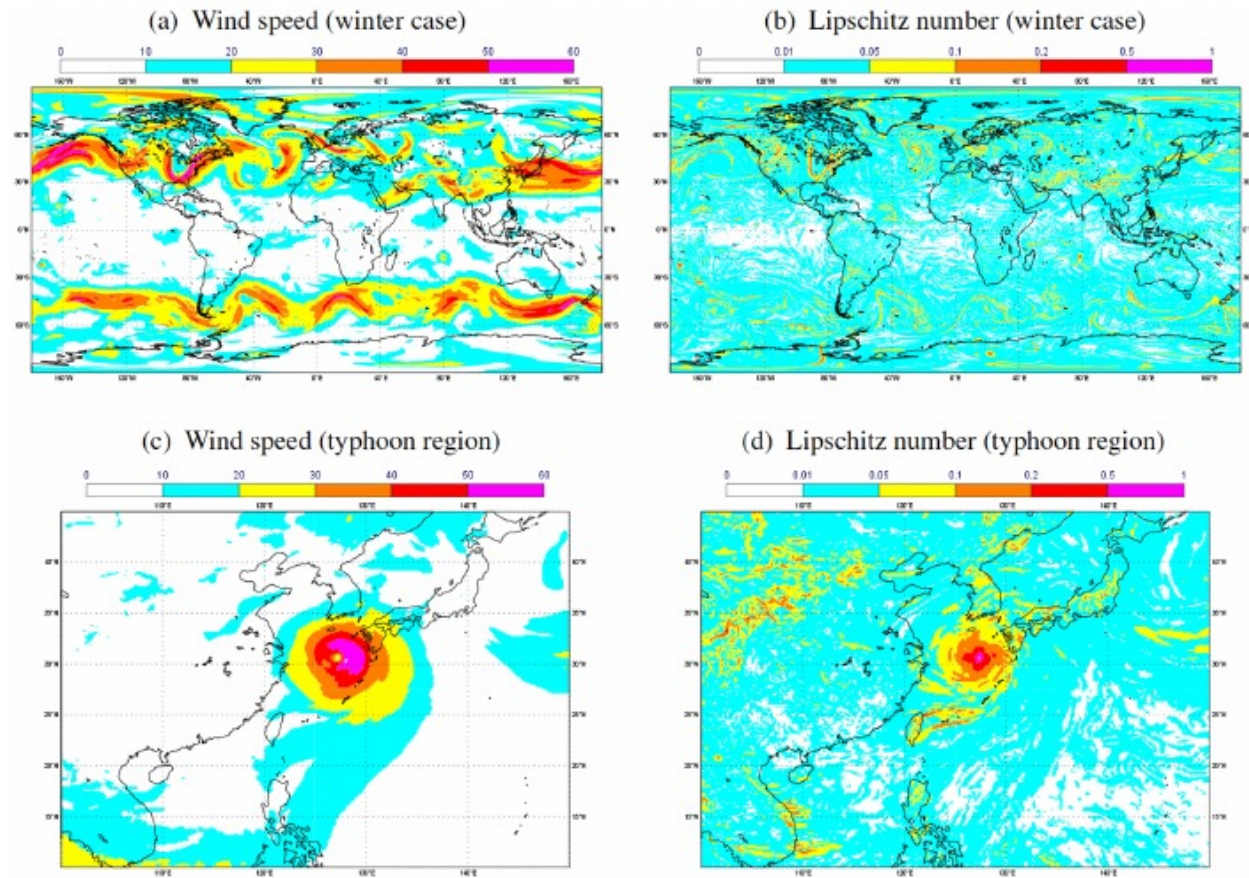
- SETTLS scheme for computing the departure point is iterative
- Its convergence depends on Lipschitz number magnitude. Let  $\mathbf{r}_D^{[\nu]}$  an estimate of the departure point D at iteration number  $\nu$ . Then:

$$\|\mathbf{r}_D^{[\nu]} - \mathbf{r}_D^{[\nu-1]}\| \leq L \|\mathbf{r}_D^{[\nu-1]} - \mathbf{r}_D^{[\nu-2]}\|, \quad \nu = 2, 3 \dots, \nu_{max}$$

$$L \equiv \Delta t \left\| \frac{\partial \mathbf{V}}{\partial \mathbf{r}} \right\| \quad \text{Lipschitz (deformational Courant) number}$$

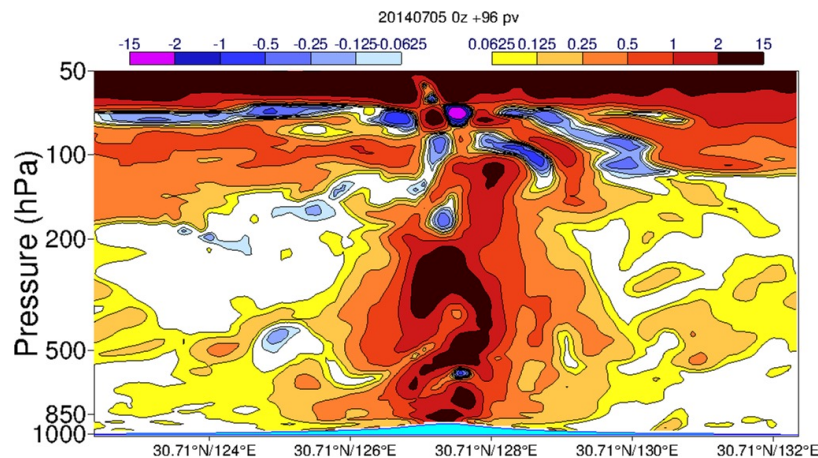
- $L < 1$  is a sufficient condition for convergence
- $L$  is an upper bound of the rate of convergence

# Lipschitz numbers in IFS forecasts

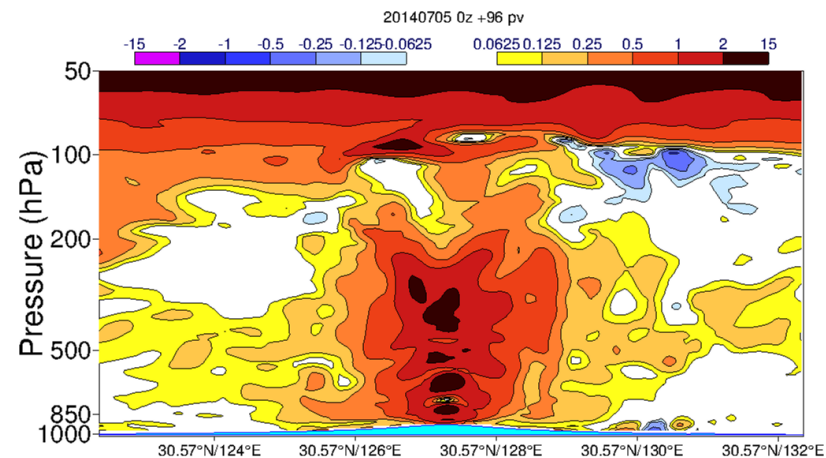


(a), (b): 00UTC 10 January 2014,  $t+48$ hrs fc at 500hPa. (c), (d): 00UTC 5 July 2014  $t+96$  hrs fc at 850hPa

# Side-effects of non-converging DP iterations

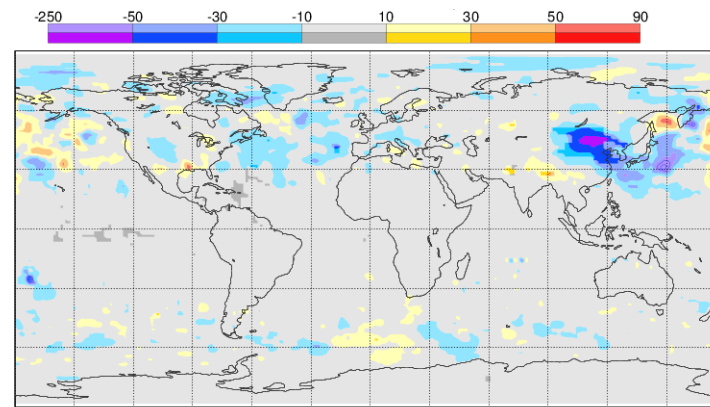


**DP iterations haven't converged: 3 –iterations with old scheme**



**DP iterations have converged: 5-iterations with old scheme or 3-iterations with new scheme**

- **Pre cy48r1: 5 DP iterations** needed for sufficient convergence (Diamantakis & Magnusson, MWR2016 doi:10.1175/MWR-D-15-0432.1)
- **From cy48r1: fast convergence in 3 iterations** starting from previous timestep DPs (Diamantakis & Vana, QJRM 2021, <https://doi.org/10.1002/qj.4224>)



