

TRAINING  
COURSE

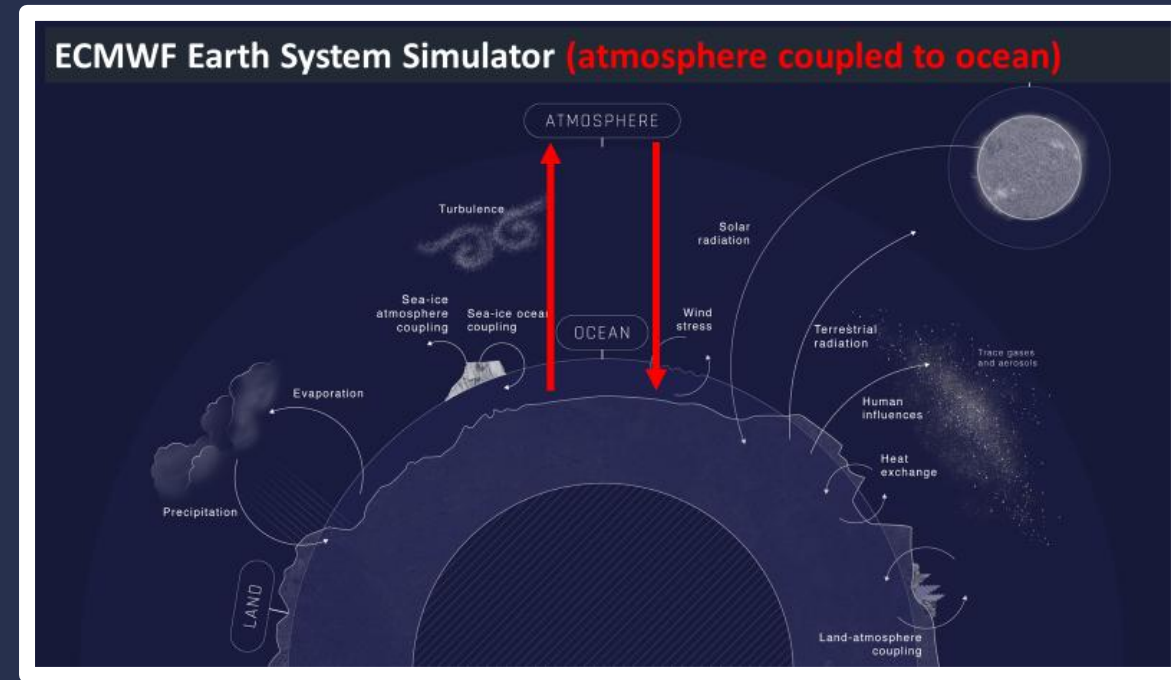
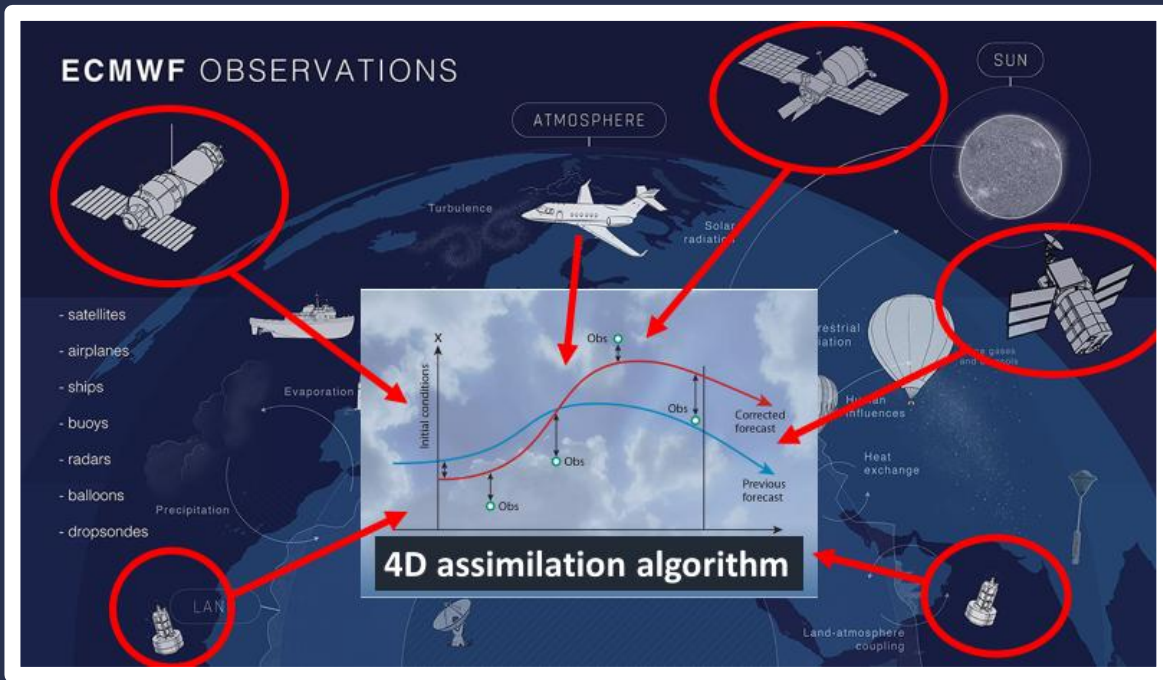
# The assimilation of satellite radiance observations

**Tony McNally**

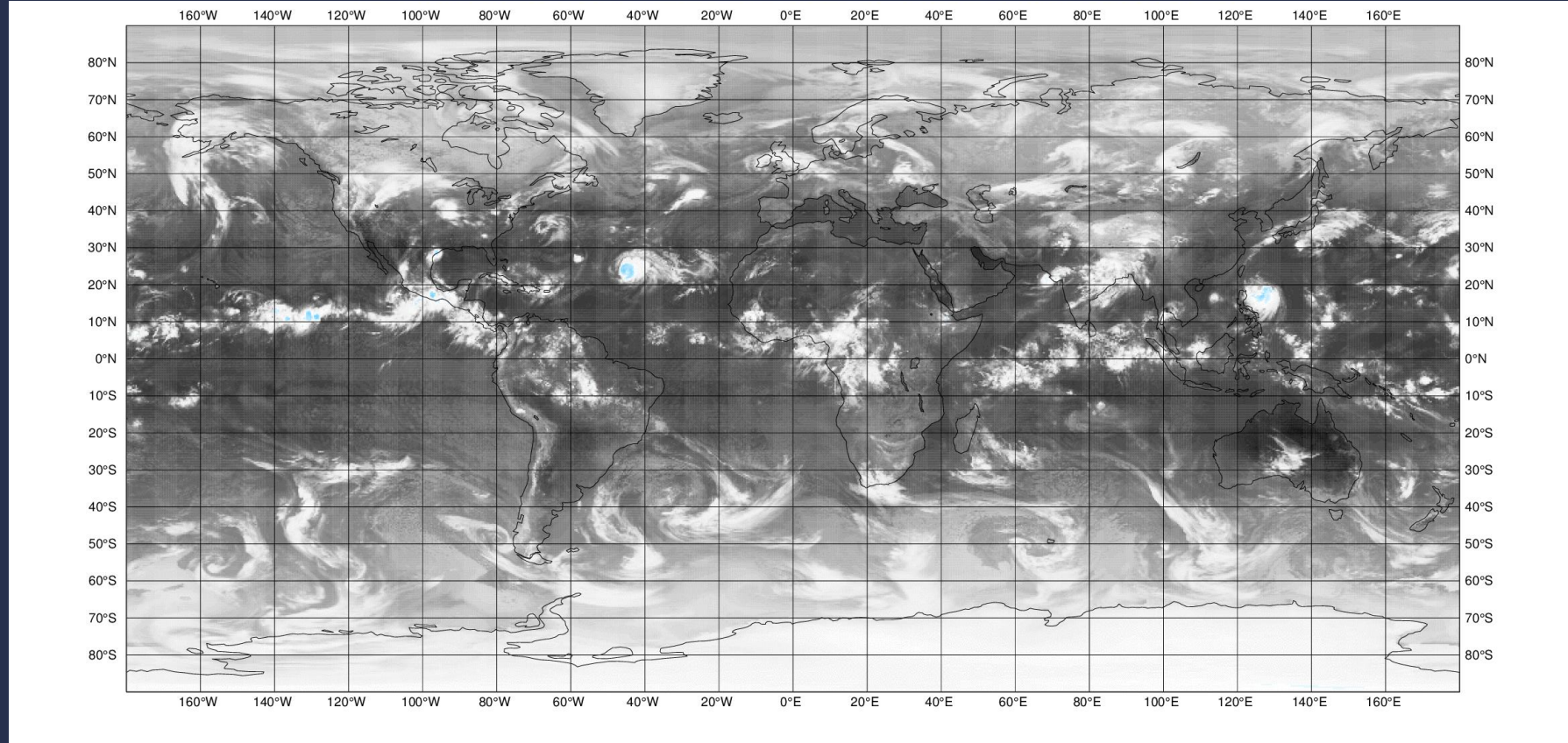
## **Overview:**

- **Why do we need satellites ?**
- **What do we have and which are most important ?**
- **What is actually measured ?**
- **Key elements of satellite data assimilation**

The Satellites and other observations provide initial conditions (what the atmosphere doing now) from which forecasts are launched

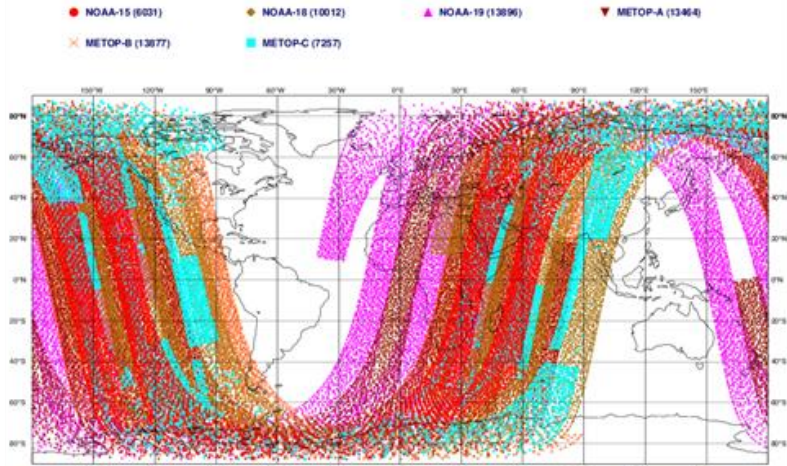


To forecast many days into the future, we need global initial conditions...and only satellites can provide this

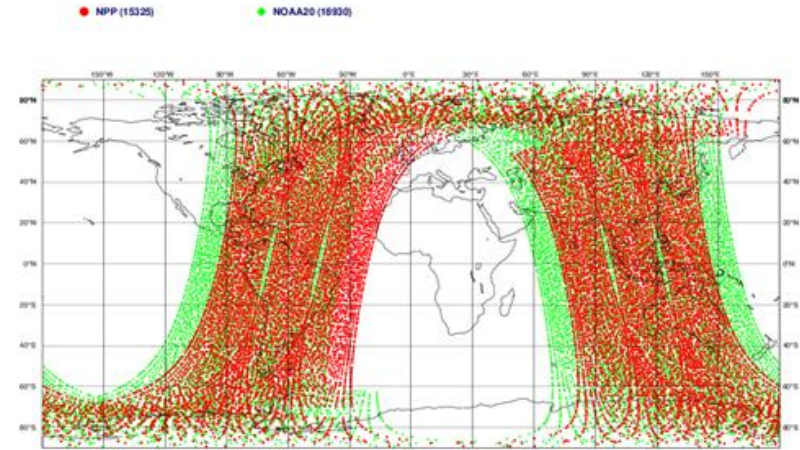


# Passive microwave (LEO)

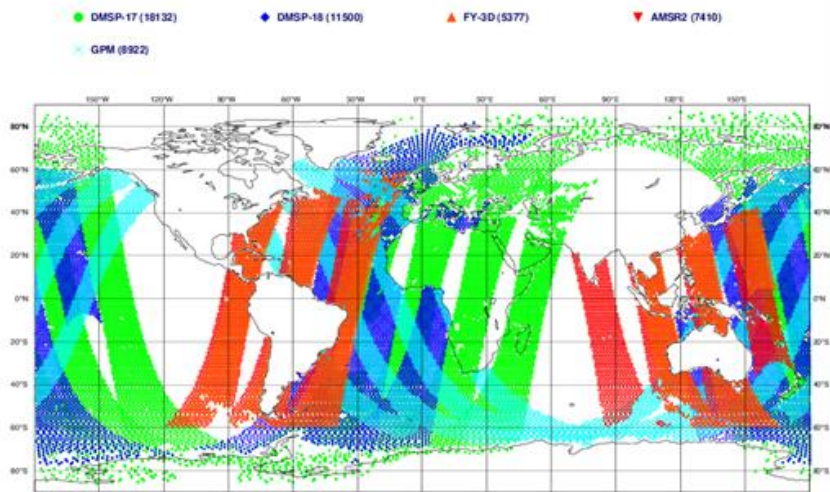
ECMWF data coverage (used observations) - AMSUA  
2021021703 to 2021021709  
Total number of obs = 64537



ECMWF data coverage (used observations) - ATMS  
2021021703 to 2021021709  
Total number of obs = 34255

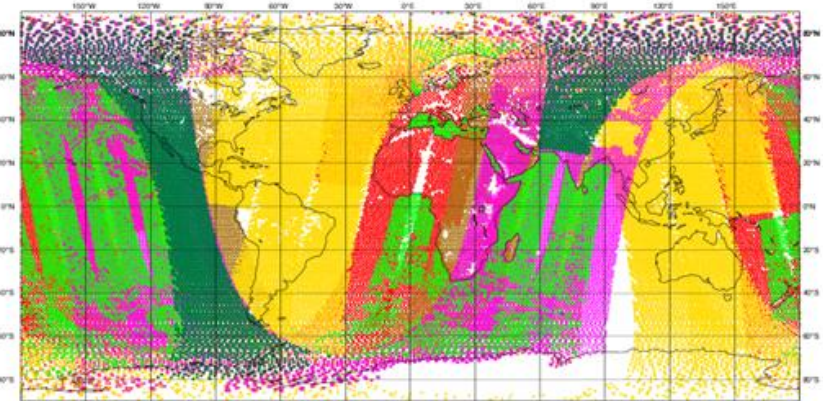


ECMWF data coverage (used observations) - MICROWAVE HUMIDITY IMAGERS  
2021021703 to 2021021709  
Total number of obs = 51341

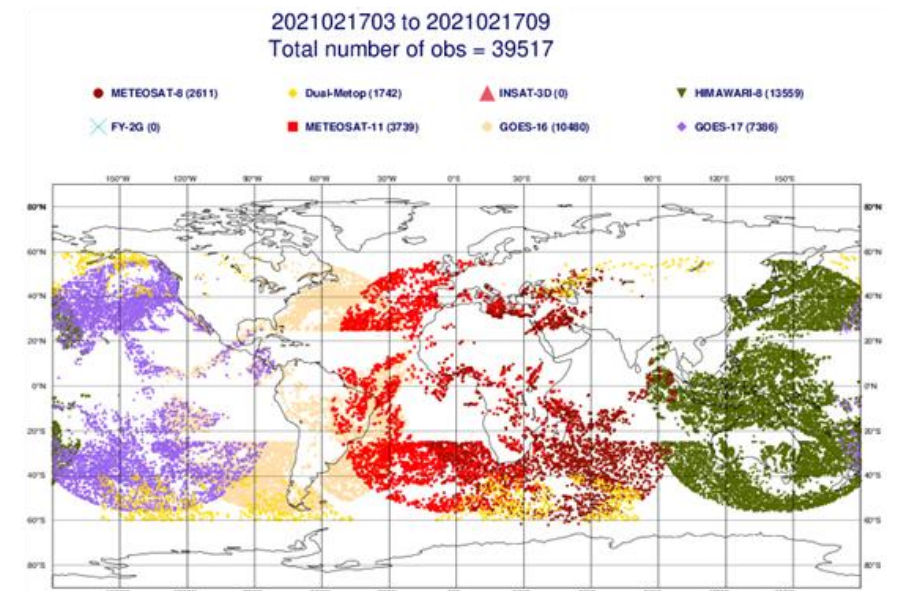
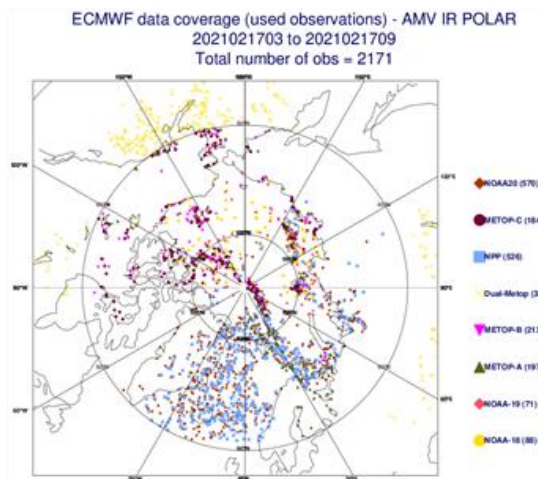
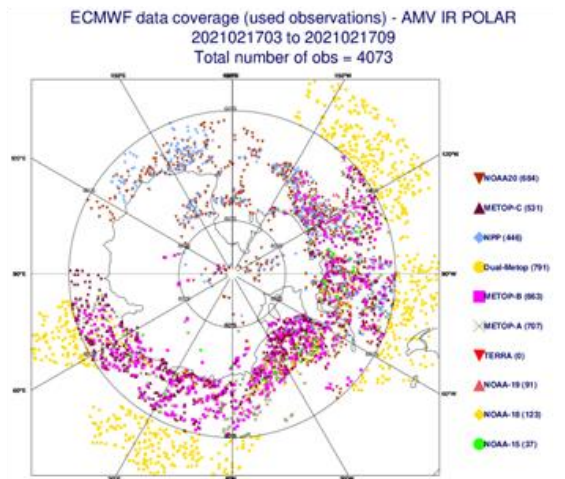
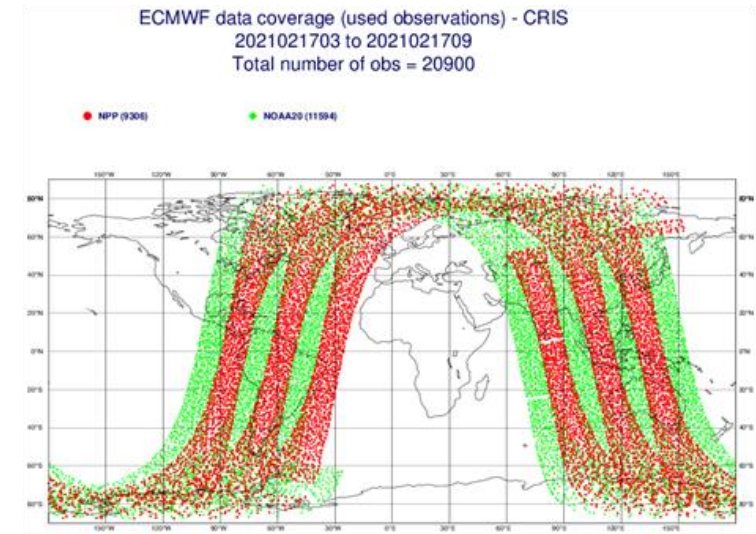
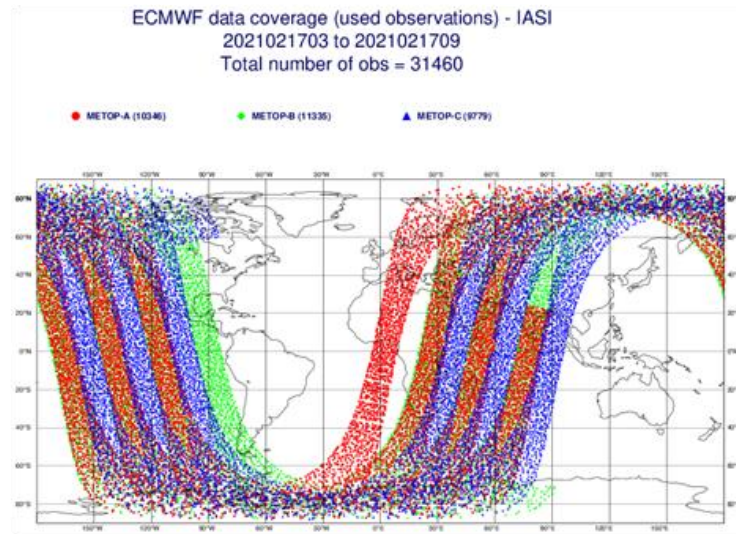


ECMWF data coverage (used observations) - MICROWAVE HUMIDITY SOUNDERS  
2021021703 to 2021021709  
Total number of obs = 110941

AEOLUS HLOS WINDS RAYLEIGH CLEAR (ASCENDING)

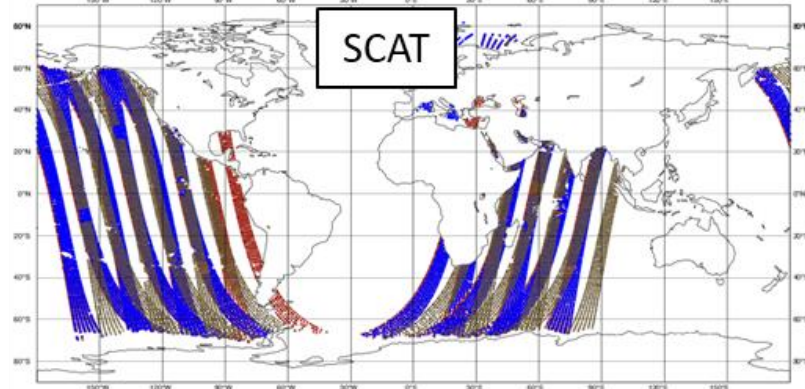


# Passive infrared (LEO and GEO)

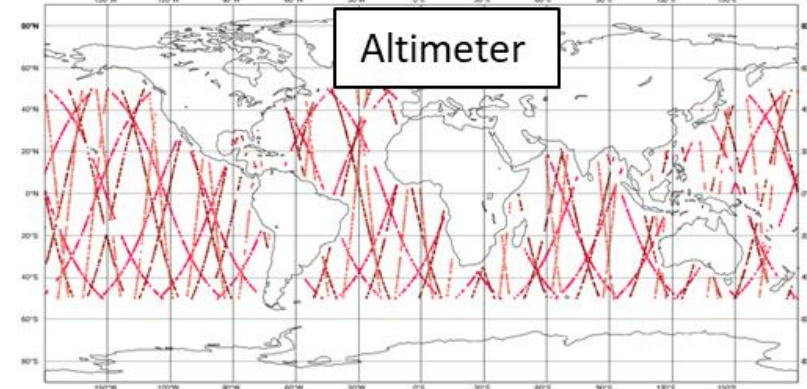


# Active sensors

ECMWF data coverage (used observations) - SCATTEROMETER  
 2021021703 to 2021021709  
 Total number of obs = 24631

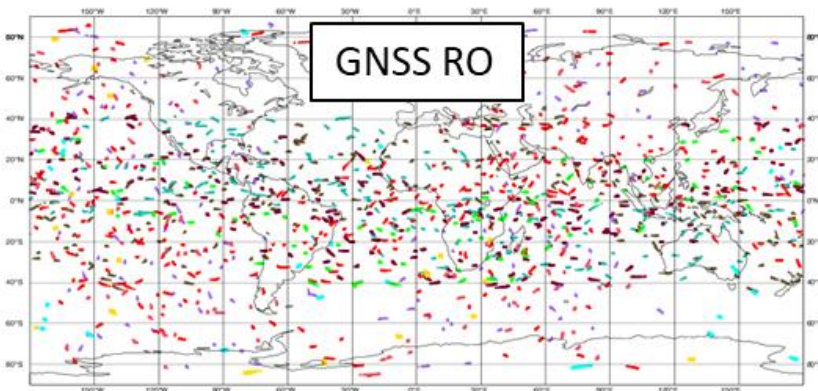


ECMWF data coverage (used observations) - SEA LEVEL ANOMALY  
 20210215 00  
 Total number of obs = 5376

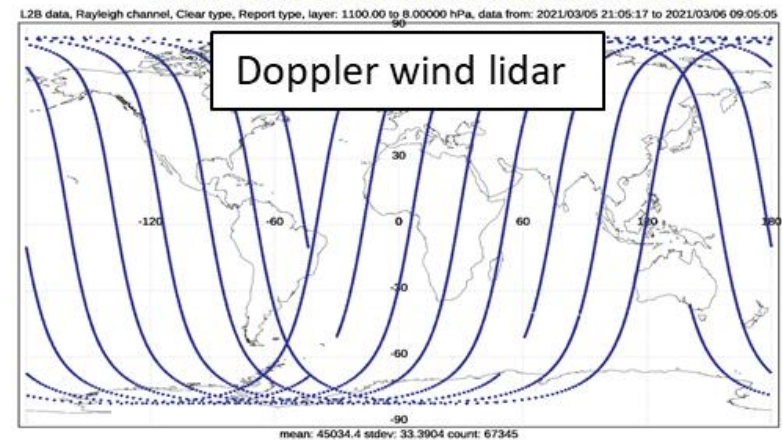


2021021703 to 2021021709  
 Total number of obs = 25832

- METOP-A (2475)
- TerraSAR-X (463)
- ▲ METOP-B (2851)
- ▼ TanDEM-X (66)
- KOMPSAT-5 (419)
- METOP-C (2275)
- PAZ (0)
- COSMIC2-E1 (3906)
- ▲ COSMIC2-E2 (3924)
- ▼ COSMIC2-E3 (3747)
- COSMIC2-E5 (1680)
- COSMIC2-E6 (4026)



AEOLUS HLOS WINDS RAYLEIGH CLEAR (ASCENDING)