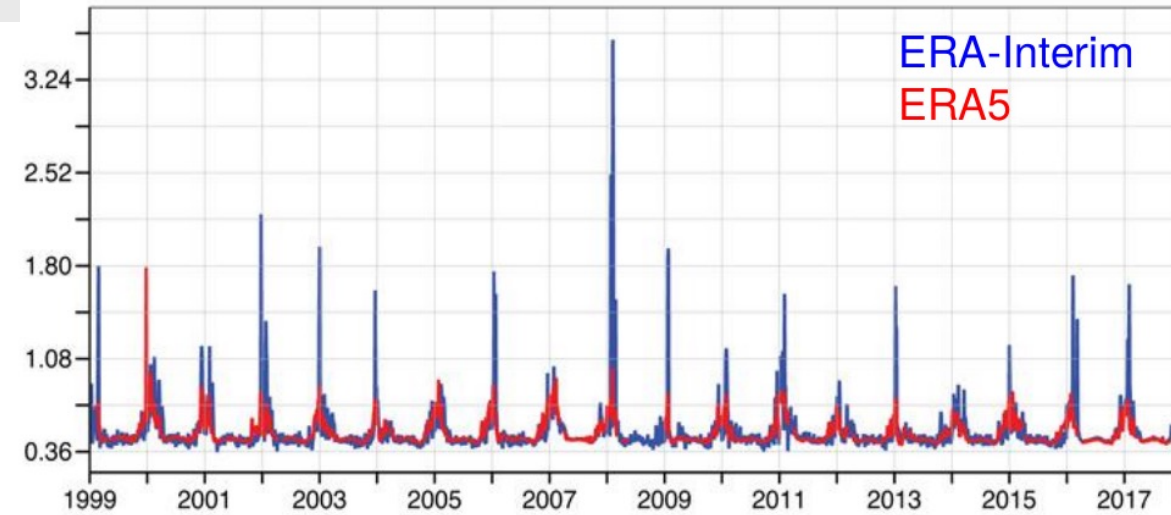
Root Mean Square Error difference for the geopotential height when DP iterations have not sufficiently converged

# Special treatment for stratospheric warming predictions

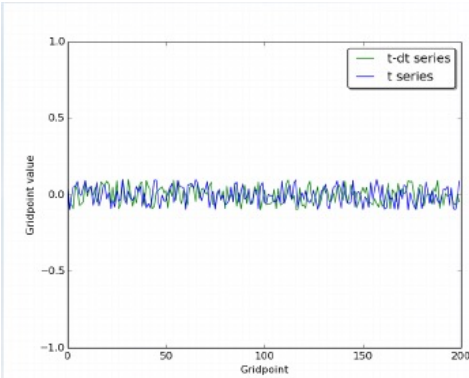
- In “Sudden Stratospheric Warmings” noise is seen in upper stratosphere and model underpredicts the temperature
- Origin of noise: **vertical velocity time extrapolation** in SETTLS
- Solution: use non-extrapolating 1<sup>st</sup> order scheme for grid-points with sudden changes in vertical velocity in 2 consecutive steps

Much better representation of Sudden Stratospheric Warming events, due to changes in the Semi-Lagrangian scheme (*Diamantakis, 2014*)

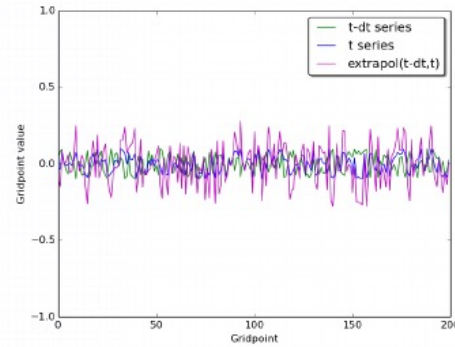
NH winter SSWs



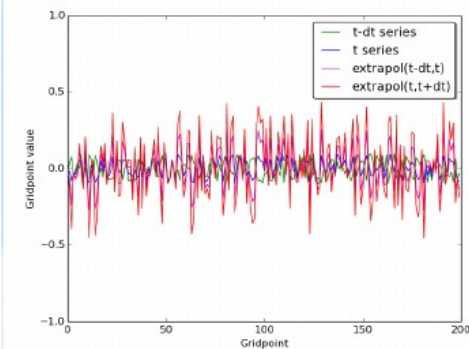
Impact of SETTLS time-extrapolation on noisy and smooth data



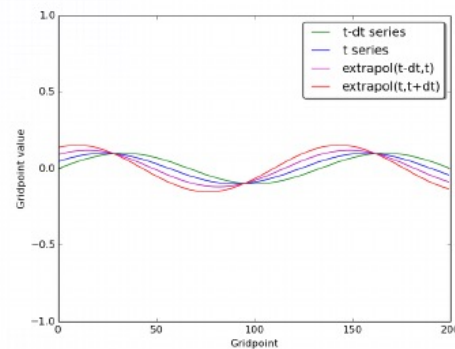
(a) Input t-series



(b)  $w^{ext1} = 2w^t - w^{t-\Delta t}$



(c)  $w^{ext2} = 2w^{ext1} - w^t$



(d) Smooth data

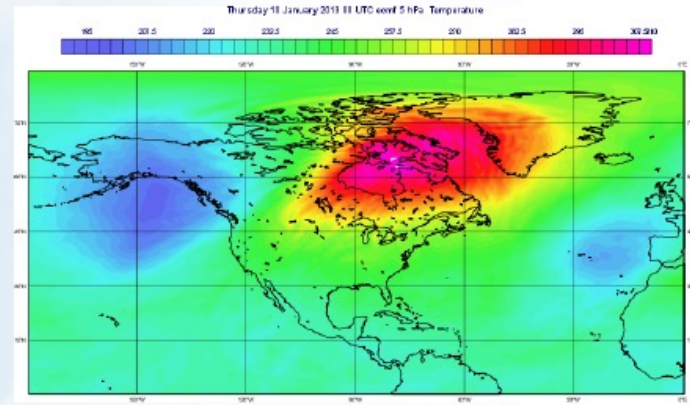
Standard deviation of MW radiances observed vs simulated temperature fields of ERA-Interim (blue) and ERA5 (red) using satellite channel (noaa15) peaking around 5hpa.

*T. McNally, A. Simmons*

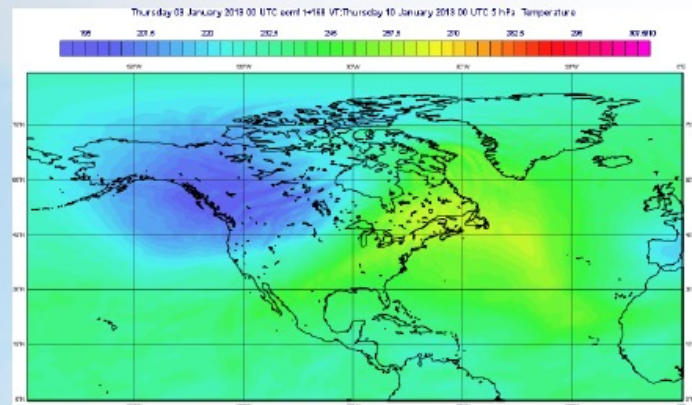
A reference: “Improving ECMWF forecasts of sudden stratospheric warmings”, ECMWF newsletter No.141 Autumn 2014



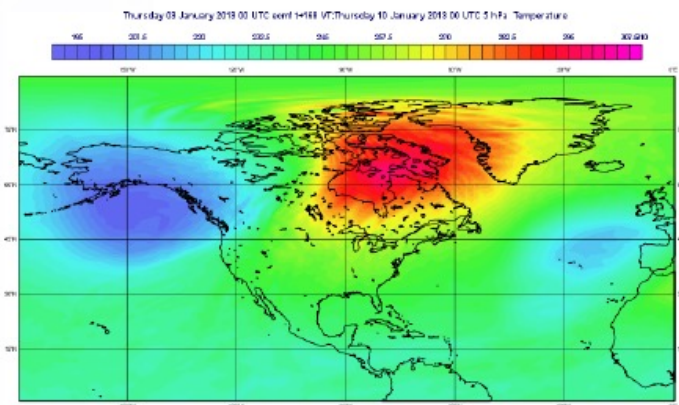
# Major SSW January 2013



(a) Analysis



(b) t+7d CONTROL



(c) t+7d NEW

Old scheme (CONTROL) versus currently SETTLS scheme

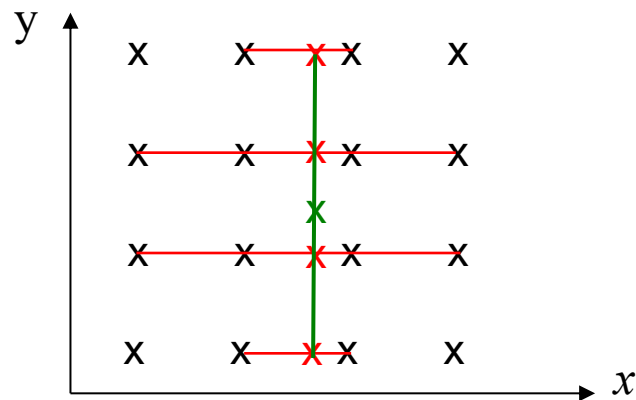
# The role of interpolation in the semi-Lagrangian scheme

After computing the departure points we need to:

- *Interpolate the advected field at the DP*
- *Interpolation must use the grid-points that lie in the neighbourhood of the DP*

ECMWF model uses quasi-monotone quasi-cubic Lagrange interpolation

Cubic Lagrange interpolation:  $\phi(x) = \sum_{i=1}^4 w_i(x)\phi_i$ ,  $w_i(x) = \frac{\prod_{k \neq i}^4 (x - x_k)}{\prod_{k \neq i} (x_i - x_k)}$



Number of 1D cubic interpolations in 2D: 5 => 3D: 21  
(64pt stencil)

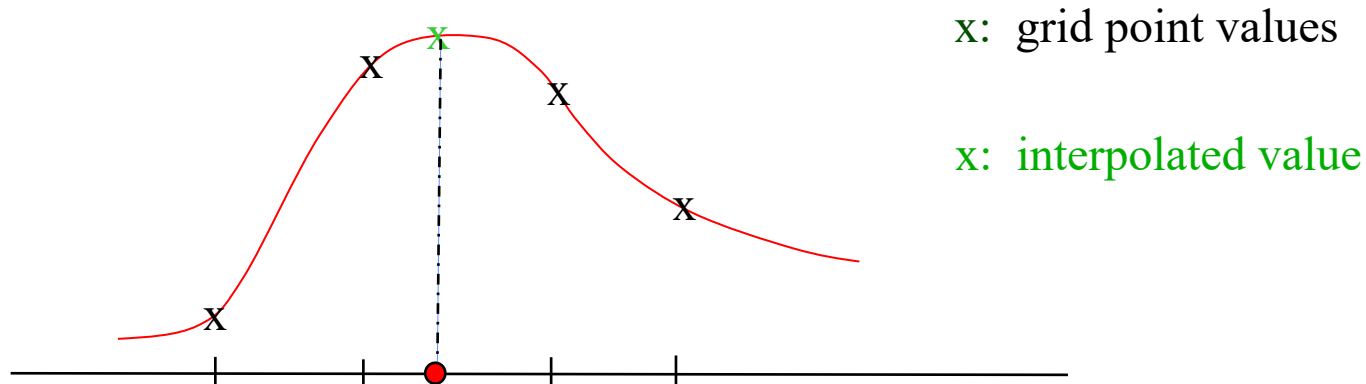
To save computations: use *cubic interpolation only for nearest neighbour rows and linear interpolation for remaining rows. “quasi-cubic interpolation”:*

*3\*cubic+2\*linear* interpolations in 2D

*7\*cubic+10\*linear* in 3D (32 pt stencil)

# Shape-preserving (locally monotonic) interpolation

- Creation of "artificial" maxima /minima



- Shape-preserving (quasi-monotone) interpolation

- Quasi-monotone cubic interpolation:  $\varphi_{qm} = \max(\varphi_{\min}, \min(\varphi_{\max}, \varphi_{cub}))$



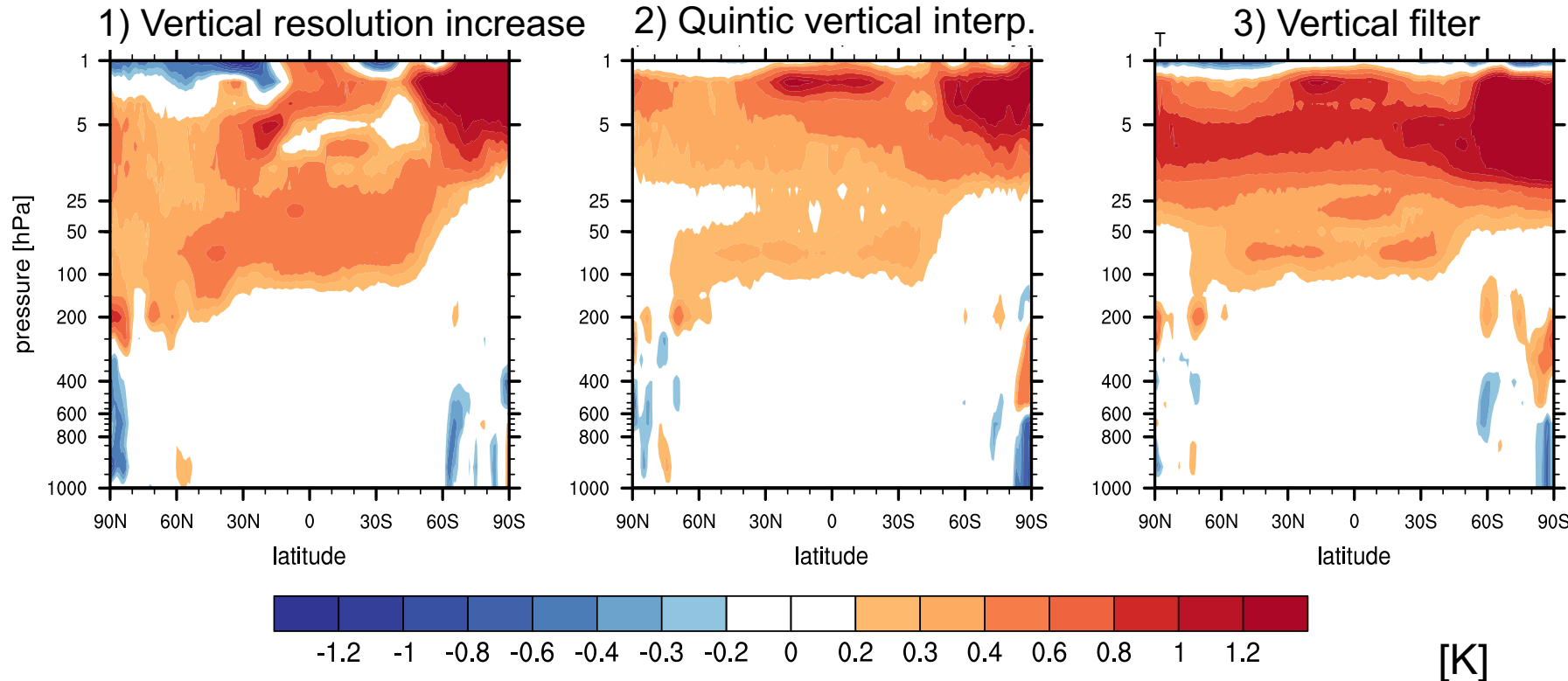
# Reducing stratospheric T-bias

Spurious  $2\Delta z$  noise due to **inadequate vertical-to-horizontal resolution aspect ratio** spuriously cools the stratosphere at high horizontal resolution.