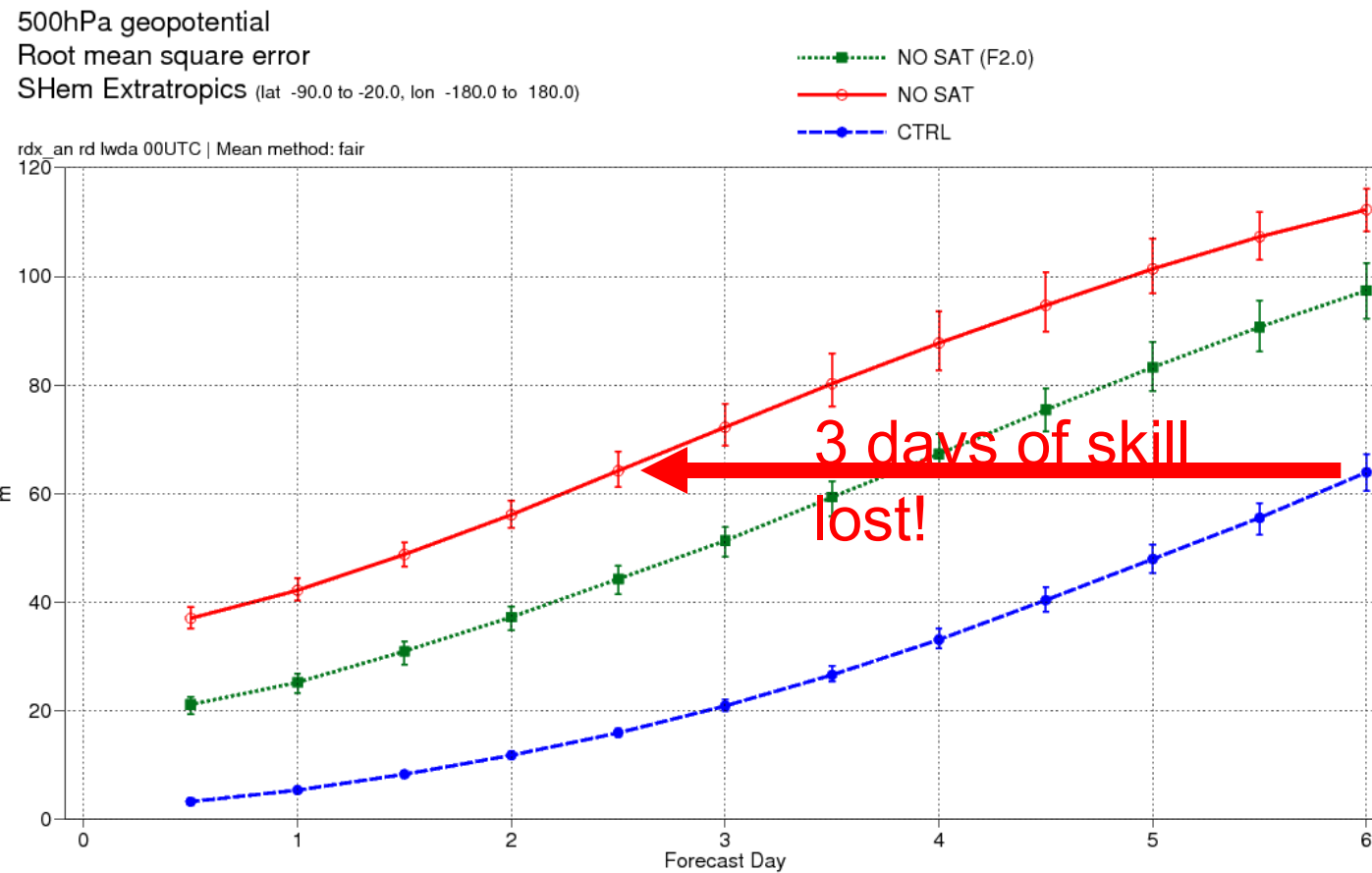
**Can we quantify how important  
are satellites for NWP ?**

**...denial experiments...**

# Can we quantify how important are satellites for NWP ?



# Can we quantify how important are satellites are for NWP ?



# Dorian viewed from the Sentinel-3 satellite



**Dorian viewed from the Sentinel-3 satellite**

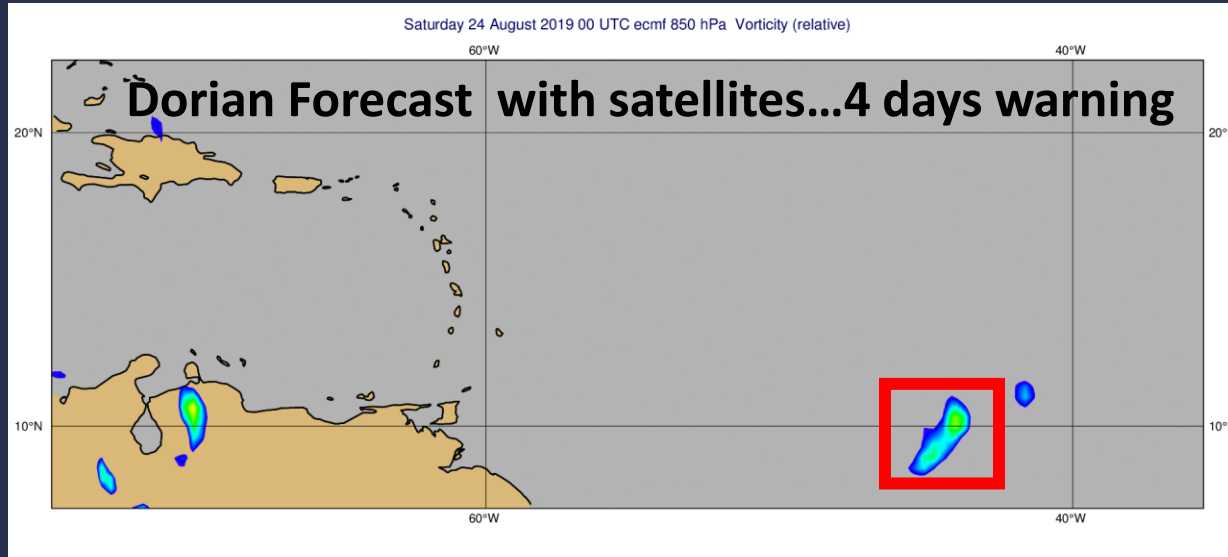


**Dorian viewed from the Bahamas**



**Most deadly event in recent history is Nargis (2008) that claimed ~ 130,000 lives**

# Early identification of storm genesis with satellites saves many thousands of lives

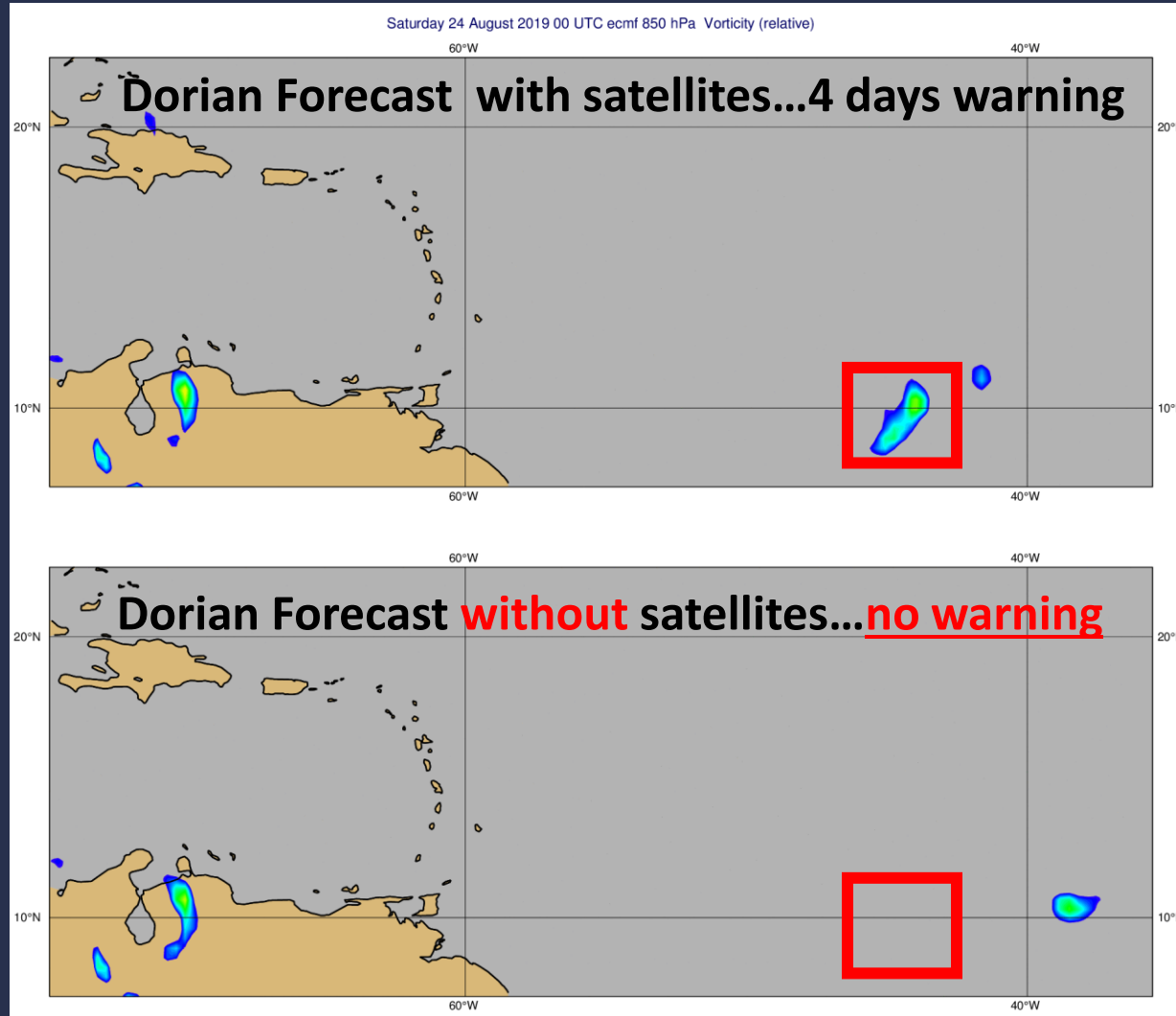


## Key information

1. Ocean surface temperature
2. mid level humidity
3. wind sheer

Satellites provide this ...

# Without satellites we would often give no warning of severe weather!



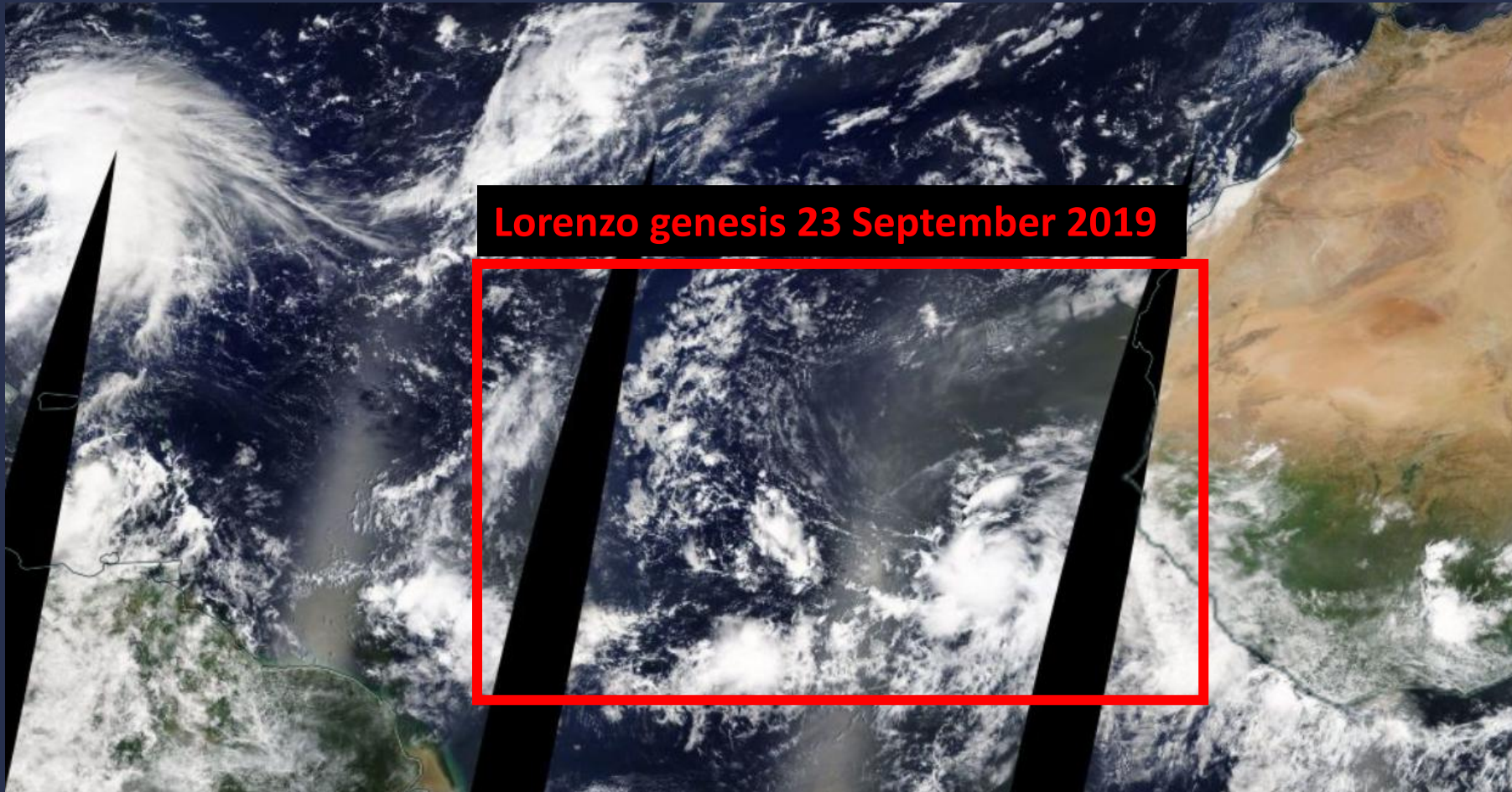
## Key observations

1. Ocean surface temperature
2. mid level humidity
3. wind sheer

# Early identification of storm genesis...Lorenzo

Key observations

- Ocean surface temperature ?
- mid level humidity ?
- wind sheer ?



# Early identification of storm genesis...in a challenging environment

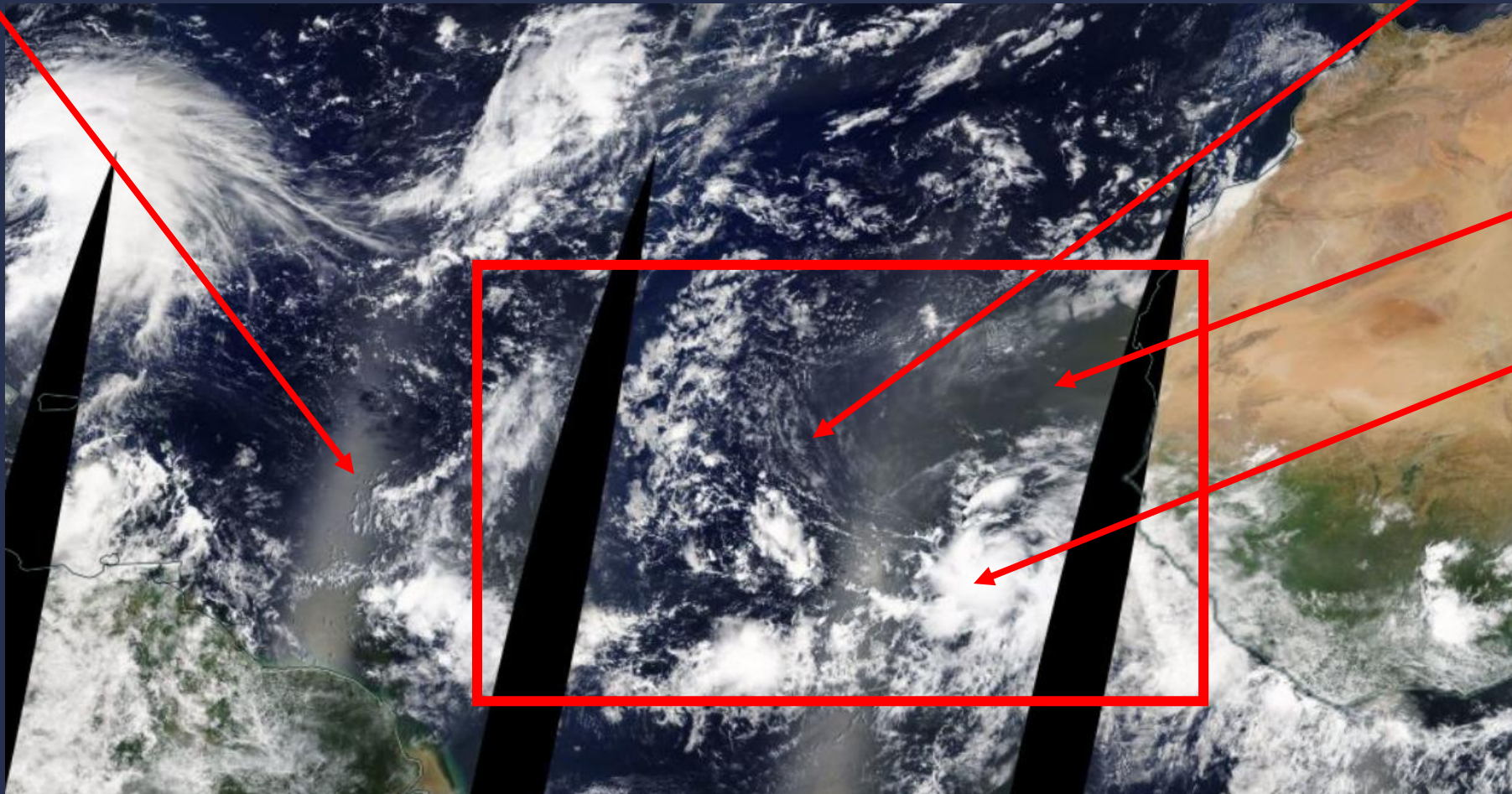
- Ocean surface temperature ?
- mid level humidity ?
- wind sheer ?

Sun glint

Semi-transparent ice clouds

Desert dust

opaque clouds

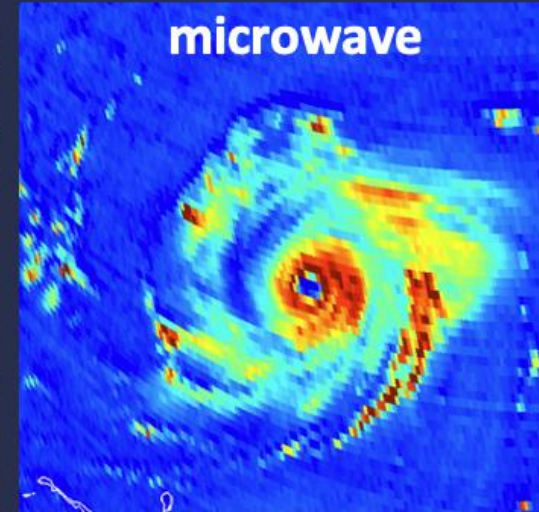


# Satellite sensors operating at different frequencies are used to understand the full atmospheric state...

Cloud phase and motion (wind)



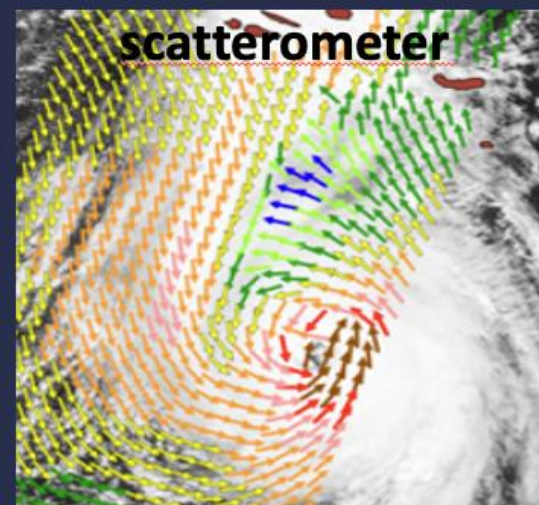
Water and rain content within clouds



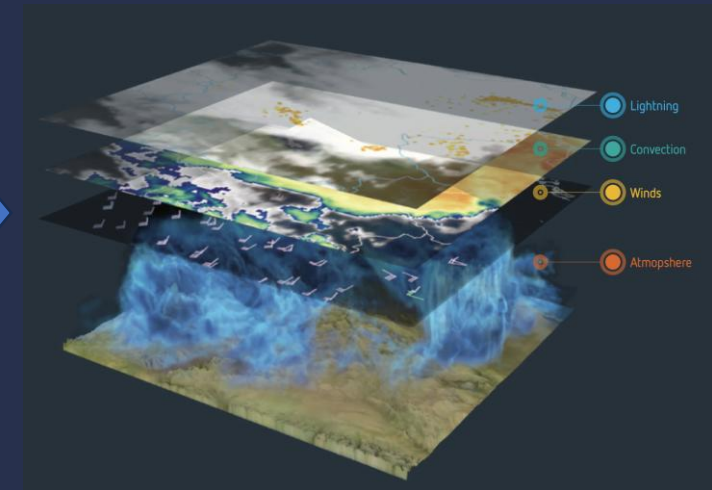
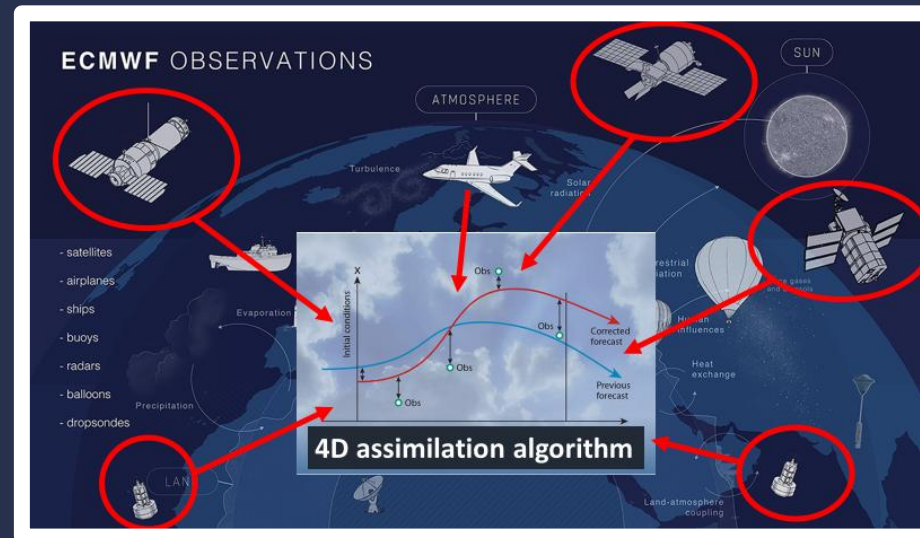
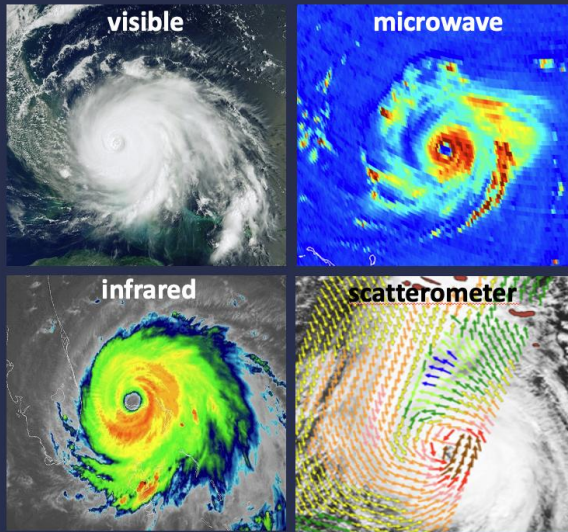
Temperature and height of clouds, humidity in clear sky



Penetrating the clouds to look at ocean roughness and land state



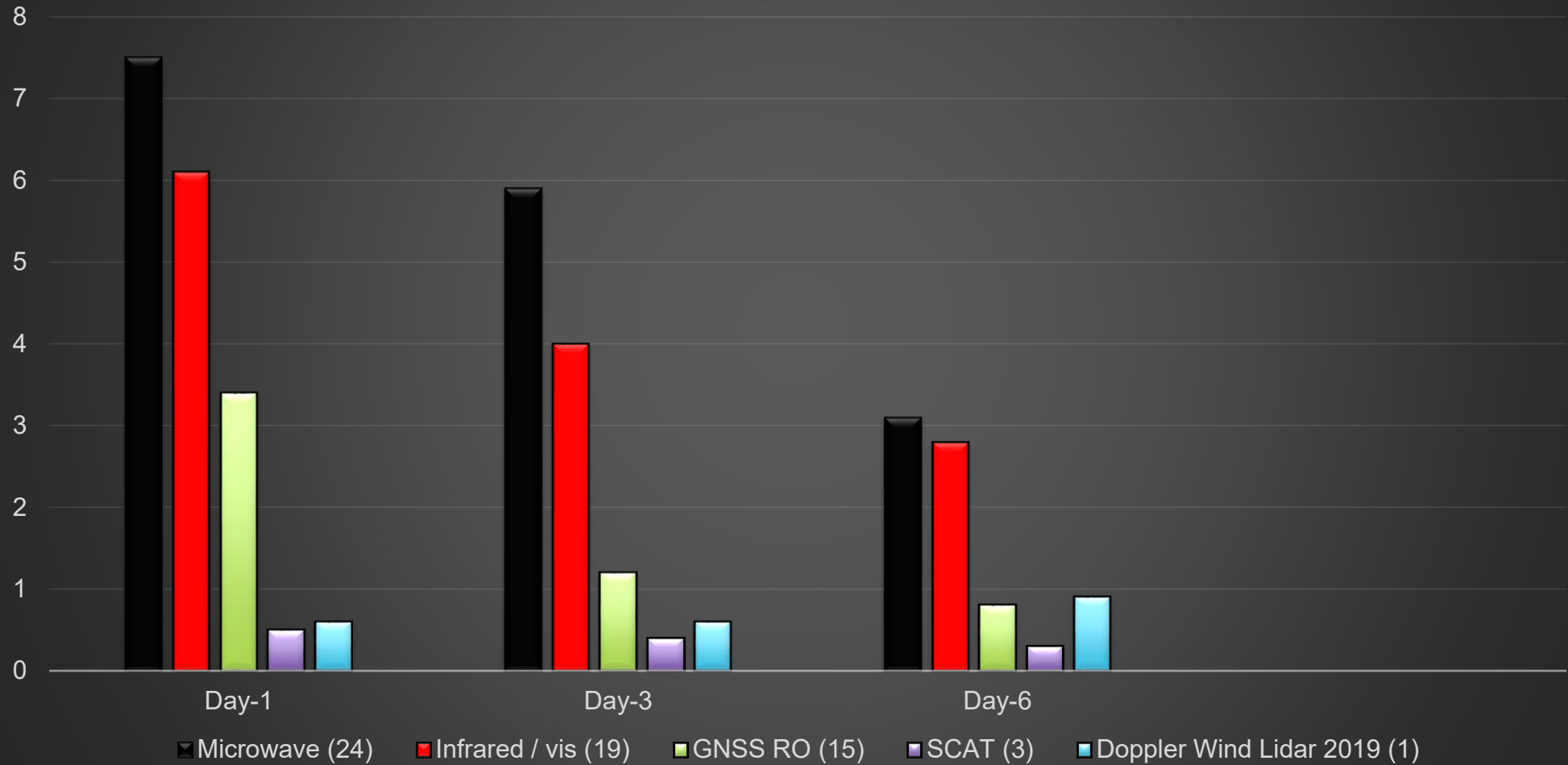
# ...But require highly sophisticated Data Assimilation Systems to combine these into a coherent 3D picture



**Which satellite observations  
are most important for NWP ?**

# Impact of different sensor technologies

Percentage loss of forecast skill on denial  
(global z500 anomaly correlation – SON 2020)



# Which satellite observations are most important for NWP ?

Sensor technology	Processing route
Passive microwave	L1 Radiances
Passive infrared	L1 Radiances / AMV
Radio occultation	Bending angles
SCAT / Altimeter	L2 wind / SLA / SWH
Doppler wind lidar	L2 LOS wind

Note that sensors available for NWP are typically downward looking instruments (not limb viewing)

**What do passive microwave  
and infrared satellite  
instruments measure ...?**

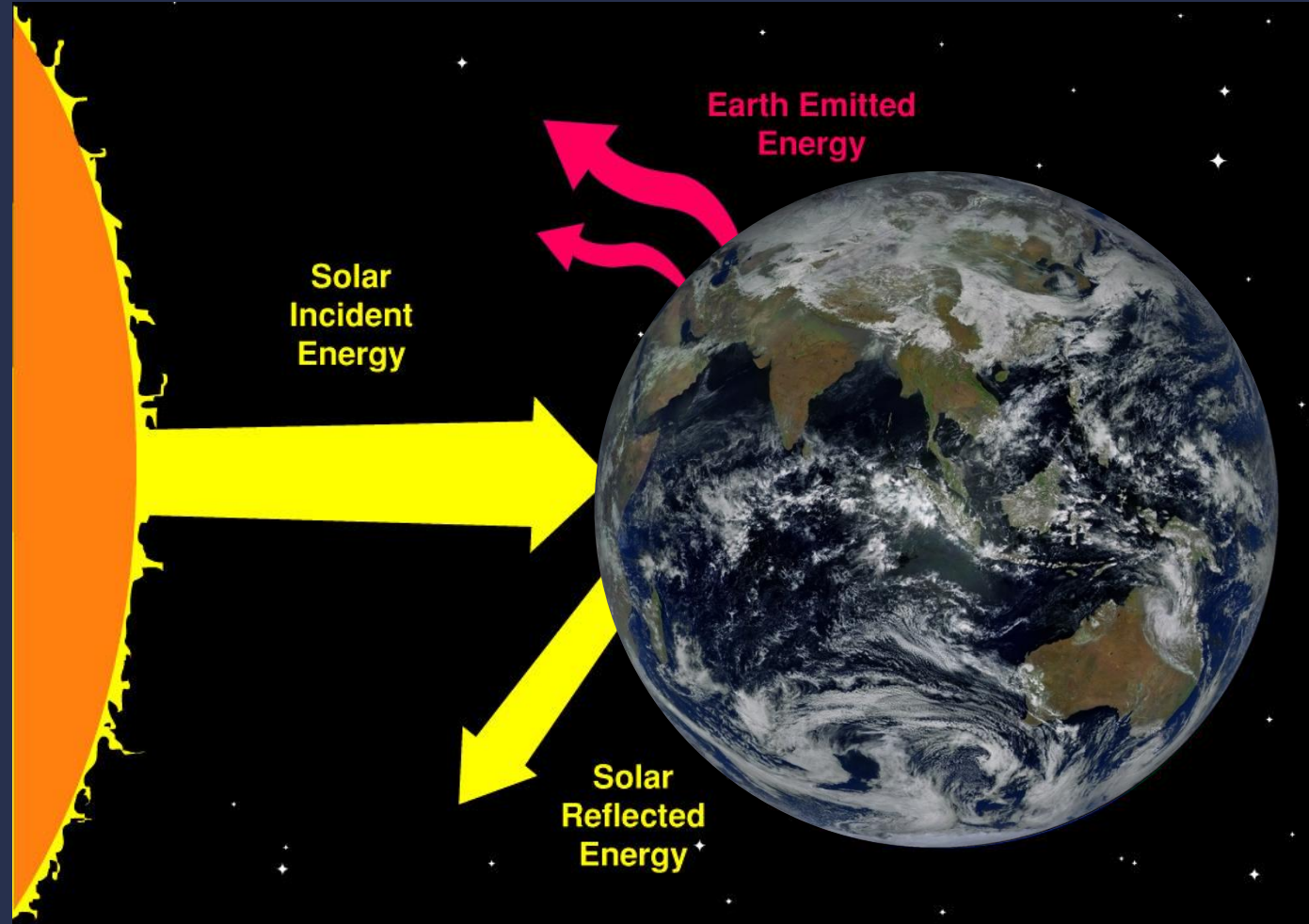
# What do passive microwave and infrared satellite instruments measure ...?