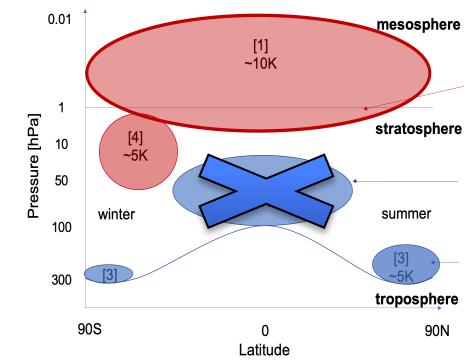
## Solutions:

- 1) increase **vertical resolution** (ENS in 47r3); **Expensive!**
- 2) use **quintic vertical interpolation** on T & q in the semi-Lagrangian advection (47r1)
- 3) **filter  $2\Delta z$  noise** in T in the semi-Lagrangian advection (SLVF filter by F. Vana, 48r1)

ECMWF newsletter 163,  
spring 2020 Polichtchouk et al



## T response from CTRL.



Also thinner sponge layer (above 0.78hPa) from cycle 48r1  
(work by I. Polichtchouk)

# SL advection on the sphere in cycle 48r1+

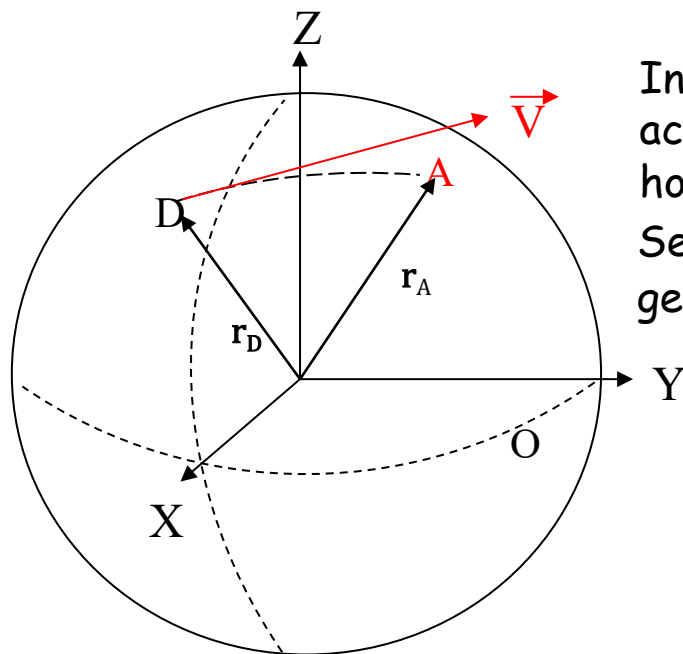
To compute DP on the sphere:

1. Transform horizontal velocities (u,v) in a geocentric Cartesian system (X, Y, Z )
2. Apply SETTLS algorithm to compute  $r_d = (X_d, Y_d, Z_d, \eta_d)$
3. Compute lon/lat of DP from  $(X_d, Y_d, Z_d)$   $\longrightarrow$

$$\lambda_d = ATAN2(Y_d, X_d)$$

$$\theta_d = \arcsin \frac{Z_d}{\sqrt{X_d^2 + Y_d^2 + Z_d^2}}$$

Details of the implementation on the IFS terrain following coordinate in: Diamantakis & Vana QJRMS 2021 10.1002/qj.4224.



In SL transport, vector quantities transported from D to A must be rotated to account for curvature effects: multiply with a "rotation matrix" R the interpolated horizontal wind vector at D

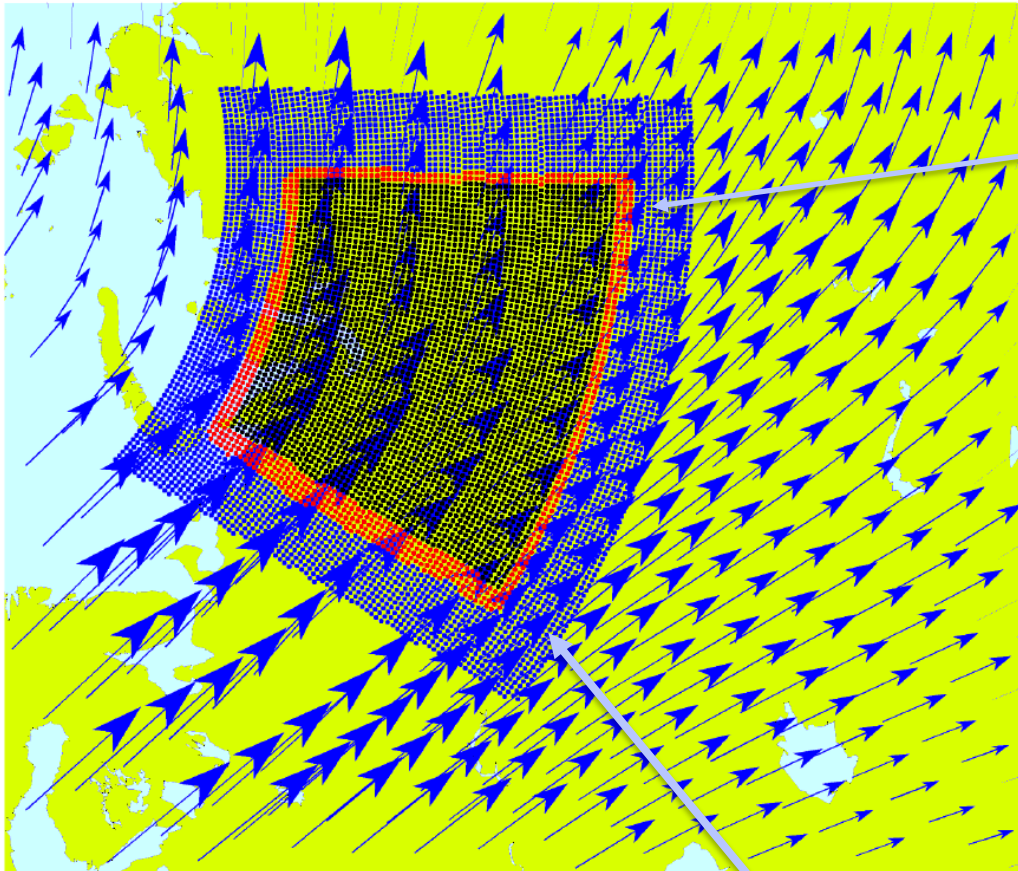
See Temperton et al QJRMS 2001, Staniforth et al QJRMS 2010 (provides general formula independent of  $\varphi = \text{angle } \widehat{DOA}$  between position vectors  $r_A$  and  $r_D$  )

$$\begin{pmatrix} u_A \\ v_A \end{pmatrix} = \underbrace{\begin{pmatrix} p & q \\ -q & p \end{pmatrix}}_{R(V_D): \text{rotation matrix}} \begin{pmatrix} u_D \\ v_D \end{pmatrix}, \quad q = \frac{(\sin \theta_A + \sin \theta_D) \sin(\lambda_A - \lambda_D)}{1 + \cos \varphi}$$

$$p = \frac{\cos \theta_A \cos \theta_D + (1 + \sin \theta_A \sin \theta_D) \cos(\lambda_A - \lambda_D)}{1 + \cos \varphi}$$

# Parallel implementation of advection

Interpolation at the DP near the edges of MPI domains requires data from neighbouring domain