They DO NOT measure TEMPERATURE

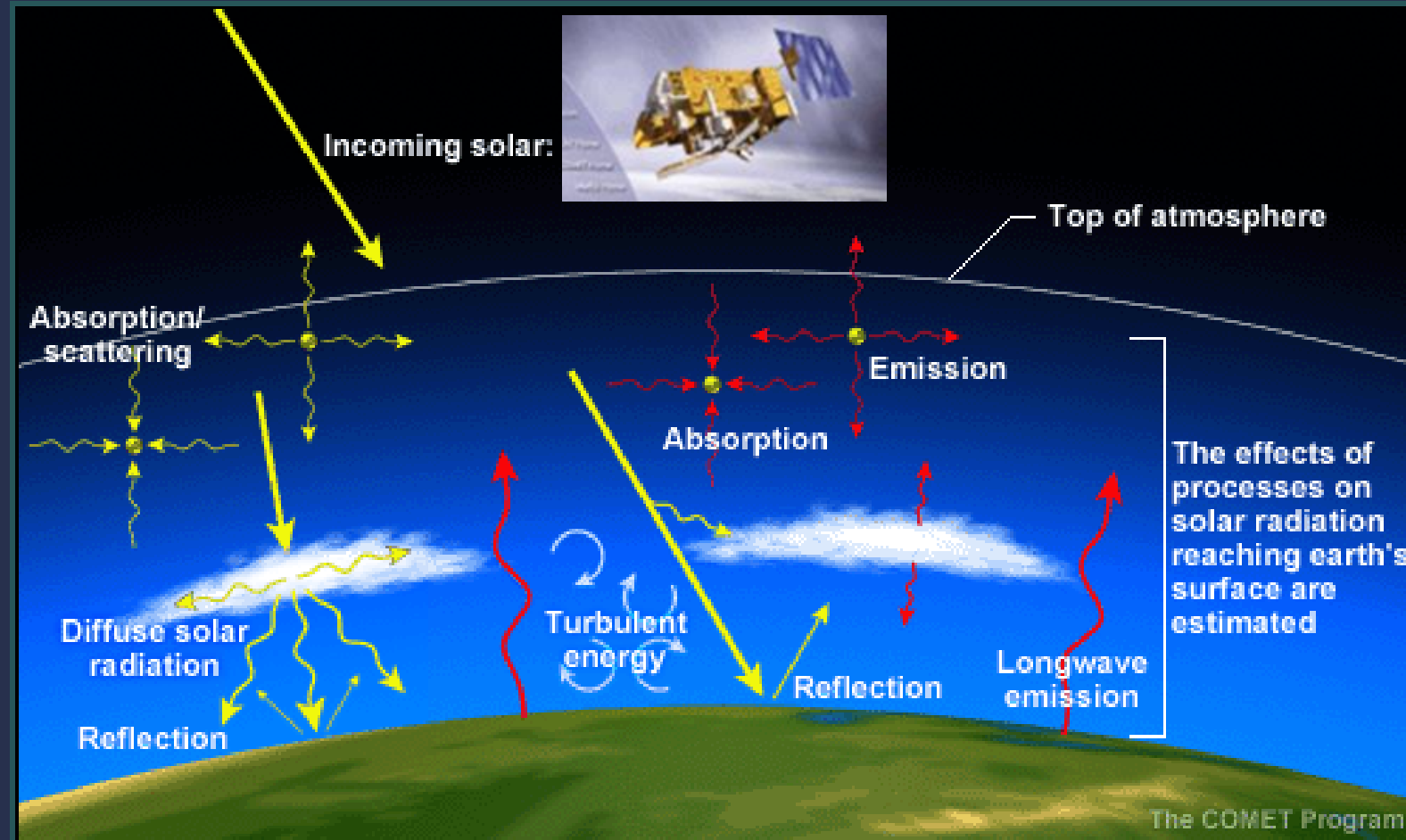
They DO NOT measure HUMIDITY or OZONE

They DO NOT measure WIND

# SATELLITES CAN ONLY MEASURE OUTGOING THERMAL RADIATION FROM THE ATMOSPHERE



# SATELLITES CAN ONLY MEASURE OUTGOING THERMAL RADIATION FROM THE ATMOSPHERE



# What do satellite instruments measure ?

Satellite instruments measure the **radiation**  $L$  that reaches the top of the atmosphere at given **frequency**  $\nu$ .

The measured radiance is **related** to geophysical atmospheric variables ( $T, Q, O_3$ , clouds etc...) by the

## Radiative Transfer Equation

measured by the satellite

Our description of the atmosphere

$$L(\nu) = \int_0^\infty B(\nu, T(z)) \left[ \frac{d\tau(\nu)}{dz} \right] dz + \text{Surface emission} + \text{Surface reflection/scattering} + \text{Cloud/rain contribution} + \dots$$

Planck source term\* depending on temperature  $T(z)$  of the atmosphere

Transmittance / Absorption in the atmosphere

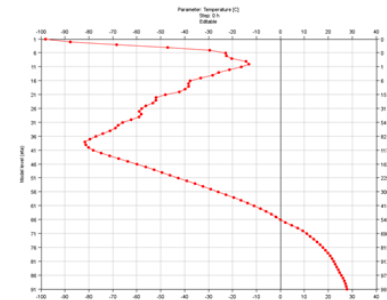
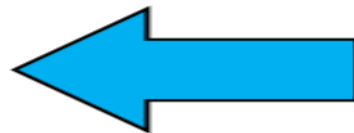
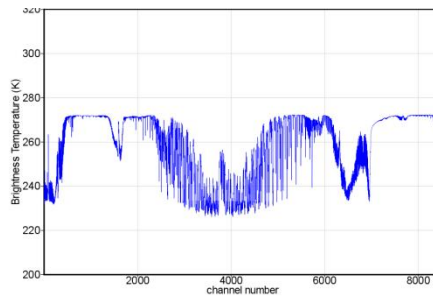
Other contributions to the measured radiances

# The Radiative Transfer (RT) equation

measured by the  
satellite

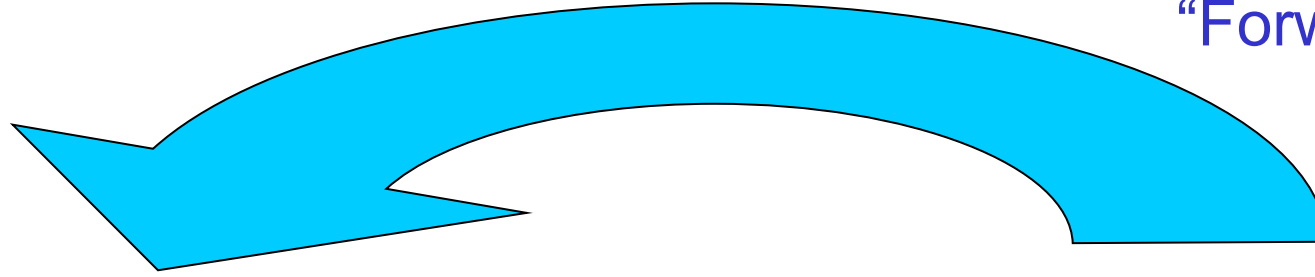
depends on the state of the atmosphere

$$L(\nu) = \int_0^\infty B(\nu, T(z)) \left[ \frac{d\tau(\nu)}{dz} \right] dz + \text{Surface emission} + \text{Surface reflection/scattering} + \text{Cloud/rain contribution} + \dots$$



# The Radiative Transfer (RT) equation

“Forward problem”



measured by the  
satellite

depends on the state of the atmosphere

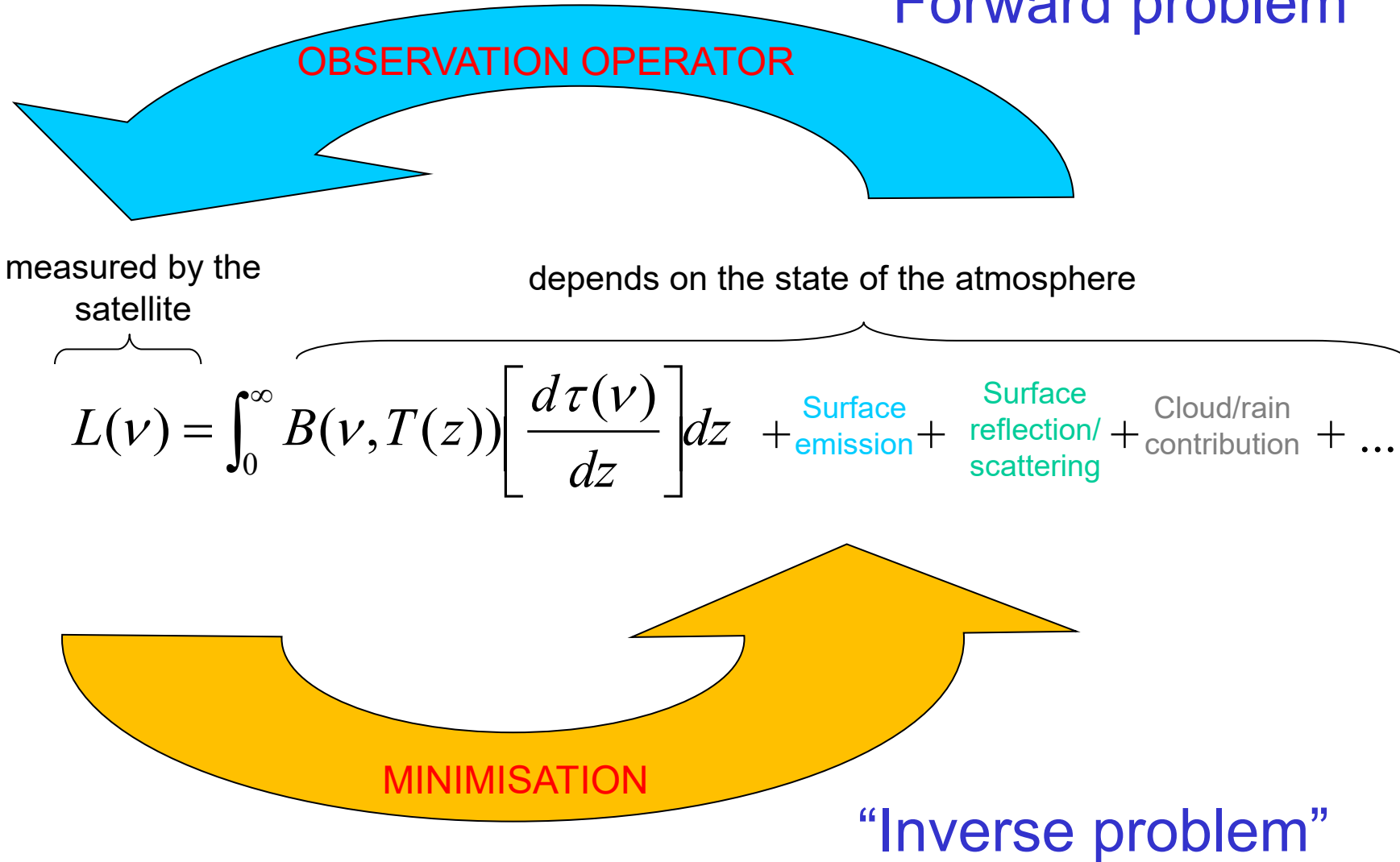
$$L(\nu) = \int_0^\infty B(\nu, T(z)) \left[ \frac{d\tau(\nu)}{dz} \right] dz + \text{Surface emission} + \text{Surface reflection/scattering} + \text{Cloud/rain contribution} + \dots$$

*...given the state of the atmosphere, what is the radiance...?*

*i.e. we can **simulate** what radiation would reach the satellite from a particular atmosphere...*

# The Radiative Transfer (RT) equation

“Forward problem”



...but first we have to simplify things a bit...

“Channel selection” ...

...designing satellite instruments to measure atmospheric radiation at very specific frequencies (channels)

# Measuring radiances in different frequencies (channels)

By deliberately **selecting** radiation at different frequencies or **CHANNELS** satellite instruments can provide information on specific geophysical variables for different regions of the atmosphere.

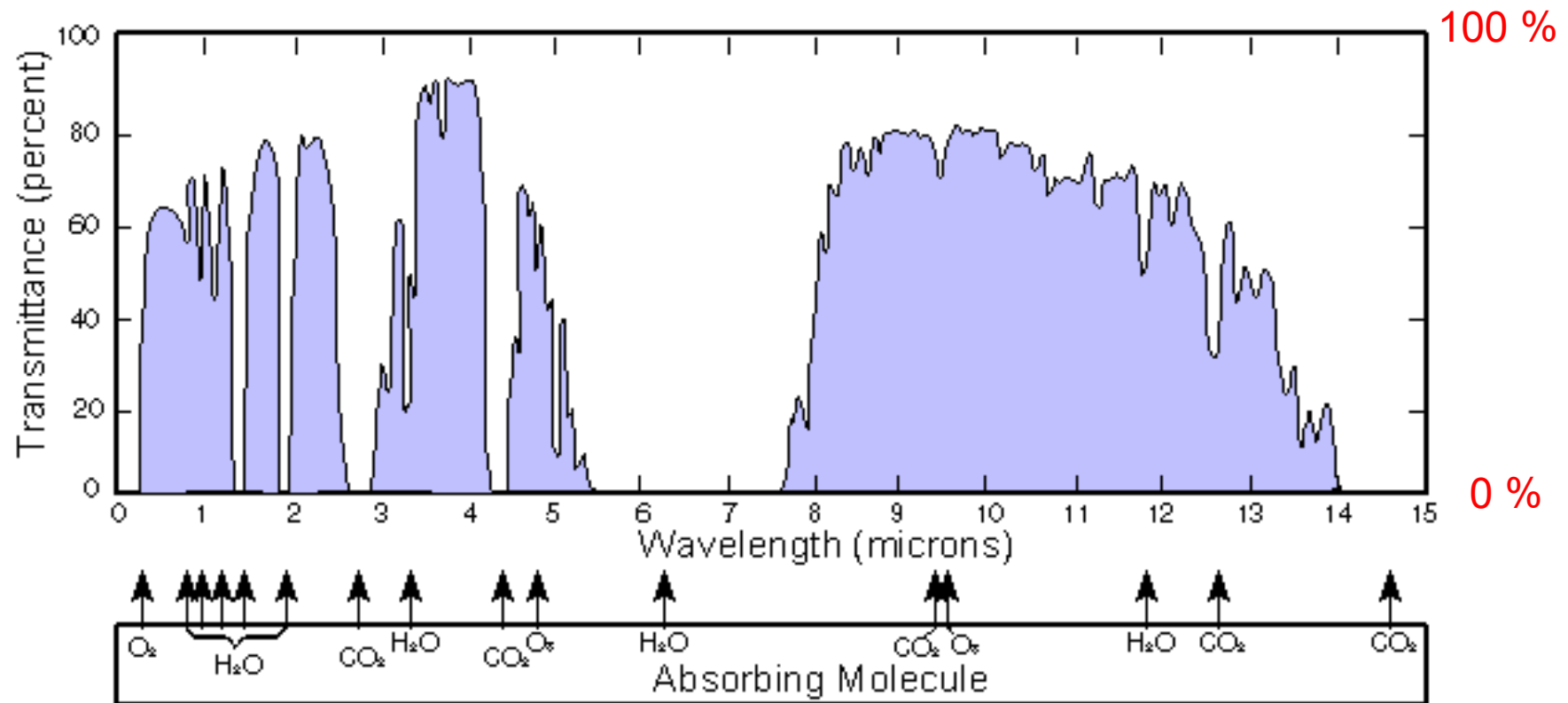
In general, the frequencies / channels used within NWP may be categorized as one of **2** different types ...

1. **atmospheric sounding** channels
2. **surface sensing** channels

Note:

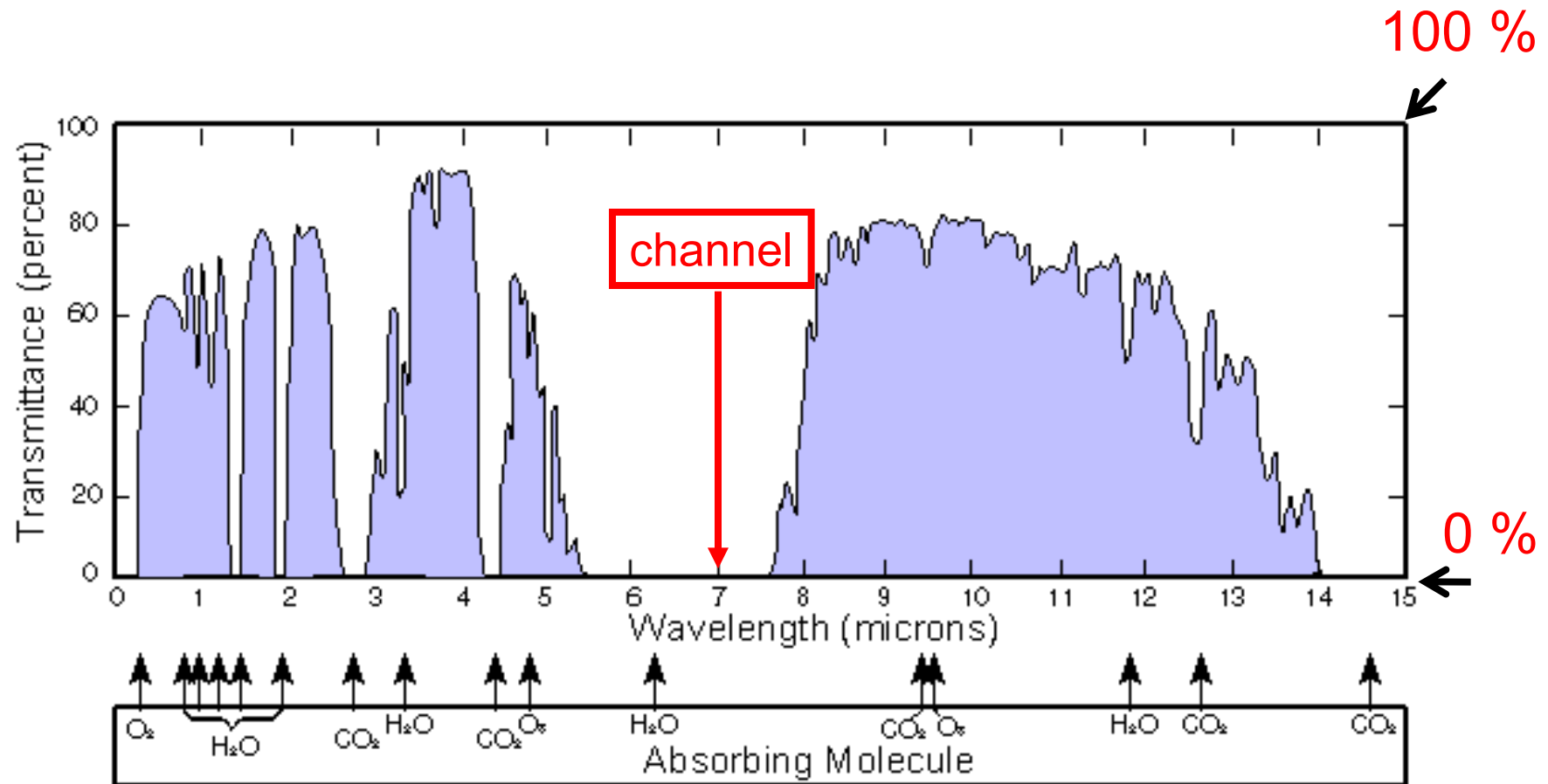
*In practice (and often despite their name!) real satellite instruments have channels which are a **combination** of atmospheric sounding and surface sensing channels*

# Atmospheric transmission at different wavelengths

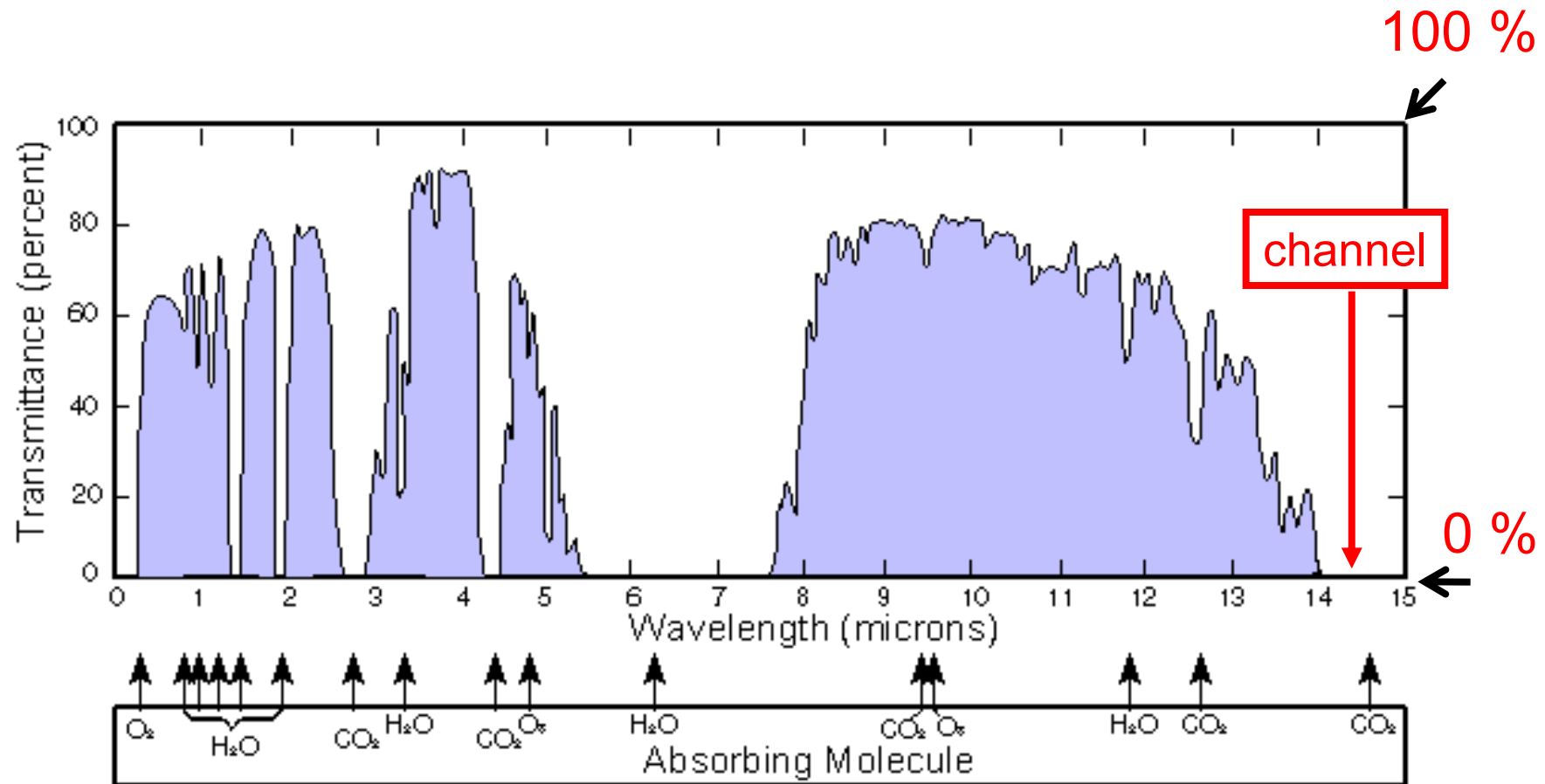


# **Atmospheric sounding channels...**

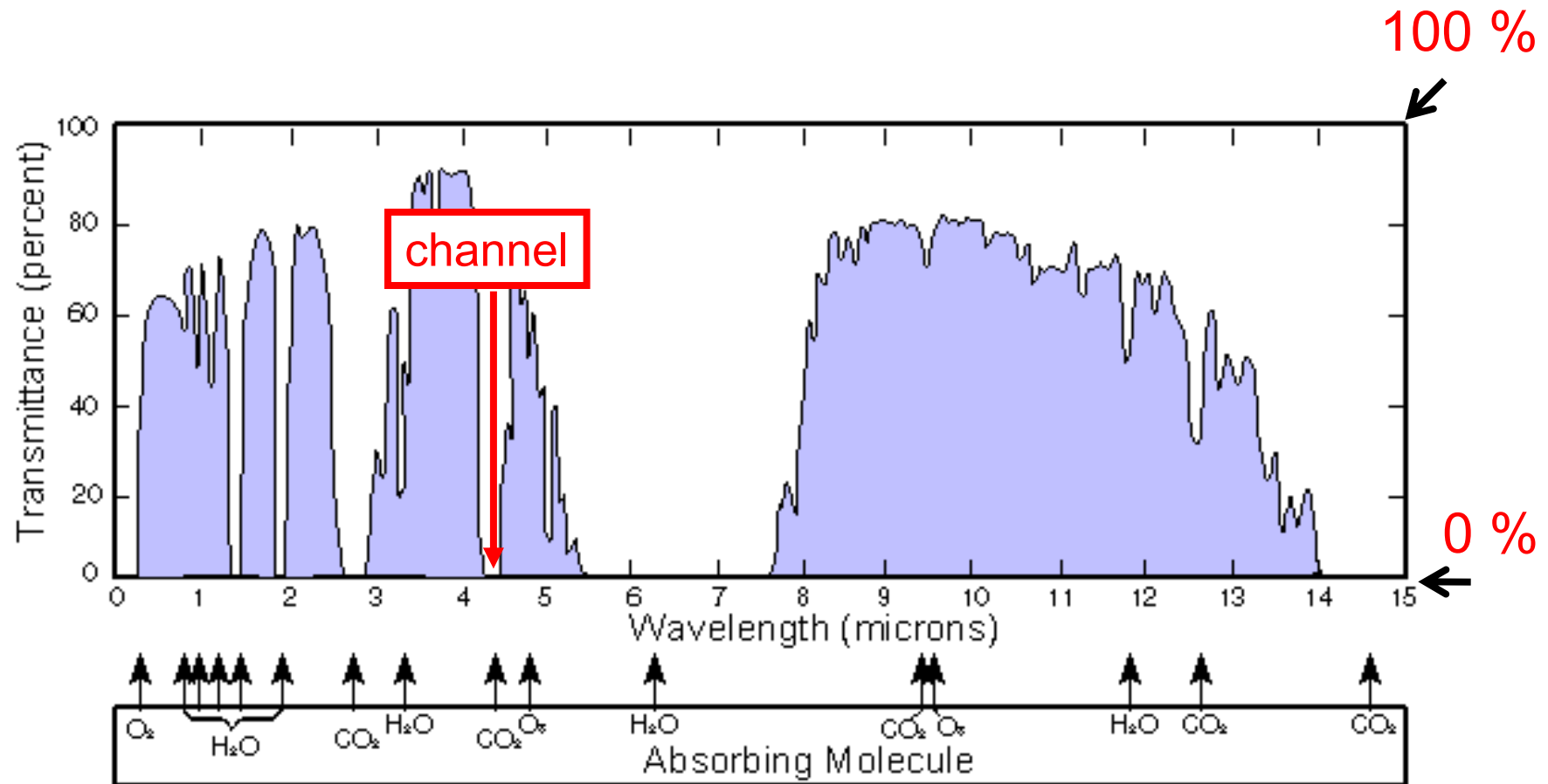
# Atmospheric sounding channels...



# Atmospheric sounding channels...



# Atmospheric sounding channels...



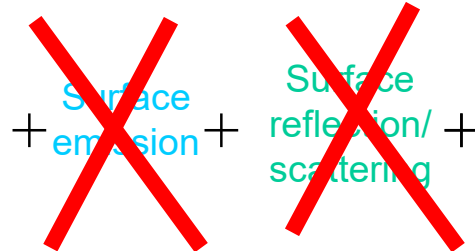
# Atmospheric sounding channels...

...selecting channels where there is **no** contribution from the **surface**....

$$L(\nu) = \int_0^{\infty} B(\nu, T(z)) \left[ \frac{d\tau(\nu)}{dz} \right] dz + \text{Surface emission} + \text{Surface reflection/scattering} + \text{Cloud/rain contribution} + \dots$$

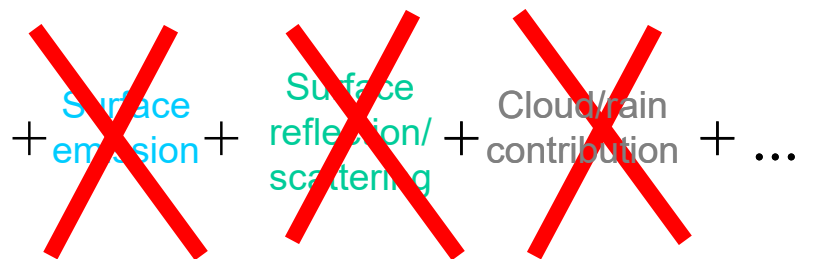
# Atmospheric sounding channels...

...selecting channels where there is **no** contribution from the **surface**....

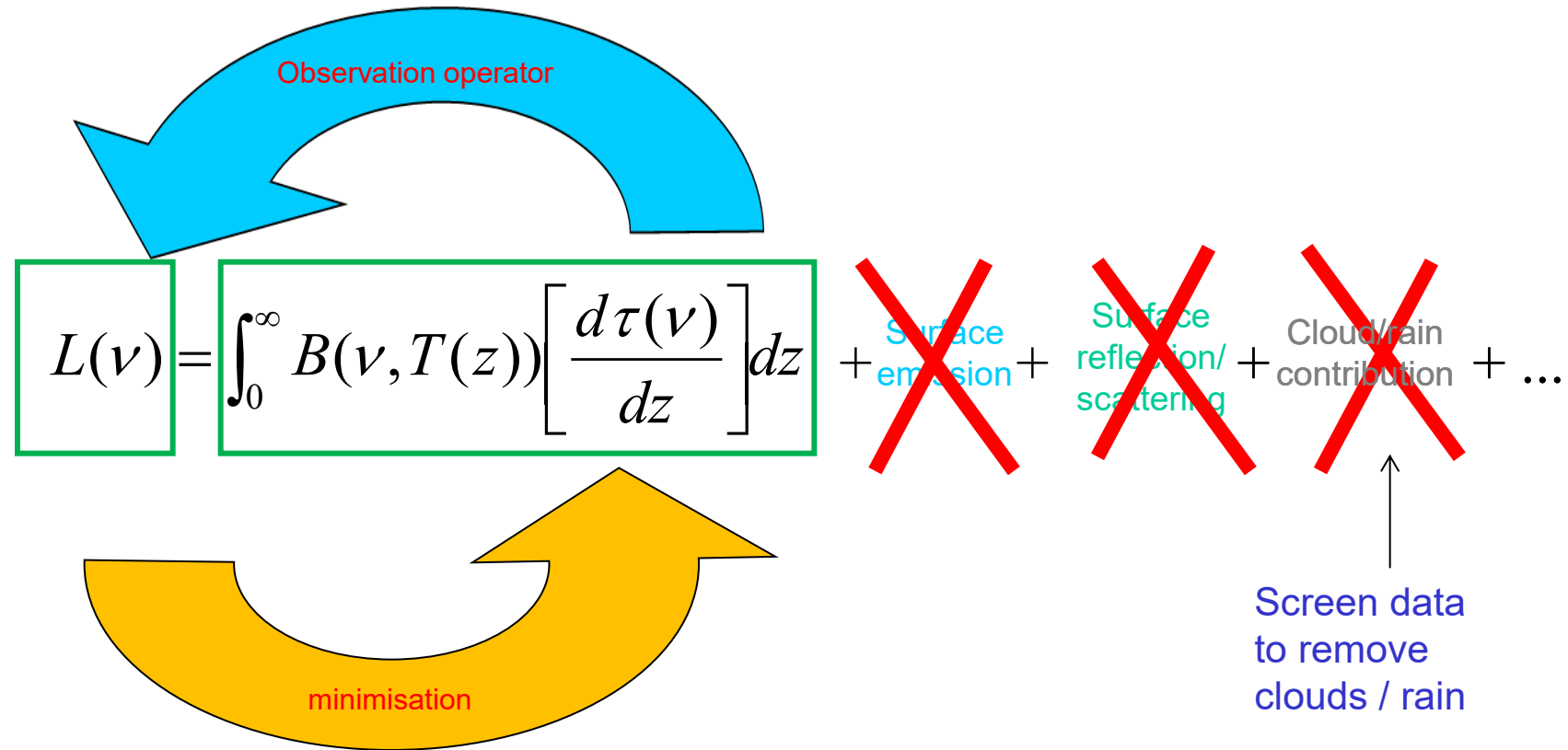
$$L(\nu) = \int_0^{\infty} B(\nu, T(z)) \left[ \frac{d\tau(\nu)}{dz} \right] dz + \text{Surface emission} + \text{Surface reflection/scattering} + \text{Cloud/rain contribution} + \dots$$
The diagram shows the radiance equation with two terms crossed out with large red 'X' marks. The first term is 'Surface emission' in blue text, and the second term is 'Surface reflection/scattering' in green text. The remaining terms are 'Cloud/rain contribution' in grey text and an ellipsis '...'.

# Atmospheric sounding channels...

...if we additionally **screen observations** to remove measurements in cloudy or rain locations...

$$L(\nu) = \int_0^{\infty} B(\nu, T(z)) \left[ \frac{d\tau(\nu)}{dz} \right] dz + \text{Surface emission} + \text{Surface reflection/scattering} + \text{Cloud/rain contribution} + \dots$$


# We now have a much simpler forward ...and inverse problem for the DA



# Atmospheric sounding channels...

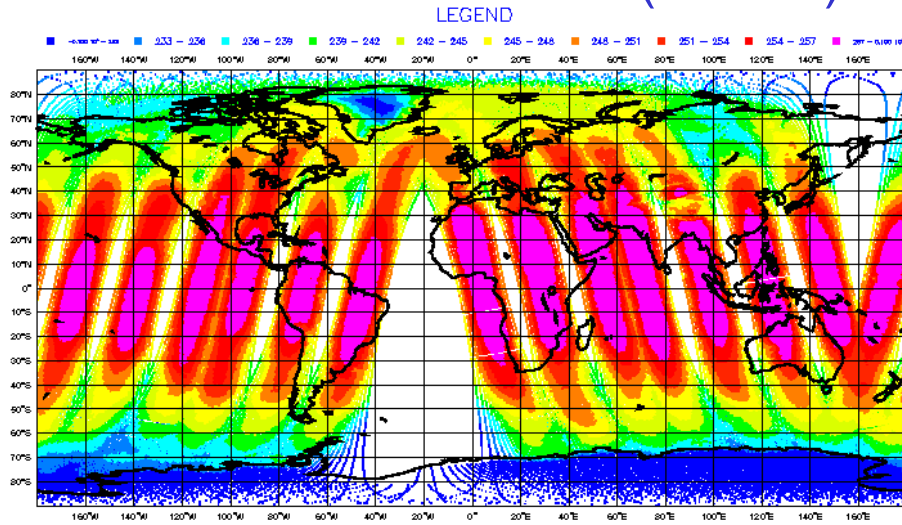
These channels are located in parts of the infra-red and microwave spectrum for which the main contribution to the measured radiance is from the atmosphere and can be written:

$$L(\nu) \approx \int_0^\infty B(\nu, T(z)) \left[ \frac{d\tau(\nu)}{dz} \right] dz$$

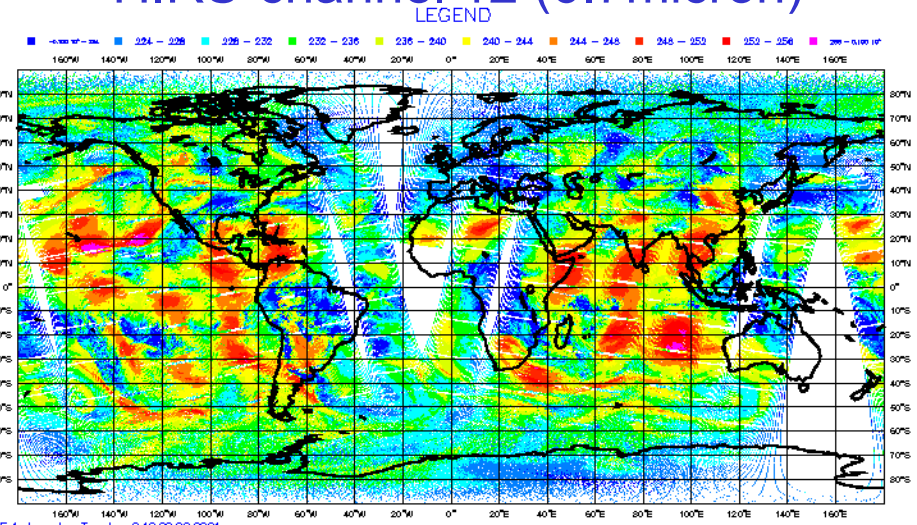
Where  $B$ =Planck function  
 $t$  = transmittance  
 $T(z)$  is the temperature  
 $z$  is a height coordinate

That is they try to **avoid** frequencies for which **surface radiation** and cloud contributions are important. They are primarily used to obtain **information about atmospheric temperature and humidity** (or other constituents that influence the transmittance e.g. CO<sub>2</sub>).

AMSUA-channel 5 (53GHz)

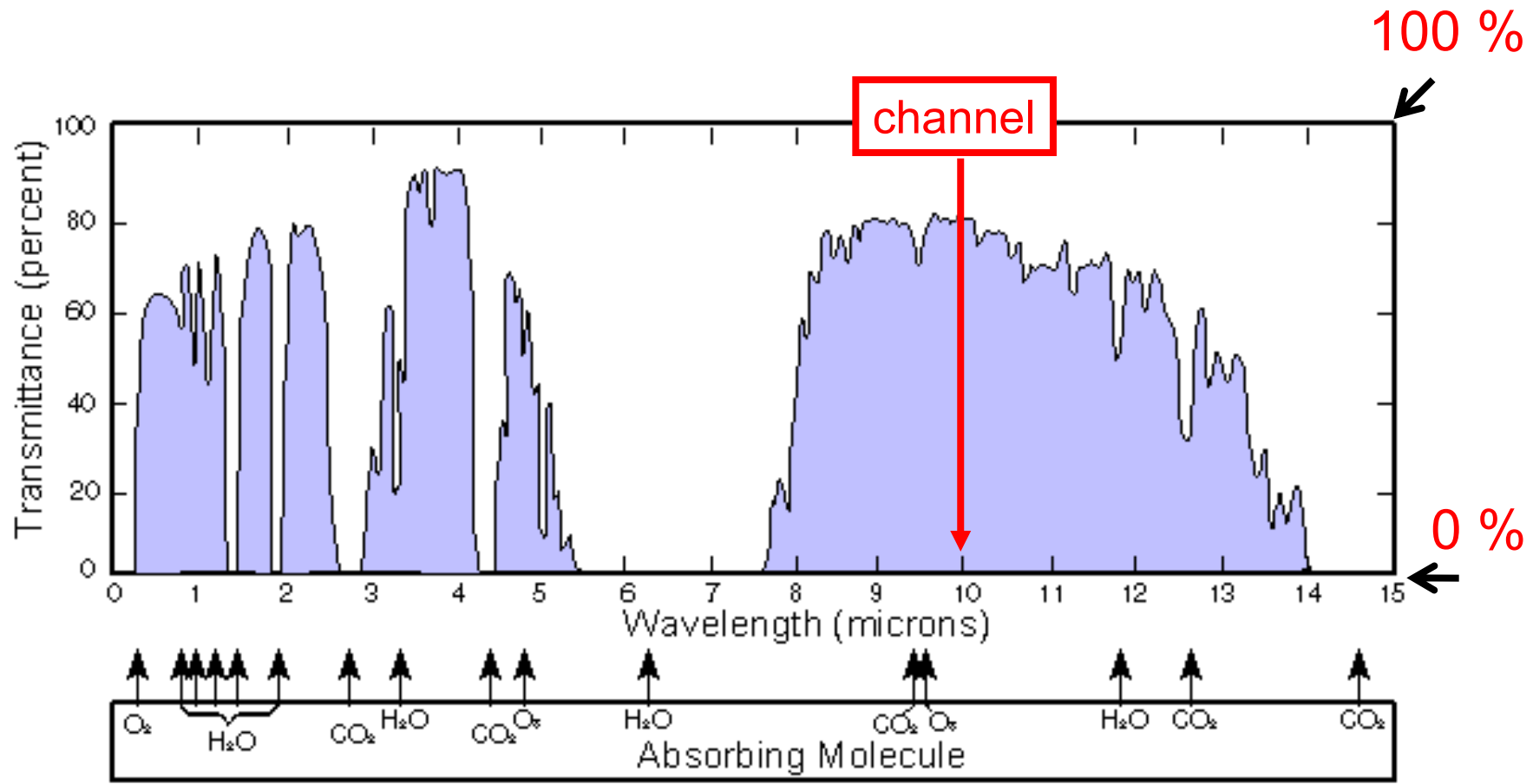


HIRS-channel 12 (6.7micron)

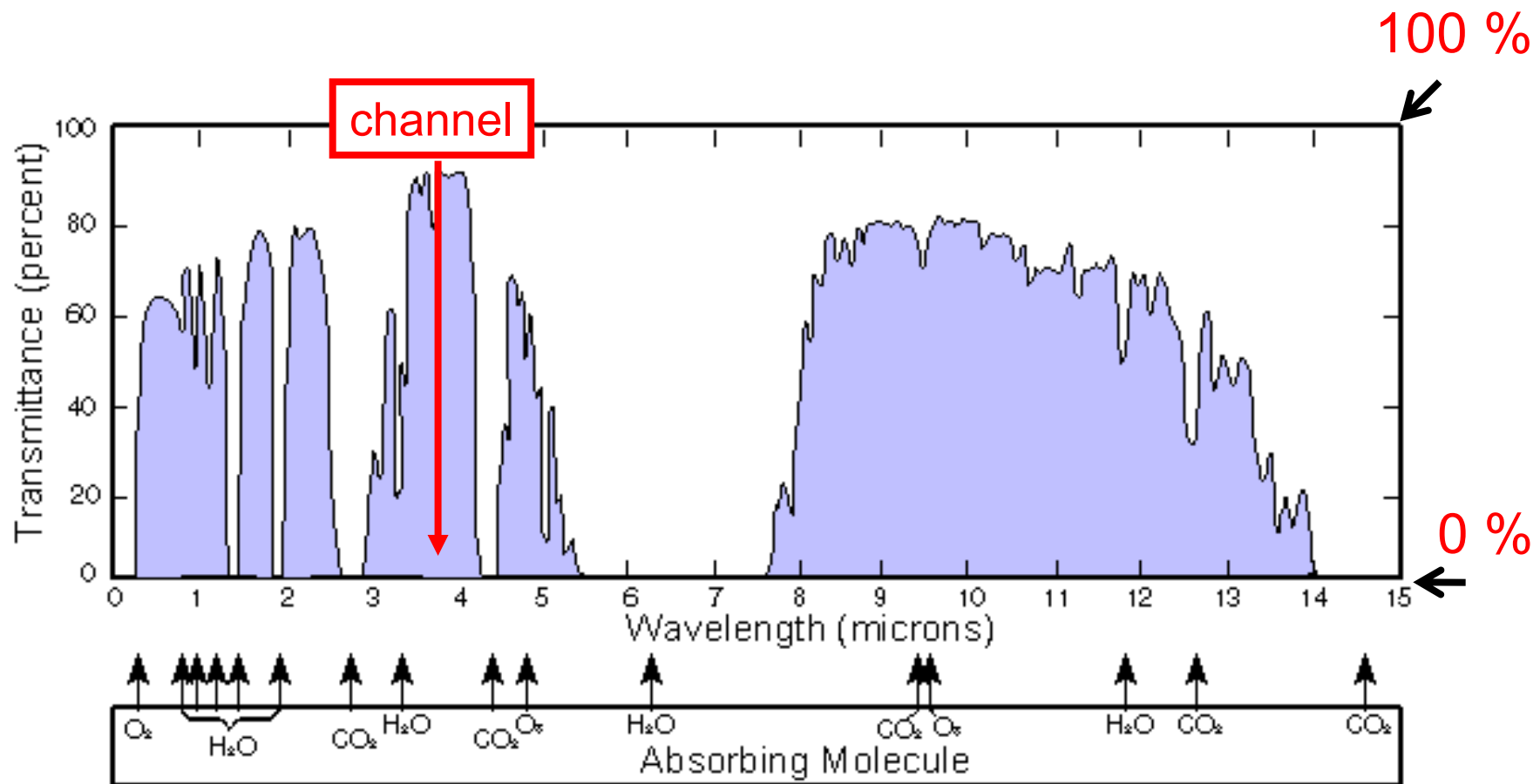


# Surface sensing Channels...

# Surface sensing Channels



# Surface sensing Channels



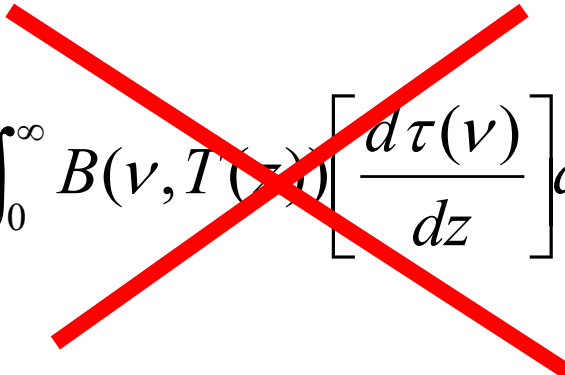
# Surface sensing Channels

...selecting channels where there is **no** interaction in the **atmosphere**....

$$L(\nu) = \int_0^{\infty} B(\nu, T(z)) \left[ \frac{d\tau(\nu)}{dz} \right] dz + \text{Surface emission} + \text{Surface reflection/scattering} + \text{Cloud/rain contribution} + \dots$$

# Surface sensing Channels

...selecting channels where there is **no** interaction in the atmosphere....

$$L(\nu) = \int_0^\infty B(\nu, T(z)) \left[ \frac{d\tau(\nu)}{dz} \right] dz + \text{Surface emission} + \text{Surface reflection/scattering} + \text{Cloud/rain contribution} + \dots$$


# Surface sensing Channels

...selecting channels where there is **no** interaction in the atmosphere....

$$L(\nu) = \int_0^\infty B(\nu, T(z)) \left[ \frac{d\tau(\nu)}{dz} \right] dz + \text{Surface emission} + \text{Surface reflection/scattering} + \text{Cloud/rain contribution} + \dots$$

↑  
IR ~ zero

# Surface sensing Channels

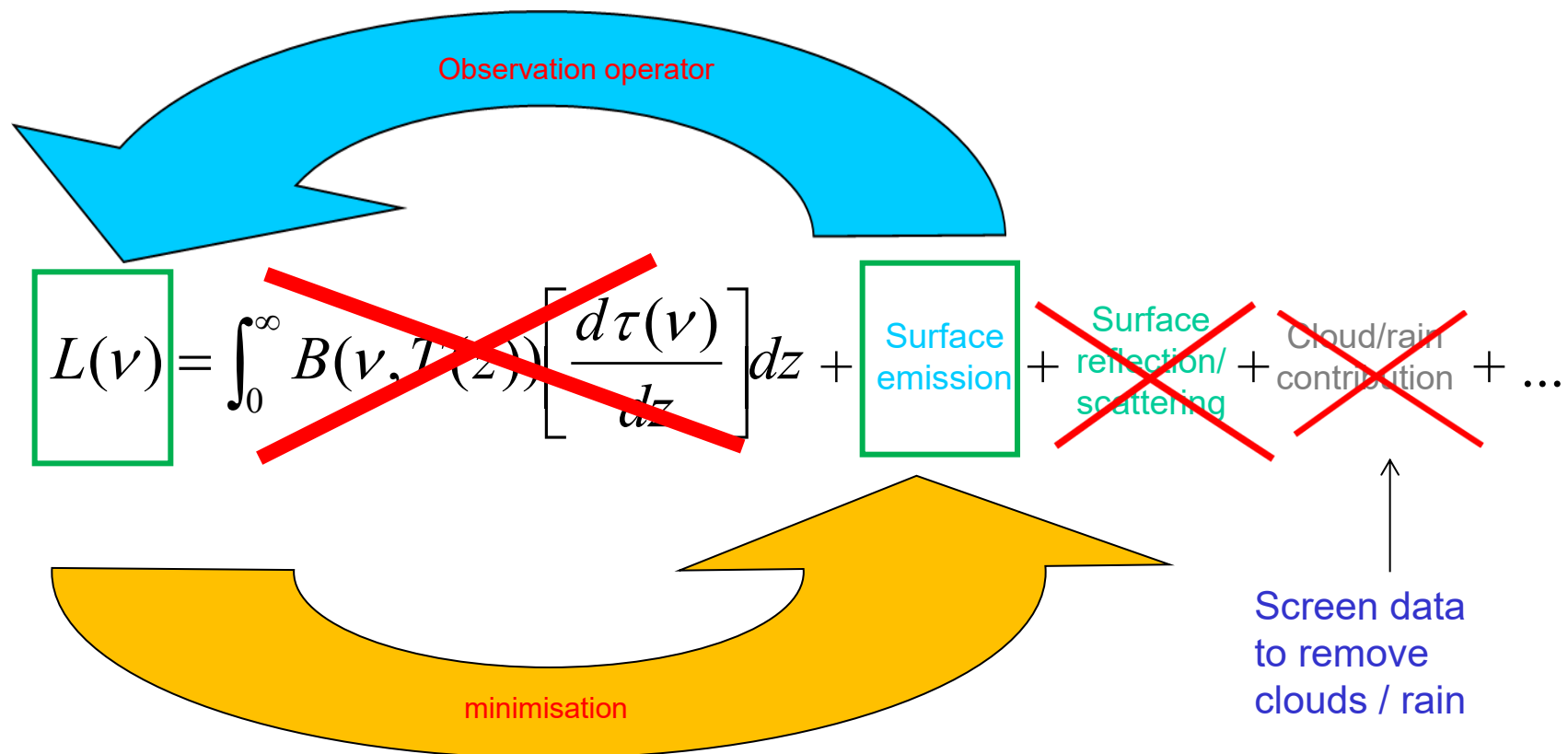
...selecting channels where there is **no** interaction in the atmosphere....

$$L(\nu) = \int_0^\infty B(\nu, T(z)) \left[ \frac{d\tau(\nu)}{dz} \right] dz + \text{Surface emission} + \text{Surface reflection/scattering} + \text{Cloud/rain contribution} + \dots$$

↑  
Screen data to remove clouds / rain

The diagram illustrates the radiance equation  $L(\nu) = \int_0^\infty B(\nu, T(z)) \left[ \frac{d\tau(\nu)}{dz} \right] dz + \text{Surface emission} + \text{Surface reflection/scattering} + \text{Cloud/rain contribution} + \dots$ . A large red 'X' is drawn over the integral term, indicating that atmospheric interaction is to be avoided. Another red 'X' is drawn over the 'Surface reflection/scattering' and 'Cloud/rain contribution' terms. An arrow points from the text 'Screen data to remove clouds / rain' to the 'Cloud/rain contribution' term.