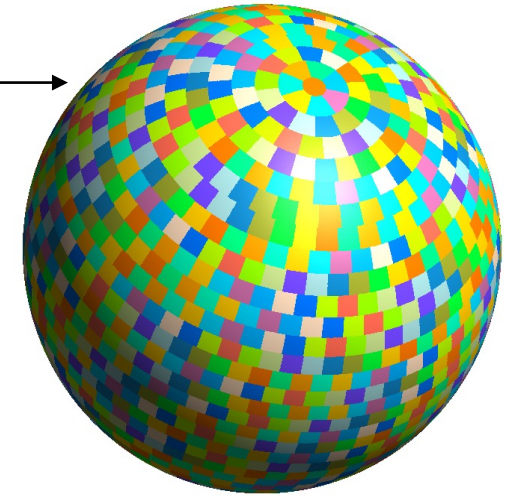
Blue: Halo region

Equal region domain decomposition + MPI and openMP parallel

Halo width for MPI assumes a maximum wind speed larger than the ones observed in the atmosphere e.g. 250m/s

Two levels of communication:

- Entire wind halo filled for the DP iterations
- When the DP is known then only a smaller sub-region around the DP needs to be filled
- No need to fetch data from remote processors at the expense of extra memory use



# Combining SL with SI to solve prognostic equations

- ◆ A nonlinear system of m-prognostic equations must be solved:

$$\frac{DX}{Dt} = M(X), \quad X = (X_1, X_2, \dots, X_m) \quad \text{e.g. } X=(u,v,T,p,q,\dots)$$

- ◆ Integrate along SL trajectory using 2<sup>nd</sup> order semi-implicit Crank-Nicolson scheme:

$$X^{t+\Delta t} - X_d^t = \int_t^{t+\Delta t} M(X) dt \Rightarrow X^{t+\Delta t} - X_d^t = \frac{\Delta t}{2} (M_d^t + M^{t+\Delta t})$$

Convention: when no subscript then the variable "sits" at an arrival (grid) point

- ◆ An isothermal reference profile is used to linearise terms in M which are responsible for fast wave propagation.

$$\mathfrak{R} = M - L$$

R: nonlinear residual terms; these are changing slowly and can be integrated explicitly

L: "Fast linearized" (e.g. GW) terms. These should be integrated implicitly to permit stable long timesteps

## IFS-SISL for NWP prognostic equations

Splitting in fast linear and slow nonlinear residual terms the two-time-level, 2<sup>nd</sup> order IFS discretization (Temperton et al, QJRMS 2001):

$$\frac{X^{t+\Delta t} - X_d^t}{\Delta t} = \frac{1}{2} (L_d^t + L^{t+\Delta t}) + \frac{1}{2} \overbrace{(\mathcal{R}_d^{t+\Delta t/2} + \mathcal{R}^{t+\Delta t/2})}^{\text{time-extrapolated nonlinear res}}$$

terms interpolated at the DP

The time-extrapolated non-linear residual of the right hand-side is at a trajectory mid-point and can be approximated by the 2<sup>nd</sup> order SETTLS expansion:

$$\mathcal{R}_M^{t+\Delta t/2} = \mathcal{R}_d^t + \frac{\Delta t}{2} \left( \frac{d\mathcal{R}}{dt} \right)_{AV} \approx \mathcal{R}_d^t + \frac{\Delta t}{2} \frac{\mathcal{R}^t - \mathcal{R}_d^{t-\Delta t}}{\Delta t}$$

Re-arranging terms, yields the familiar **SETTLS** formula resulting in a 2<sup>nd</sup> order discretization scheme

$$\frac{X^{t+\Delta t} - X_d^t}{\Delta t} = \frac{1}{2} (L_d^t + L^{t+\Delta t}) + \mathcal{R}_M^{t+\Delta t/2}, \quad \mathcal{R}_M^{t+\Delta t/2} = \frac{1}{2} \left( \mathcal{R}^t + \{2\mathcal{R}^t - \mathcal{R}^{t-\Delta t}\}_d \right)$$

all right-hand side terms are given



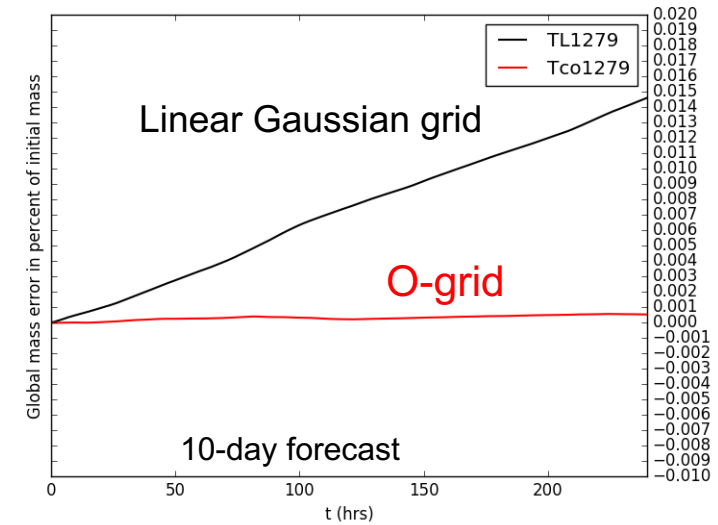
# Helmholtz equation

- ◆ Through elimination of variables, previous discretized system is reduced to a single Helmholtz elliptic equation in terms of horizontal wind **divergence**
- ◆ Helmholtz equation is solved in **spectral space** at the end of each timestep
- ◆ Constant in time reference profiles  $\implies$  constant coefficient Helmholtz equation
- ◆ Using spherical Harmonics properties Helmholtz equation can be solved very cheaply with a direct diagonal solver (or 5-diagonal when Coriolis terms are implicit)
  - ◆ Having a cheap Helmholtz solver + being able to use large  $\Delta t$  (due to unconditional stability and good dispersion properties of SISL) contributes to high computational efficiency
- ◆ Remaining prognostic variables are computed with back substitution

# Mass conservation in semi-Lagrangian advection

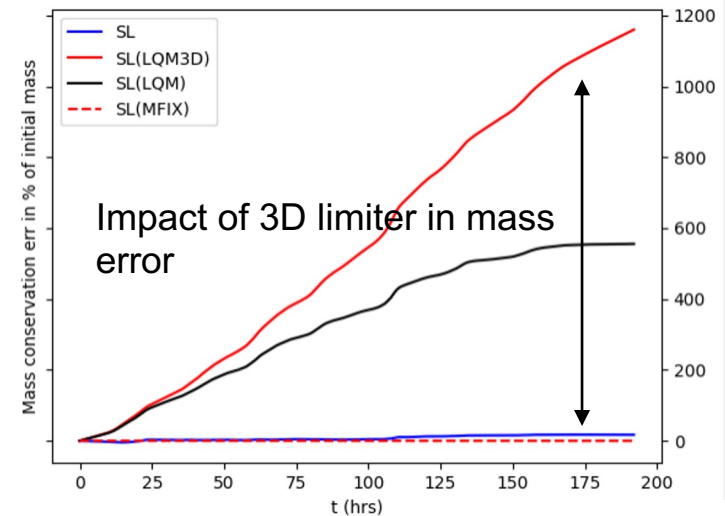
Mass conservation: important for **composition forecasts, long range, climate, high-resolution forecasts**

- Semi-Lagrangian time-stepping does not conserve mass, energy, momentum
- **Why?** Continuity expressed in non-conservation form + numerical errors (interpolation, etc)
  - Small conservation error for smooth tracers and total air mass
  - **Large for localised tracers with large gradients**
  - **Monotone interpolation limiters amplify greatly cons errors**
  - **Orography amplifies conservation errors**
  - **Interaction with boundary conditions amplifies cons errors: much larger near the surface**
    - COMAD interpolation available in openIFS (Malardel and Ricard QJRM, 2014) improves conservation of tracers near the surface



With O-grid **total air** mass conservation error is very small in double precision

Mass errors as percent of initial mass



Case study: Idealised **discontinuous** tracer 4x5 degrees rectangle placed on the near surface level :

- Large mass conservation error growth in time
- Monotone limiter greatly amplifies mass con errors but needed ...