# We now have a much simpler forward ...and inverse problem for the DA



# Surface sensing Channels

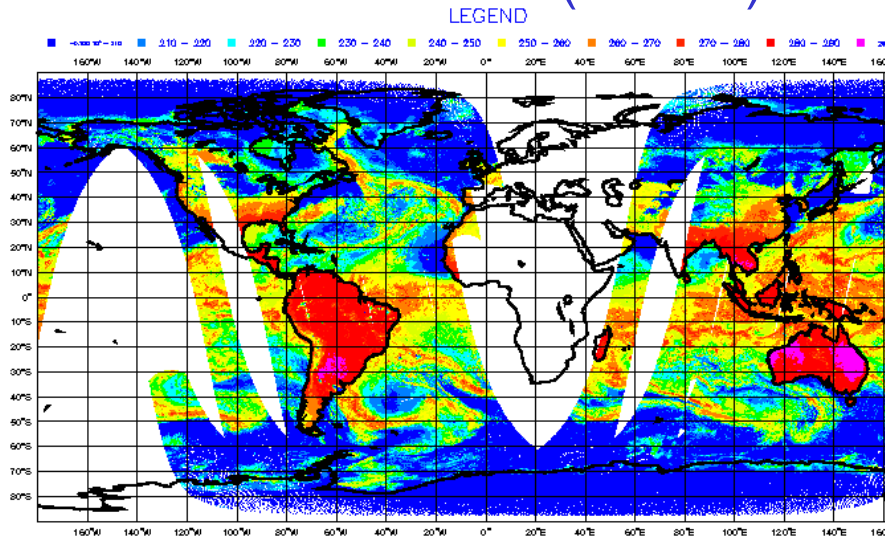
These are located in **window regions** of the infra-red and microwave spectrum at frequencies where there is very little interaction with the atmosphere and the primary contribution to the measured radiance is:

$$L(\nu) \approx B[\nu, T_{\text{surf}}] \epsilon(\mathbf{u}, \nu) \quad (\text{i.e. surface emission})$$

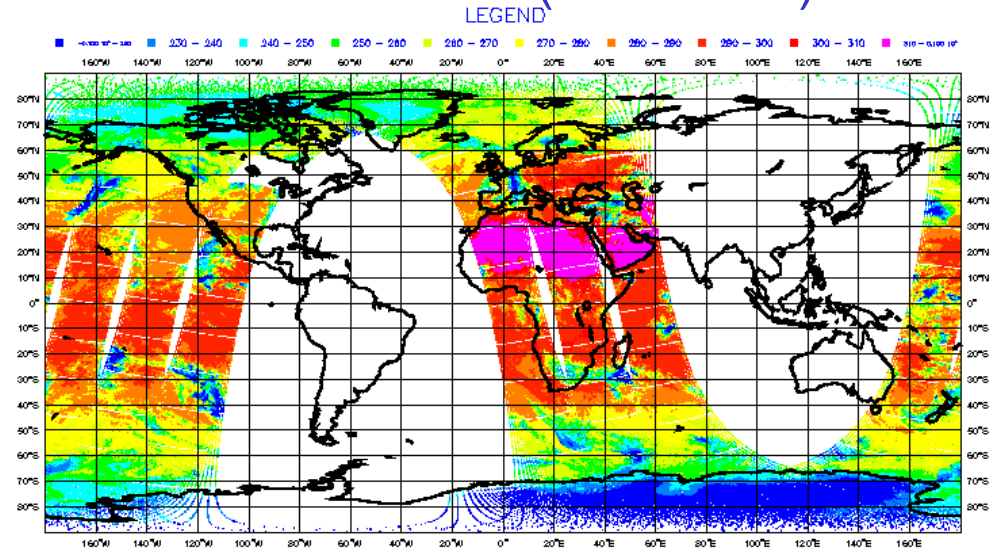
Where  $T_{\text{surf}}$  is the surface skin temperature and  $\epsilon$  the surface emissivity

These are primarily used to obtain information on the **surface temperature** and quantities that influence the **surface emissivity** such as wind (ocean) and vegetation (land). They can also be used to obtain information on **clouds/rain** and cloud movements (to provide **wind** information)

SSM/I channel 7 (89GHz)



HIRS channel 8 (11microns)



**What type of channels are most important for NWP ?**

# **Atmospheric temperature sounding...**

# Atmospheric temperature sounding – *weighting functions*

If radiation is selected in an **atmospheric sounding channel** for which

$$L(\nu) = \int_0^{\infty} B(\nu, T(z)) \left[ \frac{d\tau(\nu)}{dz} \right] dz$$

and we define a function  $H(z) = \left[ \frac{d\tau}{dz} \right]$

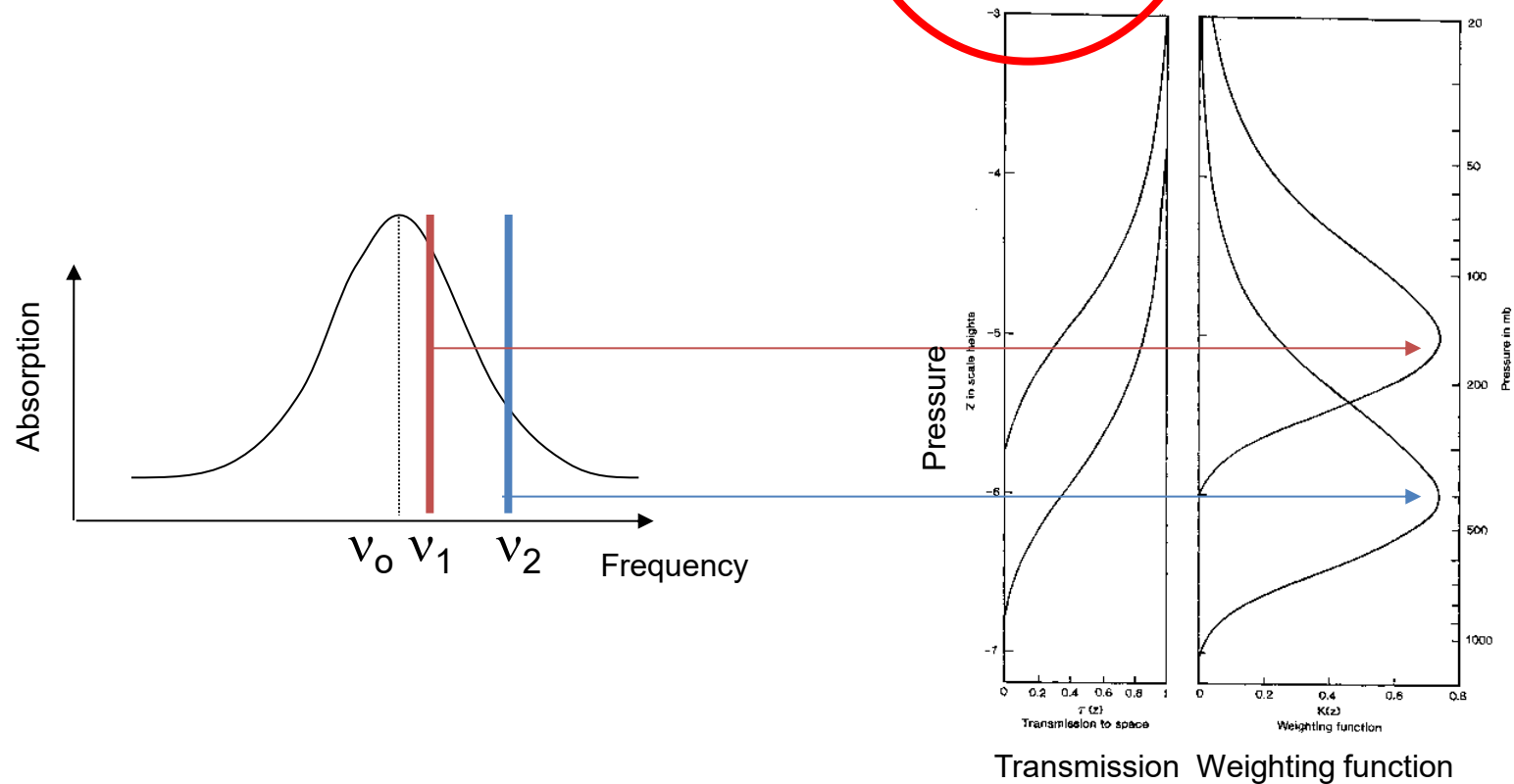
When the primary absorber is a well mixed gas (e.g. oxygen or CO<sub>2</sub>) with known concentration it can be seen that the **measured radiance** is essentially a **weighted average of the atmospheric temperature profile**, or

$$L(\nu) = \int_0^{\infty} B(\nu, T(z)) H(z) dz$$

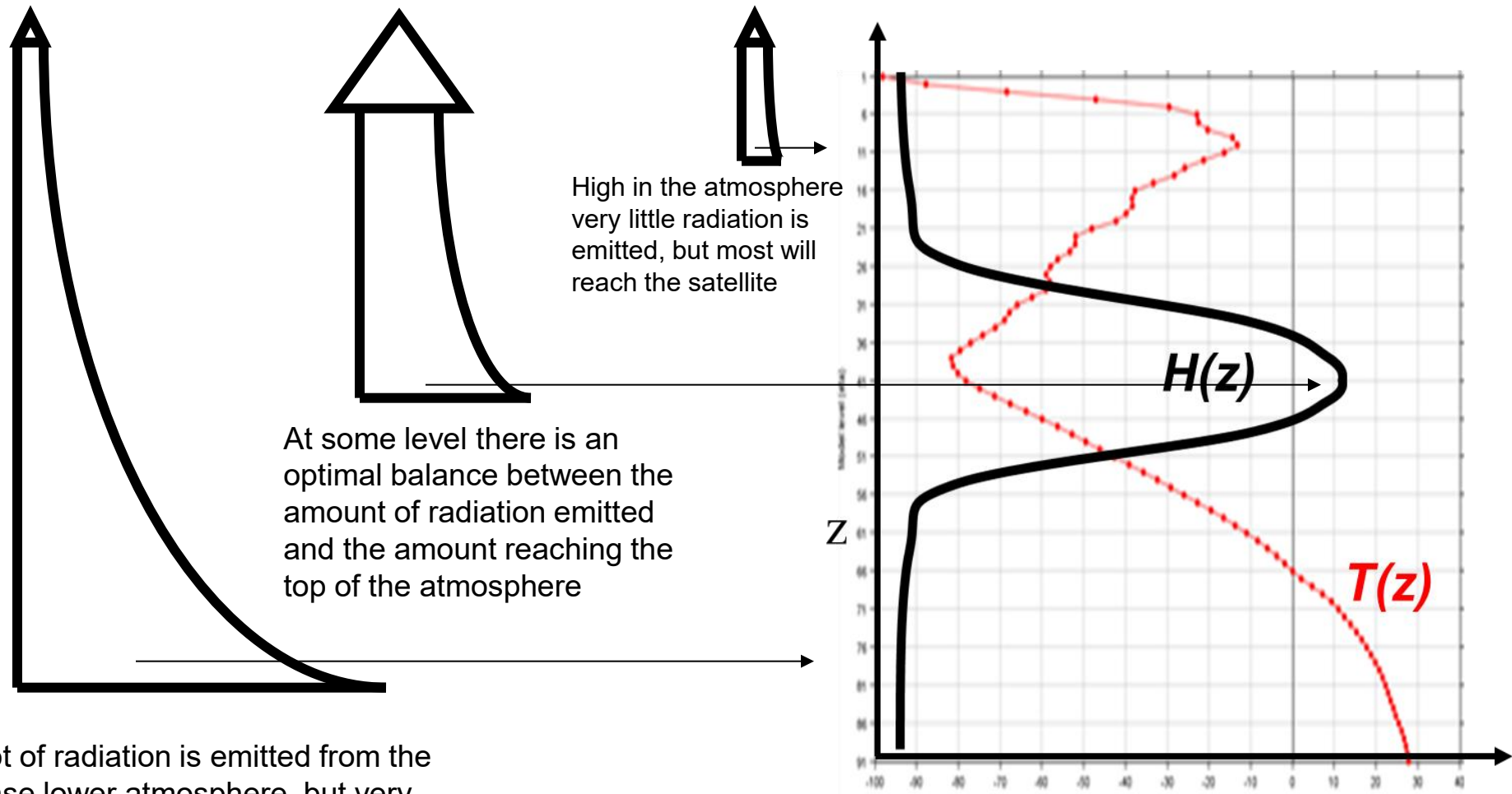
The function  $H(z)$  that defines this vertical average is known as a **WEIGHTING FUNCTION**

# What do weighting functions look like ?

$$L(\nu) = \int_0^{\infty} B(\nu, T(z)) \left[ \frac{d\tau(\nu)}{dz} \right] dz$$

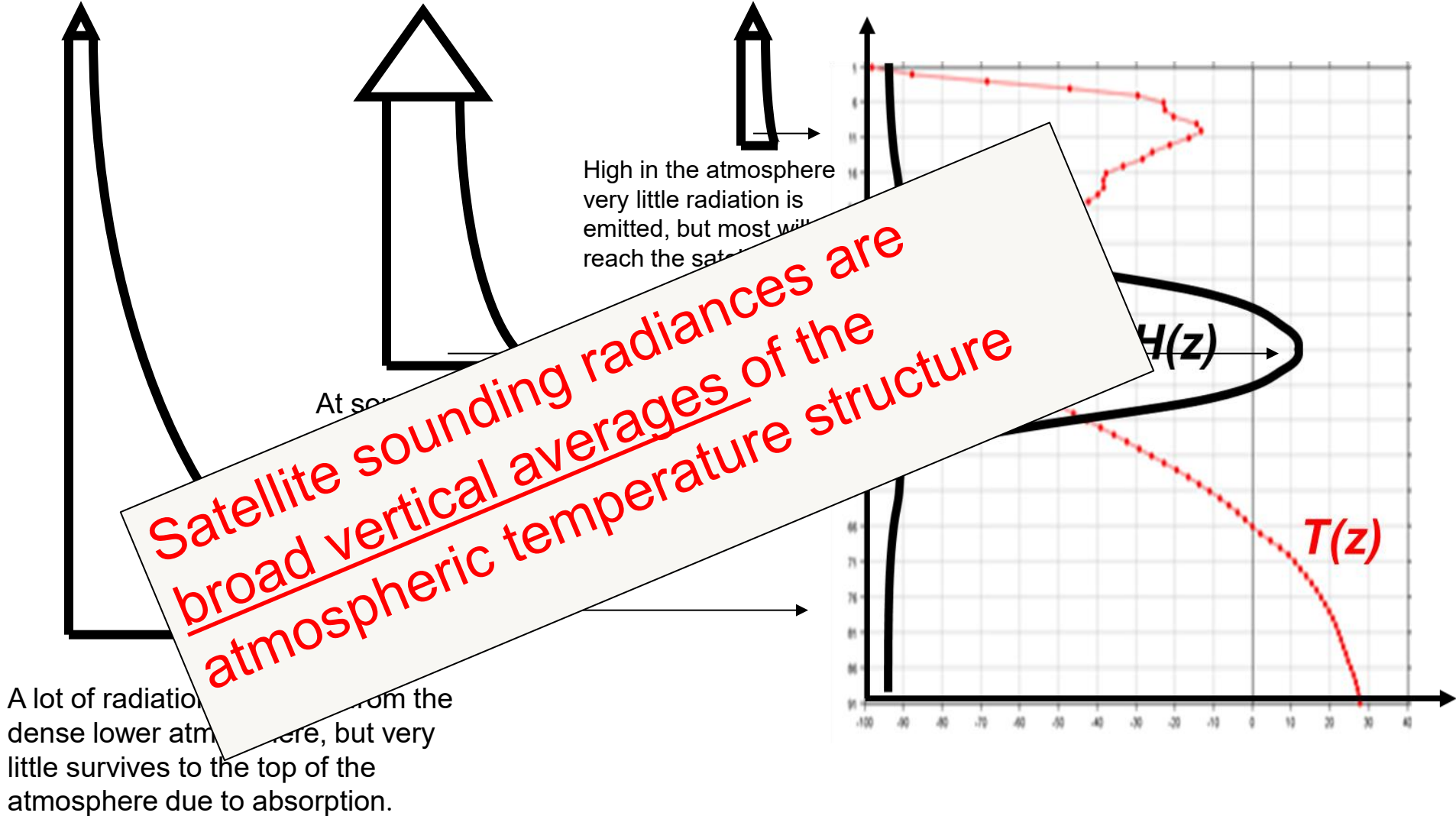


# What do weighting functions look like ?



A lot of radiation is emitted from the dense lower atmosphere, but very little survives to the top of the atmosphere due to absorption.

# What do weighting functions look like ?



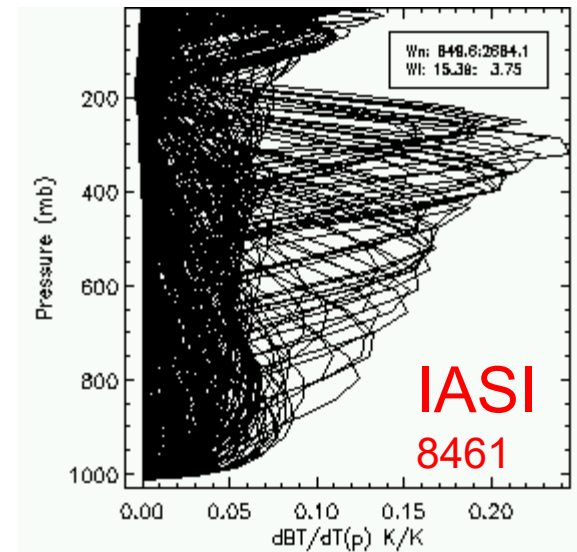
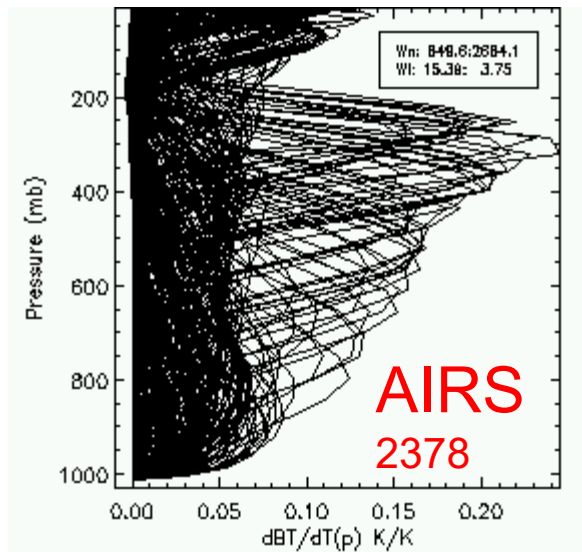
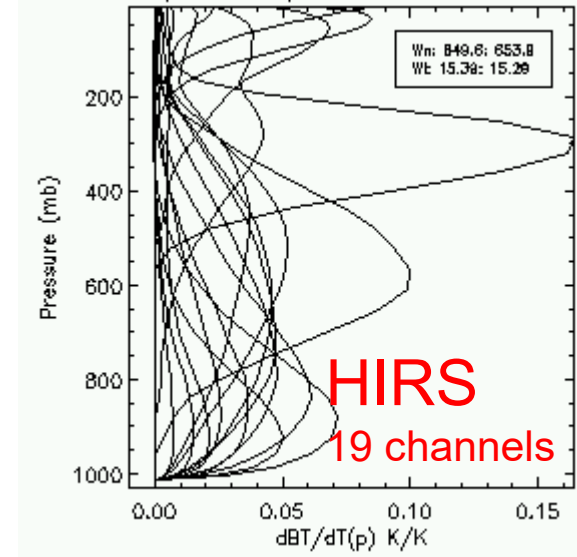
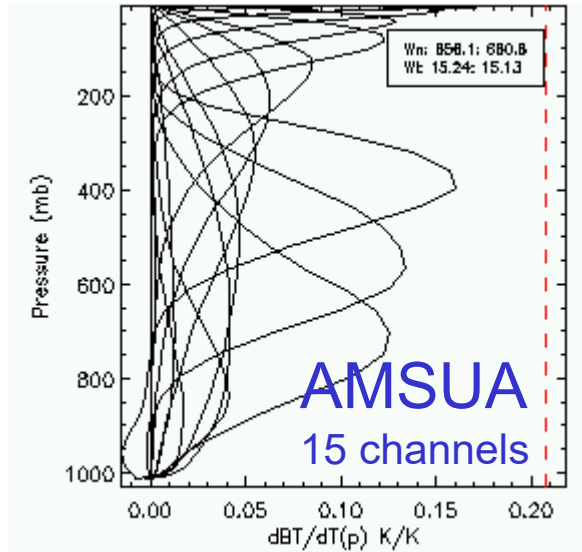
# What do weighting functions look like ?

For any given channel the altitude at which the peak of the weighting function occurs depends on the strength of atmospheric absorption :

- Channels in parts of the spectrum where the absorption is **strong** (e.g. near the centre of CO<sub>2</sub> or O<sub>2</sub> lines ) peak **high** in the atmosphere
- Channels in parts of the spectrum where the absorption is **weak** (e.g. in the wings of CO<sub>2</sub> O<sub>2</sub> lines) peak **low** in the atmosphere

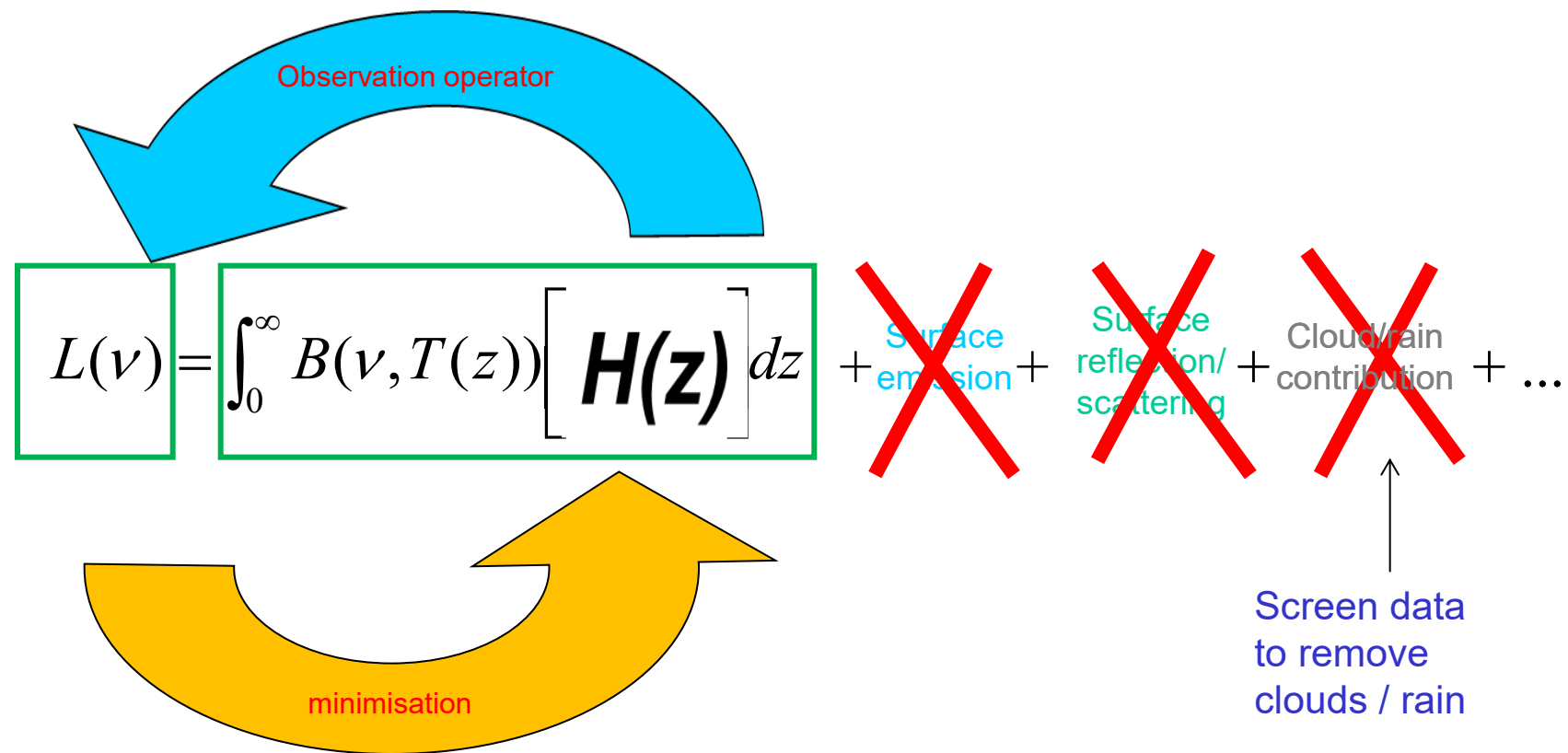
By building a satellite instrument that measures radiation in **many different channels**, all with varying absorption strengths we sample the atmospheric temperature profile at **different altitudes** (but of course not independently!)

# What do real weighting functions look like ?

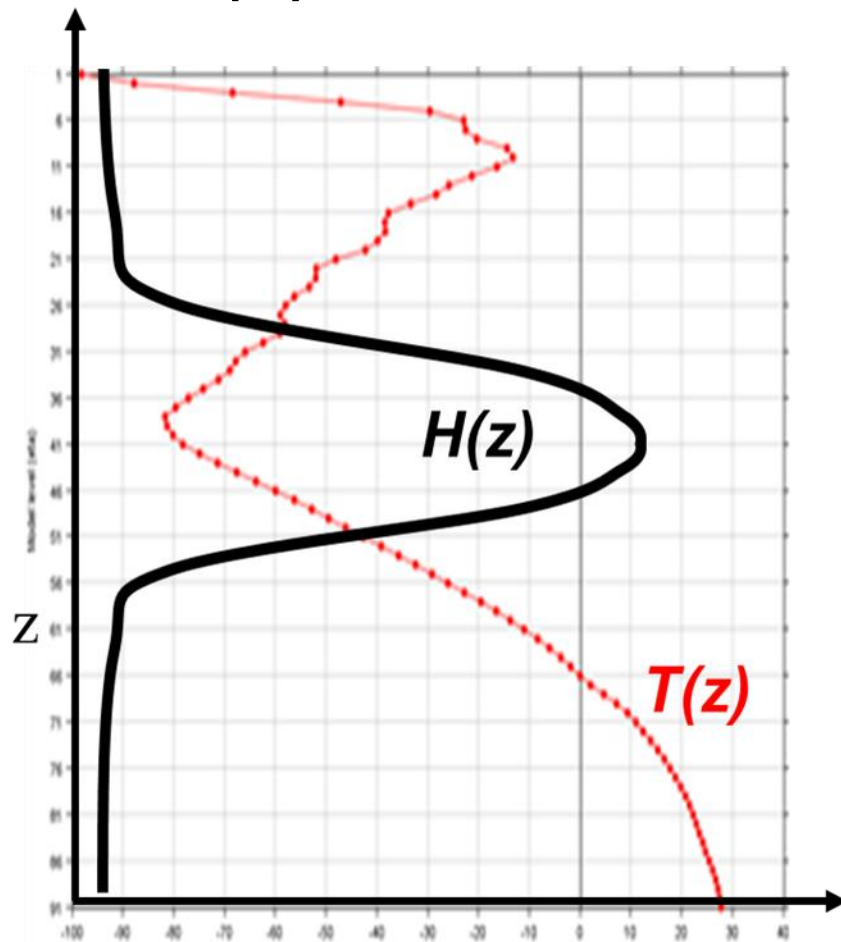


What are the implications of these broad weighting functions for Data Assimilation ?