# IFS mass fixers

- A simple mass fixer (rescaling) is applied on surface pressure field to keep air mass constant in time
- A more sophisticated tracer mass fixer is applied on water tracers, GHG gases, aerosols
  - The tracer mass fixer used is a locally weighted scheme (ECMWF TM 819, 2017 Diamantakis & Agusti-Panareda, scheme based on Bermejo & Conde MWR 2002) which gives more skilful tracer concentration predictions apart of correcting their global mass error

Corrected tracer mixing ratio

Tracer mixing ratio after advection

Lagrange multiplier

$$\phi_{jk} = \phi_{jk}^{adv} - \lambda w_{jk}, \quad \lambda = \frac{\delta M}{\underbrace{\sum_j A_j \sum_k w_{jk} \frac{\Delta p_{jk}^{adv}}{g}}_{\text{mass integral}}}, \quad \delta M = M(\phi_\chi^{adv}) - M(\phi_\chi^n)$$

M total mass for tracer  $\phi$

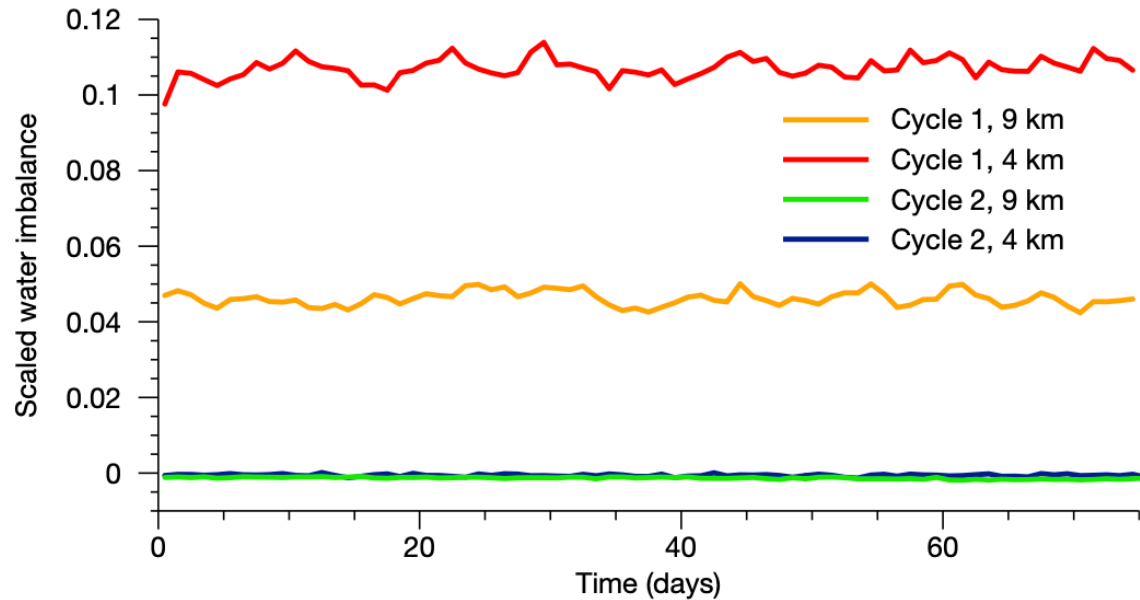
$\delta M$ : mass conservation error in a timestep after SL advection

$w_{jk}$  is a weight that depends on the sign of  $\delta M$ , it is proportional to the interpolation truncation error and the mass content of grid-box that corresponds to  $jk$

*Correction computed by the mass fixer is the solution of a constrained optimization problem that ensures that its global norm is minimized subject to the constraint that global mass remains constant*

# Fixing water leakage in IFS

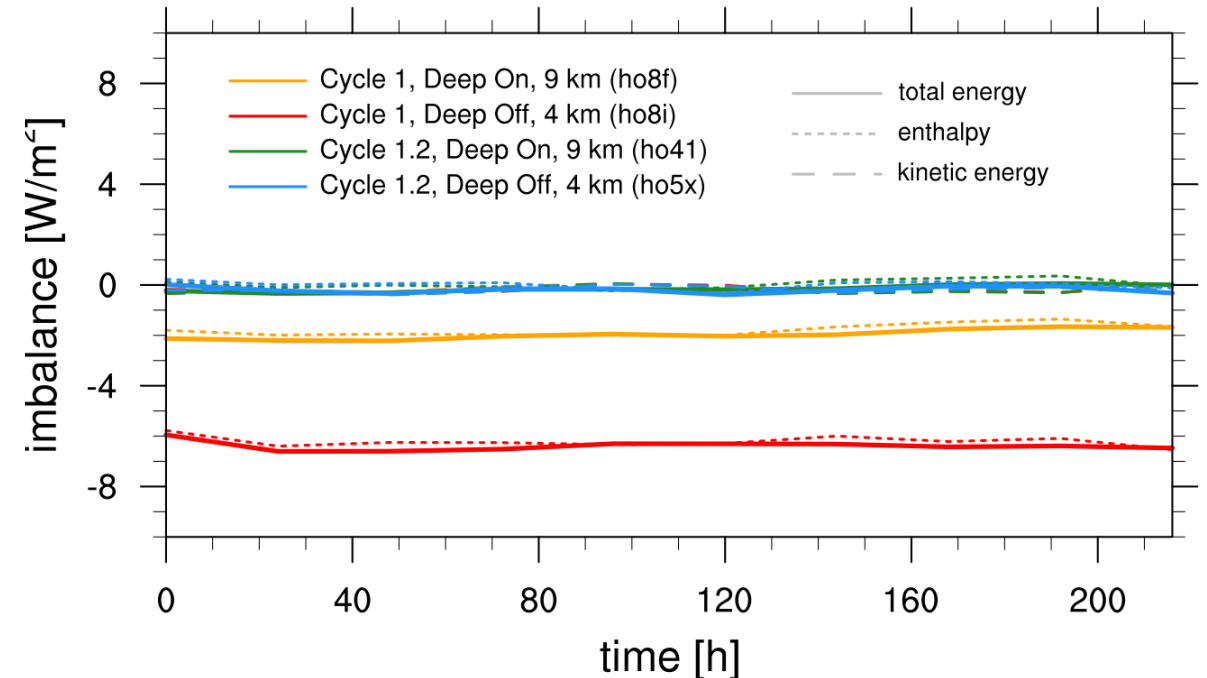
**Mass fixer on moist tracers (humidity, clouds): improvement in precipitation scores and overall skill of ENS forecasts**



**Total water conservation error as a fraction of total precipitation in long integrations**

- 10% surplus is reduced to nearly 0% with tracer mass fixer

Reference: ECMWF newsletter 172, p14



**Total Energy leakage reduction with fixer:**

2 W/m<sup>2</sup> -> -0.15 (deep conv on)

6 W/m<sup>2</sup> -> -0.32 (deep conv off)

Plots and diagnostics by Tobias Becker from **nextGEMS** project runs



Funded by the European Union

# CATRINE = Carbon Atmospheric Tracer Research to Improve Numerical schemes and Evaluation



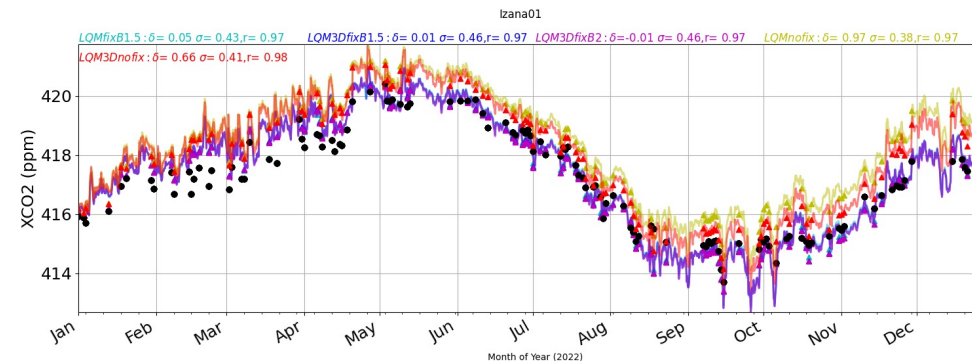
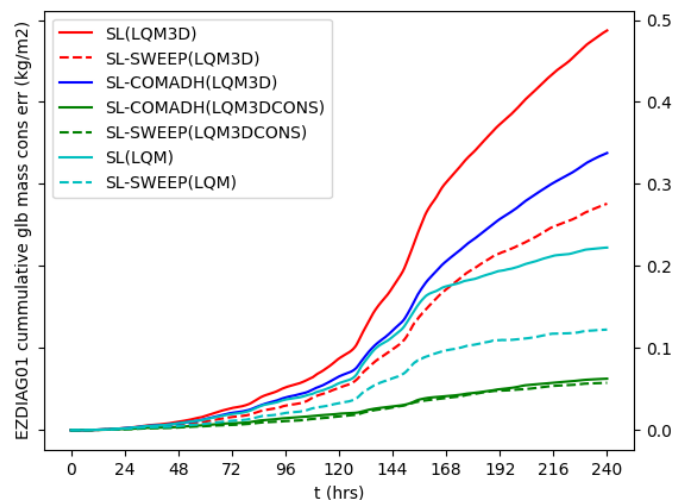
**CATRINE**  
Carbon Atmospheric Tracer  
Research to Improve  
Numerics and Evaluation

- 3-year HE project from 01-01-24 supporting CO2MVS (inversions of greenhouse gases) - ECMWF coordinator (A. Agusti-Panareda + M.D.)
- CATRINE WP1: **focus on numerical schemes**
  - Development of case studies & diagnostics to understand origin & evolution of mass conservation errors in SL advection
  - Design / implementation of improved algorithms and analysis of their impact on conservation & transport accuracy

**Project deliverable reports with detailed information on SL advection transport scheme evaluation and improvements:**

<https://www.catrine-project.eu/sites/default/files/2025-04/CATRINE-D1-1-V1.1.pdf>

<https://www.catrine-project.eu/sites/default/files/2025-06/CATRINE-D1-2-V1.0.pdf>



## Simulated time-series of CO<sub>2</sub> concentration versus observations at Izana site using optimized fluxes

Impact of enforcing conservation through mass fixer.

Conservation improves CO<sub>2</sub> simulation accuracy. Mass fixer (purple, blue) compared to run without mass fixer (yellow, red)

Advection case study: tracer emitted from a single-point source  
Reduction of mass conservation error (kg/m<sup>2</sup>) accumulation from CATRINE developments. Max reduction of conservation error ~ O(10).

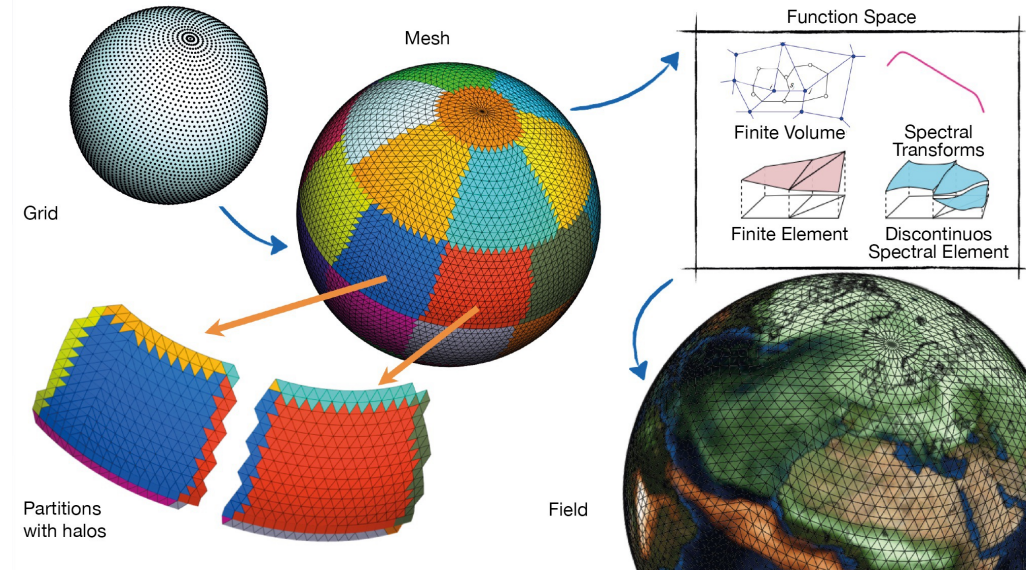
# Atlas: a library for NWP and Climate modelling

**Atlas (Deconinck et al, Computer Phys Coms 2017) : A library for NWP and Climate**

Open source code: <https://github.com/ecmwf/atlas>

Documentation: <https://sites.ecmwf.int/docs/atlas/>

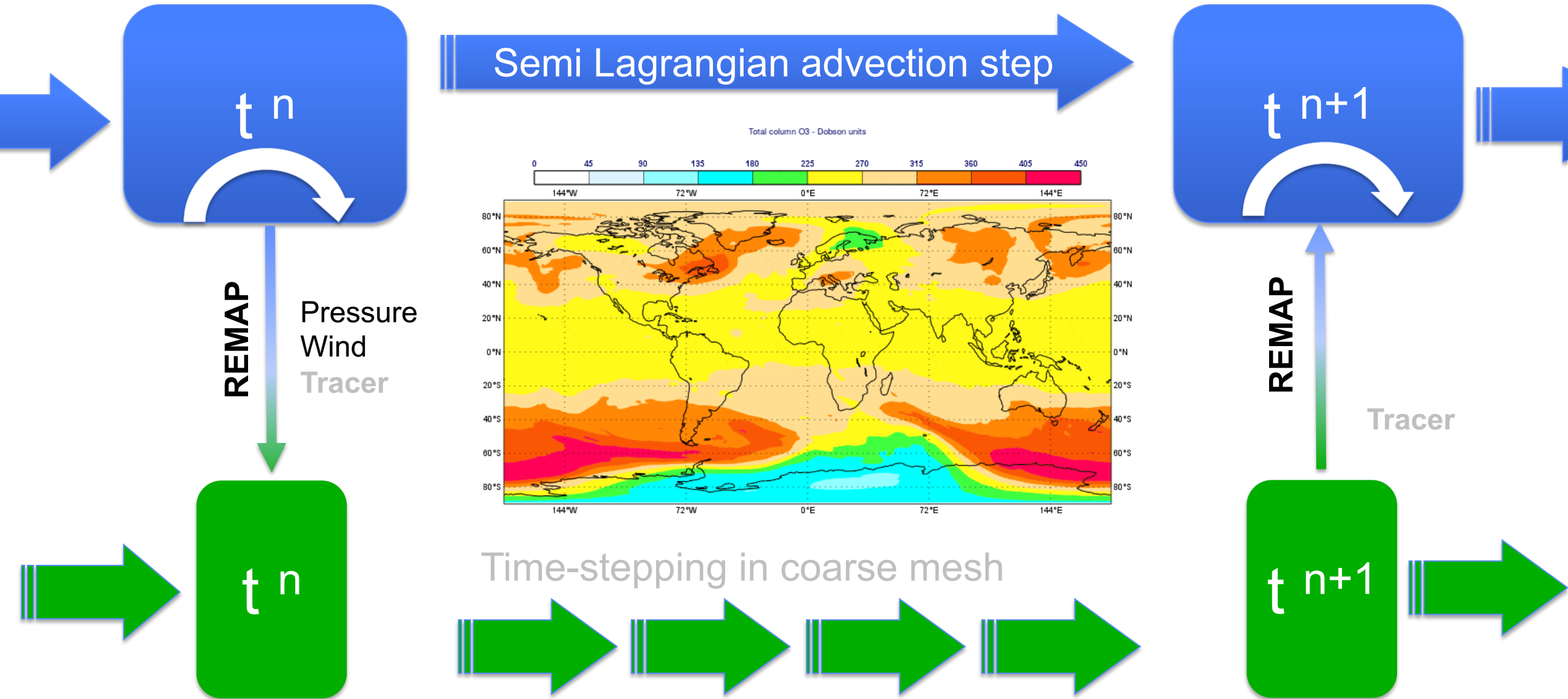
- C++ or Fortran interface
- Grid/mesh generation capabilities with parallelization (faster)
  - structured grids
  - unstructured hybrid meshes
- Mathematical operators for NWP & climate in HPC environment
- Parallel data structures and algorithms for mesh-to-mesh interpolation
- Flexible memory management and CPU-GPU offloading capabilities
  - Capabilities to couple models (e.g. ocean & atmos)
  - Capabilities parametrizations with the dynamics (e.g. radiation, cloud scheme)
- Can facilitate porting of alternative transport schemes for tracers in a non-disruptive way



```
grid = atlas_Grid("01280") ! Create 01280 octahedral
                             Gaussian grid
meshgenerator = atlas_MeshGenerator("structured")
mesh = meshgenerator%generate(grid) ! Generate
mesh from grid
method = atlas_fvm_Method(mesh) ! Setup finite
volume method
nabla = atlas_Nabla(method) ! Create FVM
nabla operator
call nabla%gradient(scalarfield, gradientfield) !
Compute gradient
```