# The implications of broad weighting functions $H(z)$



# The implications of broad weighting functions $H(z)$

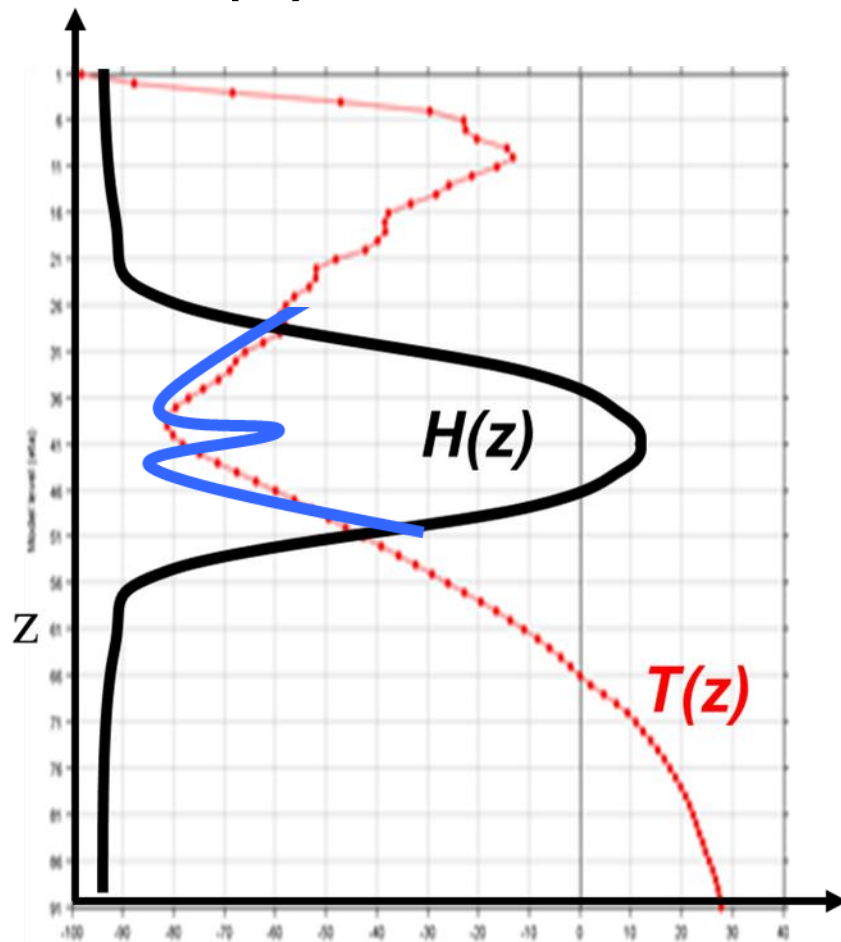


In principle for a single channel an **infinite** number of different temperature profiles could produce exactly the **same measured radiance**...

The extraction of temperature information within the data assimilation for these observations is mathematically **ill-posed**

*See paper by Rodgers 1976 Retrieval of atmospheric temperature and composition from remote measurements of thermal radiation. Rev. Geophys.Space. Phys. 14, 609-624*

# The implications of broad weighting functions $H(z)$

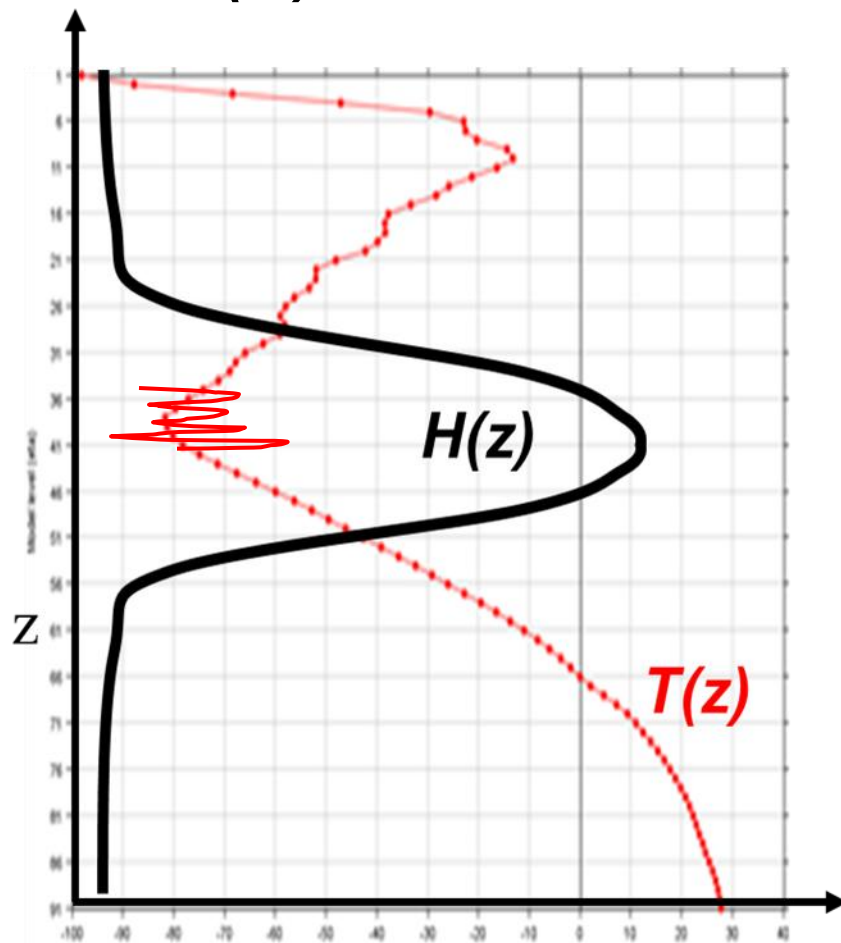


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*See paper by Rodgers 1976 Retrieval of atmospheric temperature and composition from remote measurements of thermal radiation. Rev. Geophys.Space. Phys. 14, 609-624*

# The implications of broad weighting functions $H(z)$



In principle for a single channel an **infinite** number of different temperature profiles could produce exactly the **same measured radiance**...

The extraction of temperature information within the data assimilation for these observations is mathematically **ill-posed**

But having **lots of different channels** improves resolution...see later lecture

*See paper by Rodgers 1976 Retrieval of atmospheric temperature and composition from remote measurements of thermal radiation. Rev. Geophys.Space. Phys. 14, 609-624*

What are the implications of these broad weighting functions for Data Assimilation ...?

...there are some vertical scales we cannot measure...

...the assimilation of satellite radiance data relies heavily on prior or background information ...

# A QUICK REVIEW OF KEY CONCEPTS

- Satellite instruments measure radiance (not T,Q or wind)
- Downward looking satellite radiances are broad vertical averages of the temperature /humidity profile (defined by the weighting functions)
- The estimation of atmospheric temperature (or humidity) from the radiances is mathematically ill-posed and all DA algorithms rely heavily on background prior information

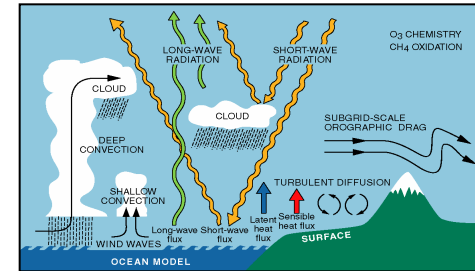
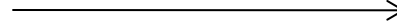
# Basic principles of data assimilation

# What is Data Assimilation ?

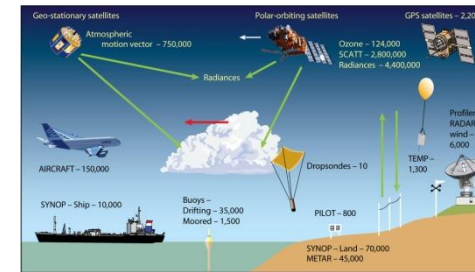
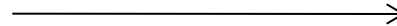
- Models give a complete description of the atmospheric, but **errors grow rapidly** in time
- Observations provide an **incomplete description** of the atmospheric state, but bring up to date information
- Data assimilation **combines** these two sources of information to produce an optimal (best) estimate of the atmospheric state
- This state (the *analysis*) is used as **initial conditions** for extended forecasts.

# The assimilation system:

- Model



- Observations



- Assimilation algorithm



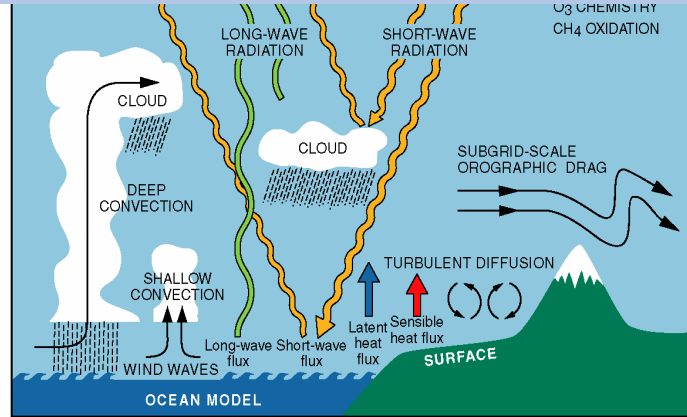
$$J(x) = (x - x_b)^T \mathbf{B}^{-1} (x - x_b) + (y - H[x])^T \mathbf{R}^{-1} (y - H[x])$$

# The forecast model

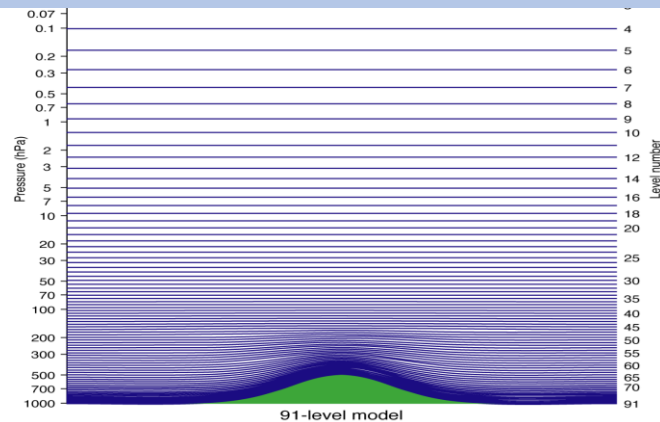


# The forecast model

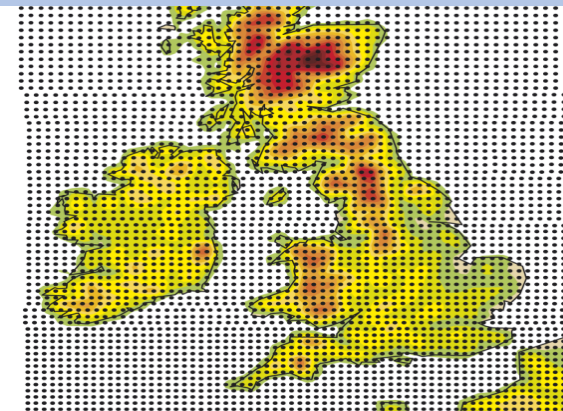
Physical and dynamical processes updated every 10 minutes



91 (**137**) vertical levels from the surface to 0.01hPa (approx: 80Km)

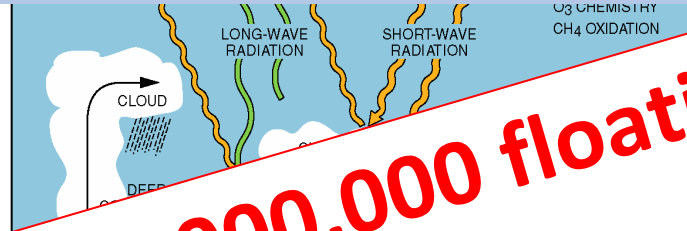


Global TCO1279 spectral resolution (9km grid point spacing)



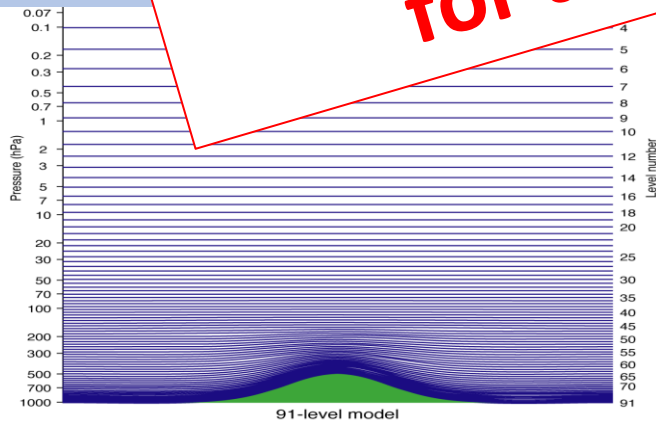
# The forecast model

Physical and dynamical processes updated every 10 minutes

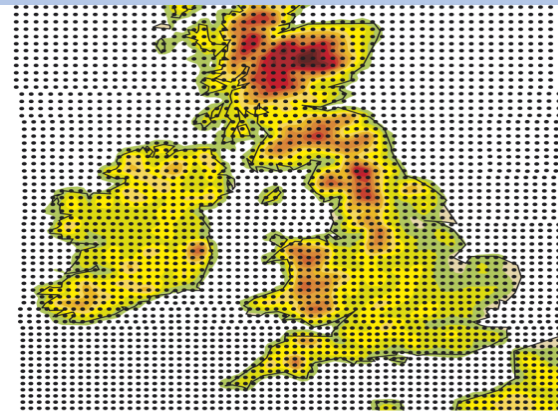


**6,300,000,000,000 floating point operations for a single 10-day forecast**

91 (137) vertical levels  
to 0.01hPa



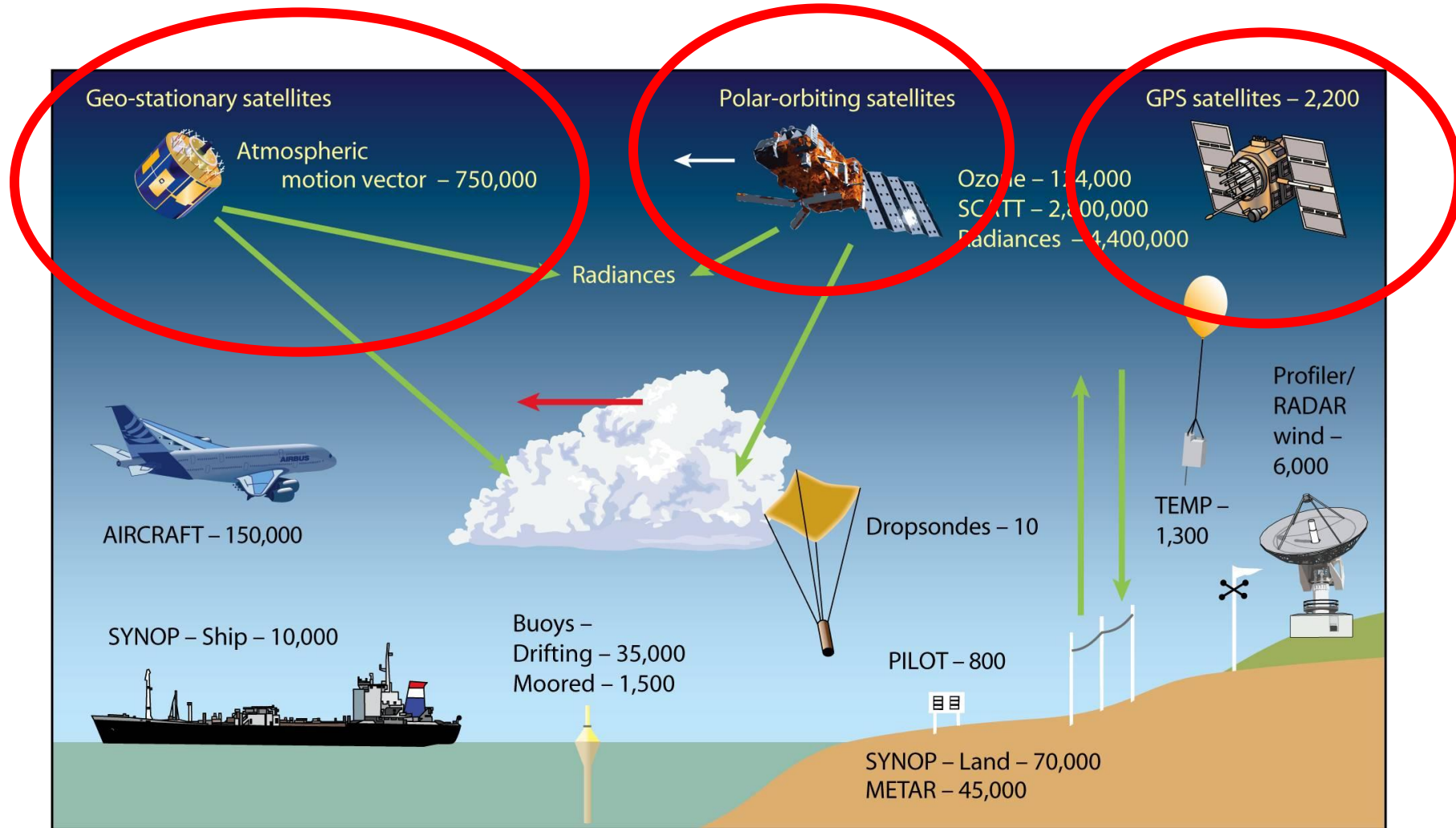
Global TCO1279 spectral resolution  
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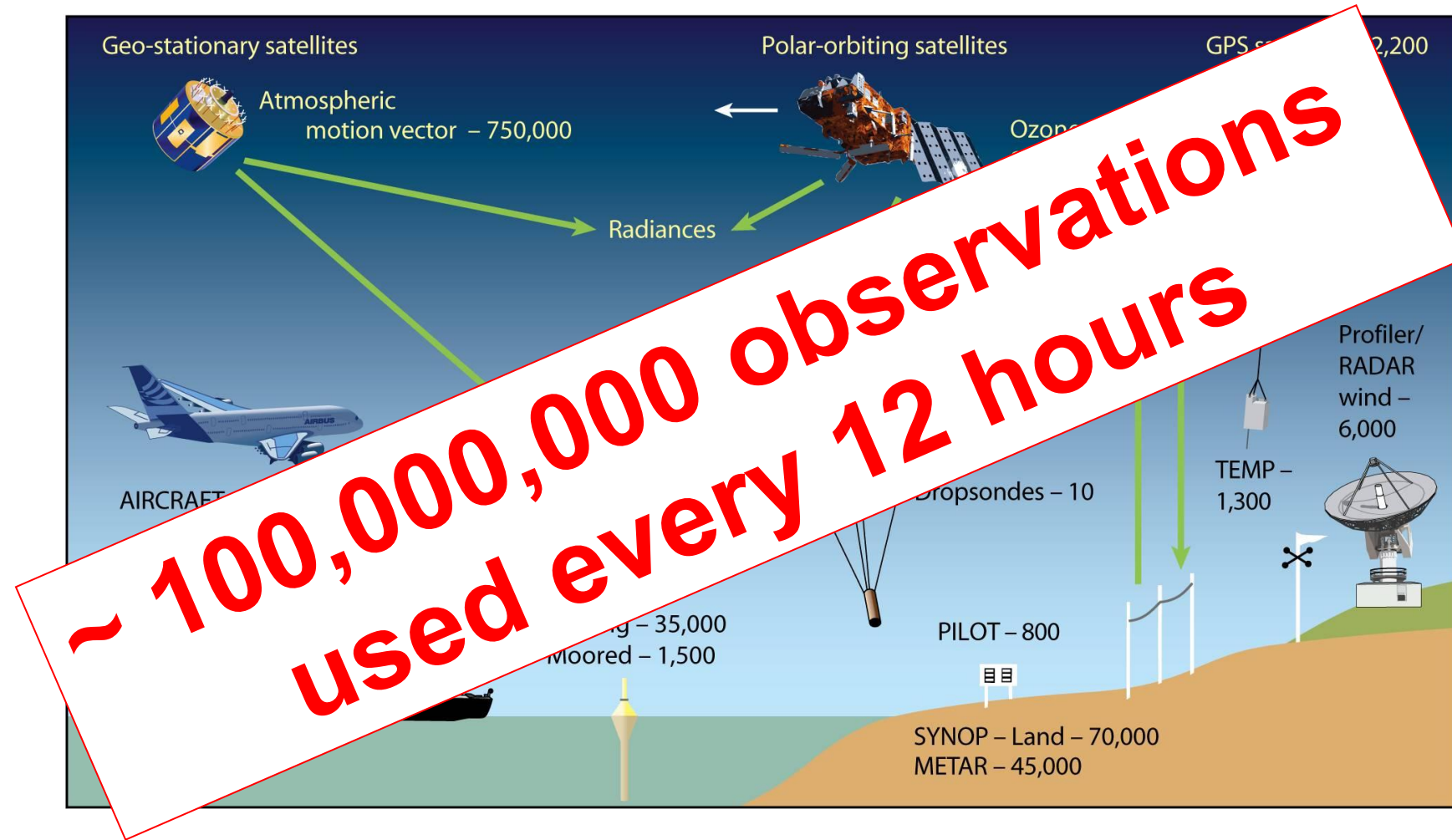
# The Observations

**Y**<sub>*obs*</sub>

# Operational Global Observing Network



# Operational Global Observing Network

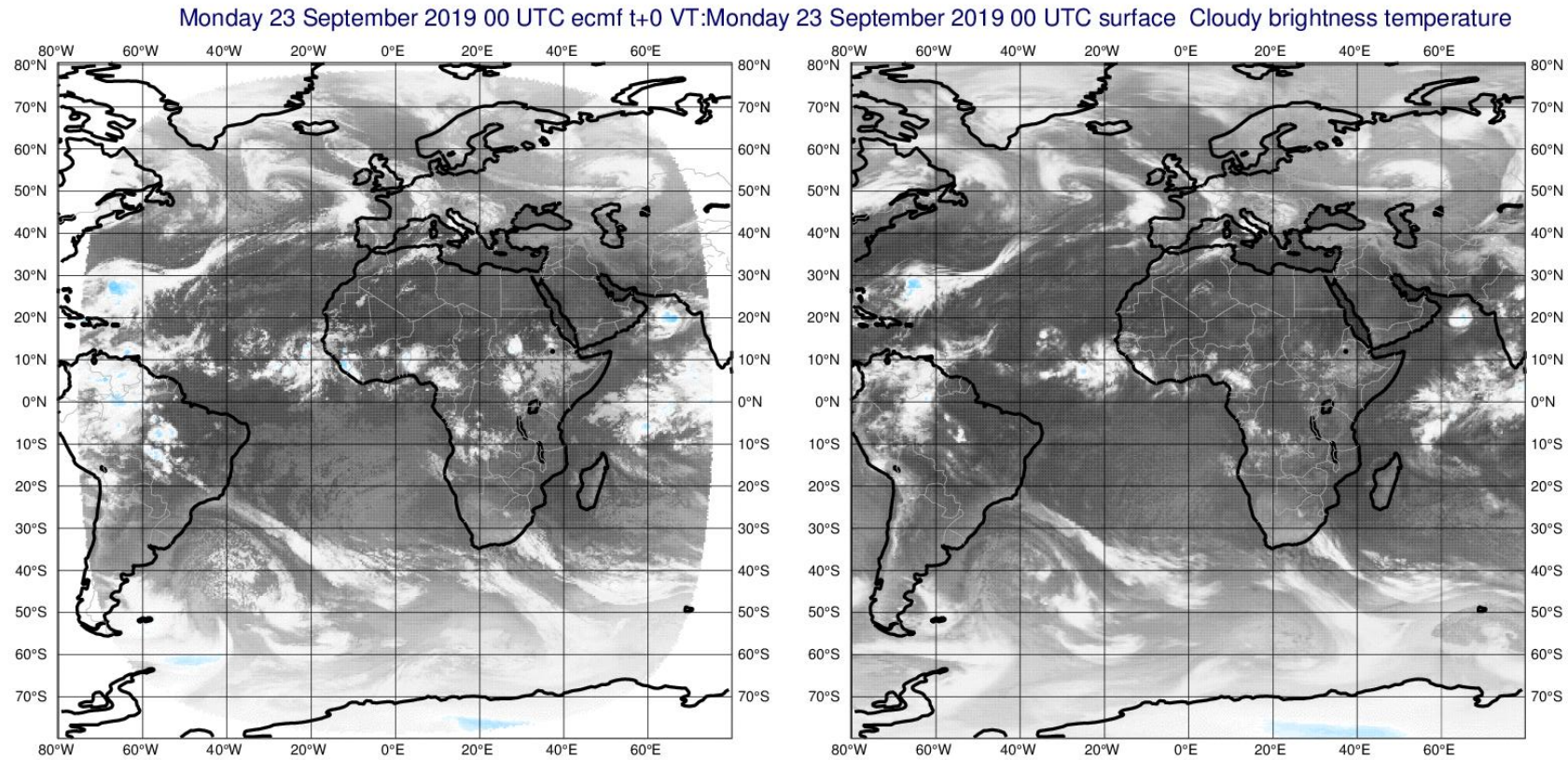


# **The assimilation algorithm**

# Comparing OBS with model in OBS space

Observations from Meteosat-11

Simulated by forecast model



Modern radiative transfer can simulate atmospheric radiation very accurately ...so why do these diverge ?

# Combining information

- At ECMWF we employ **variational data assimilation** methods
- These are based upon the **maximum likelihood combination** of observations and background information
- It can be shown that the most probable state of the atmosphere given a background  $\mathbf{X}_b$  and some observations  $\mathbf{Y}$  is that which minimises a **cost or penalty function  $J$**
- The solution obtained is **optimal** in that it fits the prior (or background) information and measured radiances **respecting the uncertainty in both.**

# The cost function $J(\mathbf{X})$

model state

background error covariance

$$J(x) = (x - x_b)^T \mathbf{B}^{-1} (x - x_b) +$$
$$(y - \mathbf{H}[x])^T \mathbf{R}^{-1} (y - \mathbf{H}[x])$$

observations

observation\* error covariance

observation operator  
(maps the model state to the observation space)

The diagram illustrates the cost function  $J(x)$  with five labeled components and arrows pointing to them. 'model state' points to  $x$  in the first term. 'background error covariance' points to  $\mathbf{B}^{-1}$ . 'observations' points to  $y$  in the second term. 'observation\* error covariance' points to  $\mathbf{R}^{-1}$ . 'observation operator' points to  $\mathbf{H}$  and includes the text '(maps the model state to the observation space)'.

# The cost function components ( $J_b$ )

$$J(x) = \boxed{(x - x_b)^T \mathbf{B}^{-1} (x - x_b)} + (y - H[x])^T \mathbf{R}^{-1} (y - H[x])$$

Fit of the solution to the background estimate of the atmospheric state weighted inversely by the background error covariance  $\mathbf{B}$

# The cost function components ( $J_o$ )

$$J(x) = (x - x_b)^T \mathbf{B}^{-1} (x - x_b) +$$

$(y - \mathbf{H}[x])^T \mathbf{R}^{-1} (y - \mathbf{H}[x])$

Fit of the solution to the observations weighted inversely by the measurement error covariance  $\mathbf{R}$  (observation error + error in observation operator  $\mathbf{H}$ )

# ...a helpful linear analogue ...

It can be shown that the state that minimizes the cost function is equivalent to a linear **correction** of the background using the observations:

$$\underline{x_a} = \underline{x_b} + \underline{[\mathbf{HB}]^T [\mathbf{HBH}^T + \mathbf{R}]^{-1} (y - \mathbf{H}x_b)}$$

**correction term**

...and the **improvement** can be quantified in terms of the key parameters of the assimilation...(i.e. **B**, **R**, **H**)

$$S_a = B - \underline{[\mathbf{HB}]^T [\mathbf{HBH}^T + \mathbf{R}]^{-1} \mathbf{HB}}$$

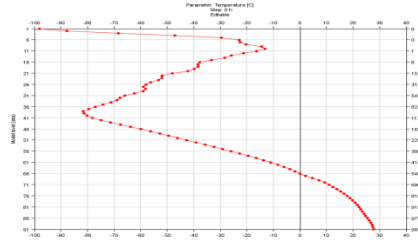
**improvement term**

# Various implementations of the assimilation algorithm

- 1D-Var
- 3D-Var
- 4D-Var

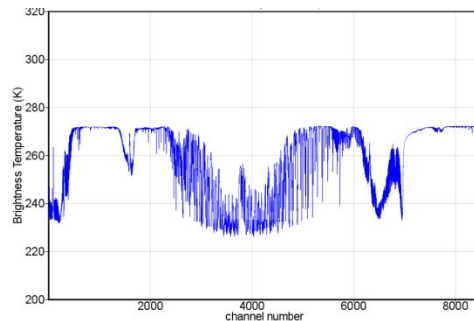
# One dimensional variational analysis (1D-Var)

1D model state profile



$$J(x) = (x - x_b)^T \mathbf{B}^{-1} (x - x_b) + (y - H[x])^T \mathbf{R}^{-1} (y - H[x])$$

vector of measured  
radiances at one location

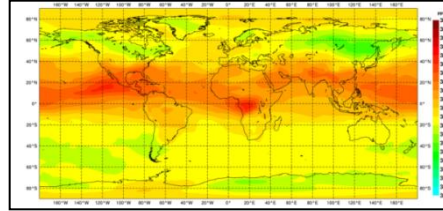


observation Operator  
= radiative transfer model

$$L(\nu) = \int_0^\infty B(\nu, T(z)) \left[ \frac{d\tau(\nu)}{dz} \right] dz$$

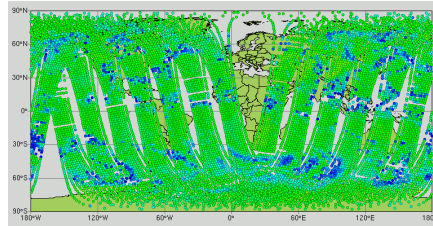
# Three dimensional variational analysis (3D-Var)

3D model state



$$J(x) = (x - x_b)^T \mathbf{B}^{-1} (x - x_b) + (y - H[x])^T \mathbf{R}^{-1} (y - H[x])$$

global vector of  
measured radiances

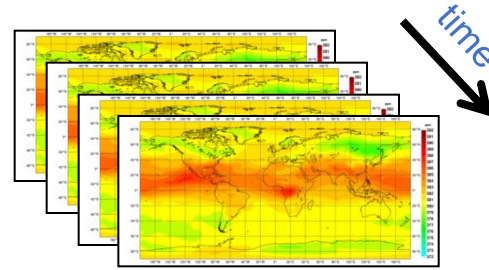


observation operator  
= spatial interpolation +  
radiative transfer model

$$L(\nu) = \int_0^{\infty} B(\nu, T(z)) \left[ \frac{d\tau(\nu)}{dz} \right] dz$$

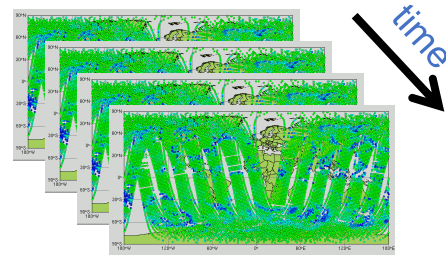
# Four dimensional variational analysis (4D-Var)

4D model state



$$J(x) = (x - x_b)^T \mathbf{B}^{-1} (x - x_b) + (y - H[x])^T \mathbf{R}^{-1} (y - H[x])$$

global time windows of measured radiances



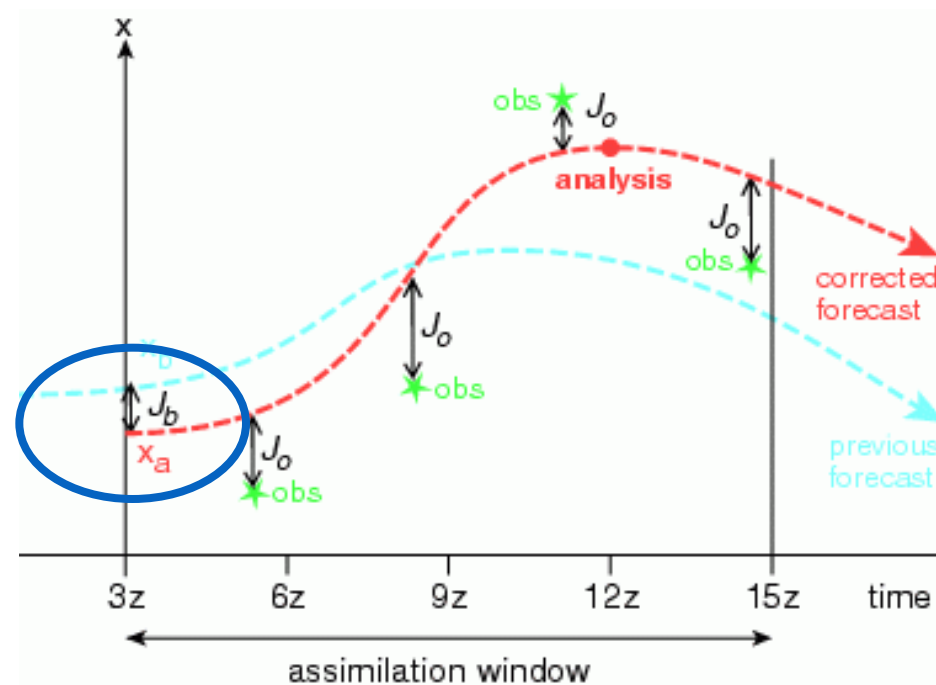
observation operator  
= spatial interpolation + forecast model  
radiative transfer model

$$L(\nu) = \int_0^\infty B(\nu, T(z)) \left[ \frac{d\tau(\nu)}{dz} \right] dz$$



# The 4D-Var Algorithm $J_b$

$$J(x) = \boxed{(x - x_b)^T \mathbf{B}^{-1} (x - x_b)} + (y - H[x])^T \mathbf{R}^{-1} (y - H[x])$$





# **The key elements of a satellite data assimilation system**

# Key elements of a data assimilation system

- **observation operator**
- **background errors**
- **observation errors**
- **bias correction**
- **data selection and quality control**

# Key elements of a data assimilation system

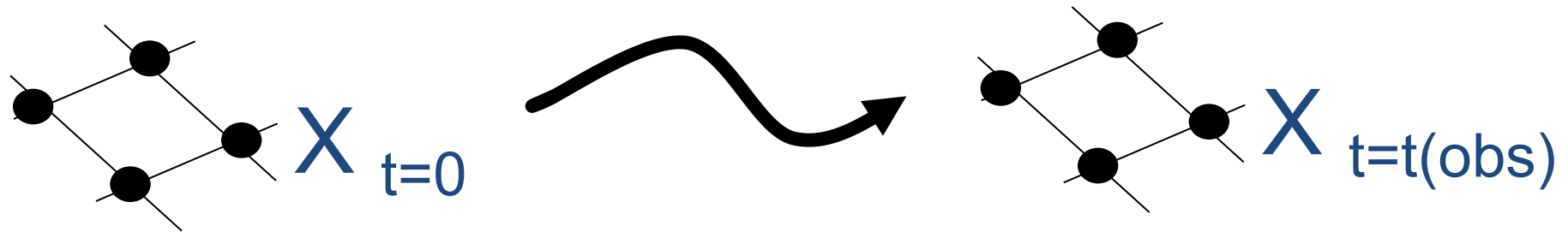
- **observation operator**
- **background errors**
- **observation errors**
- **bias correction**
- **data selection and quality control**

# Observation operator

- The observation operator must map the model state at beginning of the assimilation window ( $t=0$ ) to the observation time and location.
- In the **direct assimilation of radiance observations**, the observation operator must incorporate an additional step to compute radiances from the model state variables (radiative transfer model RTTOV).
- This means that radiance observations are significantly more computationally expensive than conventional observations (e.g. radiosonde temperature data)

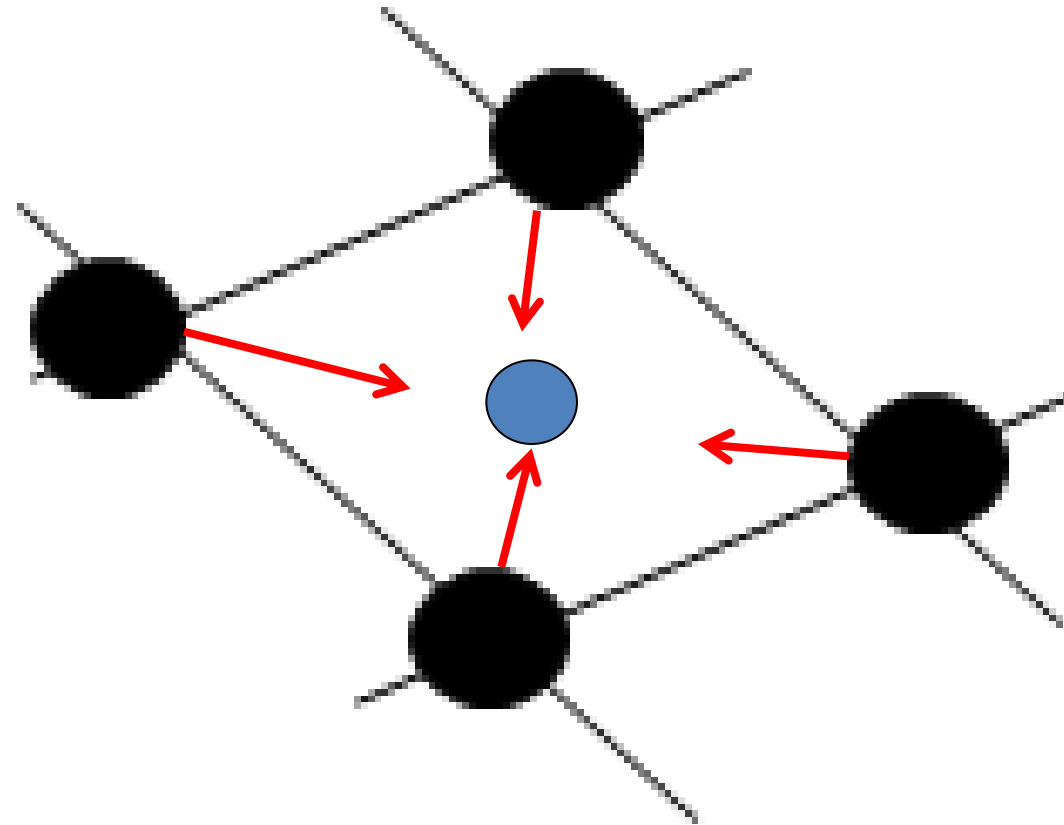
# Observation operator

1) Time evolution of forecast model field to OBS time



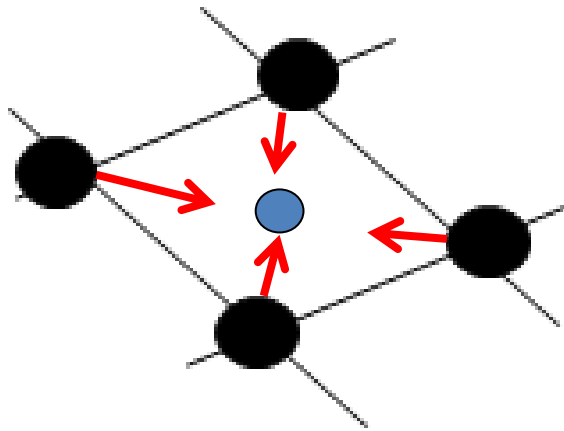
# Observation operator

2) Spatial interpolation of model grid to OBS location

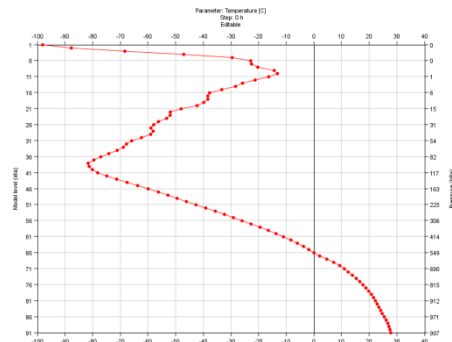


# Observation operator

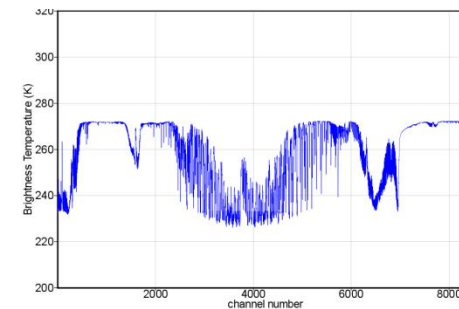
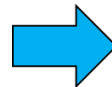
3) Radiative transfer calculation from model state at that location to radiances at that location



$$(y - H[x])^T \mathbf{R}^{-1} (y - H[x])$$



RTTOV



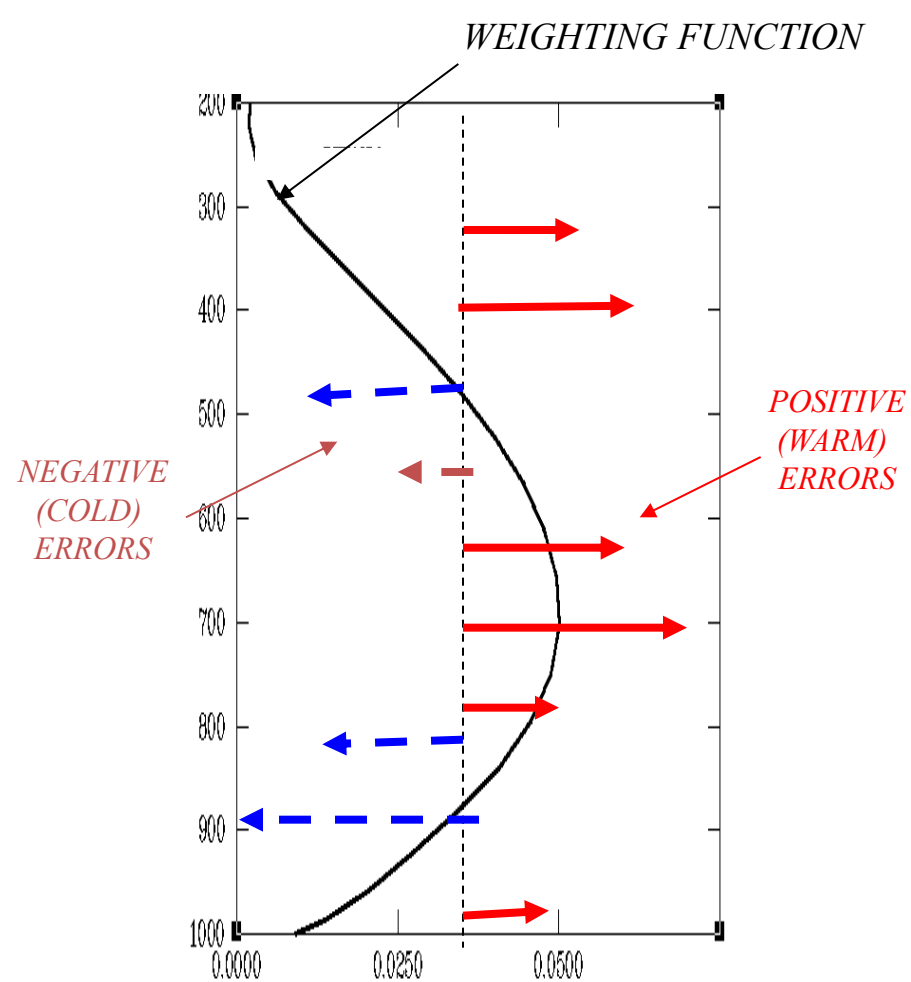
# Key elements of a data assimilation system

- observation operator
- **background errors**
- observation errors
- bias correction
- data selection and quality control

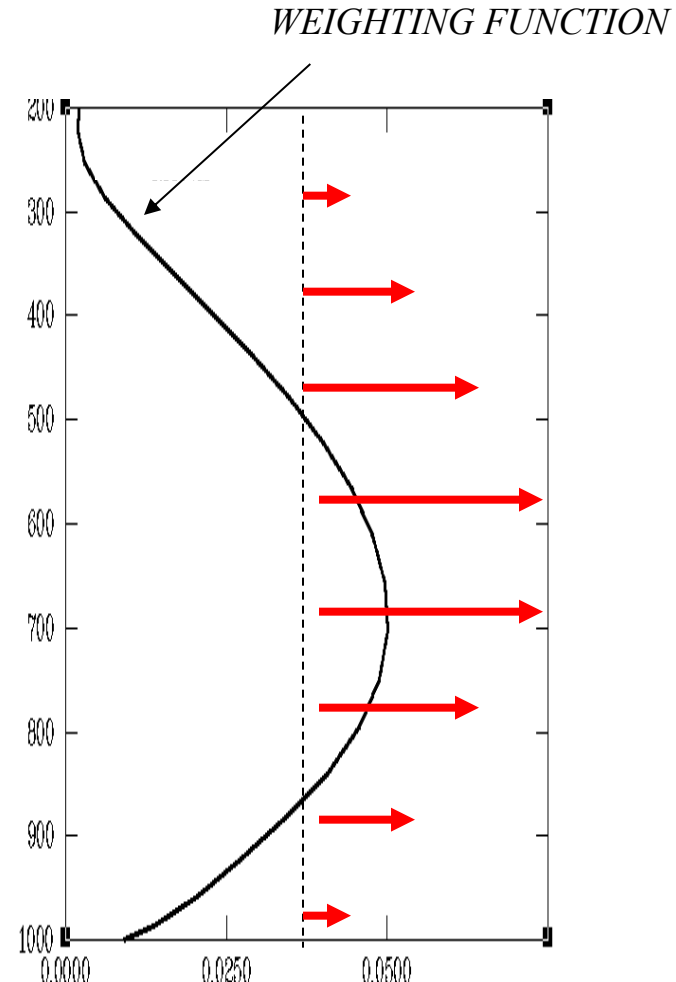
# Background errors (and vertical resolution)

- The matrix  $B$  must accurately describe errors in the background estimate of the atmospheric state. It determines the weight given to the background information.
- A very important aspect for the assimilation of near-nadir viewing satellite radiances are the **vertical correlations** that describe how background errors are distributed in the vertical (sometimes called structure functions)
- These are important because satellite radiances have very **limited vertical resolution** (previous lecture)

# Background errors (and vertical resolution)



*“Difficult” to correct*



*“Easy” to correct*

# ...a helpful linear analogue ...

It can be shown that the state that minimizes the cost function is equivalent to a linear **correction** of the background using the observations:

$$\underline{x_a} = \underline{x_b} + \underline{[\mathbf{HB}]^T [\mathbf{HBH}^T + \mathbf{R}]^{-1} (y - \mathbf{H}x_b)}$$

**correction term**

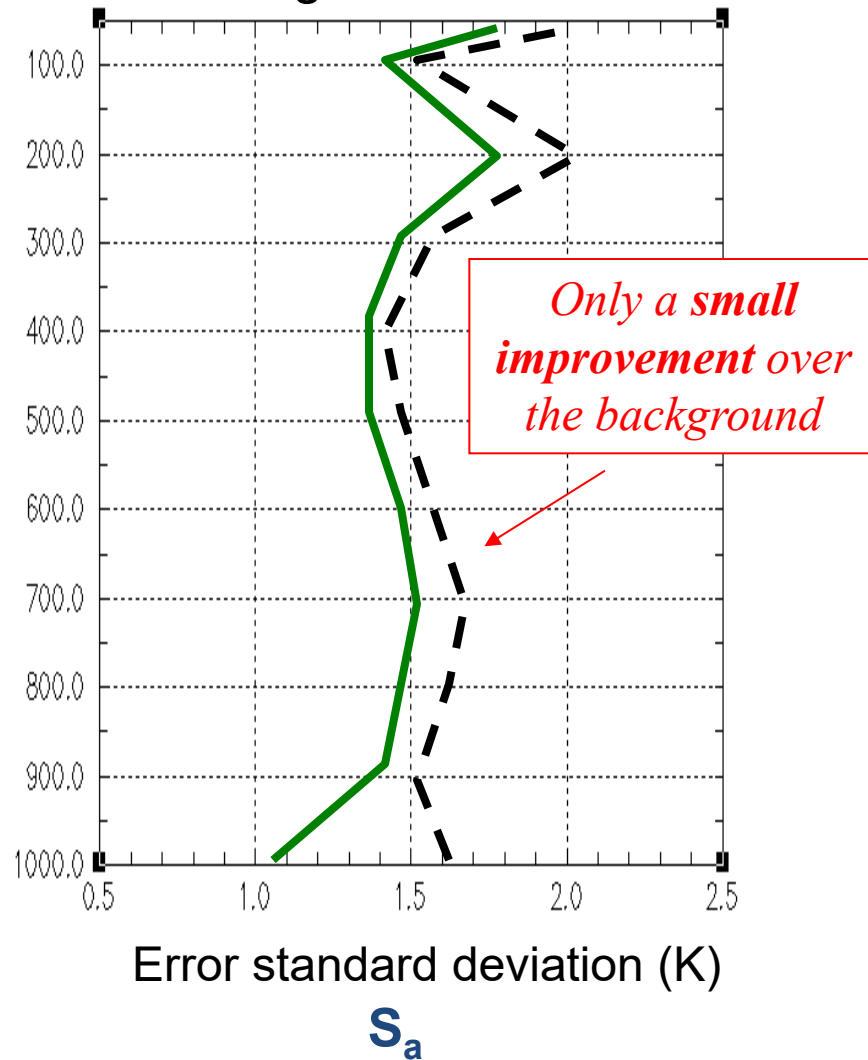
...and the **improvement** can be quantified in terms of the key parameters of the assimilation...(i.e. **B**, **R**, **H**)

$$S_a = B - \underline{[\mathbf{HB}]^T [\mathbf{HBH}^T + \mathbf{R}]^{-1} \mathbf{HB}}$$

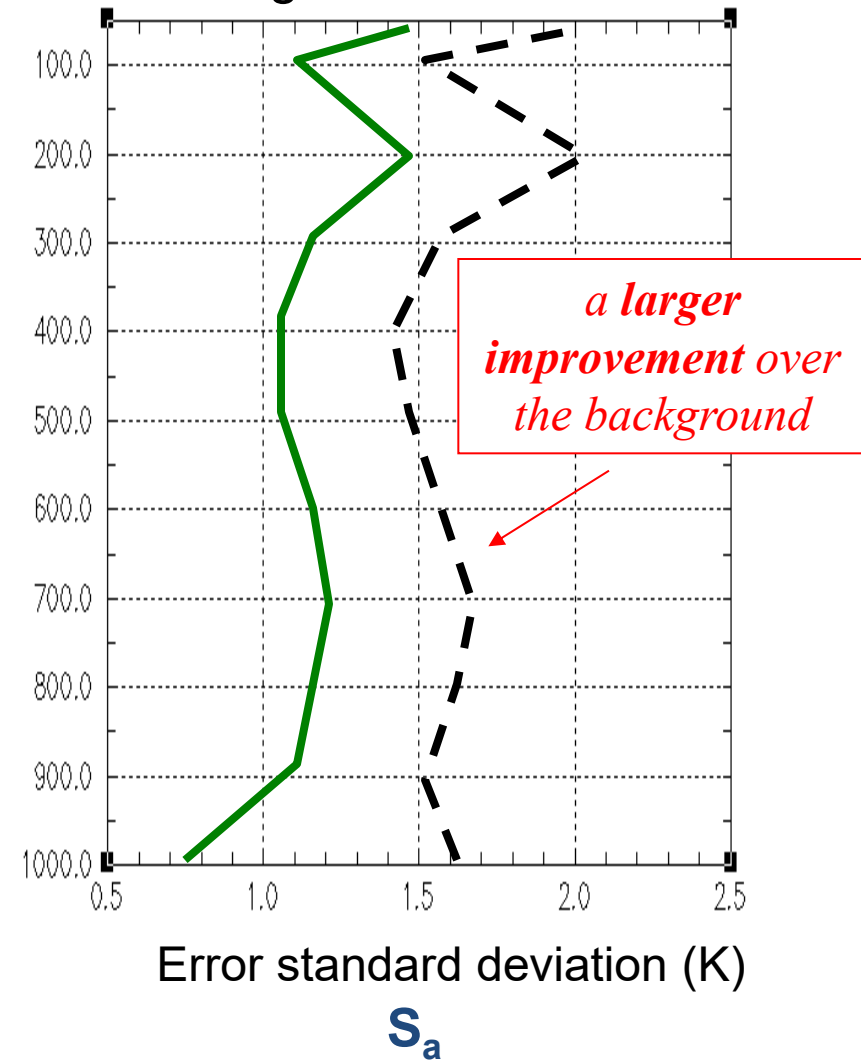
**improvement term**

# Background errors (and vertical resolution)

**Sharp** / anti-correlated background errors

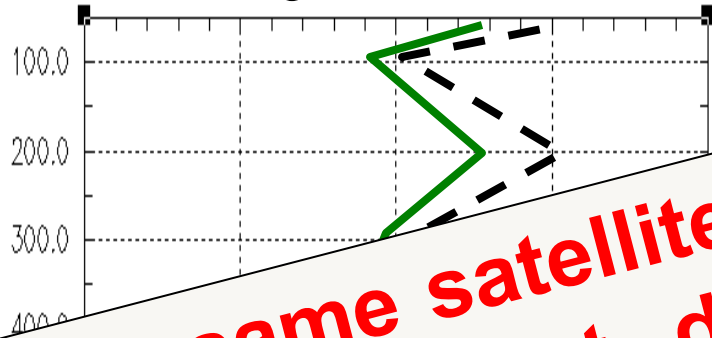


**Broad** / deep correlated background error



# Background errors (and vertical resolution)

**Sharp** / anti-correlated background errors



**Broad** / deep correlated background errors



**So the same satellite can have a big impact or small impact depending on how the background errors are distributed (i.e. what type of forecast errors are being "corrected")**

Error standard deviation (K)

$S_a$

Error standard deviation (K)