# Cycle 48r1 Atlas capabilities: advection on multiple grids

**Demo: O3 advected at 32km grid forced by winds from a 18km grid**

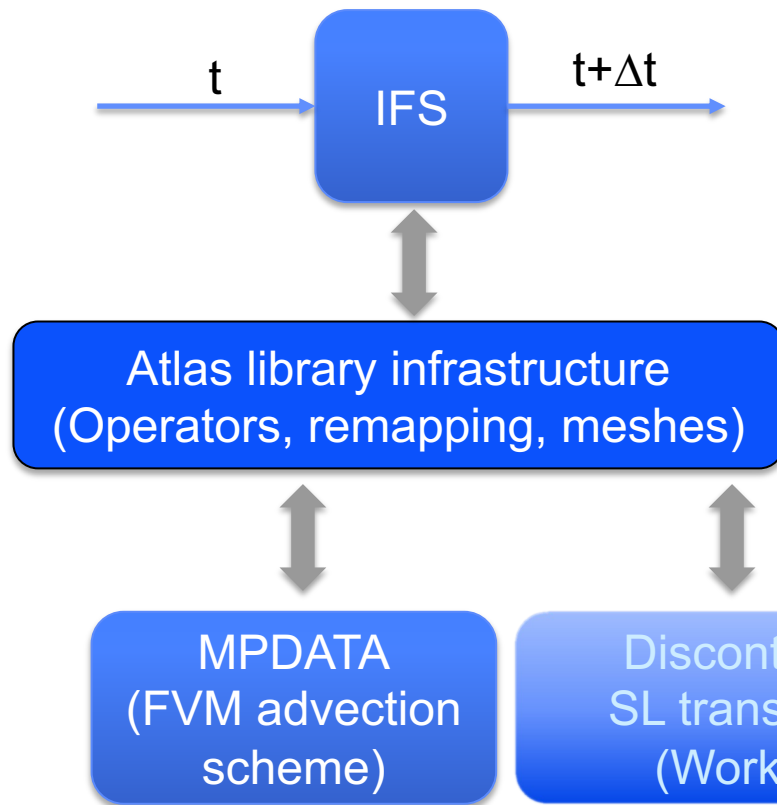


Remapping using linear interpolation (cubic also available)

Thanks to W. Deconinck for ppt schematic

# Example: plug-in MPDATA advection into IFS with Atlas MGRIDS

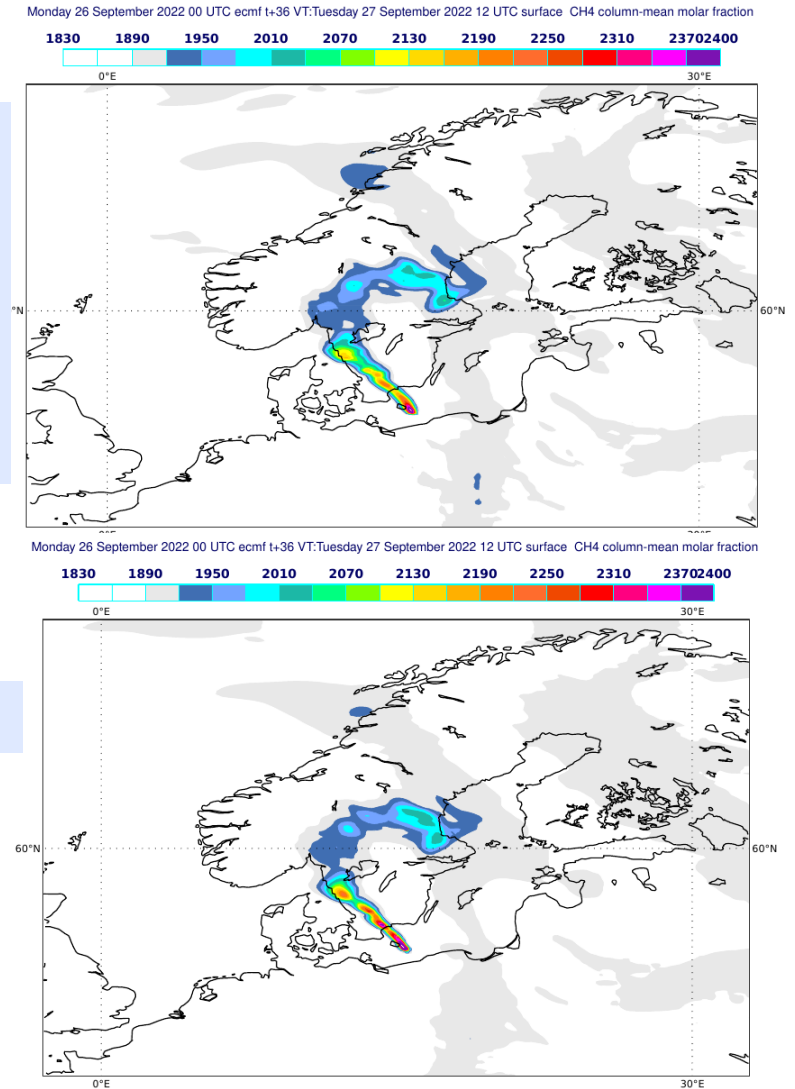
Nordstream gas leak simulation case study (9km)



## MPDATA simulation using Atlas MGRIDS (driven by IFS winds)

- Same grid Tco1279L137
- Sub-stepping per IFS step due to CFL limit
- Local conservation of MPDATA can be advantageous for plumes

## SL advection with mass fixer





# Work in progress in the dynamical core

*IFS relies on an efficient and accurate dynamical core that is constantly improved*

Current plans:

- New **faster** but **equally (or more) accurate interpolation** scheme **SWEEP** for semi-Lagrangian advection in progress
- Work on dry mass conserving forms of continuity equation with potential benefits
  - Improvement of intense precipitation systems
  - Improvement in the representation of tracers in CAMS
- Overall work to improve further tracer transport of the IFS (conservation properties, accuracy)

Long term plans: PMAP (Portable Model for multi-scale Atmospheric Predictions)

- Global and Regional model (PMAP-LES) written in Python Gt4Py
- Performance portable (CPU/GPU seamless execution)
- Inherently conserving and stable at very steep orographic slopes – PMAP-LES tested down to O(10) m resolution

**Thank you for your attention!**

IFS demo: Hurricane Ida simulation (10m wind gust) at 1.4km simulation by Inna Polichtchouk (INCITE 2022 project)