$S_a$

# Key elements of a data assimilation system

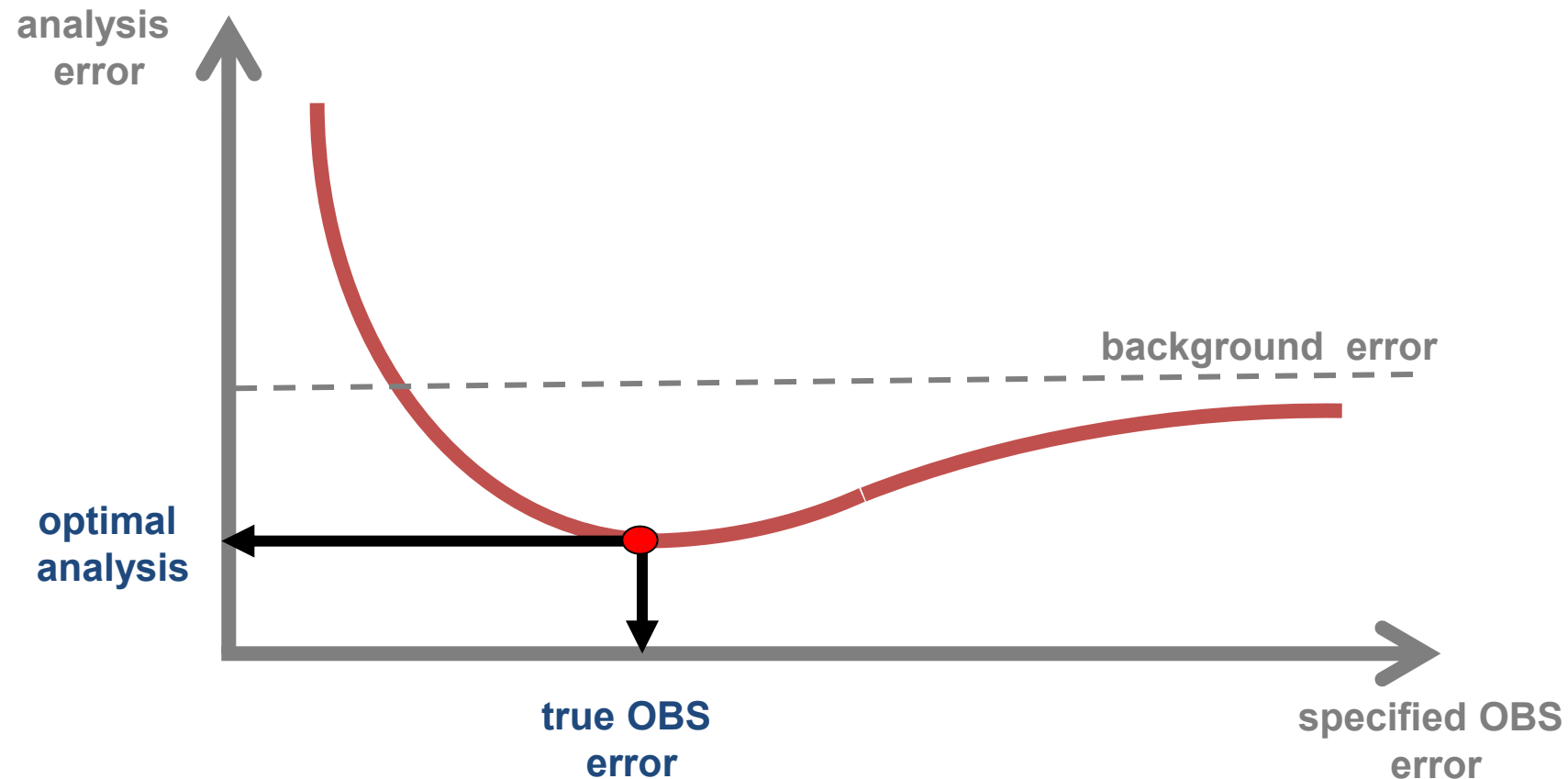
- observation operator
- background errors
- **observation errors**
- bias correction
- data selection and quality control

# Observation errors:

- These determine the weight we give to the radiance observations. The observation error must account for **instrument noise**, random uncertainties in the **observation operator** (e.g. RT model), errors in data **screening** (e.g. residual clouds) and errors of representativeness (e.g. scale mismatch).
- It is important to model both the magnitude of errors (diagonals of  $R$ ) and **any inter-channel correlations**
- Wrongly specified observation errors can lead to an analysis with **larger errors than the background!**

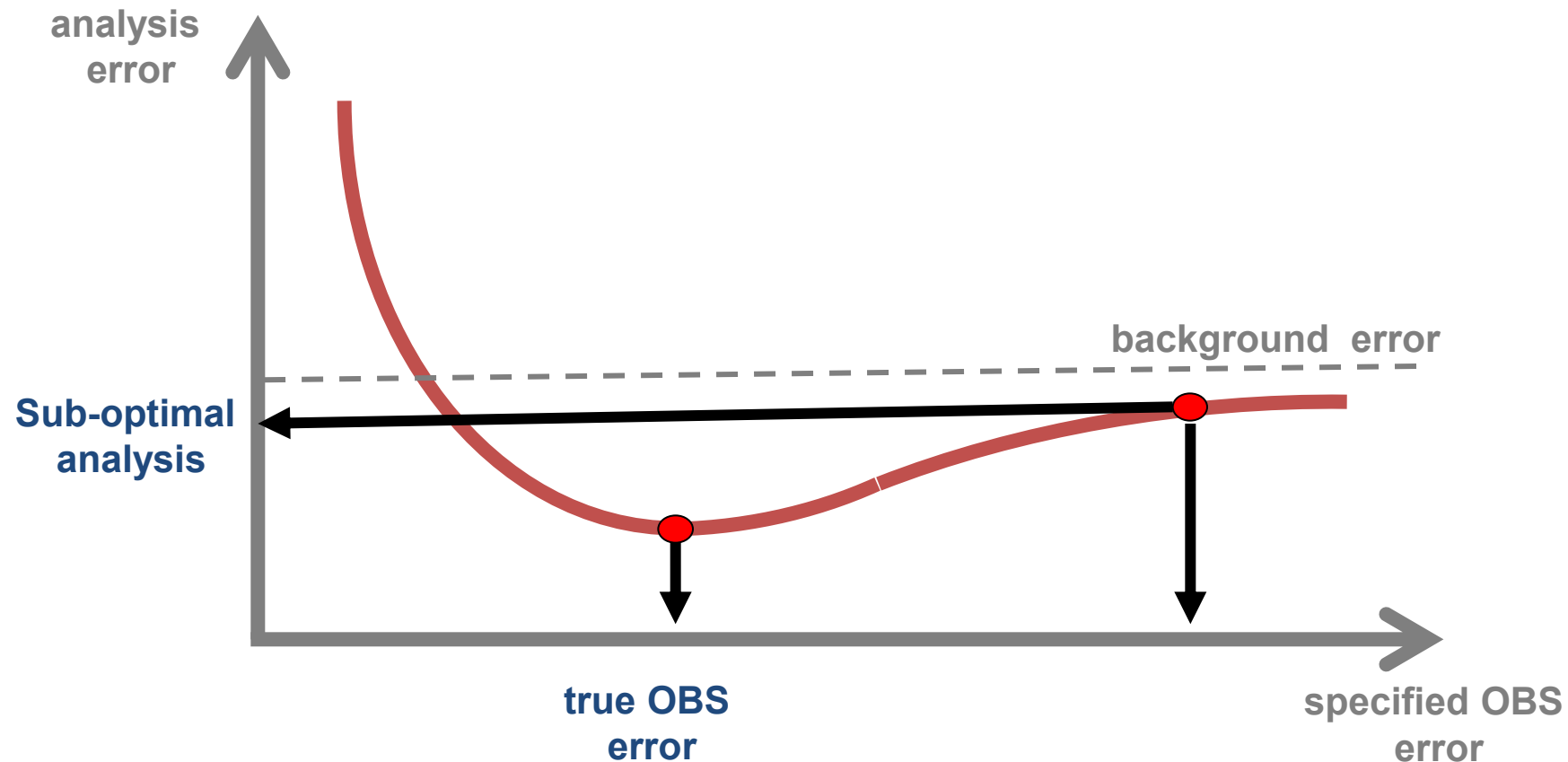
# Observation errors:

- Specifying the correct observation error produces an optimal analysis with minimum error.



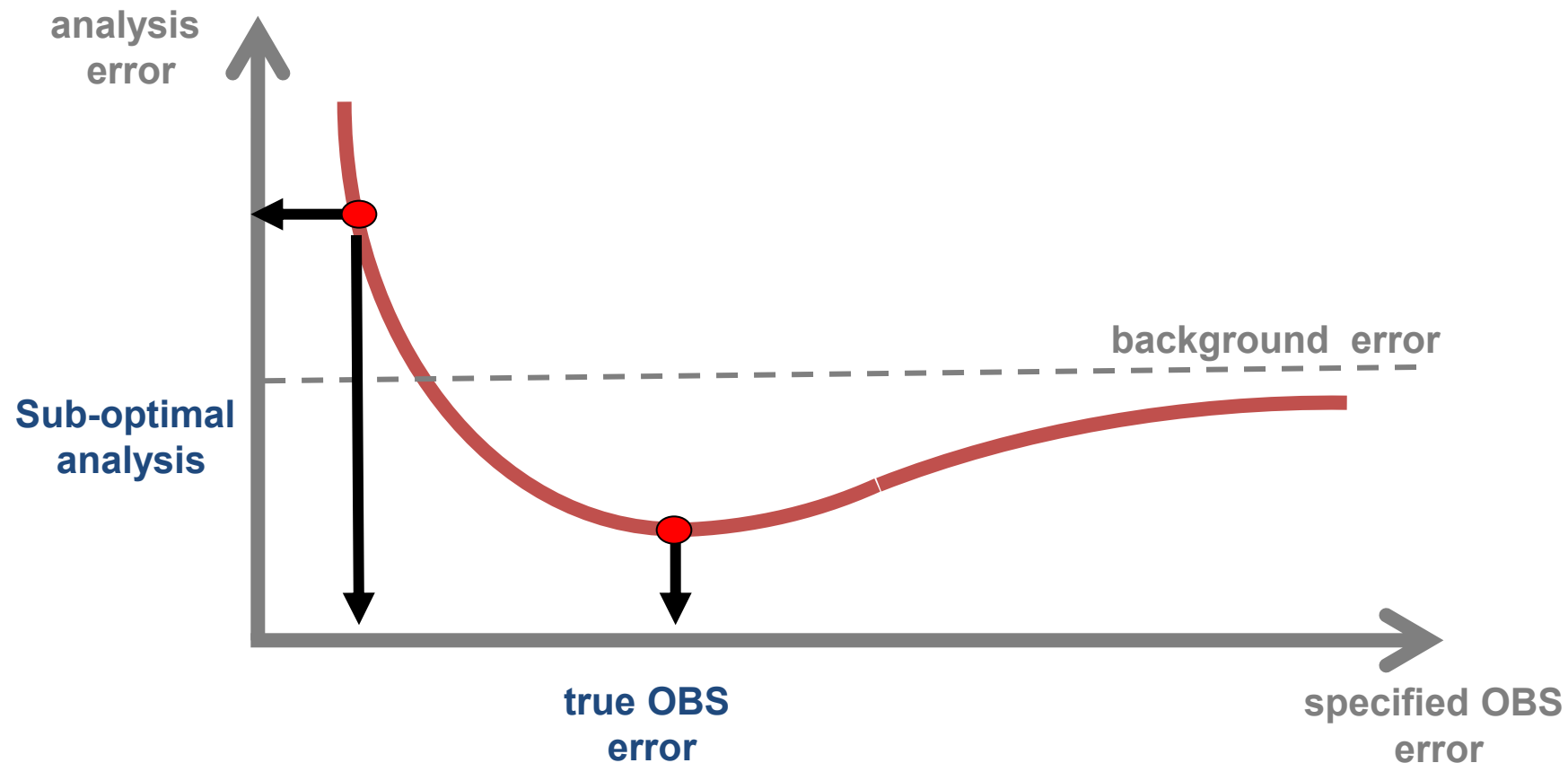
# Observation errors:

- Over-estimating the OBS error degrades the analysis, but the result will not be worse than the background.



# Observation errors:

- Under-estimating the OBS error degrades the analysis, and **the result can be worse than the background!**



# Key elements of a data assimilation system

- observation operator
- background errors
- observation errors
- **bias correction**
- data selection and quality control

# Bias correction:

Systematic errors must be removed otherwise biases will propagate in to the analysis (causing **global damage** in the case of satellites!). A bias in the radiances is defined as:

$$bias = mean [ Y_{obs} - H(X_{true}) ]$$

Sources of systematic error in radiance assimilation include:

- instrument error (scanning or calibration)
- radiative transfer error (spectroscopy or RT model)
- cloud / rain / aerosol screening errors

# Key elements of a data assimilation system

- observation operator
- background errors
- observation errors
- bias correction
- **data selection and quality control**

# Data selection and quality control (QC):

The primary purpose of this is to ensure that the observations entering the analysis are consistent with the assumptions in the observations error covariance ( $\mathbf{R}$ ) and the observation operator ( $\mathbf{H}$ ).

Primary examples include the following:

- Rejecting bad data with **gross error** (not described by  $\mathbf{R}$ )
- Rejecting data affected by **clouds** if  $\mathbf{H}$  is a clear sky RT
- Thinning data if no **correlation** is assumed (in  $\mathbf{R}$ )
- Always **blacklisting** data where we do not trust our QC!

# Data selection and quality control (QC):

Often checks are performed using the forecast background as a reference. That is an observations is rejected if the departure from the background exceeds a threshold  $T_{QC}$ :

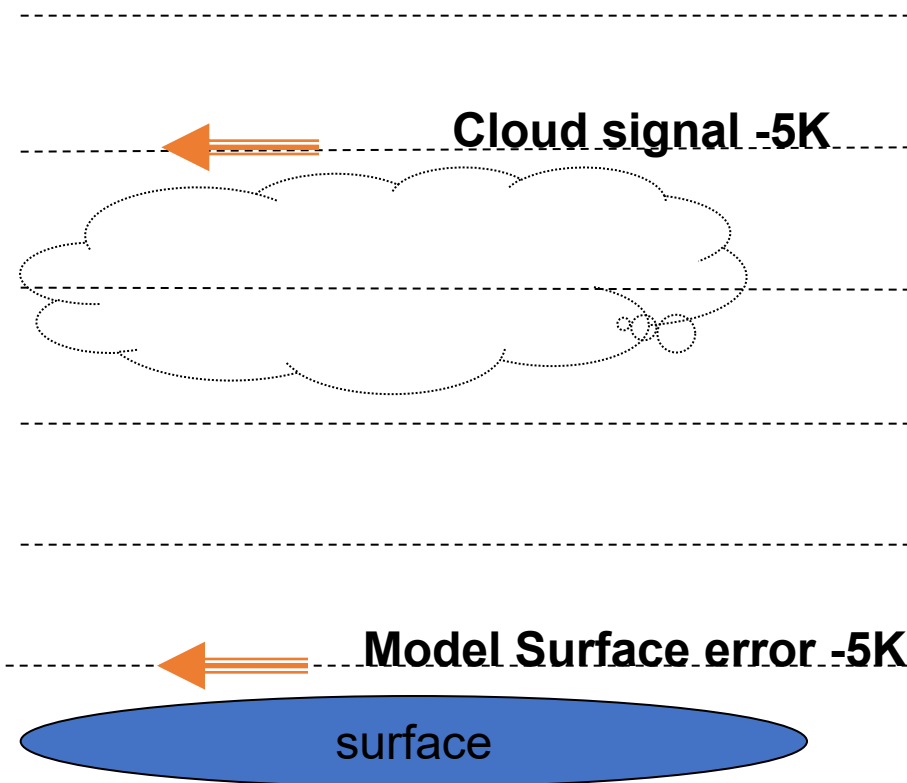
$$Y_{\text{obs}} - H(X_{\text{true}}) > T_{QC}$$

But sometimes large errors in the background can lead to:

- False rejection of a good observation
- Missed rejection of a bad observation

# Data selection and quality control:

- Missed rejection of a **bad** observation



The radiance are contaminated by cloud (**cold 5K**) compared to the clear sky value.

But our computation of the clear sky value from the background is also **cold by 5K** due to an error in the surface skin temperature.

Thus our checking (against the background) sees no reason to reject the observation and is it **passed!**

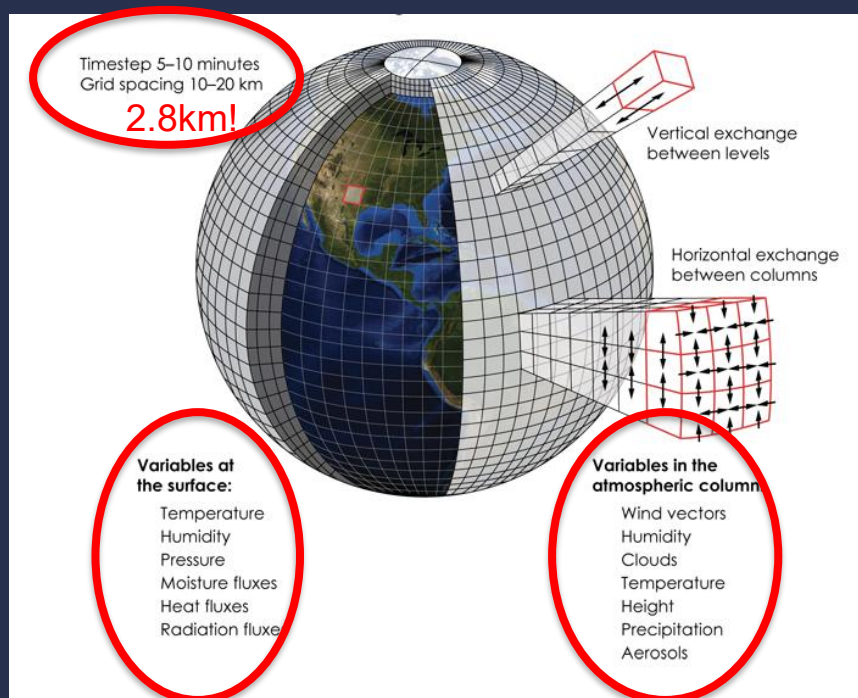
# Summary

- **observation operator**  
(complex and expensive for radiances)
- **background errors**  
(important due to limited vertical resolution)
- **observation errors**  
(a challenge to specify correctly)
- **bias correction**  
(small, but global impact of bias)
- **data selection and quality control**  
(primarily data selection, few bad observations)

# High-resolution and highly complex physics-based models present extreme challenges for DA

Observations are simply insufficient and generally of the wrong variables to provide initial conditions for NWP models of this resolution and complexity!

...so we are forced to blend observations with a background using DA....

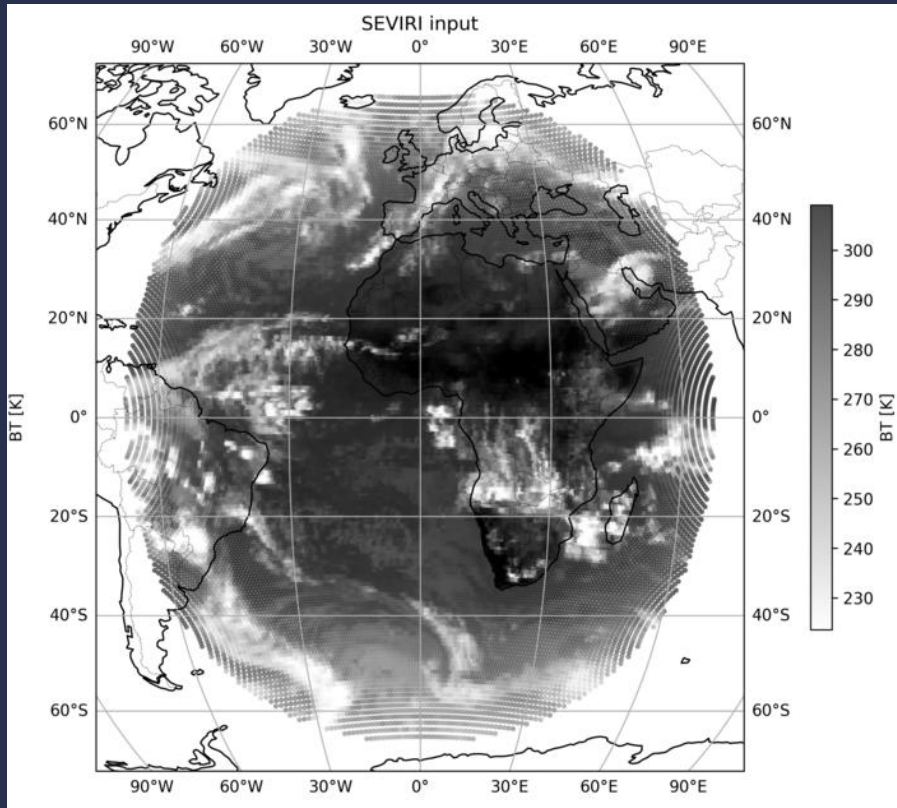


...requiring an exacting specification of poorly known error covariances (all huge multivariate tensors)

$$J(\mathbf{x}) = \frac{1}{2}(\mathbf{x} - \mathbf{x}_b)^T \mathbf{B}^{-1} (\mathbf{x} - \mathbf{x}_b) + \frac{1}{2}[\mathcal{H}(\mathbf{x}) - \mathbf{y}]^T \mathbf{R}^{-1} [\mathcal{H}(\mathbf{x}) - \mathbf{y}]$$

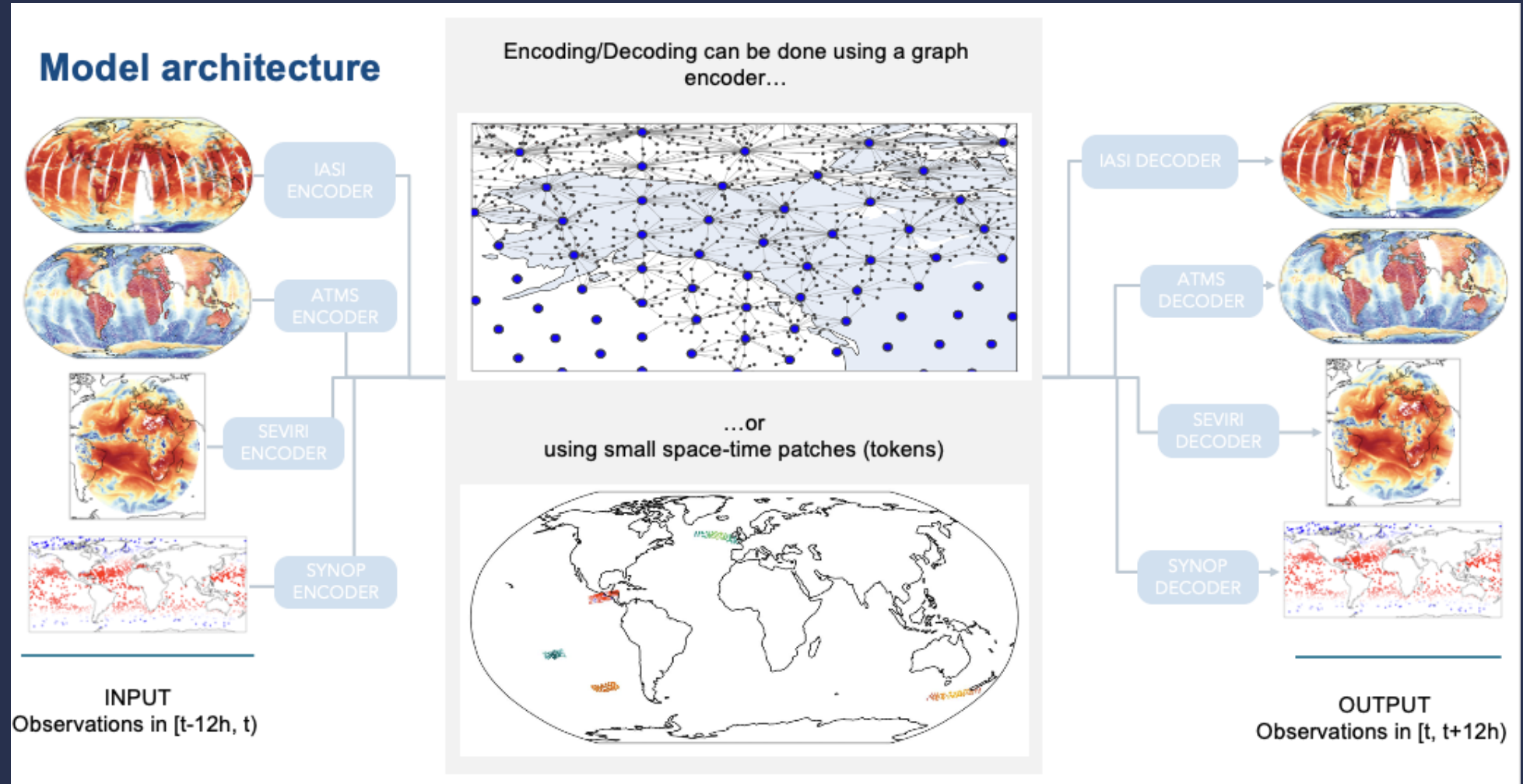
Accurate observation operators potentially limiting limiting the observations we can exploit...

# Enhanced exploitation of satellite observations using Artificial Intelligence...Direct Observation Prediction



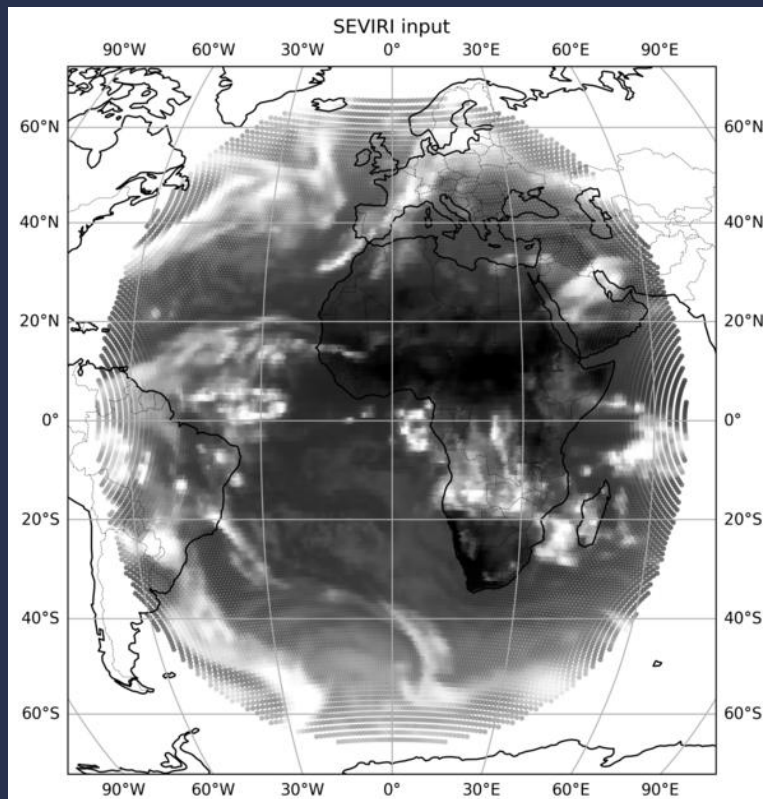
- We use historical observations to train a Neural Network (NN) to forecast future observations
- Include observations of the full Earth system (atmosphere, ocean, land) simultaneously
- Use all observations, without demanding a detailed physical model of the measurement
- Once trained, we initialize the model directly with the observations themselves, allowing much faster access to forecast warnings

# Artificial Intelligence...Direct Observation Prediction (AI-DOP)



# First medium-range forecasts made directly from observations:

AI-DOP model



Target real observations

